

Alma Mater Studiorum Università di Bologna
Archivio istituzionale della ricerca

Emission taxation, green innovations and inverted-U aggregate R&D efforts in a linear state differential game

This is the final peer-reviewed author's accepted manuscript (postprint) of the following publication:

Published Version:

Emission taxation, green innovations and inverted-U aggregate R&D efforts in a linear state differential game / Dragone, D; Lambertini, L; Palestini, A. - In: RESEARCH IN ECONOMICS. - ISSN 1090-9443. - ELETTRONICO. - 76:1(2022), pp. 62-68. [10.1016/j.rie.2021.11.001]

Availability:

This version is available at: <https://hdl.handle.net/11585/903498> since: 2022-11-17

Published:

DOI: <http://doi.org/10.1016/j.rie.2021.11.001>

Terms of use:

Some rights reserved. The terms and conditions for the reuse of this version of the manuscript are specified in the publishing policy. For all terms of use and more information see the publisher's website.

This item was downloaded from IRIS Università di Bologna (<https://cris.unibo.it/>).
When citing, please refer to the published version.

(Article begins on next page)

This is the final peer-reviewed accepted manuscript of:

Dragone, D., Lambertini, L., & Palestini, A. (2022). Emission taxation, green innovations and inverted-U aggregate R&D efforts in a linear state differential game. *Research in Economics*, 76(1), 62-68.

The final published version is available online at:

<https://doi.org/10.1016/j.rie.2021.11.001>

Terms of use:

Some rights reserved. The terms and conditions for the reuse of this version of the manuscript are specified in the publishing policy. For all terms of use and more information see the publisher's website.

This item was downloaded from IRIS Università di Bologna (<https://cris.unibo.it/>)

When citing, please refer to the published version.

Emission taxation, green innovations and inverted-U aggregate R&D efforts in a linear state differential game

Davide Dragone[#], Luca Lambertini[§] and Arsen Palestini^{*}

[#] Department of Economics, University of Bologna

Piazza Scaravilli 2, 40126 Bologna, Italy; davide.dragone@unibo.it

[§] Corresponding author, Department of Economics and Alma Climate Centre
University of Bologna, via San Giacomo 3, 40126 Bologna, Italy; luca.lambertini@unibo.it

^{*} MEMOTEF, Sapienza University of Rome

Via del Castro Laurenziano 9, 00161 Rome, Italy; arsen.palestini@uniroma1.it

October 19, 2021

Abstract

We revisit a well known differential Cournot game with polluting emissions, to propose a version of the model in which environmental taxation is levied on emissions rather than the environmental damage. This allows to attain strong time consistency under open-loop information, and yields two main results which can be summarized as follows: (i) to attain a fully green technology in steady state, the regulator may equivalently adopt an appropriate tax rate (for any given number of firms) or regulate market access (for any given tax rate); (ii) if the environmental damage depends on emissions only (i.e., not on industry output) then the aggregate green R&D effort takes an inverted-U shape, and the industry structure maximising aggregate green innovation also minimises individual and aggregate emissions. This calls for a coordination of environmental and merger regulation so as to create the industry structure most favourable to green innovation.

Keywords: pollution, green R&D, emission taxation, differential games

JEL Codes: C73, H23, L13, O31, Q52

1 Introduction

If one takes a quick look at the static models dealing with emission taxation in oligopoly (little matters whether these models include green R&D or not), it appears that usually environmental taxation is levied on per-firm emissions rather than on the resulting (aggregate) environmental damage. The opposite applies instead if one examines the corresponding literature using optimal control or differential game theory.¹

This poses a problem of consistency between the static and the dynamic approach to modelling the environmental impact of oligopolistic interaction on the environment and the related design of emission taxation. Moreover, judging on the basis of casual observation, the two approaches are not equally realistic. To begin with, although aggregate data on emissions may well be more readily and easily available than individual data at the single firm level, taxing a magnitude defined as the environmental damage amounts to using a quite elusive concept, as the environmental damage imputable to any single industry adds up to the cauldron of a global economic system generating global warming and related effects. Additionally, current rules (for instance, in the EU) require firms to explicitly declare the CO_2 -equivalent emission rates of their products (e.g., cars), making these data accessible to the public and the authorities.

