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This is the final peer-reviewed author's accepted manuscript (postprint) of the following publication:

Published Version:

Mantiloni, L., Nespoli, M., Belardinelli, M.E., Bonafede, M. (2020). Deformation and stress in hydrothermal regions: The case of a disk-shaped inclusion in a half-space. JOURNAL OF VOLCANOLOGY AND GEOTHERMAL RESEARCH, 403, 1-12 [10.1016/j.jvolgeores.2020.107011].

Availability:

This version is available at: <https://hdl.handle.net/11585/769000> since: 2020-10-22

Published:

DOI: <http://doi.org/10.1016/j.jvolgeores.2020.107011>

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1 Deformation and stress in hydrothermal regions: the case of a disk-shaped
2 inclusion in a half-space

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6 **Abstract**

7 Hydrothermal regions are affected by a wide variety of phenomena, including ground inflation and deflation
8 episodes. Among them, calderas offer the opportunity to study the complex interactions between magmatic
9 processes at depth and permeable rocks saturated with fluids in the upper sedimentary layers. One of
10 such regions is the Campi Flegrei caldera in southern Italy, where several source models have been applied
11 over the years to reproduce the ground displacement and seismicity observed during the most recent phase
12 of major unrest (1982-1984). The present work aims at introducing a new source model consisting of a
13 thermo-poro-elastic inclusion embedded in a homogeneous poroelastic half-space. The inclusion is meant to
14 represent a permeable rock layer stressed and strained by hot and pressurized volatiles released upward by
15 an underlying magmatic reservoir and is modeled as a thin horizontal disk inside which a sudden change of
16 temperature and pore pressure occurs. We provide semi-analytical solutions for the displacement and stress
17 fields both within and outside the source and check them by comparison with those obtained through a
18 fully numerical approach. Results provided by our model are compared with two other deformation source
19 models often used to describe volcanic environments in terms of pressurized cavities describing a spherical
20 magma chamber (Mogi source) or a sill-like magma intrusion (Fialko source). For the Campi Flegrei 1982-84
21 unrest, our model provides a better reproduction of ground deformation data and manages to explain the
22 widespread presence of compressive focal mechanisms, since the stress field promoted both inside and outside
23 the thermo-poro-elastic inclusion is very different from pressurized cavities.

24 **Keywords:** Campi Flegrei, Thermo-poro-elasticity, Focal mechanisms, Deformation sources, Volcanism.

57
58 **1. Introduction**
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60

61 Hydrothermal regions are found in many areas of the Earth, and are in some cases associated with
62 calderas. They are affected by complex interactions in which convection of water and other fluids of magmatic
63 origin within the Earth's crust transfer heat and mass towards the surface. This leads to a variety of
64 observable phenomena, including ground deformation, gravity changes, hot springs, fumaroles and seismicity
65 (see e.g. the Yellowstone caldera, USA, Tizzani et al., 2015; the Rabaul caldera, Papua New Guinea,
66 Robertson and Kilburn, 2016; the Masaya complex, Nicaragua, Williams-Jones et al., 2003; the Long Valley
67 caldera, USA, Hill, 2006; Prejean et al., 2002; Sorey et al., 1991; the Hengill volcanic system, Iceland, Feigl
68 et al., 2000). According to physical models, these effects are generally connected with hydrothermal processes
69 (Rinaldi et al., 2010, Todesco et al., 2014), involving temperature and pore-pressure changes of fluids flowing
70 through permeable rocks, but also with the inflation or deflation of the parent magma chamber related to
71 the mass input/output, to internal differentiation processes or to the emplacement of a new magmatic body
72 (Macedonio et al., 2014; Di Vito et al., 2016). In particular Lima et al. (2009) consider ground deformation
73 episodes as due to the cooling and crystallization of a magma volume at shallow depth, accompanied by
74 release of magmatic fluids which are occasionally expelled from a deep, pressurized, region into the shallow
75 hydrothermal system. In the Lima et al. (2009) conceptual model, subsidence could result from a volume
76 decrease due to both crystallization and a decrease in the flux of magmatic fluids entering the system, or
77 a rapid permeability increase (and pore pressure decrease) that occurs when the fluid pressure exceeds the
78 local strength of the crust, leading to failures in the elastic matrix of the porous media. As the discrimination
79 between these processes is not trivial, the modelling of these phenomena is most important to improve the
80 comprehension of volcanic hazard.

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46 Ground deformation in volcanic areas is usually modeled in terms of the surface effects of a deformation
47 source at depth, typically consisting of a pressurized cavity representing a magma chamber (e.g. Mogi, 1958,
48 Yang et al., 1988) or a horizontal circular crack, suited to model sill-like magma intrusions (e.g. Fialko et al.,
49 2001). Such models assume the source to be embedded in a homogeneous, elastic half-space and neglect
50 the presence of fluids within the rocks. In the present paper we consider the mechanical effects induced
51 by temperature and pore-pressure changes within a thermo-poro-elastic inclusion surrounded by an elastic
52 medium. Conceptually similar thermo-poro-elastic models were employed to study the effects of pressure

113
114 53 and temperature gradients around wellbores, accounting for deformation sources with cylindrical geometries
115
116 54 located within unbounded media (e.g. Myklestad, 1942; Perkins et al., 1984 and Perkins et al., 1985). To
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118 55 model subduction above gas or oil reservoirs, Geertsma et al. (1973) considered the effect of a drop in pore
119
120 56 pressure within a finite cylindrical volume in an elastic half-space, retrieving analytical solutions for surface
121
122 57 displacement components. Myklestad (1942) developed analytical solutions for stress components close to a
123
124 58 semi-infinite circular cylinder inside which a uniform increase of temperature occurs.

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126 59 In the present work we introduce a deformation source consisting of a disk-shaped horizontal Thermo-
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128 60 Poro-Elastic (TPE) inclusion embedded in a poro-elastic half space in free drainage conditions. As in
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130 61 Belardinelli et al. (2019) the TPE inclusion is meant as a region of permeable rock being affected by a
131
132 62 sudden increase in temperature and pore pressure, embedded in a surrounding medium in isothermal drained
133
134 63 conditions. It is worth to notice that purely magmatic models hardly explain long-lasting subsidence (Calò
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136 64 and Tramelli, 2018 and Troise et al., 2018) and are not suitable for the shallow source regions where the
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138 65 presence of large magma bodies can be ruled out. Moreover, differently from a pressurized cavity, the TPE
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140 66 model provides a strong deviatoric stress field even within the source. Belardinelli et al. (2019) consider a
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142 67 spherical shell-shaped TPE inclusion surrounding a fluid filled magma chamber and embedded within an
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144 68 unbounded poro-elastic medium; in the present work we (i) include the free surface boundary condition and
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146 69 (ii) consider a disk-shaped TPE inclusion. Including the free surface is fundamental in order to compare
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148 70 model predictions with observed fault mechanisms above the magma reservoir and with surface displacement.
149
150 71 With respect to a spherical shell surrounding the magmatic intrusion, a disk-shaped region is better suited
151
152 72 to describe a horizontal permeable rock layer stressed and strained by hot and pressurized volatiles. For
153
154 73 example, at Campi Flegrei at about 2 km depth, there is evidence of a seismic layer separating a deeper
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156 74 magmatic body from the shallower aquifer (Figure 8 in Calò and Tramelli, 2018), the most permeable part
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158 75 of which may allow the magmatic fluids to flow upward.

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157 76 In the next sections we present the semi-analytical formulation of the model. As the present model is
158
159 77 inspired by observations made in the Campi Flegrei caldera in southern Italy (fig. 1), in the last section we
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161 78 provide an application focused on one of its unrest episodes. During the period 1982-84 the recorded uplift
162
163 79 at Campi Flegrei was nearly axi-symmetric and centered in the town of Pozzuoli (Bonafede and Ferrari,
164
165 80 2009) where it reached its maximum with rate values up to 1 m/yr. One of the most relevant aspects of
166
167 81 the 1982-84 unrest was the important increase in seismic activity, while the previous episodes of uplift were
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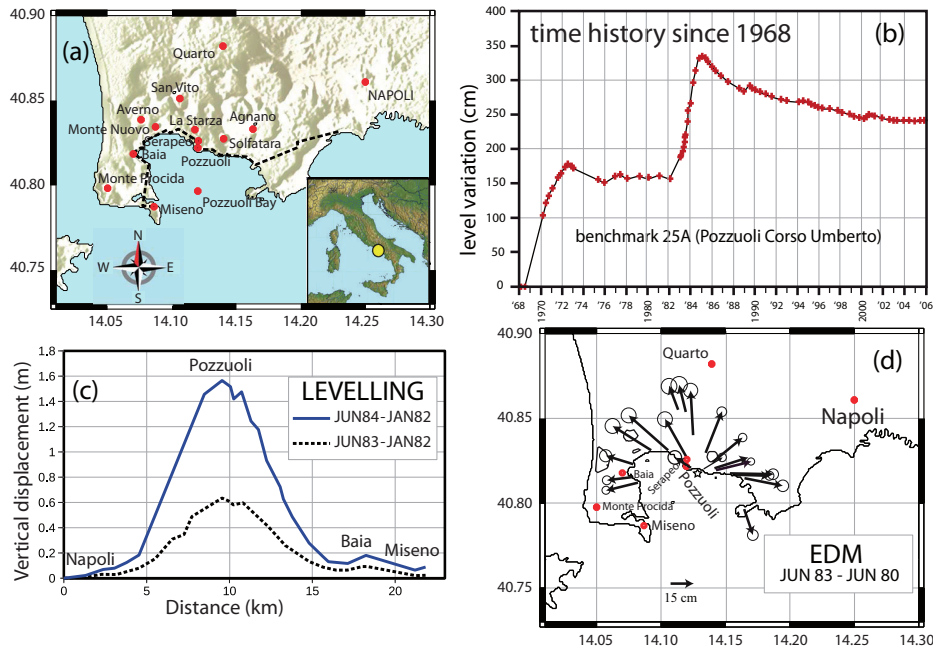


Figure 1: Map and deformation data of the studied area. a) Map of the Campi Flegrei region. b) evolution of uplift at benchmark 25A (Pozzuoli Corso Umberto) since 1968 to 2006. c) pattern of uplift measured on the baseline between Napoli and Miseno (drawn in a) as a dashed black line) in June 1983 (black dotted line) and in June 1984 (blue) with respect to January 1982; the maximum uplift was close to the center of Pozzuoli. d) displacement vectors estimated from EDM (Electromagnetic Distance Measurement) from Jun 80 to Jun 83 referred to the point shown as a star (Amoruso et al., 2014). White circles represent errors.

