

Revisiting the Oldest Stars as Cosmological Probes: New Constraints on the Hubble Constant

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Abstract

Despite the tremendous advance of observational cosmology, the value of the Hubble constant (H_0) is still controversial (the so-called "Hubble tension") because of the inconsistency between local/late-time measurements and those derived from the cosmic microwave background. As the age of the Universe is very sensitive to H_0 , we explored whether the present-day oldest stars could place independent constraints on the Hubble constant. To this purpose, we selected from the literature the oldest objects (globular clusters, stars, white dwarfs, and ultrafaint and dwarf spheroidal galaxies) with accurate age estimates. Adopting a conservative prior on their formation redshifts ($11 \le z_f \le 30$) and assuming $\Omega_M = 0.3 \pm 0.02$, we developed a method based on Bayesian statistics to estimate the Hubble constant. We selected the oldest objects (>13.3 Gyr) and estimated H_0 both for each of them individually and for the average ages of homogeneous subsamples. Statistical and systematic uncertainties were properly taken into account. The constraints based on individual ages indicate that $H_0 < 70.6 \text{ km s}^{-1} \text{ Mpc}^{-1}$ when selecting the most accurate estimates. If the ages are averaged and analyzed independently for each subsample, the most stringent constraints imply $H_0 < 73.0 \text{ km s}^{-1} \text{ Mpc}^{-1}$ with a probability of 90.3% and errors around 2.5 km s⁻¹ Mpc⁻¹. We also constructed an "accuracy matrix" to assess how the constraints on H_0 become more stringent with further improvements in the accuracy of stellar ages and Ω_M . The results show the great potential of the oldest stars as independent and competitive cosmological probes not limited to just the Hubble constant.

Unified Astronomy Thesaurus concepts: Cosmology (343); Observational cosmology (1146); Cosmological parameters (339); Hubble constant (758); Stellar ages (1581)

1. Introduction

Our understanding of the Universe improved dramatically during the last century. However, in spite of the high precision achieved in observational cosmology, several fundamental questions remain open. For instance, the nature and origin of dark matter and dark energy are still unknown despite their major contribution to the total cosmic budget of matter and energy (Planck Collaboration et al. 2020). Another key question regards the present-day expansion rate (the Hubble constant, H_0), for which independent methods give inconsistent results, e.g., 67.4 ± 0.5 km s⁻¹ Mpc⁻¹ (Planck Collaboration et al. 2020, hereafter Planck2020) and 73.04 ± 1.04 km s⁻¹ Mpc⁻¹ (Riess et al. 2022, hereafter SH0ES), leading to the so-called "Hubble tension" (Verde et al. 2019; Abdalla et al. 2022; Kamionkowski & Riess 2022). Today, it is unknown whether the H_0 discrepancy is a signal of "new physics" or the result of unaccounted systematic effects. Thus, before venturing into the uncharted territory of new physics, it is essential to combine as many cosmological probes as possible in order to mitigate the unavoidable systematic uncertainties inherent to each of them (for a review, see Moresco et al. 2022). In this regard, stellar ages play a key role simply because the current age of the Universe today cannot be less than the age of the present-day oldest stars. Historically, the ages of the oldest globular

Original content from this work may be used under the terms of the Creative Commons Attribution 4.0 licence. Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI. clusters appeared inconsistent with the mostly younger ages of the Universe allowed by the cosmological models in the 1980s and early 1990s (Jimenez et al. 1996; Krauss & Chaboyer 2003, and references therein). This age crisis was rapidly solved with the discovery of the accelerated expansion, which implied an older Universe. More recently, stellar ages have been reconsidered as promising probes independent of the cosmological models (Bond et al. 2013; Jimenez et al. 2019; Valcin et al. 2020, 2021; Boylan-Kolchin & Weisz 2021; Vagnozzi et al. 2022; Weisz et al. 2023a). As a matter of fact, age dating is based either on stellar physics and evolution (isochrone fitting) or on the abundance of radioactive elements (nucleochronometry) (Soderblom 2010). The downside is that stellar ages are still affected by substantial systematic uncertainties (e.g., Chaboyer et al. 1995; Soderblom 2010; Valcin et al. 2021; Joyce et al. 2023). In particular, isochrone fitting relies on the assumption of a given theoretical stellar model and requires accurate estimates of metal abundance, absolute distance, and dust reddening along the line of sight. Thus, although the age precision can be very high for a given set of assumptions (i.e., statistical errors can be very small), high accuracy is usually prevented by systematic errors. In nucleochronometry, an additional difficulty is the accurate derivation of the abundances of elements (e.g., U, Th) characterized by very weak, and often blended, absorption lines (e.g., Christlieb 2016).

The main aim of this paper is to revive and investigate the potential of the oldest stars as independent clocks to place new constraints on the Hubble constant.

2. Method

In a generic cosmological model, the Hubble constant H_0 can be derived as

$$H_0 = \frac{A}{t} \int_0^{z_f} \frac{1}{(1+z')E(z')} dz' \tag{1}$$

where $E(z) = H(z)/H_0$, *t* is the age of an object formed at redshift z_f , and A = 977.8 allows one to convert from Gyr (units of *t*) to km s⁻¹ Mpc⁻¹ (units of H_0). For $z_f = \infty$, the age *t* converges to the age of the Universe t_U . In a flat Λ CDM universe, Equation (1) reduces to

$$H_0 = \frac{A}{t} \int_0^{z_f} \frac{1}{1+z'} [\Omega_M (1+z')^3 + (1-\Omega_M)]^{-1/2} dz'.$$
(2)

Based on Equation (2), it is therefore possible to estimate H_0 provided that Ω_M , z_f , and stellar ages are known. The sensitivity of this method is described in Section 5.