In view of these considerations, here we propose a differential Cournot game in which firms are being taxed in proportion to their individual emissions and react to the environmental tax rate by both modifying output levels and investing in R&D for green technologies.² This setup allows us to obtain several results. The first is that - taxation being linear in each firm's emission volume - the game at hand exhibits a linear state structure and therefore yields a subgame perfect equilibrium under open-loop information. The second result is that there exists a unique tax rate driving to zero the volume of emissions for any number of firms, or equivalently there exists a unique industry structure attaining the same outcome for any environmental tax rate. The third result is that - if the environmental damage is unaffected by industry output and the tax rate is optimally set - the aggregate R&D effort at the steady state equilibrium is non-monotone in the number of firms and has an inverted-U shape, i.e., there exists a unique industry structure that maximises the collective equilib-

¹For exhaustive surveys of both strands of research, where these features clearly emerge, see Montero (2002a,b), Requate and Unold (2003), Requate (2005), Long (2010) and Lambertini (2013).

²A recent overview of the debate on green innovation and its interplay with environmental regulation in imperfectly competitive markets is in Lambertini (2017).

rium investment in green technologies. The emergence of an analogous inverted-U shaped aggregate R&D curve has been illustrated by Feichtinger *et al.* (2016) using a differential game in which the public authority regulates market price (or tariff) in combination with an emission standard to which firms react by investing in green technologies over time. A static Cournot model also featuring an inverted-U curve, this time in presence of emission taxation, is in Lambertini *et al.* (2017). The present paper can be viewed as a properly dynamic representation of the latter model, illustrating additionally the possibility of reconstructing analogous results in a fully analytical way in more realistic setups properly accounting for the dynamics of global warming associated with firms' and consumers' intertemporal decisions. Moreover, the ensuing analysis shows that the appearance of a concave and single-peaked aggregate R&D curve is not necessarily associated with any form of price regulation.

The appearance of a concave and single-peaked relationship between innovation and market structure has a clearcut connection with an ongoing discussion in the theory and empirics of the economics of technical progress, which deserves to be illustrated in some more detail before delving into the analysis of our specific setup.

The acquired industrial organization approach to the bearings of market power on the size and pace of technical progress can be traced back to the indirect debate between Schumpeter (1934, 1942) and Arrow (1962) on the so-called Schumpeterian hypothesis, which, in a nutshell, says that one should expect to see an inverse relationship between innovation and market power or market structure. Irrespective of the nature of innovation (either for cost reductions or for the introduction of new products), a large theoretical literature attains either Schumpeterian or Arrowian conclusions (for exhaustive accounts, see Tirole, 1988; and Reinganum, 1989).³ That is, partial equilibrium theoretical IO models systematically predict a *monotone* relationship, in either direction.

The picture drastically changes as soon as one takes instead the standpoint of modern growth theory. In particular, Aghion *et al.* (2005) stress that empirical evidence shows a *non-monotone* relationship between industry concentration (or, the intensity of market competition) and aggregate R&D efforts: this takes the form of an *inverted-U curve*, at odds with all existing theoretical IO models; in the same paper, the authors provide a model yielding indeed such a concave result, and fitting the data. A thorough discussion, accompanied by an exhaustive review of the related lively debate, can be found in Aghion

³See also Gilbert (2006), Vives (2008) and Schmutzler (2010) for add-on's on this discussion, where still the Schumpeter vs Arrow argument is unresolved.

et al. (2013, 2015).

One could say that the inverted-U emerging from data says that Arrow is right for small numbers, while Schumpeter is right thereafter. Alternatively, on the same basis one could also say that neither Arrow nor Schumpeter can match reality, if our interpretation of their respective views is that “competition (resp., monopoly) outperforms monopoly (resp., competition) along the R&D dimension”. Be that as it may, there arises the need of constructing models delivering a non-monotone relationship between some form of R&D (for process, product or environmental-friendly innovations) and the number of firms in the industry. This is particularly true for green R&D in view of its relevance in the framework of the Paris Agreement and, as we shall briefly illustrate at the end of the analysis of the model, calls for a joint design of environmental and competition policies (in particular, towards horizontal mergers).

The remainder of the paper is organised as follows. The setup is illustrated in section 2. The equilibrium analysis and the main results are laid out in section 3. Section 4 contains concluding remarks.

2 The model

Consider a Cournot oligopoly with a population $n \geq 2$ of single-product homogeneous-good firms interacting over continuous time $t \in [0, \infty)$. At any time t , the demand function is $p(t) = a - \sum_{i=1}^n q_i(t)$, $q_i(t) \geq 0$ being the instantaneous individual output of firm i . The demand function is based on the assumption that consumers do not internalise any external effects, i.e., consumers in this market have not developed any environmental awareness. All firms use the same productive technology, described by the cost function $C_i(t) = cq_i(t)$.

