

Supporting Information for

The double exciton state of conjugated chromophores with strong diradical character: insights from TDDFT calculations.

Sofia Canola^{a,b}, Juan Casado^c and Fabrizia Negri^{a,b}

^aUniversità di Bologna, Dipartimento di Chimica ‘G. Ciamician’, Via F. Selmi, 2, 40126 Bologna, Italy

^bINSTM, UdR Bologna, Italy.

^cDepartment of Physical Chemistry, University of Málaga, Andalucía-Tech, Campus de Teatinos s/n,
29071 Málaga, Spain

Table S1 Absolute energies of the CS and BS equilibrium structures for the systems investigated. The functional used in the calculations is indicated in each column, the basis set is 6-31G*

molecule	<i>CS B3LYP</i>	<i>BS B3LYP</i>	<i>CS CAM-B3LYP</i>	<i>BS CAM-B3LYP</i>
2TIO	-1716.112835	-1716.114497	-1715.587518	-1715.599069
QDTBDT	-2654.823343	-2654.826237	-2654.205229	-2654.221908
FP	-1460.135601	-1460.141536	-1459.271501	-1459.289888
DFB	-1919.852877	-1919.857490	-1918.738459	-1918.752805
BISPHE	-1382.737494	-1382.743254	-1381.914852	-1381.939840
TPQ	-1447.944339	-1447.952670	-1447.121301	-1447.148836
SHZ	-1535.228557	-1535.240897	-1534.329870	-1534.361897
QANTHENE	-2147.467558	-2147.481580	-2146.230673	-2146.264864

Table S2 Tetraradical character computed at different levels of theory (PUHF and PUDFT) for CS and BS optimized structures of the systems investigated. The basis set is 6-31G*

	y_1 <i>PUHF</i>			
Geometry →	<i>CS CAM-B3LYP</i>	<i>CS-B3LYP</i>	<i>BS UCAM-B3LYP</i>	<i>BS UB3LYP</i>
2TIO	0.10	0.11	0.09	0.11
QDTBDT	0.05	0.05	0.04	0.05
FP	0.15	0.17	0.16	0.17
DFB	0.14	0.19	0.19	0.20
BISPHE	0.06	0.06	0.02	0.02
TPQ	0.14	0.14	0.10	0.12
SHZ	0.22	0.24	0.25	0.26
QANTHENE	0.16	0.16	0.14	0.15
	y_1 <i>PUCAM</i>	y_1 <i>PUB3LYP</i>	y_1 <i>PUCAM</i>	y_1 <i>PUB3LYP</i>
Geometry →	<i>CS CAM-B3LYP</i>	<i>CS-B3LYP</i>	<i>BS UCAM-B3LYP</i>	<i>BS UB3LYP</i>
2TIO	0.00	0.00	0.00	0.00
QDTBDT	0.00	0.00	0.00	0.00
FP	0.00	0.00	0.00	0.00
DFB	0.00	0.00	0.00	0.00
BISPHE	0.00	0.00	0.00	0.00
TPQ	0.00	0.00	0.00	0.00
SHZ	0.01	0.00	0.01	0.00
QANTHENE	0.00	0.00	0.00	0.00

Table S3 Computed number of unpaired electrons N_u at different levels of theory for CS and BS optimized structures of the systems investigated. The basis set is 6-31G*

	$N_u(\text{UHF})$			
Geometry →	CS CAM-B3LYP	CS B3LYP	BS UCAM-B3LYP	BS UB3LYP
2TIO	3.83	4.12	4.21	4.27
QDTBDT	3.57	3.86	3.86	3.98
FP	5.66	6.02	5.98	6.15
DFB	6.49	7.81	7.68	7.95
BISPHE	5.45	5.66	4.68	4.80
TPQ	5.03	5.38	5.20	5.44
SHZ	6.92	7.19	7.13	7.29
QANTHENE	9.12	9.42	9.17	9.44
	$N_u(\text{UCAM})$	$N_u(\text{UB3LYP})$	$N_u(\text{UCAM})$	$N_u(\text{UB3LYP})$
Geometry →	CS CAM-B3LYP	CS B3LYP	BS UCAM-B3LYP	BS UB3LYP
2TIO	0.87	0.41	1.73	0.84
QDTBDT	1.15	0.62	1.64	0.91
FP	1.33	0.93	1.93	1.34
DFB	1.34	0.91	1.88	1.31
BISPHE	1.65	1.06	1.81	1.18
TPQ	1.54	1.10	1.96	1.43
SHZ	1.96	1.50	2.23	1.67
QANTHENE	2.08	1.68	2.23	1.82