3. The Oldest Stars in the Present-day Universe

The age of the Universe (t_U at z = 0) is very sensitive to H_0 . For instance, for $\Omega_M = 0.3$ and $\Omega_{\Lambda} = 0.7$, the age of the Universe is $t_U \sim 14.1$ Gyr and $t_U \sim 12.9$ Gyr for $H_0 = 67$ km s⁻¹ Mpc⁻¹ and $H_0 = 73$ km s⁻¹ Mpc⁻¹, respectively. From this example, it is clear that only the *oldest* stars play a discriminant role in the context of the Hubble tension. With this motivation, we searched the literature for the oldest stars in the Milky Way and in the Local Group with estimates of ages based on different methods and with a careful evaluation of systematic errors.

- 1. Galactic globular clusters (GCs). For our purpose, we focused on the most recent results of O'Malley et al. (2017), Brown et al. (2018), Oliveira et al. (2020), and Valcin et al. (2020) with state-of-art age dating and a careful assessment of the statistical and systematic uncertainties. The oldest GCs have ages $\gtrsim 13.5$ Gyr with total errors (i.e., combined statistical and systematic) from ~ 0.5 Gyr to $\gtrsim 1$ Gyr. In particular, in the case of O'Malley et al. (2017) we used the weighted ages based on the most accurate parallaxes available (i.e., the combined ages in their Table 5). Finally, we also added the recent estimate of the absolute age of the globular cluster M92 by Ying et al. (2023) $(13.80 \pm 0.75 \text{ Gyr})$ where a careful analysis of the error budget is also presented. It is important to emphasize that these different works span a variety of statistical methods (Bayesian, Monte Carlo), stellar models (BaSTI, Dotter et al. 2008; VandenBerg et al. 2014), ranges of fitted parameters (age, [Fe/H], $[\alpha/Fe]$, distance, reddening), sometimes exploiting Gaia parallaxes.
- 2. Galactic individual stars. Very old individual stars are reported in the literature. For instance, Schlaufman et al. (2018) estimated an age of 13.5 Gyr (with a systematic error $\gtrsim 1$ Gyr) for an ultra-metal-poor star belonging to a binary system. For HD 140283, an extremely metal-poor star in the solar neighborhood, an age of 14.5 ± 0.8 Gyr (including systematic uncertainties) was derived by Bond et al. (2013), although recent results suggest younger ages (Plotnikova et al. 2022). Recent works (based on Gaia parallaxes, sometimes with asteroseismology measurements and without adopting priors on the age of the

Universe) found evidence of stars with ages \gtrsim 13.5 Gyr (e.g., Montalbán et al. 2021; Plotnikova et al. 2022; Xiang & Rix 2022). Regarding the data from Plotnikova et al. (2022), we used the ages estimated with BaSTI isochrones because they provide a larger data set.

- 3. White dwarfs (WDs). If the distance, magnitude, color, and atmospheric type for a WD are known, its age can be derived based on the well-understood WD cooling curves and initial-final mass relations calibrated using star clusters. Fouesneau et al. (2019) exploited the Gaia parallaxes and reported ages as old as 13.9 ± 0.8 Gyr. The potential of WDs as chronometers has recently been highlighted by Moss et al. (2022).
- 4. Nucleochronometry (NC). The relative abundances of nuclides with half-lives of several gigayears (e.g., U, Th, Eu) can be exploited as chronometers (Christlieb 2016; Shah et al. 2023). However, the application of nucleo-chronometry requires reliable theoretical modeling of the rapid neutron capture (*r*-process) nucleosynthesis and spectroscopy with very high resolution and signal-to-noise ratio. To date, this method has been applied only to a few stars, whose ages turned out to be as old as ≈ 14 Gyr, but with large errors of 2–4 Gyr. However, Wu et al. (2022) suggested that the uncertainties could be reduced to ~0.3 Gyr through the synchronization of different chronometers.
- 5. Ultrafaint galaxies (UFDs) and dwarf spheroidals (dSph). UFDs in the Local Group have old stellar populations and may be the fossil remnants of systems formed in the reionization era. Brown et al. (2014) found that the oldest stars have ages in the range 13.7–14.1 Gyr, with systematic uncertainties of ~1 Gyr. Moreover, based on the reconstruction of their star formation histories, some dSph systems of the Local Group formed the bulk of their stars at z > 14, therefore implying ages >13.5 Gyr in the standard Λ CDM cosmology (e.g., Weisz et al. 2014; Simon et al. 2023).

The oldest ages selected for our work are based on a variety of astrophysical objects, methods, and independent studies, and show unambiguously that the most ancient stars in the presentday Universe are significantly older than 13 Gyr, but with uncertainties (dominated by systematic errors) from ~ 0.5 to $\gtrsim 1$ Gyr.