82 accompanied by weak to moderate seismicity (D’Auria et al., 2014). The contribution of both magmatic
 83 intrusions and hydrothermal dynamics to surface ground deformation was envisaged for this episode (e.g.
 84 Belardinelli et al., 2019). Our results will be compared with some of the principal source models used for
 85 the 1982-84 unrest, in particular attention is paid to inversion of surface deformation data and the expected
 86 distributions of focal mechanisms versus related evidences.

87 It is worth to notice that, despite having been inspired by the features of one particular case of study,
 88 the simple geometry and characteristics of our model make it applicable to the study of other hydrothermal
 89 regions around the world.

90 2. Methods

91 Following Eshelby (1957) we retrieve the displacement and stress fields associated to the TPE inclusion.
 92 The procedure has already been outlined in details by Belardinelli et al. (2019). The strain field e_{ij} of a
 93 thermo-poro-elastic medium (McTigue, 1986) undergoing changes of stress τ_{ij} , temperature ΔT and pore
 94 pressure Δp is

$$e_{ij} = \frac{1}{2\mu} \left(\tau_{ij} - \frac{\nu}{1+\nu} \tau_{kk} \delta_{ij} \right) + \frac{1}{3H} \Delta p \delta_{ij} + \frac{1}{3} \alpha \Delta T \delta_{ij} \quad (1)$$

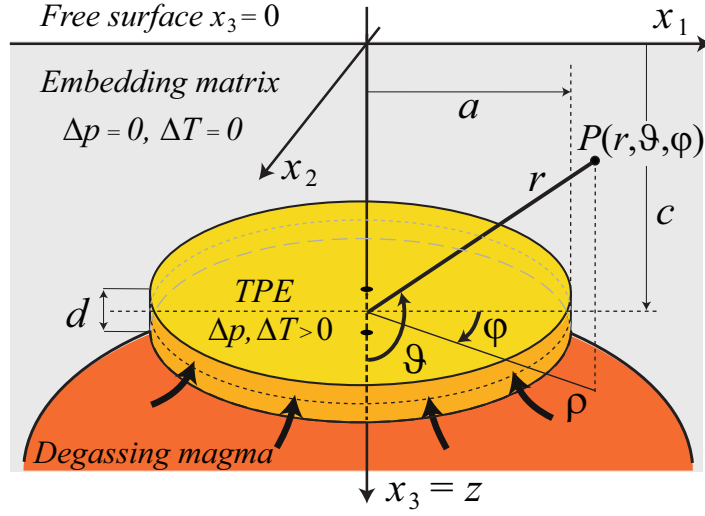


Figure 2: Schematic picture of the disk-shaped thermo-poro-elastic inclusion. The inclusion (yellow region) has a radius a and thickness d ; it is located at depth c and embedded in a poro-elastic half-space (grey region). The inclusion undergoes a sudden change in temperature ΔT and pore pressure Δp caused by degassing of a underlying magma body (orange region). The median plane of the disk is drawn with a dotted line. The spherical and cylindrical coordinates (r, θ, φ) and (ρ, φ, z) , respectively, are expressed in a reference frame with origin in $x_1 = 0, x_2 = 0, x_3 = c$.

95 while the inverse relation is

$$\tau_{ij} = 2\mu e_{ij} + \lambda e_{kk}\delta_{ij} - K \left(\frac{1}{H}\Delta p\delta_{ij} + \alpha\Delta T\delta_{ij} \right) \quad (2)$$

96 where H is the Biot's constant, α the coefficient of thermal expansion, μ the rigidity, ν the drained isothermal

97 Poisson's ratio and $K = \frac{2\mu(1+\nu)}{3(1-2\nu)} = \lambda + \frac{2}{3}\mu$ the drained isothermal bulk modulus of the poroelastic medium.

98 Following eq. (1), the stress-free strain e_{ij}^* that the inclusion would undergo in absence of the hosting medium

99 (Belardinelli et al., 2019) can be expressed as:

$$e_{ij}^* = e_0\delta_{ij} \quad \text{where} \quad e_0 = \frac{1}{3H}\Delta p + \frac{1}{3}\alpha\Delta T \quad (3)$$

100 Surface tractions $T_k = -3Ke_0n_k$ must be applied in isothermal and drained conditions to restore the original

101 volume and shape of the inclusion. Outside the inclusion the tractions vanish, so that a traction discontinuity

102 $[T_k]_-^+ = 3Ke_0n_k$ appears on the TPE inclusion boundary S . When removing the traction discontinuity across

103 S , the following displacement is produced (see e.g. Aki Richards, p. 58)

$$u_i(\mathbf{x}) = \oint_S G_{ik}(\mathbf{x}, \mathbf{x}') [T_k]_-^+ dS' = 3Ke_0 \oint_S G_{ik}(\mathbf{x}, \mathbf{x}') n_k(\mathbf{x}') dS' \quad (4)$$

104 where G_{ik} is the elastic Green's tensor for a half-space with drained, isothermal elastic parameters, whose

105 components are given by Mindlin (1936). The Green's function $G_{ik}(\mathbf{x}, \mathbf{x}')$ yields the displacement in the

281
282 106 i - th direction at point \mathbf{x} due to a unitary point force acting in the k - th direction at \mathbf{x}' . By applying
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284 107 Gauss' theorem we obtain
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$$287 \quad u_i(\mathbf{x}) = 3Ke_0 \int_{V_S} \frac{\partial G_{ik}}{\partial x'_k}(\mathbf{x}, \mathbf{x}') dv(\mathbf{x}') \quad (5)$$

290 where V_S is the volume of the TPE inclusion. The displacement caused by the TPE source everywhere in
291
292 109 the half-space is provided by equation (5). Instead the stress field τ_{ij} caused by the TPE source is provided
293
294 110 by eq. (2) and should be defined separately within the inclusion, where $\tau_{ij} = \tau_{ij}^{in}$, and outside it, where
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296 111 $\Delta p = 0$, $\Delta T = 0$ and $\tau_{ij} = \tau_{ij}^{out}$, so that

$$300 \quad \tau_{ij}^{in} = \lambda e_{kk} \delta_{ij} + 2\mu e_{ij} - 3Ke_0 \delta_{ij} \quad (6a)$$

$$302 \quad \tau_{ij}^{out} = \lambda e_{kk} \delta_{ij} + 2\mu e_{ij} \quad (6b)$$

303
304
305 112 with $e_{ij} = \frac{1}{2} \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right)$. Since $G_{ik}(\mathbf{x}, \mathbf{x}')$ is singular, when $\mathbf{x} \rightarrow \mathbf{x}'$ particular care must be taken when
306
307 113 computing u_i , e_{ij} and τ_{ij} within the inclusion.
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310 2.1. Retrieval of the displacement field: singular and non-singular terms

311
312 115 The three components of the displacement field u_i are found by first evaluating the sum of Green's tensor
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314 116 partial derivatives in eq. (5), employing cartesian coordinates. Their expressions can be written as
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$$317 \quad u_1 = 3KCe_0 \int_{-a}^a dx'_1 \int_{-f(x'_1)}^{f(x'_1)} dx'_2 \int_{c-\frac{d}{2}}^{c+\frac{d}{2}} dx'_3 (x_1 - x'_1) \left\{ \frac{1}{R_1^3} + \frac{(3-4\nu)}{R_2^3} - \frac{6x_3(x_3 + x'_3)}{R_2^5} \right\}$$

$$319 \quad u_2 = 3KCe_0 \int_{-a}^a dx'_1 \int_{-f(x'_1)}^{f(x'_1)} dx'_2 \int_{c-\frac{d}{2}}^{c+\frac{d}{2}} dx'_3 (x_2 - x'_2) \left\{ \frac{1}{R_1^3} + \frac{(3-4\nu)}{R_2^3} - \frac{6x_3(x_3 + x'_3)}{R_2^5} \right\} \quad (7)$$

$$321 \quad u_3 = 3KCe_0 \int_{-a}^a dx'_1 \int_{-f(x'_1)}^{f(x'_1)} dx'_2 \int_{c-\frac{d}{2}}^{c+\frac{d}{2}} dx'_3 \left\{ \frac{(x_3 - x'_3)}{R_1^3} - \frac{(3-4\nu)(x_3 + x'_3)}{R_2^3} - \frac{6x_3(x_3 + x'_3)^2}{R_2^5} + \frac{2x_3}{R_2^3} \right\}$$

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329 117 where
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$$R_1 = \sqrt{(x_1 - x'_1)^2 + (x_2 - x'_2)^2 + (x_3 - x'_3)^2} \quad (8a)$$

$$R_2 = \sqrt{(x_1 - x'_1)^2 + (x_2 - x'_2)^2 + (x_3 + x'_3)^2} \quad (8b)$$

$$f(p) = \sqrt{a^2 - p^2}, \quad C = \frac{1 - 2\nu}{8\pi\mu(1 - \nu)} \quad (8c)$$

and the intervals of integration are given by the geometry of the TPE inclusion (Figure 2). The integrand functions in eqs. (7) can be divided into two parts: the terms depending on $\frac{1}{R_1^3}$ which diverge within the volume of the inclusion (V_s) and those depending on powers of $\frac{1}{R_2}$ which are bounded within V_s . For this reason, the terms depending on $\frac{1}{R_1^3}$ are referred to as the *singular* terms (apex *s*), while those depending on powers of $\frac{1}{R_2}$ are referred to as the *non-singular* terms (apex *ns*).

