Supplementary Information:

Mechanistic Investigation of Sustainable Heme-inspired Biocatalytic

Synthesis of Cyclopropanes for Challenging Substrates

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Table of contents

Supplementary Note 1.	Spin state effect	S2
Supplementary Note 2.	Substrate substituent effect	S4
Supplementary Note 3.	Axial ligand effect	S6
Supplementary Note 4.	Effects of experimentally studied macrocycle (reactions 7-9)	S8
Supplementary Note 5.	Effects of macrocycles not being experimentally studied yet (reactions 10-13)	S10
Supplementary Note 6.	Imaginary frequencies of transition states	S13
Supplementary references		S14

Supplementary Note 1. Spin state effect

Experimental studies on iron porphyrin carbenes have demonstrated that the most favorable spin state is closed-shell singlet (CSS)^{1,2} with Fe^{II}-based features, providing accurate predictions of experimental features including Mössbauer, X-ray, and NMR properties, as opposed to Fe^{III}based open-shell singlet (OSS) structures.^{1,3} Such a CSS feature is supported by additional experimental XANES studies and high-level multi-reference quantum chemical calculations.^{2,4} Therefore, the spin states of the iron-containing reactants (heme carbenes) in all of the studied reactions are CSS. The spin state of the iron-containing His-ligated product was previously determined to be quintet.⁵⁻⁷ As such, to determine the best spin state for **TS**, both singlet and quintet **TS**s were investigated here for the representative transition states in each studied pathway category as described below, including that of reactions 3, 6, 7, 8, 10, and 13. TS(3) was selected to explore the effect of spin under the substrate substituent effect (as opposed to TS(1, 2), which share similar features with each other). Compared to TS(3), TS(6) exhibited the largest difference in free energy and geometric and electronic parameters under the axial ligand effect, so this was also investigated. Under the experimentally studied macrocycle effect, TS(7) and TS(8) were selected as candidates due to their unique geometric interactions in this category. For the computationally studied macrocycles, TS(10) and TS(13) were selected due to their low free energy barriers and thus, high potential for future experimental applications, with both being ~ 0.2 kcal mol⁻¹ within each other. Because the previous experimental results show that iron carbene heme catalyst catalyzed cyclopropanation reaction has CSS feature^{5,8-10} and the high-level multi-reference quantum chemical calculations showed that the lowest OSS state has a significantly higher ΔE of 22.14 kcal mol⁻¹ than the CSS ground state of a similar heme carbene,⁴ only CSS was studied for the singlet. For quintet, we investigated different spin features including A) Fe^{II} (S=2) and carbene (S=0), B) ferromagnetically coupled Fe^{III} (S=3/2) and carbene (S=1/2), and C) anti-ferromagnetically coupled Fe^{III} (S=5/2), carbene (S=-1/2).

As seen from Supplementary Table 1, for **TS(3)**, only two spin features, A and B, were successfully located after geometry optimizations, while the initial spin feature C was optimized to A with Fe^{II} (S=2) feature (spin density $\rho^{Fe}_{\alpha\beta} = 3.996$ e). Quintet calculations for **TS(6)** are similar with only two spin features, A and B, found after geometry optimizations. For **TS(7)**, although two stable states were finally optimized, one resembles the Fe^{II} (S=2) feature A with $\rho^{Fe}_{\alpha\beta}$ of 3.956 e, while the other is close to Fe^{III} (S=3/2) coupled with radical carbene and substrate of opposite spins based on spin densities of 3.595 e on Fe ($\rho^{Fe}_{\alpha\beta}$), -0.479 e on carbene's carbon C1, and 0.748 e on substrate (see Supplementary Table 1). For **TS(8)**, all tries ended up with spin feature A after optimizations. **TS(13)** shows the same trend as **TS(8)**. However, for **TS(10)**, all initial setups were optimized with spin feature B: spin densities concentrated on Fe ($\rho^{Fe}_{\alpha\beta}$ of 3.264 e) and carbene carbon ($\rho^{C1}_{\alpha\beta}$ of 0.446 e). As shown in Supplementary Table 1, although different quintet **TS** results could be obtained with different reactions, all of them are of significantly higher energy than the CSS **TS**, which is consistent with the CSS concerted mechanism found in several experimental heme catalyzed cyclopropanation studies.^{5,8-10}

The above-mentioned most favorable spin states were used in the main text discussion.