Table S4 Overlap (S) between BS frontier molecular orbitals ($H_\alpha, H_\beta, L_\alpha, L_\beta$) obtained from UB3LYP/6-31G* calculations for the singlet open-shell configuration, along with the diradical character computed at PUHF and PUB3LYP levels. All the data are computed employing the BS UB3LYP/6-31G* optimized geometry.

	y_0 PUHF	y_0 PUB3LYP	$S(H_\alpha H_\beta)$	$S(L_\alpha L_\beta)$	$S(H_\alpha L_\beta)$ and $S(H_\beta L_\alpha)$
2TIO	0.67	0.10	0,57	-0,62	0,77
QDTBDT	0.68	0.14	0,52	-0,58	0,81
FP	0.80	0.34	0,26	-0,39	0,88
DFB	0.80	0.30	0,23	-0,42	-0,87
BISPHE	0.85	0.26	-0,41	0,46	0,89
TPQ	0.86	0.42	0,14	-0,34	0,89
SHZ	0.87	0.52	-0,23	0,26	0,96
QANTHENE	0.92	0.71	-0,11	0,14	0,96

Table S5 Excited electronic states from TDB3LYP/6-31G* calculations at geometries optimized with the CAM-B3LYP functional. The reference configuration was a restricted or unrestricted configuration as indicated. The double exciton state is identified only in TDUB3LYP (unrestricted open-shell singlet reference configuration) and SF TDUB3LYP (unrestricted open-shell triplet reference configuration)

Excited state character →	$(H \rightarrow L)$	$(H \rightarrow L)$	$(H \rightarrow L)$	$(H \rightarrow L)$
Type of calculation →	<i>TD-B3LYP/6-31G*</i>	<i>TD-B3LYP/6-31G*</i>	<i>TD-UB3LYP/6-31G*</i>	<i>exp</i>
Geometry →	<i>CS CAM-B3LYP</i>	<i>BS UCAM-B3LYP</i>	<i>BS UCAM-B3LYP</i>	
2TIO	2.09	1.66	1.80	1.88 ^b
QDTBDT	1.97	1.71	1.72-1.79	1.85 ^c
FP	1.61	1.30	1.53	1.48 ^d
DFB	1.22	1.00	1.16	1.25 ^e
BISPHE	1.41	1.34	1.47	1.43 ^f
TPQ	1.74	1.39	1.49	1.46 ^g
SHZ	1.21	1.00	1.49	1.50 ^h
QANTHENE	0.96	0.75	1.20	1.35 ⁱ
Excited state character →	$(H, H \rightarrow L, L)$	$(H, H \rightarrow L, L)$	$(H, H \rightarrow L, L)$	
Type of calculation →	<i>TD-UB3LYP/6-31G*</i>	<i>SF TD-B3LYP/6-31G*</i>	<i>exp</i>	
Geometry →	<i>BS UCAM-B3LYP</i>	<i>BS UCAM-B3LYP</i>		
2TIO	1.14	1.41	1.68 ^b	
QDTBDT	1.15	1.57	1.57 ^c	
FP	1.18	1.04	1.13 ^d	
DFB	0.93	0.86	0.92 ^e	
BISPHE	1.07	1.24	1.54 ^f	
TPQ	1.21	1.01	1.13 ^g	
SHZ	1.33	0.98	1.19 ^h	
QANTHENE	0.94	0.76	1.08 ⁱ	

^a Geometry optimized at CAM-B3LYP/6-31G* (CS) or UCAM-B3LYP/6-31G* (BS) levels of theory; ^bIn n-hexane from ref. [1]; ^cMeasured in CHCl₃ from ref. [2]; ^dIn CH₂Cl₂, from ref. [3]; ^eIn CH₂Cl₂ from ref. [4]; ^fIn CHCl₃, from ref [5] ^gMeasured in CH₂Cl₂ from ref. [6]; ^hIn CH₂Cl₂ from ref. [7]; ⁱIn CH₂Cl₂ from ref. [8].

Table S6 Computed TD-UB3LYP excitation energies, S^2 , wf composition, oscillator strength of the strongly one-photon active excited state (single exciton state or $(H \rightarrow L)$) and the available experimental data for the systems investigated.