Accordingly, even the displacement field \mathbf{u} is found by summing up two contributions, as follows:

$$\mathbf{u} = \mathbf{u}^s + \mathbf{u}^{ns} \quad (9)$$

The singular contribution to displacement, \mathbf{u}^s , can be written as the gradient of a scalar potential Φ (Belardinelli et al., 2019) so that:

$$\mathbf{u}^s = -\frac{e_1}{4\pi} \nabla \Phi \quad \text{with} \quad \Phi(\mathbf{x}) = \int_{V_s} \frac{1}{R_1} dv(\mathbf{x}') \quad (10)$$

where

$$e_1 = e_0 \frac{1 + \nu}{1 - \nu} \quad (11)$$

The potential in eq. (10) is formally equivalent to the Coulomb electrostatic potential due to a cylindrical volume V_S of charge density $4\pi\epsilon_0$ (see Jackson, 1999), and therefore the integral can be computed employing an expansion in Legendre polynomials $P_l(x)$ if we make the assumption that the thickness d of the cylinder is much smaller than its radius a ($\frac{d}{a} \ll 1$)

$$\begin{aligned} \Phi(r, \vartheta) &= 2\pi ad \left[1 - |\cos \vartheta| \frac{r}{a} + \sum_{m=1}^{\infty} c_{2m} P_{2m}(\cos \vartheta) \frac{1}{2m-1} \left(\frac{r}{a}\right)^{2m} \right] \quad \text{if } r < a \\ \Phi(r, \vartheta) &= 2\pi ad \sum_{m=0}^{\infty} c_{2m} P_{2m}(\cos \vartheta) \frac{1}{2m+2} \left(\frac{a}{r}\right)^{2m+1} \quad \text{if } r > a \end{aligned} \quad (12)$$

where $c_{2m} = (-1)^m 4^{-m} (2m)! (m!)^{-2}$ and (r, ϑ, φ) are the spherical coordinates of a point (ϑ is the colatitude measured from the z axis) in a reference frame with origin in the disk center (see Figure 2). When $r \approx a$, the

393 convergence of the above series is extremely slow, so that analytical continuation may be employed. On the
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 395
 396 134 other side, the integrals of the *non-singular* terms in (7) are dealt with by performing analytical integrations
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 398 135 and simplifying them into single integrals over one coordinate dx'_i , which are computed numerically, yielding
 399
 400 136 the *non-singular* contribution \mathbf{u}^{ns} to \mathbf{u} (see supplementary material).

401 402 403 137 2.2. Retrieval of the stress field within and outside the inclusion

404
 405 138 The strain tensor $e_{ij} = e_{ij}^s + e_{ij}^{ns}$, can be also separated into a singular part, e_{ij}^s , and a non-singular
 406
 407 139 one, e_{ij}^{ns} related to derivatives of \mathbf{u}^s and \mathbf{u}^{ns} , respectively. The singular components e_{ij}^s can be obtained
 408
 409 140 analytically from spatial derivatives of the scalar potential (eq. 12) as follows

$$410 \quad e_{rr}^s = u_{r,r}^s, \quad e_{\vartheta\vartheta}^s = r^{-1}(u_{\vartheta,\vartheta}^s + u_r^s), \quad e_{\varphi\varphi}^s = (r \sin \vartheta)^{-1}(u_{\varphi,\varphi}^s + u_r^s \sin \vartheta + u_{\vartheta}^s \cos \vartheta), \quad (13)$$

411
 412
 413 141 where the spatial derivative of a scalar field Ψ with respect to the variable x is indicated as $\Psi_{,x}$,

$$414 \quad e_{r\vartheta}^s = u_{\vartheta,r}^s, \quad e_{r\varphi}^s = 0, \quad e_{\vartheta\varphi}^s = 0. \quad (14)$$

415
 416
 417
 418 142 The second members of the last equation are obtained considering that $u_{\vartheta,r}^s = r^{-1}(u_{r,\vartheta}^s - u_{\vartheta}^s)$, being from
 419
 420 143 (10) $u_r^s = \Phi_{,r}$ and $u_{\vartheta}^s = r^{-1}\Phi_{,\vartheta}$ and $u_{\varphi}^s = (r \sin \vartheta)^{-1}\Phi_{,\varphi} = 0$, while u_r^s and u_{ϑ}^s do not depend on φ . In
 421
 422 144 analogy with Belardinelli et al. (2019), it may be shown that the singular dilation outside the inclusion is
 423
 424 145 $e_{kk}^s = 0$, while inside it we have $e_{kk}^s = e_1$. The non-singular components are retrieved by analytical spatial
 425
 426 146 derivatives of \mathbf{u}^{ns} , evaluating the corresponding volume integrals in a semianalytical way as made for \mathbf{u}^{ns}
 427
 428 147 itself (see supplementary material). Then the final expressions for τ_{ij}^{out} and τ_{ij}^{in} are

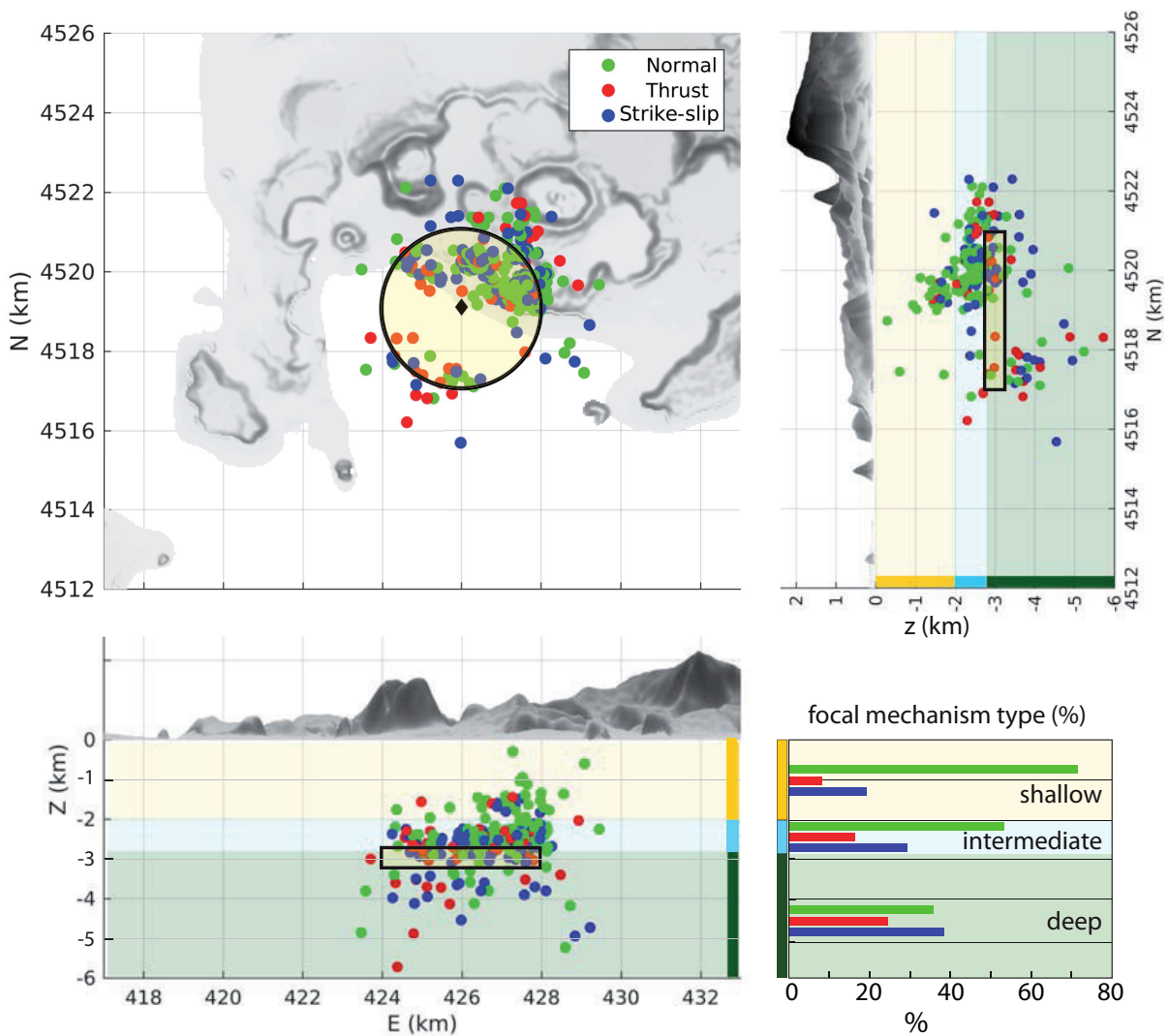
$$429 \quad \tau_{ij}^{out} = \lambda e_{kk}^{ns} \delta_{ij} + 2\mu (e_{ij}^s + e_{ij}^{ns}) \quad (15a)$$

$$430 \quad \tau_{ij}^{in} = \lambda (e_1 + e_{kk}^{ns}) \delta_{ij} + 2\mu (e_{ij}^s + e_{ij}^{ns}) - 3K e_0 \delta_{ij} \quad (15b)$$

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 436
 437 148 In order to test the robustness of our results, and to check the correctness of the numerical integration used
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 439 149 in the present work, we compare our semi-analytical solutions to the one obtained through a completely
 440
 441 150 numerical method, which employs a surface distribution of orthogonal forces on the surface of the TPE
 442
 443 151 disk to account for the traction discontinuity on it. In fact, as the Green's function $G_{km}(\mathbf{x}, \mathbf{x}')$ yields the
 444
 445 152 displacement in the k -th direction at point \mathbf{x} due to a point force in the m -th direction at \mathbf{x}' , the surface
 446
 447 153 integral in eq. (4) can be seen as the displacement field given by point forces distributed over the surface

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 450 S of the inclusion and perpendicular to it. The difference between the results of the semi-analytical and
 451
 452 numerical methods for a shallow TPE inclusion with $c/a < 3$ (when non-singular contributions are relevant)
 453
 454 for both surface displacement and stress in the plane $x_3 = c$ (the median plane of the TPE disk, Figure S1)
 455
 456 are negligible, provided that, in the numerical model, the force distribution over the TPE source boundary
 457
 458 is dense enough.

