

Supplementary Information 4

• TOPSIS Analysis Method

For evaluating all the solution sets according to the economic criteria (i.e., IT), we use the TOPSIS (Technique for Order Preference by Similarity to Ideal Solution) method.

By exploiting a weighted decision matrix in which M alternatives are evaluated in terms of N weighted criteria it's possible to identify an ideal best-case solution and an ideal worst-case solution; the alternatives are then ranked according to the Euclidean distance from the ideal and non-ideal solutions.

The weighted decision matrix (C) is composed by a total of 255 possible alternatives M ($M = 1, \dots, 255$; i.e., all the UHI-mitigation individual solutions and solution sets) and the IT criteria N ($N = 1, 2$). Both the weight of the criteria (W_N) and the weight of alternatives (W_{MN}) are obtained from the AHP analysis.

$$C = \begin{pmatrix} W_1 W_{1,1} & W_2 W_{1,2} & \dots & W_N W_{1,N} \\ W_1 W_{2,1} & W_2 W_{2,2} & \dots & W_N W_{2,N} \\ W_1 W_{3,1} & W_2 W_{3,2} & \dots & W_N W_{3,N} \\ W_1 W_{4,1} & W_2 W_{4,2} & \dots & W_N W_{4,N} \\ W_1 W_{5,1} & W_2 W_{5,2} & \dots & W_N W_{5,N} \\ \dots & \dots & \dots & \dots \\ W_1 W_{M,1} & W_2 W_{M,2} & \dots & W_N W_{M,N} \end{pmatrix} \quad (10)$$

For simplicity's sake the elements of the weighted decision matrix C (i.e., $W_N W_{MN}$) will be referred as v_{MN} with N being the N^{th} criterion and M being the M^{th} alternative.

Subsequently, the ideal best-case alternative M^* is defined as an alternative which contains the highest values of the criteria considered good for the objective (N^+), and the lowest value of the criteria considered bad for the objective (N^-) (Eq 11). In our case the ideal solution would possess the highest value for time (time is structured in the polls to be a positive criterion since experts are asked to choose the solution that require the less amount of time), and the lowest value for investment.

$$M^* = \{(\max v_{MN^+} | N^+ \in N), (\min v_{MN^-} | N^- \in N) | M = 1, 2, \dots, 256\} \quad (11)$$

$$M^* = \{v_{1^*}; v_{2^*}\}$$

Similarly, the ideal worst-case alternative M^- is defined as an alternative which contains the lowest values of the criteria considered good for the objective (N^+), and the highest value of the criteria considered bad for the objective (N^-) (Eq 12). In our case the ideal solution would possess the lowest value for time, and the highest value for investment.

$$M^- = \{(\max v_{MN^-} | N^- \in N), (\min v_{MN^+} | N^+ \in N) | M = 1, 2, \dots, 256\} \quad (12)$$

$$M^- = \{v_{1^-}; v_{2^-}\}$$

Once obtained M^* and M^- , we calculate the Euclidean distance to measure the distance of each solution from both the ideal best-case solution (d_{M^*}) and worst-case solution (d_{M^-}) (Eq 13-14)

$$d_{M^*} = \sqrt{\sum_{i=1}^N (v_{Nj} - v_{j^*})^2} \quad (13)$$

$$d_{M^-} = \sqrt{\sum_{i=1}^N (v_{Nj} - v_{j^-})^2} \quad (14)$$

Then it's possible to calculate the relative closeness of the M alternative to the ideal best-case solution (C_{M^*}) (Eq 15)

$$C_{M^*} = \frac{d_{M^-}}{d_{M^*}d_{M^-}} \quad (15)$$

The relative closeness can vary between zero and one. C_{M^*} equals zero if the alternative corresponds to the worst-case solution, while C_{M^*} equals one if the alternative corresponds to the ideal best-case alternative. All the 255 alternatives are ranked according to the value of C_{M^*} .