Concerning the nature of green R&D efforts, we distinguish between investments in (i) abatement or end-of pipe technologies, which reduce the amount of CO_2 -equivalent emissions reaching the atmosphere while leaving the intrinsic nature of the technology incorporated in the final good, and (ii) replacement technologies, which involve a radical change in the nature of the product responsible of emissions. Examples fitting this distinction are, respectively, filters on the exhausts of a car engine fuelled by gasoline or diesel, and hybrid or electric propulsion. As for the modelisation of these two alternatives, we set out by assuming that consumption and/or production of the final good involve a volume of CO_2 equal to $v_i(t)q_i(t)$, with $v_i(t) > 0$. If firms invest in replacement technologies, then the

pollution dynamics at the industry level is

$$\dot{S}(t) = \frac{dS(t)}{dt} = \sum_{i=1}^n v_i(t) q_i(t) - \delta S(t) \quad (1)$$

where $\delta > 0$ is a constant decay rate. Each firm produces an effort $k_i(t)$ to reduce its coefficient $v_i(t)$, whereby we have an additional set of n state equations of the following type:

$$\dot{v}_i(t) = v_i(t) [\eta - k_i(t)] \quad (2)$$

in which $\eta > 0$. This is the scenario illustrated in Dragone *et al.* (2013), which, its intrinsic interest notwithstanding, can only be solved under open-loop rules, the latter being unable to deliver a proper feedback equilibrium.

If instead, as we intend to assume in the remainder of the paper, firms pursue the end-of-pipe route, one may model the individual emission dynamics, posing $v_i(t) = v$ for the sake of simplicity:

$$\dot{s}_i(t) = \frac{ds_i(t)}{dt} = vq_i(t) - k_i(t) - z \sum_{j \neq i} k_j(t) - \delta s_i(t), \quad (3)$$

It is worth noting that (3) defines the instantaneous variation of unabated emissions, which will be subject to regulation by the public authority. Variable $k_i(t)$ is the instantaneous R&D effort of firm i , and parameter $z \in [0, 1]$ accounts for the presence of spillovers in emission abatement (note that if $z = 1$ the green technology is a public good). The instantaneous cost associated with the R&D activity is $\Gamma_i(t) = wk_i^2(t)$, with $w > 0$, and firm i 's stock of unabated emissions $s_i(t)$ is taxed at the rate $\tau > 0$ at every instant.⁴ Hence, firm i 's instantaneous profits are

$$\pi_i(t) = [p(t) - c] q_i(t) - \tau s_i(t) - \Gamma_i(t), \quad (4)$$

and each firm i has to set $q_i(t)$ and $k_i(t)$ so as to maximise

$$\Pi_i = \int_0^{\infty} \{[p(t) - c] q_i(t) - \tau s_i(t) - \Gamma_i(t)\} e^{-\rho t} dt, \quad (5)$$

⁴A tax bill defined as a linear function of unabated polluting emissions is commonly used in static models (see Ulph, 1996; Montero, 2002b; Chiou and Hu, 2001; and Poyago-Theotoky, 2007, *inter alia*). An alternative way of modelling emission taxation consists in assuming that the tax rate is applied to the industry-wide environmental damage (see Karp and Livernois, 1994; Benckroun and Long, 1998; 2002; and Dragone *et al.*, 2014, among many others). This is, however, highly unrealistic for several reasons. The choice we make in the present model is in line with the idea that, currently, accurate and verifiable data are indeed available at the individual firm's level (e.g., this is the case in the car industry, where the amount of carbon emissions per kilometer are reported by manufacturers on their websites).

under the constraints posed by the state equation (3) and the initial conditions $s_i(0) = s_{i0} > 0$. Parameter $\rho > 0$ represents a constant discount rate common to all firms and the policy maker.

The instantaneous social welfare function is

$$SW(t) = \sum_{i=1}^n \pi_i(t) + CS(t) + \tau \sum_{i=1}^n s_i(t) - D(t) \quad (6)$$

where $\sum_{i=1}^n \pi_i(t)$ represents industry profits and $CS(t) = Q^2(t)/2$ is consumer surplus. The aggregate stock of pollution $S(t) = \sum_{i=1}^n s_i(t)$ concurs with the aggregate output $Q(t) = \sum_{i=1}^n q_i(t)$ in causing the (quadratic) environmental damage $D(t) = \varepsilon Q(t) + \gamma S^2(t)$, where γ and ε are positive parameters.