Can such old ages place meaningful cosmological constraints? We recall the obvious point that the age of an object at z=0 provides only a lower limit to the current age of the Universe because it remains unknown how much time it took for that object to form since the Big Bang:

$$t_{\rm U} = \Delta t_{\rm f} + t_{\rm age} \tag{3}$$

where t_U is the age of the Universe and Δt_f is the time interval between the Big Bang and the formation of an object observed at z = 0 with an age t_{age} . Thus, if we measure t_{age} for an object at z = 0, the main unknown remains only Δt_f . In our work, we exploited the oldest stars at z = 0 to maximize t_{age} and minimize the relevance of Δt_f with respect to the current age of the Universe. To this purpose, we decided to anchor Δt_f to the redshifts ($z \sim 11-13$) of the most distant galaxies known based on spectroscopic identification (Curtis-Lake et al. 2023), although photometric candidates exist up to $z \approx 18$ (Naidu et al. 2022). Our choice is also indirectly supported by the recent discovery of high-redshift quiescent galaxies whose star formation histories require that their first stars formed at z > 11 (see, e.g., Carnall et al. 2023). The uppermost redshift limit can be set by theoretical models that indicate 20 < z < 30as the range for the formation of the very first stars (Galli & Palla 2013). Thus, for our analysis (Section 2), we adopted $11 < z_f < 30$ as a baseline. This corresponds to $\Delta t_f \approx 0.1$ – 0.4 Gyr after the Big Bang ($H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_M = 0.3$, $\Omega_{\Lambda} = 0.7$). We remark that this choice is the most conservative possible for the Hubble tension: should the oldest stars have formed at z < 11, their ages would imply an even older Universe and, in turn, a lower value of H_0 .

4. Constraining the Hubble Constant

For our analysis, we developed a code based on a Bayesian framework, with a log-likelihood defined as

$$\mathcal{L}(\text{age}, \mathbf{p}) = -0.5 \sum_{i} \frac{(\text{age}_{i} - age_{m}(\mathbf{p}))^{2}}{\sigma(\text{age}_{i})}$$
(4)

where age_i and $\sigma(age_i)$ are the age and its error, age_m is the theoretical age from the model in Equation (2), and **p** are the parameters of the model. We adopted a flat Λ CDM cosmological model where the free parameters are H_0 , Ω_M , and z_f . We sampled the posterior with a Monte Carlo Markov Chain approach using the affine-invariant ensemble sampler implemented in the public code emcee (Foreman-Mackey et al. 2013).

While we decided to adopt flat priors on $H_0 = [50, 100]$ km s⁻¹ Mpc⁻¹ and $z_f = [11–30]$, we chose to include a Gaussian prior on Ω_M because, as can be inferred from Equation (2), there is a significant intrinsic degeneracy between the derived value of H_0 and Ω_M that is hard to break from age data alone. Most importantly, in the framework of the current Hubble tension (see, e.g., Verde et al. 2019), we kept our analysis free from priors that depend on the cosmic microwave background (CMB) by adopting $\Omega_M = 0.3 \pm 0.02$ obtained from the combination of several low-redshift results (Jimenez et al. 2019), and consistent with the latest BOSS+eBOSS clustering analysis ($\Omega_M = 0.29^{+0.012}_{-0.014}$) of Semenaite et al. (2022). In our analysis, we adopted 250 walkers and 1000 iterations each, discarding the first 300 points of the chain to exclude burn-in effects.

5. Sensitivity to the Choice of Priors

We first explored the sensitivity of the method by fitting a theoretical grid of parameters, spanning different values of ages and errors, and assessing the impact of changing the priors of z_f or Ω_M on H_0 . To this purpose, we defined a reference case with age = 13.5 ± 0.5 Gyr, a flat prior $z_f = [11-30]$, and a Gaussian prior $\Omega_M = 0.3 \pm 0.02$.

We then perturbed the reference case by changing, each time, one of the assumed values or priors within the ranges indicated in Table 1. The results for the reference case are shown in Figure 1.

The general findings can be summarized as follows.

1. As expected, the estimated value of H_0 decreases linearly with increasing age, varying from 69 to 65 km s⁻¹ Mpc⁻¹ for ages from 13.5 to 14.5 Gyr (for the fixed priors in Table 1). We note that to obtain a Hubble constant >73 km s⁻¹ Mpc⁻¹, the oldest stars in the Universe should be at most 12.75 Gyr old for the assumed priors on

 Table 1

 Range of Parameters and Priors Explored to Assess the Sensitivity of the Method

Parameter	Values and Priors
Age (Gyr)	12.5, 13, 13.5 , 14
$\sigma(age)$ (Gyr)	0.1, 0.2, 0.5 , 1, 1.5, 2
Z_f	[11–30], [15–30] , [20–30]
Ω_M	0.3 ± 0.02 , 0.27 ± 0.06 (Verde et al. 2002),
	0.341 ± 0.045 (Gil-Marín et al. 2017)

Note. The reference case discussed in the text is indicated in bold.

 Ω_M , or, alternatively, the matter density parameter should be $\Omega_M < 0.25$ for an age of ~13.5 Gyr.

- 2. The uncertainty on the Hubble constant scales almost linearly with the uncertainty on the age. For $\sigma_{\text{age}} \lesssim 0.5 \text{ Gyr}$, the probability distribution function (PDF) of H_0 (Figure 1, right panel, red curve) is Gaussian. However, the PDF becomes asymmetric for $\sigma_{\text{age}} \gtrsim 1 \text{ Gyr}$ with tails that bias the estimate of H_0 toward larger values (Figure 1, right panel, blue curve).
- 3. The H_0 - Ω_M degeneracy plays an important role. For the three cases of Ω_M shown in Table 1, the resulting values of H_0 are 71.32^{+5.8}_{-4.76}, 69.06^{+2.96}_{-2.77}, and 66.6^{+2.64}_{-2.42} km s⁻¹ Mpc⁻¹ for $\Omega_M = 0.27 \pm 0.06$, 0.30 ± 0.02 , and 0.34 ± 0.045 . The uncertainty on H_0 would decrease to ± 2.5 km s⁻¹ Mpc⁻¹ assuming the Planck2020 value ($\Omega_M = 0.315 \pm 0.007$). The systematic uncertainty due to the range of Ω_M priors in Table 1 is σ_{syst} , $\Omega_M = 2.36$ km s⁻¹ Mpc⁻¹.
- 4. The prior on z_f plays a minor role. For the ranges of z_f in Table 1, the systematic uncertainty is only $\sigma_{\text{syst, } z_f} = 0.25 \text{ km s}^{-1} \text{ Mpc}^{-1}$. As a further example, adopting $6 < z_f < 11$, age = 13.5 ± 0.5 Gyr, and $\Omega_M = 0.30 \pm 0.02$, H_0 would decrease to $66.97^{+2.94}_{-2.76}$ compared to $69.09^{+2.96}_{-2.75}$ km s⁻¹ Mpc⁻¹ for the case with $11 < z_f < 30$.

