## -Supporting Information-Time-Resolved Optical-Pump, Resonant X-ray Probe Spectroscopy of 4-Thiouracil; a Simulation Study

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## 1 Loop Diagram Rules

The loop diagram of the optical pump - resonant X-ray probe signal is shown in Scheme 1b in the main manuscript and Figure S6. The Diagram rules are as follows:

- Time runs along the loop clockwise from bottom left to bottom right.
- Each field interaction is represented by an arrow, which either points to the right (photon annihilation and excitation of the molecule) or to the left (photon creation and de-excitation of the molecule).
- Free evolution periods on the left branch indicate forward propagation in real time, and on the right branch to backward propagation respectively.
- The last field interaction is the detected photon mode. In addition, the gray bar represents the period of free evolution.

## 2 Supplementary Figures



Figure S 1: Nonadiabatic couplings versus the two nuclear coordinates of the 4-thiourail. The location of the FC, CoIn, and S2 min are marked with X. The spiky nature due to the phase change across the CoIn is observed.



Figure S 2: CASSCF(20,16) active space. Active space for 4-thiouracil at the optimized ground state at the MP2 level (20 electrons in 16 orbitals) averaged over 3 lowest valence states,  $S_0 - S_2$  and 30 core states for each sulfur and 10 core states for oxygen and nitrogen K-edges.

Figure S 3: The nuclear wavepacket molecular dynamics movie on  $S_2$ ,  $S_1$ , and  $S_0$  PES.  $S_2$  wavepacket (gray contours),  $S_1$  wavepacket (pink contour), and  $S_0$  wavepacket (black contour). The location of the FC,  $S_2$  min, and CoIn is marked with "X". The pump-probe time-delay and the populations are shown in the bottom left corner. see the attached movie



Figure S 4: Time-evolving electronic states levels for (a) S, (b) O, (c)  $N_1$ , and (d)  $N_2$  K-edges. The valence states,  $S_0$ ,  $S_1$ , and  $S_2$  are shown in black, pink, and gray lines, respectively. See the left y-axis for the valence energy levels and the right y-axis for the core energy levels.



Figure S 5: Transition dipole moment between valence ( $S_0$ ,  $S_1$ , and  $S_2$ ) and core states over twodimensional nuclear grids. (a) sulfur, (b) oxygen, and (c) nitrogen K-edges. Profiles pertaining to the same heteroatom are plotted in the same [min:max] range to allow easier comparison.



Figure S 5: (continued)



Figure S 6: (a) Pulse configuration for X-ray narrowband/broadband hybrid probe pulse and (b) the relevant Loop diagram. A hybrid X-ray field  $\mathcal{E}_B$  (broad) and  $\mathcal{E}_N$  (narrow) is used instead of a single broadband pulse that interacts twice. An incoming X-ray pulse ( $\mathcal{E}_N$ ) excites a molecule on a valence electronic surface  $|e\rangle$  into a core level  $|f\rangle$  after time delay *T* following an initial excitation into a non-stationary state and free evolution period (gray box). The signal field emission is stimulated by a broadband attosecond X-ray pulse ( $\mathcal{E}_B$ ).