159 **3. THE APPLICATION TO THE 1982-84 CAMPI FLEGREI UNREST**



496 Figure 3: Map and N-S (view from east) and E-W (view from south) vertical sections of the Campi Flegrei Caldera. The
 497 topography is vertically exaggerated. Dots represent earthquake locations (D'Auria et al., 2014) occurred during the 1982-84
 498 unrest episode. Normal, thrust and strike-slip mechanisms are associated respectively to green, red and blue colours. The black
 499 circle and its projection on the vertical sections represent a tentative location of the TPE inclusion, whose center is shown with
 500 a black diamond. Histograms show the percentage of focal mechanism type over the total number of earthquakes located in
 501 the relative depth range. The three depth ranges define the shallow (0-2 km, yellow background), intermediate (2-2.8 km, light
 502 blue background) and deep (2.8-6 km, dark green background) zone, respectively.

505
506 160 Campi Flegrei is a nested caldera (Figure 1) located west of the city of Naples, with external and internal
507
508 161 diameters of about 14 km and 12 km, respectively. Volcanic activity has occurred there since 47,000 years
509
510 162 ago (De Vivo, 2006), seeing two major eruptive episodes approximately 39,000 and 14,900 years BP, the
511
512 163 last magmatic eruption being that of Monte Nuovo in 1538 AD (Di Vito et al., 2016). In historical times
513
514 164 the whole caldera has experienced several cycles of subsidence and uplift (e.g. Di Vito et al., 1999; Di Vito
515
516 165 et al., 2016). Two significant phases of uplift recorded by leveling data started in the second half of the 20th
517
518 166 century, reaching their peaks in two major unrest episodes in 1969-1972 and 1982-1984 (Figure 1). At the
519
520 167 end of 1984 the uplift trend stopped, starting a subsidence phase with a much slower rate which lasted until
521
522 168 2005, when a new period of inflation took over at a slower rate. Both the subsidence and the recent uplift
523
524 169 phases were characterized by minor peaks of uplift superimposed on the global trend, which have always
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526 170 been followed by a fast recovery of their whole deformation (Gaeta et al., 2003).

526 171 The shape of ground deformation (Figure 1) remained practically unaltered during both up and down
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528 172 movements, maintaining the same features of the 1982-84 episode (Troise et al., 2018). Phases of unrest at
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530 173 Campi Flegrei have been monitored through several techniques over the time, including GPS and InSAR
531
532 174 data (Trasatti et al., 2015), seismic (D'Auria et al., 2014) and geochemical data (e.g. Chiodini et al., 2015),
533
534 175 gravimetry surveys (Berrino, 1994) and deep drillings (De Natale et al., 2016). Moreover, thanks to the
535
536 176 seismic tomography the annular shaped buried rim of the caldera was detected from 800-2000 m to 1800-
537
538 177 4000 m of depth beneath which a depressed limestone basement is present at less than 4000 m depth (Zollo
539
540 178 et al., 2003, Judenherc and Zollo, 2004). The TPE inclusion is expected within the buried rim of the inner
541
542 179 caldera, then in a depth range of 2-4 km as suggested by the tomographic study of Calò and Tramelli (2018).
543
544 180 Actually most of geothermal processes (gas emission and boiling pools) are located within few kilometers
545
546 181 from the center of the caldera (e.g. Solfatara crater in Figure 1; Chiodini et al., 2015) below which we assume
547
548 182 that the TPE source is located (Figure 3).

548 183 It is worth to notice that even if the caldera is located in the tectonic environment of the Campania
549
550 184 margin, which is characterized by extensional structures and normal fault activity (Lima et al., 2009), the
551
552 185 focal mechanisms distribution retrieved from the 1982-84 seismic data series, below the caldera (D'Auria
553
554 186 et al., 2014), is very heterogeneous (Figure 3), suggesting a dominant role of local deformation mechanisms
555
556 187 related to the volcanic environment. Moreover, the distribution of focal mechanisms is not uniform along
557
558 188 depth, as confirmed by the percentage of focal mechanism type computed over the total number of earth-

561
562 189 quakes occurred in the shallow (0-2 km), intermediate (2-2.8 km) and deep (2.8-6 km) zones, respectively
563
564 190 (Figure 3). Below the caldera there is a progressive increase of strike-slip mechanisms over depth (from 20
565
566 191 to 39%). The same is true for thrust mechanisms whose percentage changes from about 8 to 25%, while,
567
568 192 in contrast, there is a strong decrease in normal mechanisms percentage that reduces from 72 to 36%. The
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570 193 cut-off of the seismicity can be identified at about 4 km depth, even if the hypocenter depth was generally
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572 194 above 3 km (D’Auria et al., 2014).

573 195 Different deformation sources have been considered over the years to interpret the cause of the 1982-84
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575 196 unrest. Berrino et al. (1984) found that the observed bell-shaped pattern of ground uplift can be nicely fitted
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577 197 by a Mogi source located at about 3 km depth beneath the center of the caldera. Battaglia et al. (2006)
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579 198 inverted deformation and gravity data determining pressurized penny-shaped horizontal cracks located in
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581 199 the depth range 2.5 and 3.5 km, probably filled with aqueous fluids, as the probable sources of inflation at
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583 200 Campi Flegrei. Other authors (Amoruso et al., 2008), considering the same source model within a layered
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585 201 embedding medium, support the presence of magma in its interior. More recently, based on considerations
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587 202 about the ratios of the three moment tensor eigenvalues retrieved from the data, Trasatti et al. (2011)
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589 203 concluded that a mixed mode dislocation with both shear and tensile components, through which a magma
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591 204 volume might have intruded, is the most suitable deformation source for the event, ruling out the applicability
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593 205 of a pressurized ellipsoid.

593 206 Shallow magmatic intrusions (3-4 km depth) have been advocated as the origin of both the 1982-84 and
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595 207 the 2011-13 unrest episodes (Dvorak and Berrino, 1991; Macedonio et al., 2014). Purely magmatic models,
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597 208 however, fail in explaining the observed long lasting subsidence after the 1982-84 peak (Troise et al., 2018).
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599 209 Moreover, seismic tomography surveys (Judenherc and Zollo, 2004) found no evidence of shallow magma
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601 210 batches in the 3-4 km depth range, while they have highlighted a large sill at about 8 km depth which may
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603 211 feed the entire Neapolitan volcanic area (Zollo et al., 2008). Even the temperature profiles inferred from
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605 212 deep drilling projects (Carlino et al., 2012) are generally incompatible with the presence of magma at shallow
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607 213 depths (Trasatti et al., 2011).

608 609 214 *3.1. Choice of parameters*

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611 215 Firstly, we have to define an adequate set of parameters both for the dimensions of the inclusion and
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613 216 the properties of the medium. However we normalize all the TPE inclusion results to $|u_z|^{max}$, the maximum
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618 217 uplift at the free surface, which realizes on the symmetry axis of the system, and we show patterns using
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620 218 spatial coordinates normalized to the radius of the TPE disk. Accordingly the choice of parameters slightly
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622 219 affects the results shown. The radius of the TPE inclusion and its depth are preliminarily chosen as $a = 2000$
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624 220 m and $c = 3000$ m as suggested by Battaglia et al. (2006), Amoruso et al. (2008) and D’Auria et al. (2014),
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626 221 employing pressurized horizontal cavities. These parameters are also suggested by the seismicity distribution
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628 222 and the location (between 2 and 4 km) of a shallow V_P/V_S -anomaly possibly related to an overpressurized
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630 223 fluid volume (Chiarabba and Moretti, 2006, Zollo et al., 2008; Calò and Tramelli, 2018). The disk height is
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632 224 chosen so that the ratio $\frac{d}{a} \ll 1$ is suitable to allow the potential expansion in equation (12). For the chosen
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634 225 parameters $|u_z|^{max}$ is in the order of tens of centimeters.

635 226 According to Belardinelli et al. (2019), the elastic parameters in isothermal and drained conditions of
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637 227 the poro-elastic matrix are $\lambda = 4$ GPa, $\mu = 6$ GPa ($\nu = 0.2$). The thermal expansion coefficient of the TPE
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639 228 source is $\alpha = 3 \cdot 10^{-5} \text{K}^{-1}$, while $H = 10$ GPa (see eq. 3). These values are pertinent to highly porous
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641 229 sedimentary rocks (Rice and Cleary, 1976), such as those constituting much of the upper stratigraphy of the
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643 230 Campi Flegrei caldera (Lima et al., 2009).