Based on this analysis, the total systematic error associated with the prior assumptions is $\sigma_{\text{syst, prior}}(H_0) = \sqrt{\sigma_{\text{syst, }z_f}^2 + \sigma_{\text{syst, }\Omega_M}^2} = 2.37 \text{ km s}^{-1} \text{ Mpc}^{-1}$. However, this is a conservative additional systematic error because the range of our priors already covers a parameter space well constrained by observations (see Section 3).

6. From the Oldest Ages to H_0

The method described in Section 4 was then applied to the observed data. In particular, we followed two different approaches.

6.1. Individual Ages

As a first step, we analyzed the individual age estimates of each object presented in Section 3, considering an age threshold >13.3 Gyr to select the oldest objects. This value has been chosen to select at least one object for each sample, in order to preserve the variety of age-dating results obtained with different methods and samples, therefore mitigating the possible biases. In the context of the Hubble tension, this is a conservative choice because an older age threshold would have provided lower H_0 values. We verified that our main results are robust and do not significantly depend on this assumption, as discussed in more detail in Section 6.3. Based on this approach, 39 objects older than 13.3 Gyr were selected, and the Hubble

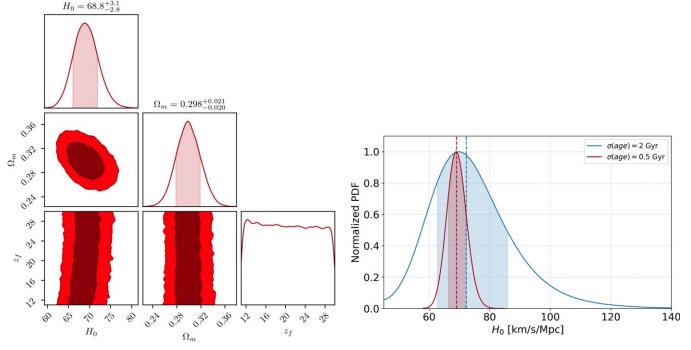


Figure 1. Left panel: constraints on H_0 for the reference case with an age of 13.5 ± 0.5 Gyr, a flat prior of $z_f = [11-30]$, and a Gaussian prior on $\Omega_M = 0.3 \pm 0.02$. The results have a very weak dependence on z_f (showing a flat distribution), as also confirmed from the analysis in Section 5. Right panel: the effects of different age errors on the H_0 estimate. The two curves show the normalized PDF for the reference case, but with two different age errors as indicated in the label; the shaded area represents the 1σ confidence level. For increasingly large errors on the age, the PDF becomes progressively more asymmetric, biasing the estimate of H_0 toward high values, as indicated by the median of the distributions (vertical dashed lines).

constant H_0 was estimated for each of them. Figure 2 shows that $H_0 \leq 72 \text{ km s}^{-1} \text{ Mpc}^{-1}$ for the majority of our data, with values typically in the range $63 < H_0 \text{ [km s}^{-1} \text{ Mpc}^{-1} \text{]} < 72$. By inspecting the posteriors, the highest values of H_0 are due to the largest uncertainties on the ages and the consequent asymmetric PDF (Figure 1). The cases with $\sigma_{H_0}/H_0 > 30\%$ have a mean age error $\sigma_{age} = 4$ Gyr, noticeably larger than the average of the entire sample ($\sigma_{age} = 1.4$ Gyr). Instead, for the cases with $\sigma_{H_0}/H_0 < 30\%$, <20%, and <10%, the highest values of H_0 are 74.4, 71.9, and 70.6 km s⁻¹ Mpc⁻¹, respectively (see the histogram in Figure 2).

We also tested how H_0 can be constrained with the individual very oldest globular clusters with the smallest age errors. For NGC 6362 (13.6 ± 0.5 Gyr) (Oliveira et al. 2020) and NGC 6779 (14.9^{+0.5}_{-0.9} Gyr) (Valcin et al. 2020), we obtain $68.5^{+2.9}_{-3.2}$ and $63.1^{+3.9}_{-4.5}$ km s⁻¹ Mpc⁻¹, respectively. Taken at face value, this exercise highlights the importance of the oldest objects in the context of the Hubble tension. However, these two individual cases are clearly insufficient to place meaningful constraints. For this reason, we also follow another approach based on the average ages (see the next subsection).