Excited state character \rightarrow	$(H \rightarrow L)^a$					
	y_0 PUB3LYP	$E(eV)$	S^2	wf	f	Exp/eV
2TIO	0.10	1.81	0.70	0.57H α \rightarrow L α ; -0.57H β \rightarrow L β	0.883	1.88 ^b
QDTBDT	0.14	1.81	0.40	0.55H α \rightarrow L α ; -0.55H β \rightarrow L β	0.567	1.85 ^c
FP	0.34	1.51	0.35	0.67H α \rightarrow L α ; -0.67H β \rightarrow L β	0.617	1.48 ^d
DFB	0.30	1.13	0.79	0.58H α \rightarrow L α ; -0.58H β \rightarrow L β	0.177	1.25 ^e
BISPHE	0.26	1.47	0.04	0.70H α \rightarrow L α ; -0.70H β \rightarrow L β	0.552	1.43 ^f
TPQ	0.42	1.48	0.39	0.68H α \rightarrow L α ; -0.68H β \rightarrow L β	1.234	1.46 ^g
SHZ	0.52	1.49	0.44	0.62H α \rightarrow L α ; -0.62H β \rightarrow L β	0.086	1.50 ^h
QANTHENE	0.71	1.28	0.18	0.71H α \rightarrow L α ; -0.71H β \rightarrow L β	0.124	1.35 ⁱ

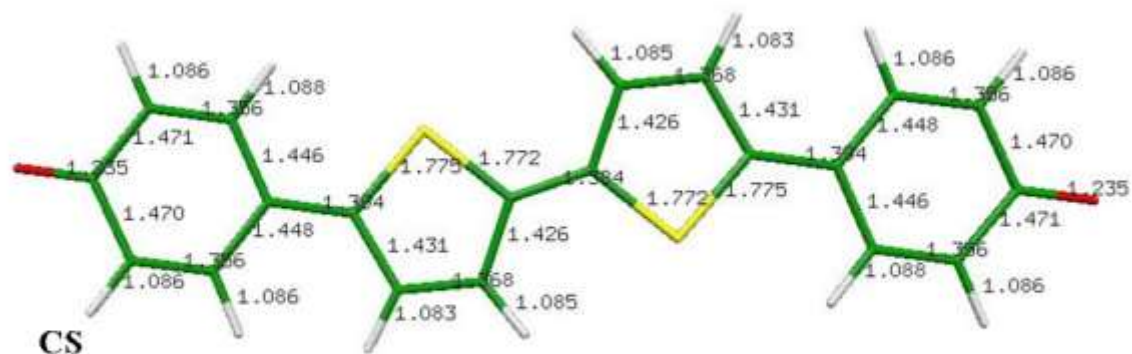
^a Geometry optimized at UB3LYP/6-31G* (BS) levels of theory; ^bIn n-hexane from ref. [1]; ^cMeasured in CHCl₃ from ref. [2]; ^dIn CH₂Cl₂, from ref. [3]; ^eIn CH₂Cl₂ from ref. [4]; ^fIn CHCl₃, from ref [5] ^gMeasured in CH₂Cl₂ from ref. [6]; ^hIn CH₂Cl₂ from ref. [7]; ⁱIn CH₂Cl₂ from ref. [8].

Table S7 Computed TD-UB3LYP excitation energies, S^2 , wf composition, oscillator strength of the one-photon forbidden excited state (double exciton state or $(H,H \rightarrow L,L)$) for the systems investigated.