3 Equilibrium analysis

Henceforth, we will omit the time argument for simplicity, whenever possible. Since the present game is a linear state one, the open-loop solution is subgame perfect (or strongly time consistent) as it yields a degenerate feedback equilibrium.⁵ The current-value Hamiltonian of firm i is:

$$\begin{aligned} \mathcal{H}_i(\cdot) &= (p - c)q_i - \tau s_i - wk_i^2 + \lambda_{ii}\dot{s}_i + \sum_{j \neq i} \lambda_{ij}\dot{s}_j = \\ &= (\sigma - Q)q_i - rk_i^2 + \lambda_{ii}\dot{s}_i + \sum_{j \neq i} \lambda_{ij}\dot{s}_j, \end{aligned} \quad (7)$$

where $\sigma \equiv a - c > 0$ denotes market size and $\lambda_{ij}(t)$ is the costate variable attached by the i -th firm to the j -th state equation.

The necessary conditions (FOCs) are:

$$\frac{\partial \mathcal{H}_i}{\partial q_i} = \sigma - 2q_i - Q_{-i} + v\lambda_{ii} = 0, \quad (8)$$

where $Q_{-i} \equiv \sum_{j \neq i} q_j$, and

$$\frac{\partial \mathcal{H}_i}{\partial k_i} = -2wk_i - \lambda_{ii} - z \sum_{j \neq i} \lambda_{ij} = 0, \quad (9)$$

⁵For more on the arising of strongly time consistent equilibria in differential games solved under open-loop information, see Fershtman (1987), Mehlmann (1988, ch. 4), Dockner *et al.* (2000, ch. 7), Cellini *et al.* (2005) and Lambertini (2018).

The adjoint equations read as follows:

$$\dot{\lambda}_{ii} = (\rho + \delta) \lambda_{ii} + \tau \quad (10)$$

and

$$\dot{\lambda}_{ij} = (\rho + \delta) \lambda_{ij} \quad (11)$$

From (11) it is apparent that the solution $\lambda_{ij} = 0$ for all $j \neq i$ is admissible at all times. This means that, at any instant t , firm i fully disregards the dynamics of any rival's emissions.

Using $\lambda_{ij} = 0$ and imposing symmetry on states and controls, i.e. $s_i = s_j = S$, $k_i = k_j = k$, $q_i = q_j = q$ and consequently $\lambda_{ii} = \lambda_{jj} = \lambda$ for all $i \neq j$, we proceed to use (9) to derive the control equation for the green R&D effort k , as follows:

$$\dot{k} = -\frac{\dot{\lambda}}{2w} = -\frac{(\rho + \delta) \lambda + \tau}{2w} \quad (12)$$

which, noting - again from (9) - that $\lambda = -2wk$, can be rewritten as

$$\dot{k} = \frac{2w(\rho + \delta)k - \tau}{2w} \quad (13)$$

The optimal output associated with the Cournot-Nash equilibrium (CN) at any time t can instead be directly obtained by solving FOC (8):

$$q^{CN} = \frac{\sigma - 2vwk}{n + 1} \quad (14)$$

which obviously collapses onto the static Cournot-Nash output any green R&D effort being absent.

We may now characterise the steady state of the system. Imposing stationarity on (13) yields

$$k^{ss} = \frac{\tau}{2w(\rho + \delta)} \quad (15)$$

where superscript ss stands for *steady state*. The above expression establishes our first result:

Lemma 1 *For any given $\tau > 0$, the individual and aggregate green R&D efforts in steady state are positive. Moreover, the aggregate R&D effort is monotonically increasing in the number of firms.*

In particular, the second part of the above Lemma says that, since the aggregate equilibrium expenditure $K^{ss} = n\tau/[2w(\rho + \delta)]$ is linearly increasing in the number of firms, the present model seems to possess an Arrovian flavour. We will come back to this important aspect in the remainder.