6.2. Average Ages

In order to minimize the potential bias induced by the larger age errors and to obtain more stringent constraints on H_0 , we refined our analysis by averaging the age estimates (always keeping the oldest objects with ages >13.3 Gyr and separating the statistical and systematic contributions to the total error). Since each sample is characterized by its own systematic uncertainties, we decided not to average all data into a single age estimate. Therefore, for each of the 11 different samples reported in Section 3, we estimated a mean age with an inverse-variance weighted average, adding a posteriori in quadrature the

systematic error of each method as discussed in the corresponding paper, so as not to artificially reduce it with the averaging procedure. We analyzed these data with the procedure described in Section 2, and the results are reported in Table 2. We underline here that, wherever possible, we adopted the systematic errors reported in the original papers. However, in the cases where the contribution to the error budget due to systematic uncertainties was not explicitly and quantitatively reported (e.g., Christlieb 2016; O'Malley et al. 2017), we adopted a conservative approach, considering the systematic error to be the dominant contribution in the total error budget and taking as a reference the smallest total error (where most of the error should be driven by the systematic contribution). For instance, in the case of O'Malley et al. (2017), where the most accurate ages have total errors (statistical plus systematic) of ± 1.3 Gyr, we adopted a systematic error of ± 1 Gyr. For Christlieb (2016), we assumed ± 2 Gyr as the systematic uncertainty. We found that $63.5 < H_0$ [km s⁻¹ Mpc⁻¹] < 70.9, with errors around 2.8 km s⁻¹ Mpc⁻¹ in the best case and around 14.1 km s⁻¹ Mpc⁻¹ in the worst. If the systematic errors due to the choice of our priors (see Section 5) are also added, the total uncertainties increase slightly to 3.7 and 14.3 km s⁻¹ Mpc⁻¹, respectively.

The results are presented in the framework of the Hubble tension and show, for each subsample, the average probability (weighted with the sample size) of each H_0 to be larger than the Planck value (Planck Collaboration et al. 2020) or smaller than the SH0ES one (Riess et al. 2022).

The results indicate an average probability of 90.3% for the Hubble constant to be $H_0 < 73.0 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (weighted on the number of data points in each sample), with a minimum value of 56% and a maximum value of 99.9%. Instead, the average probability to have $H_0 > 67.4 \text{ km s}^{-1} \text{ Mpc}^{-1}$ is 35.7%,

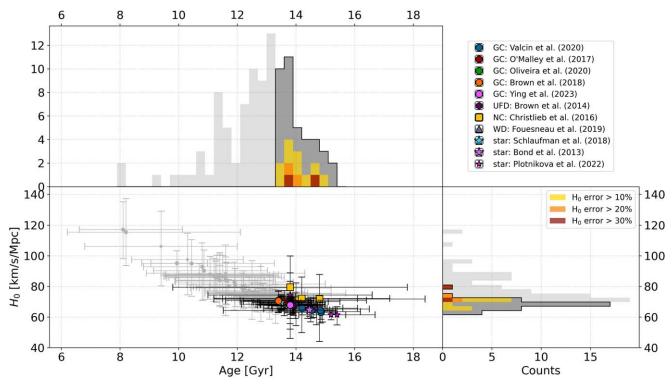


Figure 2. Constraints on H_0 derived from the oldest stellar ages. In the bottom left panel the distribution of the derived H_0 from the individual ages is shown, highlighting with colored points the 39 data used in our analysis (age >13.3 Gyr) on top of the data sample without any cut on age (gray points). The error bars include the statistical and systematic errors provided in each work. The top and right histograms show the distribution of ages and H_0 , respectively, with the lighter gray representing the entire distribution and the darker gray our selected sample. We also further highlighted the data with larger errors on H_0 , color-coded according to the percentage error (red considering a percentage error on $H_0 > 30\%$, orange for >20\%, and yellow for >10\%).

 Table 2

 Constraints on the Hubble Constant H_0 Based on the Average Ages of the Objects Older than 13.3 Gyr Present in Each of the 11 Independent Samples

Method	# of Objects	Mean Age (Gyr)	$H_0 (\text{km s}^{-1} \text{Mpc}^{-1})$	$P(H_0 \ge H_{0,\text{Planck}})$	$P(H_0 \leqslant H_{0,\text{SH0ES}})$
GC (Valcin et al. 2020)	14	14.08 ± 0.53	$66.32^{+2.91}_{-2.75}$	0.35	0.99
GC (O'Malley et al. 2017)	2	13.49 ± 1.4	$70.28_{-6.85}^{+8.64}$	0.65	0.64
GC (Oliveira et al. 2020)	2	13.57 ± 0.85	$68.82^{+3.43}_{-3.20}$	0.67	0.90
GC (Brown et al. 2018)	1	13.4 ± 1.2	$70.52_{-5.99}^{+7.25}$	0.68	0.65
GC (Ying et al. 2023)	1	13.80 ± 0.75	$67.76_{-3.75}^{+4.10}$	0.54	0.91
UFD (Brown et al. 2014)	1	13.9 ± 1	$67.69_{-4.83}^{+5.46}$	0.52	0.85
NC (Christlieb 2016)	4	14.17 ± 2.5	$70.89^{+17.37}_{-11.86}$	0.59	0.56
WD (Fouesneau et al. 2019)	1	13.89 ± 0.84	$67.37_{-4.02}^{+4.56}$	0.50	0.91
Individual star (Schlaufman et al. 2018)	1	13.5 ± 1	$69.66^{+5.81}_{-5.08}$	0.66	0.73
Individual star (Bond et al. 2013)	1	14.46 ± 0.8	$64.67^{+3.99}_{-3.54}$	0.23	0.99
Very metal-poor stars (Plotnikova et al. 2022)	11	14.73 ± 0.59	$63.45^{+2.93}_{-2.80}$	0.08	0.999

Note. For each sample, we report the number of objects available, their mean age including statistical and systematic errors, and the estimated H_0 . The last two columns report the probability that the estimated H_0 is respectively higher than the one obtained from Planck2020 and lower than the value from SH0ES (Riess et al. 2022).

with a minimum value of 8% and a maximum value of 68%. If also the conservative systematic error due to the choice of priors (Section 5) is added, the average probabilities discussed above change only by a few percent. In Figure 3, we compare our estimates with other H_0 constraints from the literature including a collection of H_0 measurements obtained with late-Universe probes. even if the current error bars are still quite large and dominated by systematics. In Section 6.3 we explore how our conclusions are affected by the choice of the adopted age threshold.