		$\langle \rangle$										
TS	S	ρ_{Fe}	ρ_{C1}	pc2	рсз	$\rho_{R'}$	ρ_{Por}	ρ_L	ΔΕ	ΔE_{ZPE}	ΔH	ΔG
3	0	/	/	/	/	/	/	/	0.00	0.00	0.00	0.00
	2	3.996	-0.345	0.111	-0.167	-0.024	0.351	0.041	11.38	9.67	10.28	19.68
	2	3.269	0.455	-0.144	0.216	0.034	0.151	0.015	15.39	12.43	13.47	7.65
6	0	/	/	/	/	/	/	/	0.00	0.00	0.00	0.00
	2	3.987	-0.322	0.113	-0.174	-0.024	0.355	0.031	12.46	8.98	10.14	4.68
	2	3.319	0.423	-0.135	0.199	0.031	0.145	0.013	14.21	12.27	13.12	8.76
7	0	/	/	/	/	/	/	/	0.00	0.00	0.00	0.00
	2	3.956	-0.296	0.067	-0.107	-0.015	0.342	0.016	15.53	12.00	13.22	8.55
_	2	3.595	-0.479	-0.084	0.674	0.158	0.132	0.030	15.47	12.53	13.52	9.83
8	0	/	/	/	/	/	/	/	0.00	0.00	0.00	0.00
	2	3.980	-0.342	0.074	-0.110	-0.016	0.338	0.038	15.01	11.76	12.63	9.42
10	0	/	/	/	/	/	/	/	0.00	0.00	0.00	0.00
	2	3.264	0.446	-0.154	0.234	0.039	0.144	0.016	14.02	12.25	12.77	10.59
13	0	/	/	/	/	/	/	/	0.00	0.00	0.00	0.00
	2	3.928	-0.284	0.043	-0.059	-0.007	0.294	0.045	17.85	14.76	15.69	11.44
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Supplementary Table 1. TS Spin States and their Relative Energies* (unit: *kcal mol⁻¹*) and Spin Densities (unit: *e*)

* Energies are relative to CSS species.

Supplementary Note 2. Substrate substituent effect

Reaction	Species	Е	E _{ZPE}	Н	G
1 ^{a)}	R ₁	-1683.67858	-1683.20091	-1683.16901	-1683.26230
	\mathbf{R}_2	-309.59817	-309.46383	-309.45613	-309.49592
	TS	-1993.28963	-1992.67451	-1992.63575	-1992.74350
	P ₁	-1377.27975	-1376.90283	-1376.87739	-1376.95905
	P ₂	-616.08496	-615.84844	-615.83452	-615.88945
2	\mathbf{R}_2	-314.43944	-314.21538	-314.20394	-314.25200
	TS	-1998.12778	-1997.42309	-1997.38038	-1997.49887
	P ₂	-620.92923	-620.60232	-620.58479	-620.64811
3	\mathbf{R}_2	-345.75738	-345.63270	-345.62389	-345.66536
	TS	-2029.44078	-2028.83575	-2028.79583	-2028.90676
	P ₂	-652.24758	-652.02060	-652.00542	-652.06407

Supplementary Table 2. Absolute Energies of Species in Cyclopropanation Pathways of Different Olefins (unit: *Hartrees*)

^{a)} All results for X=Ph are from previous work.⁵

Supplementary Table 3. Relative Energies of Species in Cyclopropanation Pathways of Different Olefins (unit: *kcal mol⁻¹*)

Reaction	System	ΔΕ	ΔE_{ZPE}	ΔH	ΔG
1	R_1+R_2	0.00	0.00	0.00	0.00
	TS	-8.08	-6.13	-6.66	9.24
	P_1+P_2	-55.20	-54.30	-54.45	-56.65
2	R_1+R_2	0.00	0.00	0.00	0.00
	TS	-6.13	-4.27	-4.66	9.68
	P_1+P_2	-57.08	-55.76	-55.99	-58.27
3	R_1+R_2	0.00	0.00	0.00	0.00
	TS	-3.02	-1.34	-1.84	13.11
	$\mathbf{P}_1 + \mathbf{P}_2$	-57.34	-56.36	-56.42	-59.90

Supplementary Table 4. Geometric Parameters of Species in Cyclopropanation Pathways of Different Olefins