644 231 Finally, the changes in temperature and pore pressure within the inclusion are assumed respectively in
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646 232 the order of $\Delta T = 100$ K, $\Delta p = 10$ MPa. The assumption of a 100 K temperature jump is a reasonable
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648 233 order of magnitude if we consider the injection of overheated and overpressurized volatiles from a deep
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650 234 reservoir into a shallower system as sketched in Figure 2. Shallow water reservoirs in the Campi Flegrei
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652 235 area are associated with temperatures between 150°C and 250°C (Carlino et al., 2012), while the critical
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654 236 temperature of water is 373.9°C . An order of magnitude of tens MPa for Δp is well within the difference
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656 237 between the lithostatic and hydrostatic pore pressure at 3 km depth.

657 238 4. RESULTS

660 239 Given the axial symmetry of the TPE inclusion with respect to the vertical axis z , we provide results
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662 240 using the cylindrical reference frame $(\rho, \varphi, z = x_3)$ shown in Figure 2.

663 241 At the free surface, the resulting displacement components are illustrated in Figure 4a (solid lines) as
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665 242 functions of ρ/a , where ρ is the horizontal distance from the z axis (see Figure 2). Figure 5a and b show the
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667 243 components of the stress tensor over the median plane of the TPE inclusion ($x_3 = 3$ km) and slightly above
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669 244 it ($x_3 = 2.5$ km), respectively. In Figure 5a inside the TPE inclusion ($\rho < a$), the diagonal stress components

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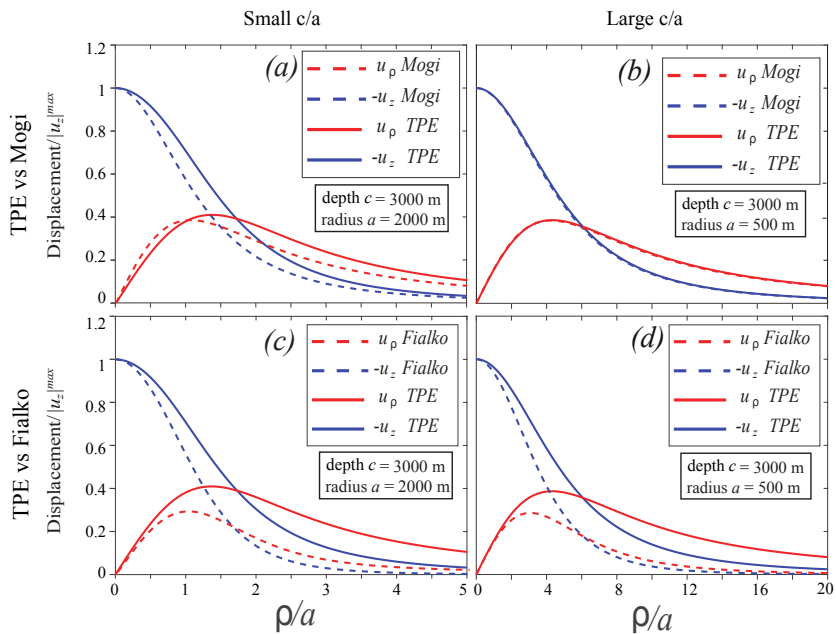


Figure 4: Displacement at the free surface. Comparison between the TPE inclusion and Mogi source (a, b) and TPE inclusion and Fialko source (c, d) of displacement (u_ρ , red lines) and vertical uplift ($-u_z$, blue lines) at free surface. Displacement components are normalized to the maximum value of the vertical uplift for each model ($|u_z|^{max}$). The horizontal distance ρ is normalized to the TPE inclusion radius a . All the source centers are placed in $(0, 0, c)$ with $c = 3000$ m. In panels (a) and (c) we assume a large c/a ratio for the TPE inclusion ($a=500$ m, $d = 40$ m), in panel (b, d) we assume a small c/a ratio for the TPE inclusion ($a=2000$ m, $d = 200$ m as used in the present work). The volume of the Mogi source is always assumed as equal to the one of the TPE inclusion, so its radius is 843 m in panel (a) and 196 m in panel (b), while Fialko sources have the same radius as the TPE source. Note the different scales in abscissa.

245 are almost constant for $\rho < 0.8a$ and $\tau_{zz}^{in} \gg \tau_{\rho\rho}^{in} > \tau_{\varphi\varphi}^{in}$ while, outside it ($\rho > a$), $\tau_{zz}^{out} > \tau_{\varphi\varphi}^{out} > \tau_{\rho\rho}^{out}$. Outside
246 the inclusion the stress components rapidly decay with ρ in agreement with the observed cut-off of seismicity
247 getting outside the TPE inclusion boundaries (black circle in Figure 3). All shear components vanish over
248 the median plane. Above the TPE inclusion, the stress strongly decreases and, at a depth of 2.5 km, it is
249 already reduced by two orders of magnitude (Figure 5b) even if the decay with ρ is less pronounced than in
250 Figure 5a. It is worth to notice that, for $\rho < a$, inside the TPE inclusion (Figure 5a), τ_{zz} is the maximum
251 normal stress, while above it (Figure 5b), it is the least one. Furthermore, a significant shear component
252 $\tau_{\rho z}$ appears above the inclusion while other shear components $\tau_{\rho\varphi}$ and $\tau_{z\varphi}$ vanish as a consequence of axial
253 symmetry.

254 Myklestad (1942) addressed the problem of a semi-infinite circular cylinder in an infinite solid inside
255 which a uniform increase in temperature occurs, retrieving analytical solutions for normal and shear stresses
256 both within and outside the source. Notably, both the models predict the same compressive stress regime
257 within the sources, with both $\tau_{\phi\phi}$ and τ_{zz} changing sign from inside to outside the cylinder (compare fig.
258 5 a with Myklestad, 1942, fig. 2, bottom right). Some differences arise in the normal stress components

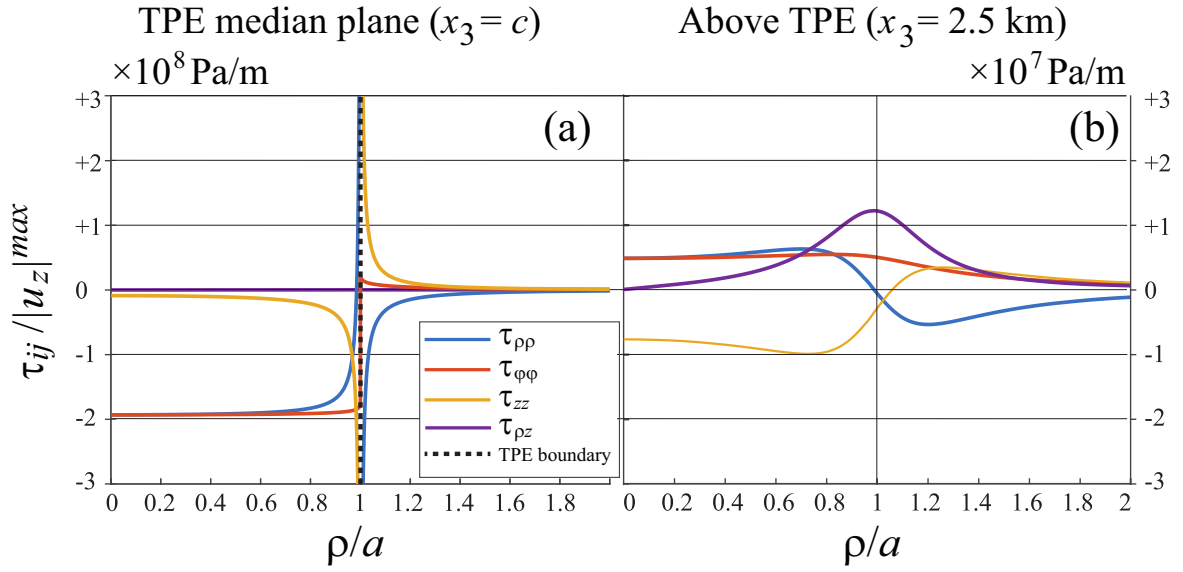


Figure 5: Stress components generated by the TPE disk. a) On the median plane ($z = c = 3$ km) of the TPE inclusion and b) above it ($z = 2.5$ km), stress components τ_{ij} as functions of horizontal distance from the center ρ/a . $|u_z|^{max}$ is the maximum value of vertical uplift. The black dashed line in panel (a) represents the TPE disk boundary $\rho = a$. The TPE disk radius is $a = 2$ km.