6.3. How Old Is Too Old?

The most stringent constraints on H_0 come from the oldest objects in the present-day Universe. However, the definition of oldest depends on the arbitrary choice of an age threshold that can be affected by statistical biases. For instance, choosing a

All our results based on the oldest stellar ages indicate a statistical preference for a value of H_0 smaller than the SH0ES constraint and more compatible with the Planck2020 results,

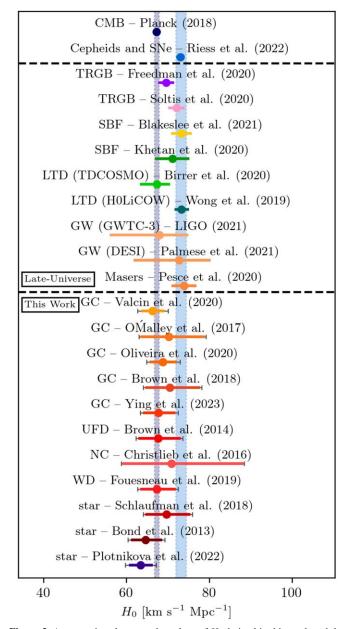


Figure 3. A comparison between the values of H_0 derived in this work and the ones available in the literature. Top part: the H_0 values from Planck Collaboration et al. (2020) and Riess et al. (2022). The vertical purple and blue shaded regions show the $\pm 1\sigma$ uncertainties of the two measurements through the entire plot. Central part: the H_0 measurements obtained with different cosmological probes of the late Universe: the tip of the red giant branch (TRGB, Freedman et al. 2020; Soltis et al. 2021), surface brightness fluctuations (SBF, Blakeslee et al. 2020; Soltis et al. 2021), lensing time delay (LTD, Birrer et al. 2020; Wong et al. 2020), gravitational waves (GW, Palmese et al. 2022). Bottom part: our estimates for each subsample in Section 3. The inner thicker error bars show the uncertainty including the statistical and systematic errors for the age estimates. The outer thinner error bars show the total errors including also the additional systematic uncertainty derived from the adopted priors discussed in Section 5.

small number of objects with the very oldest ages might bias the analysis toward fluctuations in the age distribution. In our work, we selected ages older than 13.3 Gyr because this allowed us to keep at least one object in each sample and to maximize the variety of methods for estimating the age. In other words, a threshold of >13.3 Gyr was the best trade-off between selecting the oldest objects and maximizing the variety of object types and the different methods used to derive their stellar ages, and therefore minimizing potential biases driven by specific classes of objects.

Here, we discuss how other choices may influence the final results on H_0 . In particular, we asked ourselves the question: how old is "too old"? We followed three approaches to address this question:

(i) we verified whether our chosen threshold was so high that it selected statistical fluctuations in our data set,

(ii) we checked how our result changed by lowering the adopted age threshold, and

(iii) we tested alternative criteria to select the oldest object in the Universe.

(i) As a first test, we studied the global age distribution of all the objects presented in the various papers to characterize the upper envelope of the distribution.⁴ These data are presented in the left panel of Figure 4. We found that the age distribution can be modeled as an asymmetric distribution with a distinctive peak around age ~ 13 Gyr. We modeled the upper edge of the distribution with a one-sided Gaussian, which is also shown in the figure, and calculated its width σ . We find that the threshold chosen in our analysis (age >13.3 Gyr) corresponds to $<1\sigma$ of the distribution of the upper envelope of our sample (shown as the darker shaded area in the left panel of Figure 4), showing in this way that the threshold >13.3 Gyr does not select high statistical fluctuations in our data. Note that also the distribution of the derived Hubble constant provides a similar piece of information. If we study the lower edge of the H_0 distribution (corresponding to the older ages; see the right panel of Figure 4), we find that it can also be modeled by a one-sided Gaussian, where the 1σ limit is $H_0 = 66.7 \text{ km s}^{-1} \text{ Mpc}^{-1}$, which is in very good agreement with the mean values estimated from the various samples derived in Section 6.2.

(ii) Next, we also investigated how much the main results of our analysis change by lowering the threshold from 13.3 Gyr to 13 Gyr. This clearly goes against the purpose of this work, which is to exploit the oldest objects as cosmological probes, but it allowed us to test the dependence of our findings on the chosen threshold. We decided not to choose a younger age threshold since we verified in Figure 4 that this is the peak of the age distribution, and considering younger ages would have biased the results in the opposite direction by including objects that are no longer representative of the upper edge of the distribution. We then repeated the analysis of Section 6.2 with a cut of >13 Gyr, and the results are reported in Table 3. As expected, we find that the mean ages decrease and, consequently, the derived values of H_0 move toward higher values. However, the change is limited. In particular, we find that the derived Hubble constant is more likely to be in a range between the SH0ES and Planck values, with still a slightly larger preference to be smaller than the SH0ES value. In fact, the weighted probability of H_0 being smaller than the SH0ES values changes from 90.3% to 89.9%, whereas the probability of being higher than the Planck value changes from 35.2% to 42.7%.

(iii) Finally, we also explored a different approach to select the oldest objects as those with the lowest metallicity based on the well-known anticorrelation between age and metal abundance. However, we note that this method would have been applicable homogeneously only to a subsample of our

 $^{^4}$ Here, we just consider a lower cut in age >8 Gyr, since it would be not useful to determine the upper edge of the distribution.