Reaction	System	R _{FeC1} (Å)	R _{C1C2} (Å)	R _{C1C3} (Å)	R _{C2C3} (Å)	R _{FeL} (Å)	∠ _{HC1Y} ^{a)} (°)
1	R 1	1.755	/	/	/	2.122	113.3
	\mathbf{R}_2	/	/	/	1.331	/	/
	TS	1.863	2.361	2.666	1.345	2.095	109.7
	P ₁	/	/	/	/	2.173	/
	P ₂	/	1.509	1.526	1.496	/	112.6
2	\mathbf{R}_2	/	/	/	1.328	/	/
	TS	1.869	2.404	2.578	1.341	2.072	109.6
	P ₂	/	1.519	1.518	1.490	/	112.5
3	\mathbf{R}_{2}	/	/	/	1.327	/	/

TS	1.898	2.250	2.546	1.345	2.060	110.7
P ₂	/	1.500	1.524	1.500	/	113.6

^{a)} H is the hydrogen atom connected to C1; Y is the carbonyl carbon connected to C1.

Supplementary Table 5. Atomic Charge of Species in Cyclopropanation Pathways of Different Olefins (unit: *e*)

Reaction Sys	stem	Q _{Fe}	Q _{C1}	QH	Qy	Q _{C2}	Q _{C3}	Q _R , ^{a)}	Q _{Por} ^{b)}	QL
1 F	R 1	0.089	0.087	0.193	-0.043	/	/	/	-0.583	0.246
F	\mathbf{R}_2	/	/	/	/	-0.349	-0.200	0.549	/	/
Т	ГS	0.144	-0.055	0.199	-0.032	-0.337	-0.146	0.662	-0.680	0.265
I	P ₁	1.121	/	/	/	/	/	/	-1.278	0.157
I	P ₂	/	-0.316	0.234	-0.001	-0.354	-0.210	0.647	/	/
2 F	\mathbf{R}_2	/	/	/	/	-0.386	-0.168	0.554	/	/
Т	ГS	0.142	-0.057	0.195	-0.041	-0.344	-0.115	0.650	-0.696	0.265
I	P ₂	/	-0.326	0.230	-0.012	-0.370	-0.188	0.666	/	/
3 F	\mathbf{R}_2	/	/	/	/	-0.267	-0.318	0.585	/	/
Т	ГS	0.168	-0.100	0.201	-0.037	-0.264	-0.266	0.689	-0.670	0.278
I	P ₂	/	-0.302	0.244	0.010	-0.343	-0.308	0.699	/	/

^{a)} R' is substrate excluding C2 and C3; ^{b)} Por is the whole porphyrin with substituent(s).

Supplementary Note 3. Axial ligand effect

Reaction	System	Е	Ezpe	Н	G
3	R ₁	-1683.67858	-1683.20091	-1683.16901	-1683.26230
	TS	-2029.44078	-2028.83575	-2028.79583	-2028.90676
	P ₁	-1377.27975	-1376.90283	-1376.87739	-1376.95905
4	\mathbf{R}_1	-1782.91254	-1782.44281	-1782.41008	-1782.50498
	TS	-2128.67426	-2128.07757	-2128.03667	-2128.14996
	P ₁	-1476.51585	-1476.1477	-1476.12200	-1476.20458
5	\mathbf{R}_{1}	-2026.51069	-2026.04851	-2026.01657	-2026.11137
	TS	-2372.27309	-2371.68381	-2371.64370	-2371.75522
	P ₁	-1720.11225	-1719.75138	-1719.72563	-1719.80920
6	\mathbf{R}_{1}	-1705.72980	-1705.23462	-1705.20218	-1705.29610
	TS	-2051.48901	-2050.86630	-2050.82570	-2050.93885
	P ₁	-1399.33140	-1398.93704	-1398.91095	-1398.99377

Supplementary Table 6. Absolute Energies of Species in Cyclopropanation Pathways of Different Axial Ligands (unit: *Hartrees*)

Supplementary Table 7. Relative Energies of Species in Cyclopropanation Pathways of Different Axial Ligands (unit: *kcal mol*⁻¹)