Now observe that the steady state individual output is

$$q^{ss} = \frac{\sigma - 2vwk^{ss}}{n + 1} \quad (16)$$

which is lower than the static Cournot-Nash output, and strictly positive provided that

$$v \in \left(0, \frac{\sigma(\rho + \delta)}{\tau}\right). \quad (17)$$

Substituting (k^{ss}, q^{ss}) into the state equation (3) and imposing stationarity, we obtain

$$s^{ss} = \max \left\{ \frac{2\sigma vw(\rho + \delta) - \tau[2v^2w + (n + 1)(1 + z(n - 1))]}{2\delta w(n + 1)(\rho + \delta)}, 0 \right\}. \quad (18)$$

The following result applies:

Proposition 2 *The steady state (s^{ss}, q^{ss}, k^{ss}) is a saddle point.*

Proof. Given that the optimal output can be identified at any time in a quasi-static way, the state-control system solely describes the dynamics of (s^{ss}, k^{ss}) , and after imposing the symmetry conditions $k_i = k$ and $s_i = s$ for all i , it can be written as follows:

$$\begin{aligned} \dot{s} &= \frac{v(\sigma - 2vwk)}{n + 1} - [1 + z(n - 1)]k - \delta s \\ \dot{k} &= \frac{2w(\rho + \delta)k - \tau}{2w} \end{aligned} \quad (19)$$

The stability properties of the above system can be assessed via the trace and determinant of the following 2×2 Jacobian matrix:

$$J = \begin{bmatrix} \frac{\partial \dot{s}}{\partial s} & \frac{\partial \dot{s}}{\partial k} \\ \frac{\partial \dot{k}}{\partial s} & \frac{\partial \dot{k}}{\partial k} \end{bmatrix} = \begin{bmatrix} -\delta & -1 - \frac{2v^2w}{n + 1} - z(n - 1) \\ 0 & \delta + \rho \end{bmatrix} \quad (20)$$

The trace is $\mathcal{T}(J) = \rho > 0$ while the determinant is $\Delta(J) = -\delta(\delta + \rho) < 0$, therefore the steady state equilibrium is a saddle point. ■

Now note that $s^{ss} > 0$ for all

$$\tau < \tau_s \equiv \frac{2\sigma vw(\rho + \delta)}{2v^2w + (n+1)[1 + z(n-1)]} > 0 \quad (21)$$

which reveals that any tax rate at least equal to τ_s drives the individual and collective volume of polluting emissions to zero in steady state, irrespective of industry structure. Equivalently, taking $\tau > 0$ in such a way that green R&D activities do take place, one easily verifies that $s^{ss} = 0$ for all

$$n \geq n_s \equiv \max \left\{ 1, \frac{-\tau + \sqrt{\tau [\tau + 4z(2\sigma vw(\rho + \delta) - \tau(1 + 2v^2w - z))]} }{2\tau z} \right\}. \quad (22)$$

This implies:

Lemma 3 *A regulator may attain a fully green technology at the steady state in two ways: either by fixing $\tau \geq \tau_s$ for any given industry structure, or by regulating market access in such a way that $n \geq n_s$ for any given tax rate $\tau > 0$.*

To this regard, it is worth noting that the above Lemma (in particular if read in terms of the industry structure driving s^{ss} to zero for any given tax rate τ on emissions), identifies n_s as the optimal number of firms in the commons, where the concept of ‘commons’ has to be interpreted as the volume of polluting emissions (or the size of the negative externality generated by them, S^2) rather than, as is traditionally the case in the extant literature dating back to Gordon (1954) and Hardin (1968), a common resource pool being overexploited. In view of this analogy, we may ask ourselves whether an optimal number of firms can be identified in this setup, in relation to either the minimization of the volume of polluting emissions or the maximization of social welfare, net of the environmental damage.⁶

However, ‘green’ here means $s^{ss} = 0$, but the overall environmental damage $D^{ss} = \varepsilon n q^{ss}$ is still strictly positive. Alternatively, the authority may tune τ so as to minimise $D^{ss} = \varepsilon n q^{ss} + \gamma (n s^{ss})^2$. The resulting tax rate is:

$$\tau_D \equiv \frac{2vw(\rho + \delta) [n\sigma(n+1)[1 + z(n-1)]\gamma + w(n+1)\delta^2\varepsilon]}{n[2v^2w + (n+1)(1 + z(n-1))]\gamma} \quad (23)$$

At τ_D , we have that the overall environmental damage D is strictly positive unless $\varepsilon = 0$. A related - and intuitive - result can be outlined by comparing (21) and (23):

⁶In adopting this viewpoint, we broadly follow a path opened by Cornes and Sandler (1983), Cornes *et al.* (1986), Mason *et al.* (1988) and Mason and Polasky (1997), where the exploitation of natural resources in oligopoly is considered.

Lemma 4 $\tau_D > \tau_s$ for all $\varepsilon > 0$.

That is, if industry output contributes to the environmental damage, the tax rate minimising D^{ss} strictly exceeds the tax rate driving steady state emissions s^{ss} to zero.