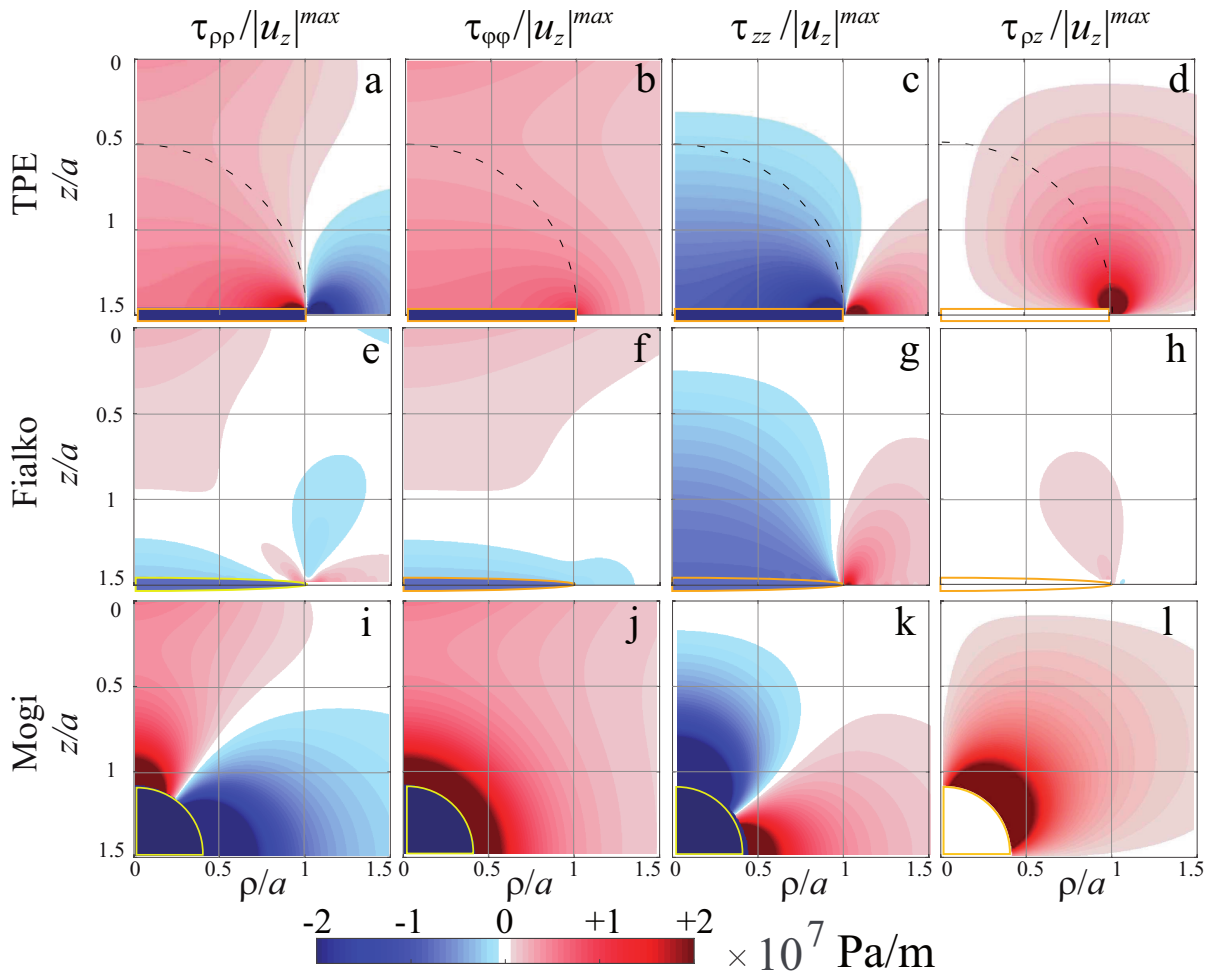
259 calculated on a plane perpendicular to the axis of the cylinder and just below its base (Myklestad, 1942,
 260 fig. 2, bottom left) with respect to the ones we retrieved above the TPE disk (fig. 5 b), likely due to the
 261 different geometry of the sources and the free surface condition affecting the results of fig. 5 b.

262 In Figure 4 the TPE disk displacement is compared with results for a point-source approximation of a
 263 spherical pressurized source (Mogi, 1958, Figure 4a and b, dashed lines) and a penny-shaped crack (Fialko
 264 et al., 2001, Figure 4c and d, dashed lines); in the following these sources are simply referred as Mogi and
 265 Fialko, respectively. We recall that outside the spherical TPE shell inclusion considered in Belardinelli et al.
 266 (2019) for assumed values of e_1 , external radius a_2 and internal radius $a_1 < a_2$, (please note the different
 267 notation with respect to that paper), results are the same of a Mogi source with the same center, radius
 268 $a = a_2$ and overpressure $\Delta P = \frac{4}{3}\mu e_1 \frac{a_2^3 - a_1^3}{a_2^3}$. Accordingly outside the source, $r > a_2$, the Mogi source results
 269 are coincident with the ones for the TPE shell inclusion considered in Belardinelli et al. (2019).

270 In order to compare results for both displacement and stress, we assume the same source depth ($c =$
 271 3000 m) while the same volume as in the TPE inclusion is assumed for the Mogi source and the same radius
 272 ($a = 2000$ m) for the Fialko source. Results are normalized to $|u_z|^{max}$, the maximum uplift predicted by
 273 each model at the surface of the half-space. In this way we can compare the results of the three kinds of
 274 sources as if each of them would produce the same (1 m) maximum uplift at free surface, regardless of the

785 particular choice made for the parameters which affect the displacement linearly.
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788 In Figure 4b and d the displacement is evaluated assuming for the TPE inclusion a smaller radius a than
 789 stated in section 3.1, in order to evaluate the effect of a TPE disk with greater c/a ratio. In the case of the
 790 stated in section 3.1, in order to evaluate the effect of a TPE disk with greater c/a ratio. In the case of the
 791 larger c/a ratio, both the radial and the vertical displacement components produced at the free surface by the
 792 Mogi source and TPE disk are indistinguishable (Figure 4b). As the Mogi source already managed to fit in
 793 good approximation the geodetic data at Campi Flegrei (Dvorak and Berrino, 1991), the similarity between
 794 Mogi source and TPE disk are indistinguishable (Figure 4b). As the Mogi source already managed to fit in
 795 good approximation the geodetic data at Campi Flegrei (Dvorak and Berrino, 1991), the similarity between
 796 these results means that the model we consider cannot be ruled out in the first place in the interpretation
 797 of the causes of the uplift. However we shall see that the stress field induced by the TPE disk and the Mogi
 798 source are significantly different, in particular within the sources.
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832 Figure 6: Depth maps of cylindrical stress components. They are plotted over the $\rho - z$ section between the free surface ($\frac{z}{a} = 0$)
 833 and the depth of the sources ($\frac{z}{a} = 1.5$). a-d): cylinder-shaped TPE source; e-h): Fialko source; i-l): Mogi source. Stress
 834 values of each model are divided by $|u_z|^{max}$, the maximum uplift at the Earth surface predicted by the same model. Horizontal
 835 and vertical axes are normalized to the radius a of the TPE inclusion. The singular components of the the TPE disk stresses
 836 (obtained from equation 12 are not convergent along the circle $r = a$ (black dashed line in panels a-d) where the solution
 837 should be compared by analytical continuation.
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842 284 As for the Fialko model (Figure 4*c* and *d*), the displacement components show similar trends, but the
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844 285 maximum horizontal displacement in the case of the TPE source occurs farther from the origin than in
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846 286 the case of the Fialko source, regardless of the c/a ratio. Furthermore, the amplitudes of displacement
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848 287 components computed by TPE inclusion decrease more slowly away from the source than for Fialko. This
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850 288 means that the TPE model may describe situations where the horizontal deformation is not negligible even
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852 289 at considerable distances from the center of the area of maximum uplift, without requiring a greater depth.

853 290 Depth maps of the stress components for all the models considered are reported in Figure 6. For the
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855 291 Mogi model, the strain (supplementary material) and stress components were retrieved from the expression
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857 292 for displacement reported by Bonafede and Ferrari (2009) and the constitutive relation (2) with $\Delta T = 0$ and
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859 293 $\Delta p = 0$. The stress components of the Fialko model were instead obtained through numerical integration
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861 294 of the analytical expressions published in Fialko et al. (2001): this has been achieved through a modified
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863 295 version of the USGS dMODELS tool (Battaglia, 2017). The stress field of the TPE source (Figure 6*a*, *b*, *c*
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865 296 and *d*) differs considerably from the Mogi source (Figure 6*i*, *j*, *k* and *l*) and even more from Fialko (Figure
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867 297 6*e*, *f*, *g* and *h*). Similarities may be noted between the τ_{zz} components for the TPE inclusion and Fialko,
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869 298 while only TPE and Mogi sources display a significant $\tau_{\rho z}$ component. It is important to note finally that an
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871 299 extremely high deviatoric stress is present within the TPE source (as shown in Figure 5), while it vanishes
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873 300 within both the Mogi and Fialko sources where an isotropic pressure applies.

873 301 The differences between the stress components related to distinct models give rise respectively to a different
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875 302 distribution of expected fault mechanisms on the basis of the Frohlich triangle (Frohlich, 2001). According to
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877 303 this method, the favoured fault mechanisms in each point of the medium is computed by evaluating principal
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879 304 stresses and related axes orientations.