Reaction	System	ΔE	ΔE_{ZPE}	ΔH	ΔG
3	R_1+R_2	0.00	0.00	0.00	0.00
	TS	-3.02	-1.34	-1.84	13.11
	P_1+P_2	-57.34	-56.36	-56.42	-59.90
4	R_1+R_2	0.00	0.00	0.00	0.00
	TS	-2.73	-1.29	-1.70	12.79
	P_1+P_2	-58.68	-58.25	-58.64	-61.69
5	R_1+R_2	0.00	0.00	0.00	0.00
	TS	-3.15	-1.63	-2.04	13.50
	P_1+P_2	-57.58	-56.96	-56.84	-60.58
6	R_1+R_2	0.00	0.00	0.00	0.00
	TS	-1.15	0.64	0.23	14.19
	$\mathbf{P}_1 + \mathbf{P}_2$	-57.61	-56.68	-56.66	-60.48

Supplementary Table 8. Geometric Parameters of Species in Cyclopropanation Pathways of Different Axial Ligands

Reaction	System	R _{FeC1} (Å)	R _{C1C2} (Å)	R _{C1C3} (Å)	R _{C2C3} (Å)	R _{FeL} (Å)	∠ _{HC1Y} (°)
3	R ₁	1.755	/	/	/	2.122	113.3
	TS	1.898	2.250	2.546	1.345	2.060	110.7
	P ₁	/	/	/	/	2.173	/
4	\mathbf{R}_{1}	1.745	/	/	/	2.196	113.5
	TS	1.894	2.235	2.529	1.346	2.119	110.5
	P ₁	/	/	/	/	2.204	/

5	\mathbf{R}_{1}	1.749	/	/	/	2.167	113.4
	TS	1.896	2.244	2.541	1.345	2.090	110.6
	P 1	/	/	/	/	2.213	/
6	\mathbf{R}_{1}	1.749	/	/	/	2.191	113.4
	TS	1.902	2.232	2.536	1.346	2.143	110.1
	P ₁	/	/	/	/	2.220	/

Supplementary Table 9. Atomic Charge of Species in Cyclopropanation Pathways of Different Axial Ligands (unit: *e*)

Reaction S	System	Q _{Fe}	Q _{C1}	Q _H	Qy	Q _{C2}	Q _{C3}	Q _{R'}	Q _{Cycle} ^{a)}	$Q_{\rm L}$
3	\mathbf{R}_1	0.089	0.087	0.193	-0.032	/	/	/	-0.583	0.246
	TS	0.168	-0.100	0.201	-0.037	-0.264	-0.266	0.689	-0.670	0.278
	P ₁	1.121	/	/	/	/	/	/	-1.278	0.157
4	\mathbf{R}_1	0.089	0.093	0.194	-0.027	/	/	/	-0.572	0.222
	TS	0.168	-0.099	0.202	-0.822	-0.265	-0.260	0.693	-0.666	0.259
	P ₁	1.116	/	/	/	/	/	/	-1.271	0.155
5	\mathbf{R}_1	0.097	0.097	0.194	-0.026	/	/	/	-0.577	0.214
	TS	0.172	-0.096	0.203	-0.033	-0.266	-0.259	0.694	-0.664	0.248
	P ₁	1.105	/	/	/	/	/	/	-1.250	0.145
6	\mathbf{R}_1	0.097	0.093	0.194	-0.026	/	/	/	-0.570	0.212
	TS	0.198	-0.100	0.202	-0.034	-0.270	-0.252	0.698	-0.677	0.234
	P ₁	1.068	/	/	/	/	/	/	-1.211	0.143

^{a)} Cycle is the macrocycle without substituent(s).

Supplementary Note 4. Effects of experimentally studied macrocycle (reactions 7-9)

Reaction	System	Е	Ezpe	Н	G
7	R ₁	-2270.90693	-2270.04962	-2269.99618	-2270.13731
	TS	-2580.52202	-2579.52664	-2579.46691	-2579.61982
	P ₁	-1964.50736	-1963.75040	-1963.70362	-1963.83230
	P ₂	-616.08626	-615.84955	-615.83570	-615.89052
8	\mathbf{R}_1	-2273.34679	-2272.44158	-2272.38776	-2272.52691
	TS	-2582.96233	-2581.91970	-2581.85897	-2582.01367
	P ₁	-1966.94695	-1966.13920	-1966.09203	-1966.21919
9	\mathbf{R}_1	-2273.33680	-2272.43202	-2272.37764	-2272.52019
	TS	-2582.95731	-2581.91385	-2581.85338	-2582.00765
	P ₁	-1966.93561	-1966.12982	-1966.08253	-1966.21136

Supplementary Table 10. Absolute Energies of Species in Pathways of Reactions 7-9 (unit: *Hartrees*)