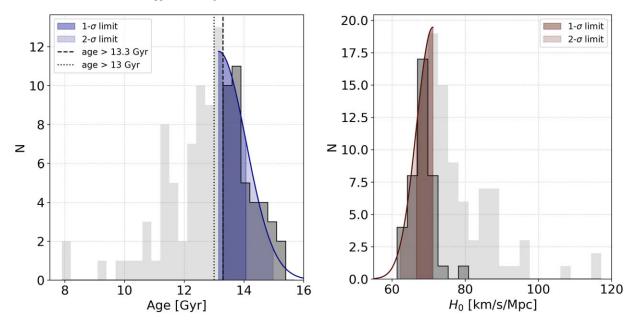


Figure 4. Left panel: the distribution of ages in our sample. The lighter and darker gray histograms show the overall sample and the objects with age >13.3 Gyr, respectively. The vertical lines show the cut adopted in the main text (age >13.3 Gyr) and the one investigated in this section (age >13 Gyr). The blue line is the one-sided Gaussian fit to the edge of the age distribution, highlighting in dark blue and light blue the 1σ and 2σ ranges, respectively. This demonstrates that 1σ of the upper edge of the age distribution is larger than both the adopted cuts. Right panel: the distribution of estimated values of H_0 . In this case, the lower envelope of the H_0 distribution is fitted with a one-sided Gaussian, corresponding to the older ages, showing in dark and light brown the 1σ and 2σ ranges, respectively. In this case, we find that 1σ of the lower edge of the H_0 distribution obtained from the individual age is compatible with the results we obtained from the average analysis in Section 6.2.

 Table 3

 Constraints on the Hubble Constant H_0 Based on the Average Ages of the Objects Older than 13 Gyr Present in Each of the 11 Independent Samples

Method	# of Objects	Mean Age (Gyr)	$H_0 ({\rm km \ s}^{-1} {\rm \ Mpc}^{-1})$	$P(H_0 \ge H_{0,\text{Planck}})$	$P(H_0 \leqslant H_{0,\text{SH0ES}})$
GC (Valcin et al. 2020)	19	13.87 ± 0.53	$67.30^{+2.99}_{-2.79}$	0.47	0.98
GC (O'Malley et al. 2017)	5	13.27 ± 1.1	$71.24_{-6.12}^{+7.26}$	0.71	0.62
GC (Oliveira et al. 2020)	2	13.57 ± 0.85	$68.82^{+3.43}_{-3.20}$	0.67	0.90
GC (Brown et al. 2018)	1	13.4 ± 1.2	$70.52_{-5.99}^{+7.25}$	0.68	0.65
GC (Ying et al. 2023)	1	13.80 ± 0.75	$67.76_{-3.75}^{+4.10}$	0.54	0.91
UFD (Brown et al. 2014)	1	13.9 ± 1	$67.69^{+5.46}_{-4.83}$	0.52	0.85
NC (Christlieb 2016)	4	14.17 ± 2.5	$70.89^{+17.37}_{-11.86}$	0.59	0.56
WD (Fouesneau et al. 2019)	1	13.89 ± 0.84	$67.37_{-4.02}^{+4.56}$	0.50	0.91
Individual star (Schlaufman et al. 2018)	1	13.5 ± 1	$69.66^{+5.81}_{-5.08}$	0.66	0.73
Individual star (Bond et al. 2013)	1	14.46 ± 0.8	$64.67^{+3.99}_{-3.54}$	0.23	0.99
Very metal-poor stars (Plotnikova et al. 2022)	16	14.40 ± 0.57	$64.80^{+2.97}_{-2.77}$	0.18	0.998

Note. For each sample, we report the number of objects available, their mean age including statistical and systematic errors, and the estimated H_0 . The last two columns report the probability that the estimated H_0 is respectively higher than the one obtained from Planck2020 and lower than the value from SH0ES (Riess et al. 2022).

data set. For this reason, we tested this approach using directly the data of Valcin et al. (2020), who defined their oldest GC sample by selecting the objects with metallicity [Fe/H] < -1.5. With such a criterion, they obtained an age = 13.32 ± 0.1 (stat.) ± 0.5 (syst.) Gyr. If we use their age estimate to derive the Hubble constant, we obtain $H_0 =$ $70.07^{+3.18}_{-2.94}$ km s⁻¹ Mpc⁻¹. Valcin et al. (2021) also revised and updated the systematic error estimate to $\sigma_{\text{stat}}(H_0) =$ 0.23 km s⁻¹ Mpc⁻¹, and if we use this estimate we obtain $H_0 = 69.87^{+1.94}_{-1.83}$ km s⁻¹ Mpc⁻¹. Both values are slightly larger than the estimate we provided in our work, but still compatible within the 1σ errors, and they do not change our general findings.

7. Accuracy Matrix and Prospects

The results presented in the previous section show the great potential of the oldest stars as cosmological probes. The constraints on H_0 can become more stringent with higher accuracy of stellar ages and Ω_M . We used the workflow presented in previous sections to construct a matrix that shows how the accuracy of H_0 depends on the errors on stellar ages and Ω_M . The uncertainty on the age in Figure 5 is the total one, i.e., including statistical and systematic errors.