880 305 Plots of the expected fault mechanisms and the maximum shear stress on the same vertical section as in
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882 306 Figure 6 are reported for each model in Figure 7. The TPE source is associated with normal faults over an
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884 307 area spanning from the free surface to the upper base of the disk (Figure 2). The lateral extension of this
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886 308 domain reduces progressively with depth, laterally bounded by a region where thrust faults are expected.
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888 309 This pattern is similar to that related to the Mogi source (Figure 7*c*); in particular, both give rise to thrust
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890 310 faults on their median plane, but it is markedly different in the case of the the Fialko source (Figure 7*b*).
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892 311 It is important to note that inside the TPE source, thrust mechanisms are predicted with extremely high
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894 312 deviatoric stress, while the other sources (Mogi and Fialko) are pressurized cavities with internal vanishing
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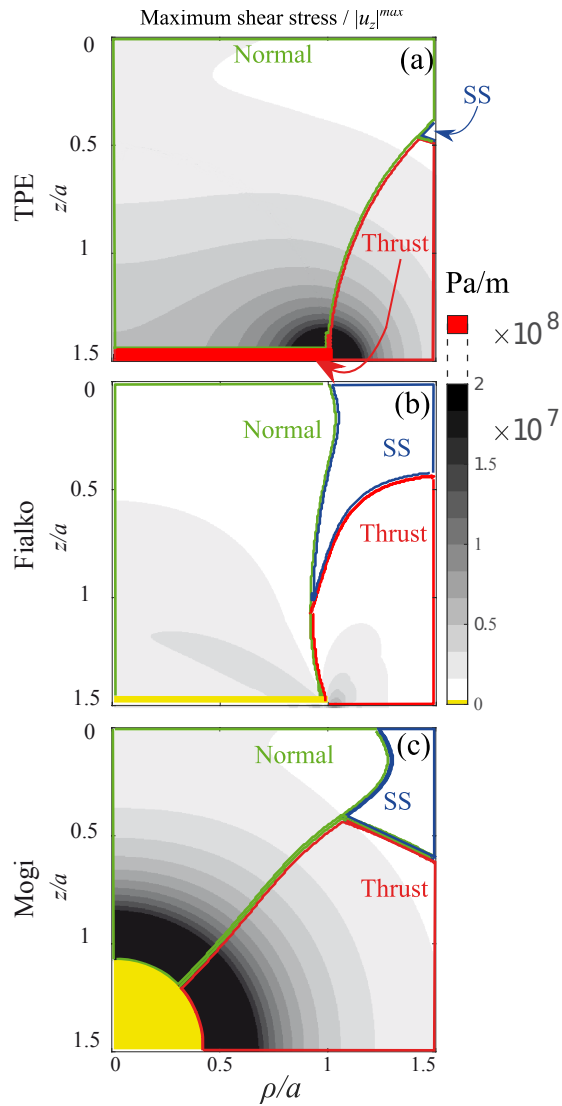


Figure 7: Vertical sections of maximum shear stress. The maximum shear stress (gray coloured palette) is plotted over the $\rho - z$ section between the free surface ($\frac{z}{a} = 0$) and the depth of the sources ($\frac{z}{a} = 1.5$). (a) TPE inclusion, (b) Fialko, (c) Mogi source. Contour includes areas in which each source promotes Normal, Thrust and Strike-Slip (SS) mechanisms. Horizontal and vertical axes are normalized to the radius a of the TPE inclusion. In panels (b) and (c) the internal domain of the sources, where shear stress vanishes, is represented in yellow.

313 deviatoric stress components.

314 In order to test the reasonability of parameters of the different models when applied to the Campi
 315 Flegrei unrest it is necessary to reproduce the actual deformation field observed during an unrest phase.
 316 We considered the data recorded through the EDM technique (changes of distance between benchmarks) and
 317 the vertical displacement recorded by leveling during the period June 1980 - June 1983 (Figure 1). The
 318 maximum uplift was 1.80 m in November 1984 (w.r.t. January 1982), about three times the uplift at the
 319 end of the considered observation period (Figure 1b). In order to accurately infer model parameter values
 320 from inversion of surface data, the hypothesis of a homogeneous medium, common to three different models

Table 1: Results of the inversions and misfits associated to the three models considered. Parameters estimated by inversion of surface data are in bold. TPE-Disk refers to the TPE disk models with fixed aspect ratios $\frac{d}{a} = 0.3$. In the case of the Mogi model the parameter estimated by inversion is $Q = \Delta P \cdot a^3 \frac{1-\nu}{\mu}$, while in the case of the TPE shell $Q = \frac{4}{3} e_0 (1 + \nu) (a_2^3 - a_1^3)$, representing the scaling factor for displacement at the surface. We assume $a = a_2 = 0.843$ km as in figures 6-7 and $\frac{a_2 - a_1}{a_2} = 0.3$, being a_1 the internal radius of the TPE shell. Values of ΔP for the Mogi model and e_0 for the TPE-shell are retrieved from the Q value estimated by inversion. Values of the Δp are retrieved from e_0 estimated through inversion assuming $\Delta T = 100$ K. The misfit in the last column refers to the sum of the absolute difference between predicted and observed EDM and leveling.

Model	c (km)	Q (m ³)	ΔP (MPa)	e_0	a (km)	Δp (MPa)	Total misfit (m)
Mogi	2.7	5.121 · 10⁶	64.1	–	–	–	3.868
Fialko	2.9	–	3	–	2.5	–	4.678
TPE-DISK	1.9	–	–	1.7 · 10⁻³	1.9	21	2.904
TPE-SHELL	2.7	5.121 · 10⁶	–	8.1 · 10⁻³	–	214	3.868

here considered, is inadequate (Trasatti et al., 2011). We are aware of this, but at least for the purpose of model comparison, the inversion of surface data is suitable.

For each model, a direct search in the parameter space was performed using a Monte Carlo sampling. Then the posterior probability density distribution (PPD) of each parameter was estimated by Bayesian inference (*e.g.* Sambridge, 1999). In Table 1 best fit values of parameters allowed free to vary during the inversion are indicated with bold numbers. Other values reported in Table 1 refer to parameters depending on free parameters and the fixed ones. Results for the Mogi source allow us to estimate the parameters of a TPE-shell model (Belardinelli et al., 2019) with the same center, an external radius a_2 and an internal radius a_1 assigned by fixing the ratio $\frac{a_2 - a_1}{a_2} = 0.3$. For the TPE-disk we fixed the geometrical ratio $\frac{d}{a} < 1$ at different values finding that smaller values require shallower and wider disks to reproduce data and the minimum misfit is realized by fixing $\frac{d}{a} = 0.3$. From Table 1 we can see that the TPE-disk provides the minimum misfit among the three considered models. An Akaike test (*e.g.* Hurvich and Tsai, 1989) shows that the misfit improvement justifies the increase in the number of parameters.

In Figure 8 we can note that employing best fit values of parameters, the TPE-disk reproduces well both kinds of data, while the Mogi model describes worse leveling data and the Fialko model underestimates EDM data. It is worth to mention that, according to Dieterich and Decker (1975), horizontal data have greater resolving power among different deformation source models.

5. DISCUSSION

We consider a disk-shaped thermo-poro-elastic inclusion embedded in a poro-elastic semi-infinite medium bounded by a free surface (Figure 2) in order to model a sudden input of hot and pressurized fluids from

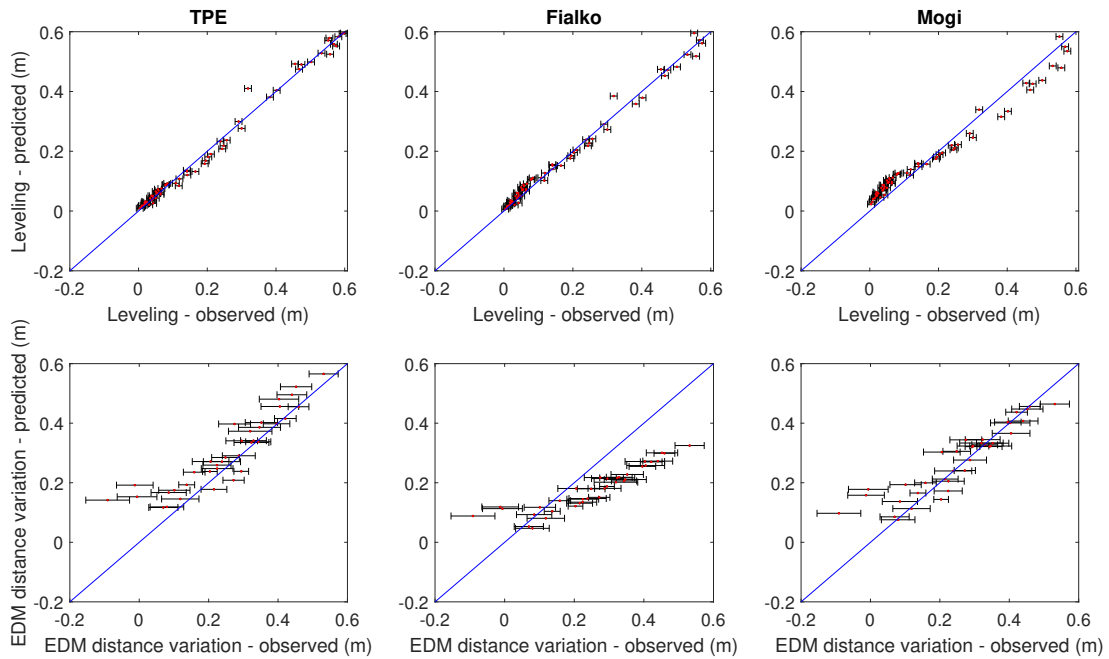


Figure 8: Results of the inversion of leveling (upper row) and EDM (lower row) data of displacement for the period June 1980 and in June 1983 at Campi Flegrei using three different source models (indicated).

341 an underlying magma body into a permeable region as envisaged by many authors for the Campi Flegrei
 342 caldera (e.g. Chiodini et al., 2015; Trasatti et al., 2019, Calò and Tramelli, 2018). Our semi-analytical
 343 computations are tested with a fully numerical approach (Figure S1).

344 The present model is intended to describe surface ground deformation and stress field at depth in
 345 hydrothermal regions, and we focus on the 1982-84 unrest episode at Campi Flegrei caldera. The adopted
 346 elastic parameters for the external medium and the inclusion represent highly-porous sedimentary rocks
 347 which constitute the upper layers of Campi Flegrei stratigraphy.

348 We compare our results to those of two axially-symmetric source models that have been employed in
 349 similar situations: Mogi and Fialko sources. The displacements on the free surface (Figure 4) are in good
 350 agreement with those of a Mogi source, in the case of a large c/a ratio, while there are some differences with
 351 the Fialko source for both small and large c/a ratio; in that, in our case, the amplitudes of the displacement
 352 components decrease more slowly with distance from the source.