Supplementary Table 11. Relative Energies of Species in Pathways of of Reactions **7-9** (unit: *kcal mol*⁻¹)

Reaction	System	ΔΕ	ΔE_{ZPE}	ΔH	ΔG
7	R ₁ +R ₂	0.00	0.00	0.00	0.00
	TS	-10.62	-8.28	-9.16	8.41
	P_1+P_2	-55.55	-54.28	-54.60	-56.23
8	R_1+R_2	0.00	0.00	0.00	0.00
	TS	-10.90	-8.97	-9.46	5.75
	P_1+P_2	-55.38	-52.30	-52.60	-54.52
9	R_1+R_2	0.00	0.00	0.00	0.00
	TS	-14.02	-11.30	-12.31	5.31
	P_1+P_2	-53.71	-51.71	-52.26	-53.15

Supplementary Table 12. Geometric Parameters of Species in Pathways of Reactions 7-9

Reaction	System	R_{FeC1}	R_{C1C2}	R _{C1C3}	Rc2c3	R_{FeL}	$\angle_{\rm HC1Y}$
Reaction	System	(Å)	(Å)	(Å)	(Å)	(Å)	(°)
7	\mathbf{R}_1	1.759	/	/	/	2.111	113.0
	TS	1.862	2.358	2.636	1.345	2.092	110.3
	P 1	/	/	/	/	2.182	/
	P ₂	/	1.509	1.523	1.495	/	115.5
8	\mathbf{R}_1	1.753	/	/	/	2.132	113.8
	TS	1.857	2.360	2.664	1.345	2.089	110.1
	P ₁	/	/	/	/	2.190	/
9	\mathbf{R}_1	1.750	/	/	/	2.139	113.5
	TS	1.866	2.330	2.639	1.346	2.075	112.1
	P ₁	/	/	/	/	2.199	/

			0			5			
Reaction System	Q_{Fe}	Q _{C1}	Q_{H}	Qy	Q _{C2}	Q _{C3}	$Q_{R'}$	Q _{Cycle}	QL
7 R ₁	0.095	0.083	0.192	-0.032	/	/	/	-0.588	0.251
TS	0.152	-0.061	0.201	-0.044	-0.328	-0.153	0.659	-0.684	0.259
P ₁	1.120	/	/	/	/	/	/	-1.273	0.153
P ₂	/	-0.320	0.233	-0.003	-0.350	-0.208	0.647	/	/
8 R ₁	0.107	0.077	0.192	-0.035	/	/	/	-0.583	0.242
TS	0.163	-0.061	0.201	-0.043	-0.344	-0.154	0.660	-0.682	0.259
P ₁	1.138	/	/	/	/	/	/	-1.283	0.146
9 R ₁	0.044	0.075	0.190	-0.039	/	/	/	-0.517	0.246
TS	0.101	-0.064	0.203	-0.059	-0.332	-0.147	0.661	-0.636	0.274
P ₁	1.119	/	/	/	/	/	/	-1.268	0.149

Supplementary Table 13. Atomic Charge of Species in Pathways of Reactions 7-9 (unit: *e*)



Supplementary Figure 1. Atomic charge changes from reactants to transition state (in black) and charge transfers (in blue) in reactions 7-9. a) reaction 7, b) reaction 8, and c) reaction 9.

Supplementary Note 5. Effects of macrocycles not being experimentally studied yet (reactions 10-13)

Reaction	System	E	E_{ZPE}	Н	G
10	R ₁	-1684.89448	-1684.39316	-1684.36072	-1684.45464
	TS	-2030.65936	-2030.03149	-2029.99067	-2030.10492
	P ₁	-1378.49910	-1378.09852	-1378.07226	-1378.15759
11	R ₁	-1683.65514	-1683.17799	-1683.14602	-1683.23970
	TS	-2029.41472	-2028.81013	-2028.77010	-2028.88191
	P ₁	-1377.24857	-1376.87204	-1376.84644	-1376.92913
12	R ₁	-2362.38104	-2361.76068	-2361.71871	-2361.83434
	TS	-2708.14448	-2707.39671	-2707.34663	-2707.48005
	P ₁	-2055.96607	-2055.44685	-2055.41140	-2055.51631
13	\mathbf{R}_1	-2052.60782	-2052.13545	-2052.09615	-2052.20666
	TS	-2398.37381	-2397.77492	-2397.72706	-2397.85726
	P ₁	-1746.20884	-1745.83714	-1745.80435	-1745.90246