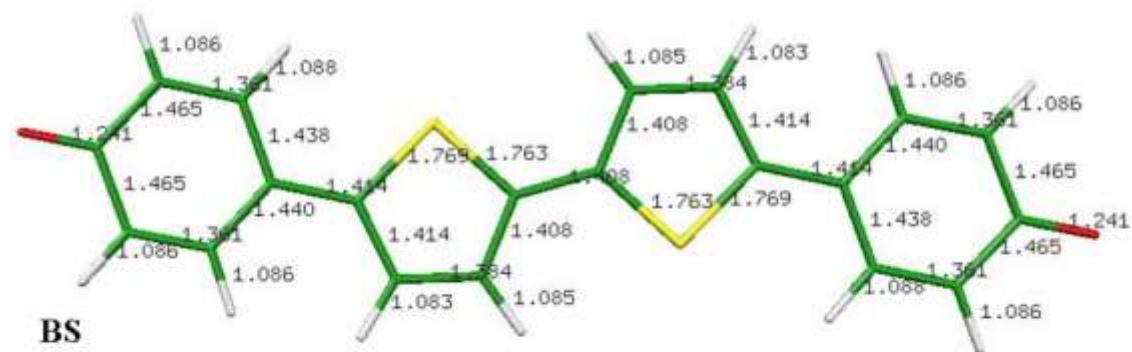
Excited state character \rightarrow	$(H,H \rightarrow L,L)^a$					
	y_0 PUB3LYP	$E(eV)$	S^2	wf	f	Exp/eV
2TIO	0.10	0.98	0.68	0.70H α \rightarrow L α ; 0.70H β \rightarrow L β	0.000	1.68 ^b
QDTBDT	0.14	1.07	0.48	0.70H α \rightarrow L α ; 0.70H β \rightarrow L β	0.000	1.57 ^c
FP	0.34	1.13	0.38	0.69H α \rightarrow L α ; 0.69H β \rightarrow L β	0.000	1.13 ^d
DFB	0.30	0.91	0.42	0.70H α \rightarrow L α ; 0.70H β \rightarrow L β	0.001	0.92 ^e
BISPHE	0.26	1.03	0.38	0.70H α \rightarrow L α ; 0.70H β \rightarrow L β	0.000	1.54 ^f
TPQ	0.42	1.16	0.35	0.69H α \rightarrow L α ; 0.69H β \rightarrow L β	0.000	1.13 ^g
SHZ	0.52	1.32	0.35	0.62H α \rightarrow L α ; 0.62H β \rightarrow L β	0.000	1.19 ^h
QANTHENE	0.71	1.17	0.30	0.69H α \rightarrow L α ; 0.69H β \rightarrow L β	0.000	1.08 ⁱ

^a Geometry optimized at CAM-B3LYP/6-31G* (CS) or UCAM-B3LYP/6-31G* (BS) levels of theory; ^bIn n-hexane from ref. [1]; ^cMeasured in CHCl₃ from ref. [2]; ^dIn CH₂Cl₂, from ref. [3]; ^eIn CH₂Cl₂ from ref. [4]; ^fIn CHCl₃, from ref [5] ^gMeasured in CH₂Cl₂ from ref. [6]; ^hIn CH₂Cl₂ from ref. [7]; ⁱIn CH₂Cl₂ from ref. [8].

B3LYP

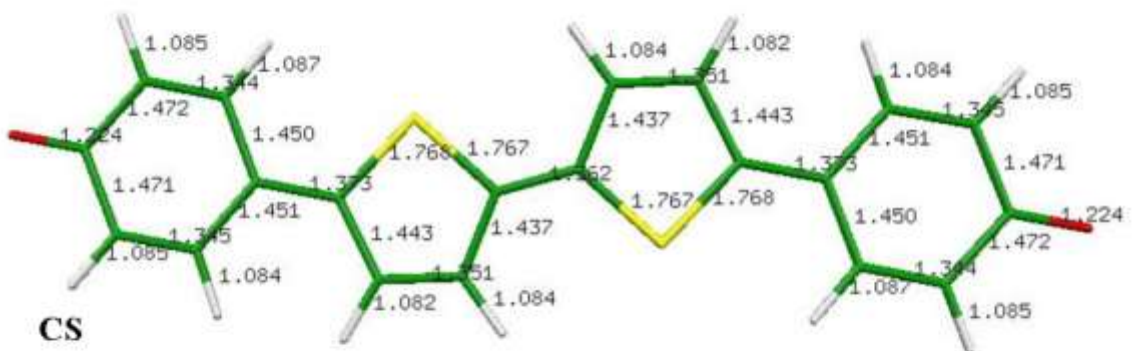


CS

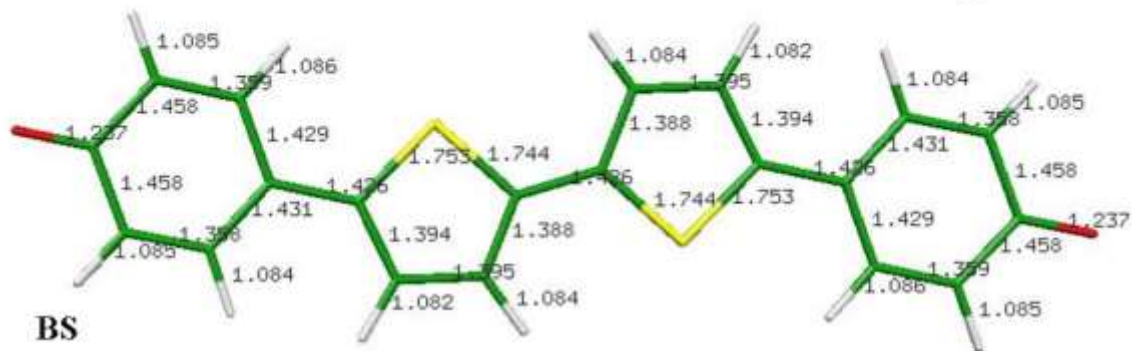


BS

CAM-B3LYP



CS



BS

Figure S1. 2TIO: (top) CS and BS equilibrium structures from B3LYP/6-31G* calculations, (bottom) CS and BS equilibrium structures from CAM-B3LYP/6-31G* calculations