353 All considered sources promote normal fault mechanisms above them (Figure 7) in agreement with data
 354 at Campi Flegrei (Figure 3), and thrust mechanisms laterally. A strong deviatoric stress is retrieved within
 355 the TPE inclusion (e.g. Figure 5a), unlike Mogi and Fialko sources. The large deviatoric stress inside the

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1066 356 TPE disk is able to promote thrust faults and exceeds by one order of magnitude the values at the same
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1068 357 depth outside the source, explaining the increasing percentage of thrust fault mechanisms at increasing depth
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1070 358 (Figure 3).

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1072 359 Results of inversion (Table 1) show that in order to obtain 1/3 of the maximum uplift observed at
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1074 360 the surface during the 1982-1984 unrest at Campi Flegrei, the Mogi and Fialko sources require magma
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1076 361 overpressures of $\Delta P = 64.1$ and 3 MPa, respectively, for a reasonable value of the radius of the Mogi source,
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1078 362 $a = 843$ m, while the TPE-disk requires a pore pressure change of $\Delta p = 21$ MPa, for a temperature change
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1080 363 $\Delta T = 100$ K (we recall that according to equation 3, for the same uplift, the requested Δp decreases with
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1082 364 increasing ΔT). Following Trasatti et al. (2011), we can assume that to realize the 1.8 m of maximum uplift
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1084 365 observed in November 1983, these pressure estimates must be scaled by a factor of 3, leading to unrealistically
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1086 366 high magma overpressure values for the Mogi source ($\Delta P \approx 190$ MPa, $Q \approx 1.5 \cdot 10^7$ m³) with respect to
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1088 367 lithostatic values at less than 3 km depth. These parameters are comparable with previous estimates (e.g.
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1090 368 Berrino et al., 1984, $Q = 1.3 \cdot 10^7$ m³, $c = 2.8 \pm 0.2$ km and Bonafede and Ferrari, 2009, $Q = 1.6 \cdot 10^7$
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1092 369 m³, $c = 3$ km). A previous inversion for the Fialko source (Amoruso et al., 2008), despite considering a
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1094 370 different rigidity modulus with respect to the present work, confirms that this kind of source leads to much
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1096 371 lower overpressure estimation than that of the Mogi one ($\Delta P = 7$ MPa, $c = 3$ km, $a = 2.7$ km). The same
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1098 372 scaling (factor of 3) of the estimates in Table 1 leads, however, to unrealistically high pore pressure changes
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1100 373 Δp also in the case of both the TPE-disk and the TPE-shell. Therefore, we can exclude that the big uplift
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1102 374 observed during that episode of unrest was totally due to the hydrothermal processes modeled by the TPE
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1104 375 source. Instead the present model could be suitable to represent subsequent smaller episodes of uplift (\sim
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1106 376 cm) at Campi Flegrei (1989, 1994, 2000 and 2006), that were most likely related to shallow hydrothermal
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1108 377 processes (D’Auria et al., 2011). Actually, since 1989 volcanotectonic hypocenters have been confined almost
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1110 378 exclusively between 1 and 3 km depth, within the area of most important geothermal output (D’Auria et al.,
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1112 379 2011).

1110 380 The 1982-84 unrest could be likely ascribed to the combined effects of both the emplacement of a magma
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1112 381 body at shallow depths and hydrothermal processes. According to Trasatti et al. (2011), the magmatic
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1114 382 intrusion can be modeled as due to a dike emplacement in a compressive stress regime region below the
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1116 383 center of the caldera, consisting of a tensile dislocation with a reverse-slip component. As the TPE source
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1118 384 provides strong compressive stress regime inside, it can give support to the model of Trasatti et al. (2011)

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1122 385 suggesting that during dike emplacement, the latter may have met the TPE source. Furthermore thrust
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1124 386 faulting mechanisms are reported by Ekstrom (1994) and Nettles and Ekstrom (1998) in different volcanic
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1126 387 regions.

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1128 388 The Fialko model requires smaller ΔP than the Mogi source (Table 1). However, the presence of a
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1130 389 large magmatic reservoir at 2.9 km depth (Table 1) seems incompatible with the brittle rheology and with
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1132 390 temperatures met during deep drilling in nearby wells (400° C at 3 km depth, e.g. Carlino et al., 2012).With
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1134 391 respect to both Fialko and Mogi model , the main advantage of the TPE inclusion is the retrieval of a stress
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1136 392 field at different depths with strong differences between the interior and the exterior of the source, which
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1138 393 could account for the high heterogeneity of closely located seismic mechanisms observed at Campi Flegrei
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1140 394 during the 1982-84 episode. Moreover the TPE source: (i) differently from the Fialko model, can easily
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1142 395 explain the increase of the percentage of thrust mechanisms over depth (Figure 3); (ii) compared to the
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1144 396 Fialko model for the same maximum uplift at the surface the TPE disk generates much larger shear stresses
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1146 397 (Figure 7). The reason is that the crack represented by the Fialko model is very efficient in producing high
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1148 398 displacement with low overpressure and then low stresses.

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1150 399 All models fail to produce strike slip faulting apart from shallow far field regions, where in any case the
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1152 400 induced shear stress is small (Figure 7). Instead at Campi Flegrei strike-slip faulting is frequent in near field
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1154 401 (Figure 3). However, even a small additional component of regional stress may easily exchange the order of
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1156 402 τ_{zz} and $\tau_{\rho\rho}$ (Figure 5b), so that strike-slip faulting can be promoted in external regions close to TPE disk.

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1158 403 Both poro-elastic and thermo-elastic effects are considered in our model. Temperature changes are more
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1160 404 effective than pore-pressure changes in inducing strain due to the relative magnitudes of $\alpha\Delta T$ and $\frac{\Delta p}{H}$ in eq.
1161
1162 405 (3) for reasonable values of sudden increases of ΔT and Δp . However it may be argued that, as demonstrated
1163
1164 406 by previous studies on ground deformation in hydrothermal regions (e.g Hutnak et al., 2009; Fournier and
1165
1166 407 Chardot, 2012), surface uplift due to the fluid migration from a deep input of hot and pressurized fluids is
1167
1168 408 predominantly driven by the poro-elastic contribution for short timescales (as depending on the hydraulic
1169
1170 409 diffusivity and the depth of the basis of the reservoir). In the present work we assume changes in Δp and
1171
1172 410 ΔT to occur suddenly and uniformly over a specific volume at basis of the reservoir, that is the TPE, so
1173
1174 411 that the model does not account for fluid migration and it is suited to estimate the contribution to the
1175
1176 412 uplift increase observed in an hydrothermal region during a given time interval. In order to reproduce the
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1178 413 temporal dependence of an unrest process, after the sudden Δp and ΔT establishment within the TPE

1177
1178 414 region, it might be necessary to model the progressive migration of the initial changes in temperature and
1179
1180 415 pore pressure that could affect a wider region, starting from the inclusion considered here. For the afore-
1181
1182 416 mentioned reasons, we expect that during unrest episodes also the subsidence following the peak of uplift
1183
1184 417 may be mainly related to the decrease of Δp due to the fluid discharge from the TPE inclusion toward the
1185
1186 418 hydrostatic aquifers above, while ΔT may be considered unchanged during this stage. The assessment of
1187
1188 419 this hint is left for future developments of the present study.

1190 420 **6. CONCLUSIVE REMARKS**

1191
1192 421 The main result of the present work is that unlike Mogi and Fialko sources, the TPE source here proposed
1193
1194 422 allows for a large deviatoric stress promoting thrust fault mechanisms inside. Accordingly, the heterogeneity
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1196 423 of focal mechanisms observed at Campi Flegrei as in other volcanic provinces supports the existence of a TPE
1197
1198 424 source. Moreover, inverted-displacement results indicate that a TPE source can better model the surface
1199
1200 425 deformation than other sources. As suggested by the case of the 1982-1984 unrest episode at Campi Flegrei a
1201
1202 426 TPE source can be considered as part of a complex system of deformation sources where both hydrothermal
1203
1204 427 and magmatic processes contribute to the observed displacement field.

1205 428 Another major advantage of the TPE disk model over the Mogi one is that a large pore pressure change
1206
1207 429 Δp may be easily and quickly accomplished through vertical motion of the magmatic volatiles exolved at
1208
1209 430 lithostatic pressure by an underlying magma reservoir. Instead the pressure P of a dense and highly viscous
1210
1211 431 magma presumably decreases faster while uprising according to a "magmastatic" gradient (at least). Thus
1212
1213 432 within the same depth range, large Δp values are transferred much more easily and faster than similar ΔP
1214
1215 433 values.

1216 434 Further developments of this model could take into account the heterogeneity of the poro-elastic half-
1217
1218 435 space, attempting at simulating the observed stratigraphy at Campi Flegrei or in other volcanic areas.
1219
1220 436 We conclude remarking that such analytical or semi-analytical models as those we consider here are of
1221
1222 437 fundamental importance when it comes: *i*) to calibrate and assess the validity of more complex numerical
1223
1224 438 models; *ii*) to study sensitivities without having to re-grid, as may be necessary in numerical models; *iii*) to
1225
1226 439 quantify driving parameters using fast models in inversion / data assimilation ; *iv*) to study forecasts and
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1228 440 their range of uncertainties much easier than in numerical models because of the calculation speed.

1233
1234 441 **7. Acknowledgements**
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1236
1237 442 Two anonymous reviewers are gratefully acknowledged for constructive comments and fruitful suggestions
1238
1239 443 that helped in improving the revised version of the manuscript. We thank Elisa Trasatti for useful suggestions
1240
1241 444 and Luca D’Auria for the catalog of focal mechanisms related to the 1982-1984 unrest episode at Campi
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1245 446 **References**
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