First, we notice that the uncertainty on the age dominates the error budget of H_0 , whereas the uncertainty on Ω_M has a subdominant effect. The minimum uncertainty

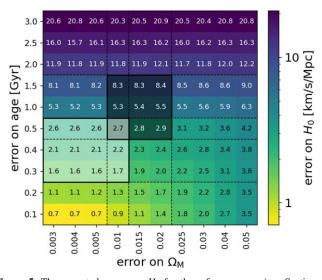


Figure 5. The expected errors on H_0 for the reference case (see Section 4; age = 13.5 Gyr and $11 < z_f < 30$) as a function of the uncertainty on Ω_M (x-axis) and on the age of the oldest stellar objects (y-axis). Given the pair (err $(\Omega_M, \text{ err(age)})$, the derived error on H_0 (in km s⁻¹ Mpc⁻¹) is shown in each square. The darker shaded square indicates the range of errors currently spanned in this paper. The lighter shaded square shows the improvement expected from the higher accuracies that could reasonably be obtained in the near future.

 $\sigma_{H_0} \sim 2.5 \text{ km s}^{-1} \text{ Mpc}^{-1}$ currently attainable (darker square) is larger by a factor of 2–4 than the most accurate estimates of H_0 available to date (Planck Collaboration et al. 2020; Riess et al. 2022). However, the matrix also shows that significant improvements are expected if the error on Ω_M is reduced to ~0.003 (e.g., with the Euclid mission, see Amendola et al. 2018) and the total error on the age decreases to ~0.3 Gyr.

More accurate ages could be achieved by increasing the sample size (i.e., minimizing the statistical error) and by further reducing the systematics (e.g., Valcin et al. 2021; Wu et al. 2022). This would allow us to reach an accuracy on H_0 of the order of ≤ 1.5 km s⁻¹ Mpc⁻¹, which could play a decisive role in the Hubble tension.

8. Summary and Outlook

The oldest stars in the present-day Universe play a key role as independent cosmological probes. In this work, we collected a sample of stellar objects for which state-of-the-art age estimates were available in the literature to revisit their potential to constrain the Hubble constant. The sample includes different types of objects (globular clusters, individual stars, white dwarfs, ultrafaint and dwarf spheroidal galaxies) whose ages were estimated with independent methods taking into account statistical and systematic uncertainties. The main results of this work can be summarized as follows.

1. We built a Bayesian framework to constrain the Hubble constant exploiting the age of the oldest stars. We adopted a flat Λ CDM model, assuming a flat prior on the formation redshifts ($11 < z_f < 30$) and a Gaussian prior on $\Omega_M = 0.30 \pm 0.02$ based on late-Universe probes independent of the CMB constraints. This prior choice has been estimated to affect our error estimate with at most a systematic error of $\sigma_{syst,prior}(H_0) = 2.37$ km s⁻¹ Mpc⁻¹, which, however, is highly conservative because the

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observational constraints significantly limit the actual range of priors.

- 2. We selected 39 objects with ages older than 13.3 Gyr, and for each object we estimated the Hubble constant. The distribution of H_0 is concentrated in the range $63 < H_0 \,[\mathrm{km \, s^{-1} \, Mpc^{-1}}] < 72$, with a preference for low values of H_0 if the most accurate estimates are selected. Although the current age uncertainties of individual objects do not allow stringent constraints on H_0 , the results clearly show the key role of the oldest objects as independent cosmological probes.
- 3. If the ages are averaged and analyzed independently for each subsample, we derive more stringent constraints that imply a high probability (90.3% on average) of H_0 being lower than the SH0ES value, and indicate that the ages of the oldest stars are more compatible with the Planck2020 estimate.
- 4. We constructed an "accuracy matrix" to assess how the constraints on H_0 can be tightened by increasing the accuracy of stellar ages and Ω_M . Should the systematic errors on stellar ages be reduced to $\lesssim 0.3-0.4$ Gyr, the accuracy of H_0 would increase to $\sim 1-2$ km s⁻¹ Mpc⁻¹ and become fully competitive with the other cosmological probes shown in Figure 3.

The results presented in this work show the great potential and a bright future for the oldest stars as cosmological probes. Several improvements can be expected thanks to massive spectroscopic surveys of extremely/very metal-poor stars (e.g., PRISTINE, WEAVE) combined with the parallax information provided by Gaia. In this regard, the recent results on the metalpoor GC M92 (Ying et al. 2023) are also indicative of the improvements expected in the estimate of the absolute ages of GCs with accuracies high enough to allow for cosmological applications with full control of the systematic uncertainties. It is indeed remarkable that in the case of M92 the error budget is dominated by the distance of this GC and not by the stellar evolution models. Moreover, spectroscopy with extremely large telescopes will allow us to apply nucleochronometry to larger samples and possibly reduce the age uncertainties to ~ 0.3 Gyr (Wu et al. 2022). Another promising opportunity will be offered by further studies of dwarf and ultrafaint galaxies in the Local Group. The imminent deep and homogeneous data obtained with space-based imaging (e.g JWST, Weisz et al. 2023b; Euclid, Laureijs et al. 2011) will allow us to reconstruct the star formation histories of these galaxies with higher fidelity and therefore to derive the ages of the oldest stellar populations (see for instance Weisz et al. 2023a for a recent example of this promising approach). In parallel, improved models of stellar evolution and white dwarf cooling will likely reduce the systematic uncertainties on age dating.

These advances will enhance the constraining power of the oldest stars in cosmology and their full exploitation in synergy with the forthcoming results expected from Euclid and other cosmological surveys. Moreover, the role of the oldest stars will not be limited to just H_0 , but will also be crucial for other cases in cosmology and fundamental physics. For instance, significant constraints could be placed to test the early dark energy (EDE) scenarios, invoked to mitigate the Hubble tension by adjusting the sound horizon. In that case, the younger age of the universe required in EDE models (e.g., Smith et al. 2022; Poulin et al. 2023) seems to be incompatible with the ages of the oldest objects in the present-day Universe,

proving how these data could be the optimal testbed on which to discriminate between different cosmological models.

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