Supplementary Table 14. Absolute Energies of Species in Pathways of Reactions **10-13** (unit: *Hartrees*)

Supplementary Table 15. Relative Energies of Species in Pathways of Reactions **10-13** (unit: $kcal mol^{-1}$)

Reaction	System	ΔΕ	ΔE_{ZPE}	ΔH	ΔG
10	R_1+R_2	0.00	0.00	0.00	0.00
	TS	-4.71	-3.54	-3.80	9.46
	$\mathbf{P}_1 + \mathbf{P}_2$	-59.50	-58.53	-58.40	-63.79
11	R_1+R_2	0.00	0.00	0.00	0.00
	TS	-1.38	0.35	-0.11	14.53
	P_1+P_2	-52.48	-51.42	-51.43	-55.31
12	R_1+R_2	0.00	0.00	0.00	0.00
	TS	-3.80	-2.09	-2.53	12.33
	P_1+P_2	-47.21	-46.48	-46.57	-50.63
13	R_1+R_2	0.00	0.00	0.00	0.00
	TS	-5.40	-4.24	-4.40	9.26
	P_1+P_2	-57.24	-56.22	-56.30	-59.30

Supplementary Table 16. Geometric Parameters of Species i	n Pathways for Reactions 10-13
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Reaction	System	R _{FeC1} (Å)	R _{C1C2} (Å)	R _{C1C3} (Å)	R _{C2C3} (Å)	R _{FeL} (Å)	∠ _{HC1Y} (°)
10	R ₁	1.757	/	/	/	2.116	113.4
	TS	1.895	2.256	2.510	1.346	2.056	110.3
	P ₁	/	/	/	/	2.173	/
11	\mathbf{R}_1	1.754	/	/	/	2.114	113.6
	TS	1.898	2.208	2.522	1.347	2.064	111.0
	\mathbf{P}_1	/	/	/	/	2.151	/

12	\mathbf{R}_{1}	1.764	/	/	/	2.136	113.1
	TS	1.901	2.305	2.524	1.343	2.075	110.7
	P ₁	/	/	/	/	2.146	/
13	R ₁	1.771	/	/	/	2.094	113.1
	TS	1.893	2.356	2.572	1.341	2.056	110.7
	P ₁	/	/	/	/	2.149	/

Supplementary Table 17. Atomic Charge of Species in Pathways for Reactions 10-13 (unit: e)

Reaction	System	Q_{Fe}	Q _{C1}	Q_{H}	Qy	Q _{C2}	Q _{C3}	$Q_{R'}$	Q _{Cycle}	Q_L
10	R ₁	0.100	0.085	0.190	-0.031	/	/	/	-0.592	0.248
	TS	0.174	-0.103	0.200	-0.033	-0.255	-0.272	0.690	-0.679	0.278
	P ₁	1.124	/	/	/	/	/	/	-1.280	0.155
11	\mathbf{R}_1	0.029	0.090	0.192	-0.036	/	/	/	-0.534	0.259
	TS	0.113	-0.105	0.203	-0.038	-0.269	-0.254	0.692	-0.629	0.287
	P ₁	1.104	/	/	/	/	/	/	-1.270	0.166
12	\mathbf{R}_1	-0.002	0.109	0.197	-0.013	/	/	/	-0.550	0.259
	TS	0.058	-0.067	0.202	-0.023	-0.262	-0.250	0.701	-0.649	0.290
	P ₁	1.093	/	/	/	/	/	/	-1.269	0.176
13	\mathbf{R}_1	0.083	0.106	0.199	-0.008	/	/	/	-0.647	0.268
	TS	0.150	-0.063	0.202	-0.019	-0.264	-0.256	0.694	-0.733	0.289
	P ₁	1.141	/	/	/	/	/	/	-1.311	0.170



Supplementary Figure 2. Atomic charge changes from reactants to transition state (in black) and charge transfers (in blue) in reactions 10-13. a) reaction 10, b) reaction 11, c) reaction 12, and d) reaction 13.

Supplementary Note 6. Imaginary frequencies of transition states

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TS	Frequency	TS	Frequency
1	-218	8	-198
2	-191	9	-242
3	-296	10	-296
4	-310	11	-328
5	-299	12	-260
6	-310	13	-215
7	-211		

Supplementary Table 18. Imaginary Frequencies of all **TS**s (unit: *cm*⁻¹)

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