The case in which $\varepsilon = 0$ and the environmental damage coincides with the square of aggregate polluting emissions lends itself to the analysis of the bearings of industry structure on the aggregate level of green R&D in steady state. If indeed $\varepsilon = 0$, and $\tau = \tau_s = \tau_D$, the industry green effort at equilibrium is

$$K^{ss}(\tau_D)|_{\varepsilon=0} = nk^{ss}(\tau_D)|_{\varepsilon=0} = \frac{\sigma v n}{2v^2w + (n+1)[1+z(n-1)]} \quad (24)$$

with

$$\frac{\partial K^{ss}(\tau_D)|_{\varepsilon=0}}{\partial n} = \frac{\sigma v [1 + 2v^2w - z(n^2 + 1)]}{[2v^2w + (n+1)(1+z(n-1))]^2} \quad (25)$$

The above expression is nil in correspondence of⁷

$$n_K = \frac{\sqrt{1 + 2v^2w - z}}{z} \geq 2 \quad \forall z \in \left[0, \min \left\{1, \frac{\sqrt{17 + 32v^2w - 1}}{8}\right\}\right) \quad (26)$$

which implies the following:

Proposition 5 *If (i) $\varepsilon = 0$; and (ii) $\tau = \tau_D$, there exists an admissible range of the technological spillover level characterising firms' green R&D activities wherein the aggregate R&D effort at the steady state equilibrium exhibits an inverted-U shape, reaching its maximum at*

$$n_K = \sqrt{\frac{1 + 2v^2w - z}{z}} \geq 2$$

Indeed, if $w > 2/v^2$, i.e., the R&D cost is steep enough, then

$$\min \left\{1, \frac{\sqrt{17 + 32v^2w - 1}}{8}\right\} = 1 \quad (27)$$

and consequently the above result holds for all z in the unit interval. The value of $K^{ss}(\tau_D)|_{\varepsilon=0}$ in $n = n_K$ is

$$K^{ss}(\tau_D, n_K)|_{\varepsilon=0} = \frac{\sigma v}{1 + 2\sqrt{z(1 + 2v^2w - z)}}. \quad (28)$$

⁷It can be easily checked that

$$\frac{\partial^2 K^{ss}(\tau_D)|_{\varepsilon=0}}{\partial n^2} < 0$$

at $n = n_K$. Hence, n_K indeed maximises $K^{ss}(\tau_D)$.

The above Proposition illustrates a case in which the aggregate innovation efforts of an industry being subject (and reacting) to environmental regulation take the form of an inverted-U curve with a single peak at some $n > 1$ (as in Aghion *et al.*, 2005, 2013). This finding - interesting in itself as it reveals the presence of an inverted-U shaped aggregate R&D curve - has a relevant consequence, which can be spelled out as follows. The sign of $n_s - n_K$ is the sign of⁸

$$nz - \sqrt{z(1 + 2v^2w - z)} \quad (29)$$

This establishes that when $n = n_K$ the expression in (29) is nil and therefore indeed $n_s = n_K$, which implies our final result:

Proposition 6 *If $\varepsilon = 0$ and $\tau = \tau_s = \tau_D$, the number of firms which drives down to zero the volume of individual and aggregate polluting emissions coincides with the number of firms at which the aggregate green R&D curve reaches its unique maximum.*

The above Proposition can be reformulated in alternative but equivalent terms by saying that a public authority in charge of regulating this industry faces no dilemma or tradeoff between the price effect and the external effect when it comes to simultaneously tailoring the pressure of environmental taxation and market access in order to maximise the effectiveness of green R&D on one side and minimise emissions on the other, as - provided aggregate output has no bearing on the environmental impact of these firms - there exists a unique pair $(n_s = n_K, \tau_D = \tau_s)$ allowing the policy maker to get two eggs in one basket.

Lemma 3 and Proposition 6 are connected with the recent debate on the impact of mergers on innovation, related to the recent Dow-Dupont merger case (see Federico *et al.*, 2017, Denicolò and Polo, 2018; and Delbono and Lambertini, 2021): in the present setting, regulating market access is somewhat equivalent to regulating horizontal mergers, as long as the initial number of firms is excessively high and mergers drive industry structure in the desired direction, namely, towards the peak of aggregate green R&D. In view of the requirements listed in the Paris Agreement, this simple dynamic model seems to indicate the presence of a clearcut and perhaps crucial interplay between antitrust or competition policy

⁸To obtain (29), one has just to plug $\varepsilon = 0$ and $\tau = \tau_s = \tau_D$ in

$$n_s = \frac{-\tau + \sqrt{\tau[\tau + 4z(2\sigma v w(\rho + \delta) - \tau(1 + 2v^2w - z))]}{2\tau z}$$

and then simplify the resulting expression for $n_s - n_K$.

and environmental policy in the overall design of the global economic system's path to the sustainability targets spelled out in the Agreement.

4 Concluding remarks

We have modified the dynamic Cournot game with environmental effects whose first formulation can be found in Benchekroun and Long (1998), supposing that a public authority adopts a linear taxation scheme by imposing an exogenous tax rate on the individual volume of pollution emitted, rather than taxing each firm in proportion to the environmental damage caused by aggregate pollution.

This construction ensures the presence of strong time consistency under open-loop strategies, a feature which in itself makes the model more easily tractable. As for the economic insight, our modelling choice delivers two main policy conclusions. The first is that to attain a fully green technology in steady state, the regulator is indifferent between adopting an appropriate tax rate (which is uniquely defined for any given number of firms) or regulating entry by identifying the optimal number of firms admitted to the industry (which is also uniquely defined for any given tax rate). The second is that, if the environmental damage depends on pollution only, then the aggregate investment takes in green innovations exhibits an inverted-U shaped curve, and, under the optimal tax rate, the number of firms maximising aggregate R&D coincides with the number of firms driving to zero aggregate pollution.

References

- [1] Aghion, P., U. Akcigit and P. Howitt (2013), “What Do We learn from Schumpeterian Growth Theory?”, mimeo, Department of Economics, Harvard University.
- [2] Aghion, P., U. Akcigit and P. Howitt (2013), “The Schumpeterian Growth Paradigm”, *Annual Review of Economics*, **7**, 557-75.
- [3] Aghion, P., N. Bloom, R. Blundell, R. Griffith and P. Howitt (2005), “Competition and Innovation: An Inverted-U Relationship”, *Quarterly Journal of Economics*, **120**, 701-28.
- [4] Arrow, K. (1962), “Economic Welfare and the Allocation of Resources for Invention”, in R. Nelson (ed.), *The Rate and Direction of Industrial Activity*, Princeton, NJ, Princeton University Press.
- [5] Benckroun, H. and N.V. Long (1998), “Efficiency Inducing Taxation for Polluting Oligopolists”, *Journal of Public Economics*, **70**, 325-42.
- [6] Benckroun, H. and N.V. Long (2002), “On the Multiplicity of Efficiency-Inducing Tax Rules”, *Economics Letters*, **76**, 331-36.
- [7] Cellini, R., L. Lambertini and G. Leitmann (2005), “Degenerate Feedback and Time Consistency in Differential Games”, in E.P. Hofer and E. Reithmeier (eds), *Modeling and Control of Autonomous Decision Support Based Systems. Proceedings of the 13th International Workshop on Dynamics and Control*, Aachen, Shaker Verlag, 185-92.
- [8] Chiou, J.-R. and J.-L. Hu (2001), “Environmental Research Joint Ventures under Emission Taxes”, *Environmental and Resource Economics*, **20**, 129-46.
- [9] Cornes, R. and T. Sandler (1983), “On Commons and Tragedies”, *American Economic Review*, **73**, 787-92.
- [10] Cornes, R., C.F. Mason and T. Sandler (1986), “The Commons and the Optimal Number of Firms”, *Quarterly Journal of Economics*, **101**, 641-46.
- [11] Delbono, F. and L. Lambertini (2021), “Innovation and Product Market Concentration: Schumpeter, Arrow and the Inverted-U Shape Curve”, *Oxford Economic Papers*, forthcoming.

- [12] Denicolò, V. and M. Polo (2018), “Duplicative Research, Mergers and Innovation”, *Economics Letters*, **166**, 56-59.
- [13] Dockner, E.J, S. Jørgensen, N. Van Long and G. Sorger (2000), *Differential Games in Economics and Management Science*, Cambridge, Cambridge University Press.
- [14] Dragone, D., L. Lambertini and A. Palestini (2013), “The Incentive to Invest in Environmental-Friendly Technologies: Dynamics Makes a Difference”, in J. Crespo Cuaresma, T. Palokangas and A. Tarasjev (eds), *Green Growth and Sustainable Development*, Heidelberg, Springer, 165-88.
- [15] Dragone, D., L. Lambertini and A. Palestini (2014), “Regulating Environmental Externalities through Public Firms: A Differential Game”, *Strategic Behavior and the Environment*, **4**, 15-40.
- [16] Federico, G., G. Langus and T. Valletti (2017), “A Simple Model of Mergers and Innovation”, *Economics Letters*, **157**, 136-40.
- [17] Feichtinger, G., L. Lambertini, G. Leitmann and S. Wrzaczek (2016), “R&D for Green Technologies in a Dynamic Oligopoly: Schumpeter, Arrow and Inverted U’s”, *European Journal of Operational Research*, **249**, 1131-38.
- [18] Fershtman, C. (1987), “Identification of Classes of Differential Games for Which the Open-Loop is a Degenerated Feedback Nash Equilibrium”, *Journal of Optimization Theory and Applications*, **55**, 217-31.
- [19] Gilbert, R. (2006), “Looking for Mr Schumpeter: Where Are We in the Competition-Innovation Debate?”, in J. Lerner and S. Stern (eds), *Innovation Policy and Economy*, NBER, MIT Press.
- [20] Gordon, H.S. (1954), “The Economic Theory of a Common-Property Resource: The Fishery”, *Journal of Political Economy*, **62**, 124-42.
- [21] Hardin, G. (1968), “The Tragedy of the Commons”, *Science*, **162**, 1243-48.
- [22] Karp, L. and J. Livernois (1994), “Using Automatic Tax Changes to Control Pollution Emissions”, *Journal of Environmental Economics and Management*, **27**, 38-48.

- [23] Katsoulacos, Y. and A. Xepapadeas (1995), “Environmental Policy under Oligopoly with Endogenous Market Structure”, *Scandinavian Journal of Economics*, **97**, 411-20.
- [24] Lambertini, L. (2013), *Oligopoly, the Environment and Natural Resources*, London, Routledge.
- [25] Lambertini, L. (2017), “Green Innovation and Market Power”, *Annual Review of Resource Economics*, **9**, 231-52.
- [26] Lambertini, L. (2018), *Differential Games in Industrial Economics*, Cambridge, Cambridge University Press.
- [27] Lambertini, L. J. Poyago-Theotoky and A. Tampieri (2017), “Cournot Competition and “Green” Innovation: An Inverted-U Relationship”, *Energy Economics*, **68**, 116-23.
- [28] Long, N.V. (2010), *A Survey of Dynamic Games in Economics*, Singapore, World Scientific.
- [29] Mason, C.F. and S. Polasky (1997), “The Optimal Number of Firms in the Commons: A Dynamic Approach”, *Canadian Journal of Economics*, **30**, 1143-60.
- [30] Mason, C., T. Sandler and R. Cornes (1988), “Expectations, the Commons, and Optimal Group Size”, *Journal of Environmental Economics and Management*, **15**, 99-110.
- [31] Mehlmann, A. (1988), *Applied Differential Games*, New York, Plenum Press.
- [32] Montero, J.-P. (2002a), “Permits, Standards, and Technology Innovation”, *Journal of Environmental Economics and Management*, **44**, 23-44.
- [33] Montero, J.-P. (2002b), “Market Structure and Environmental Innovation”, *Journal of Applied Economics*, **5**, 293-325.
- [34] Poyago-Theotoky, J. (2007), “The Organization of R&D and Environmental Policy”, *Journal of Economic Behaviour and Organization*, **62**, 63-75.
- [35] Reinganum, J. (1989), “The Timing of Innovation: Research, Development, and Diffusion”, in R. Schmalensee and R.D. Willig (eds), *Handbook of Industrial Organization*, vol. I, Amsterdam, North-Holland.

- [36] Requate, T. (2005), “Dynamics Incentives by Environmental Policy Instruments. A Survey”, *Ecological Economics*, **54**, 175-95.
- [37] Requate, T. and W. Unold (2003), “Environmental Policy Incentives to Adopt Advanced Abatement Technology: Will the True Ranking Please Stand up?”, *European Economic Review*, **47**, 125-46.
- [38] Schumpeter (1934), *The Theory of Economic Development*, Oxford, Oxford University Press.
- [39] Schumpeter, J.A. (1942), *Capitalism, Socialism and Democracy*, New York, Harper.
- [40] Tirole, J. (1988), *The Theory of Industrial Organization*, Cambridge, MA, MIT Press.
- [41] Ulph, A. (1996), “Environmental Policy and International Trade when Governments and Producers Act Strategically”, *Journal of Environmental Economics and Management*, **30**, 265-281.
- [42] Vives, X. (2008), “Innovation and Competitive Pressure”, *Journal of Industrial Economics*, **56**, 419-69.