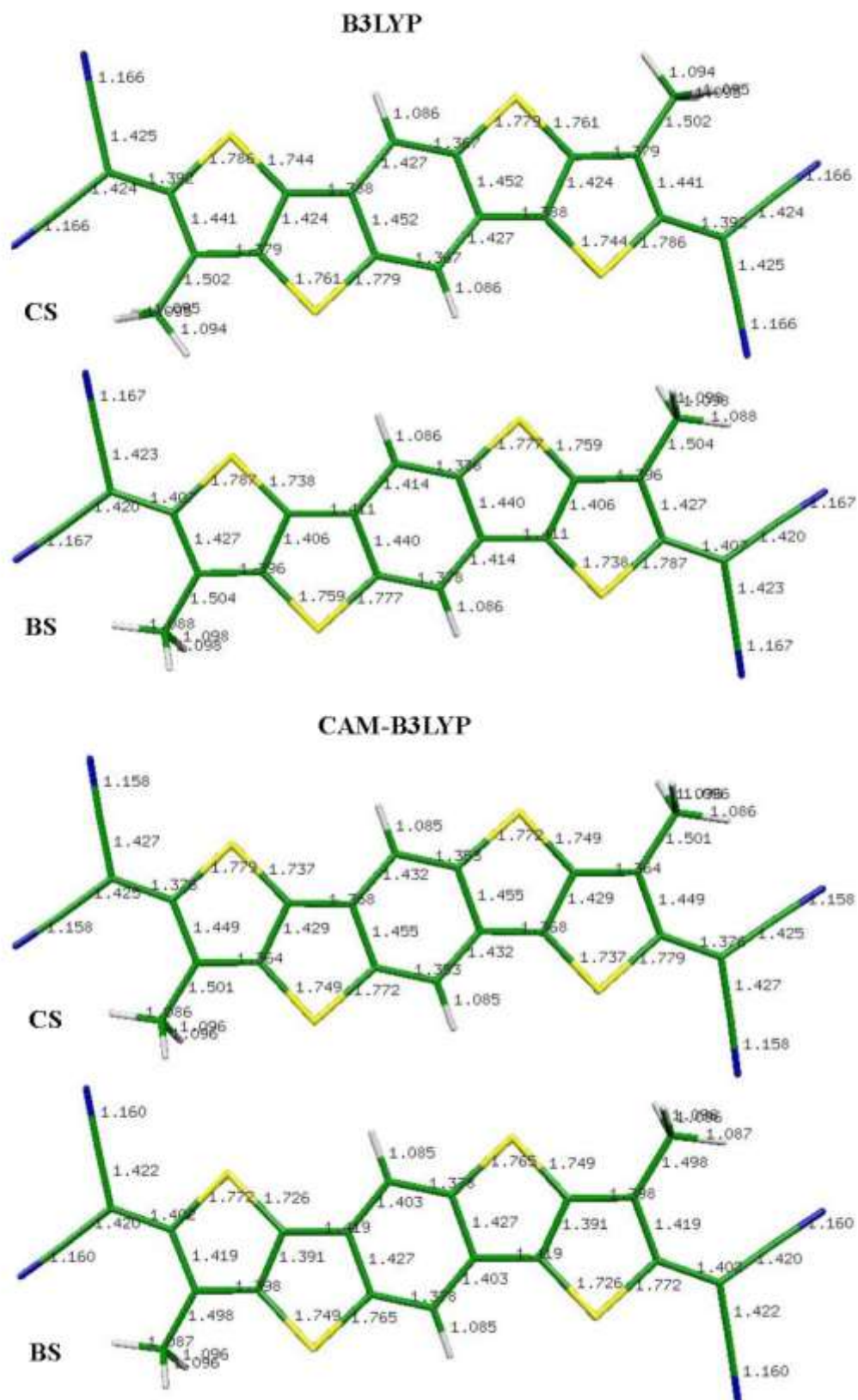


Figure S2. QDTBT: (top) CS and BS equilibrium structures from B3LYP/6-31G* calculations, (bottom) CS and BS equilibrium structures from CAM-B3LYP/6-31G* calculations

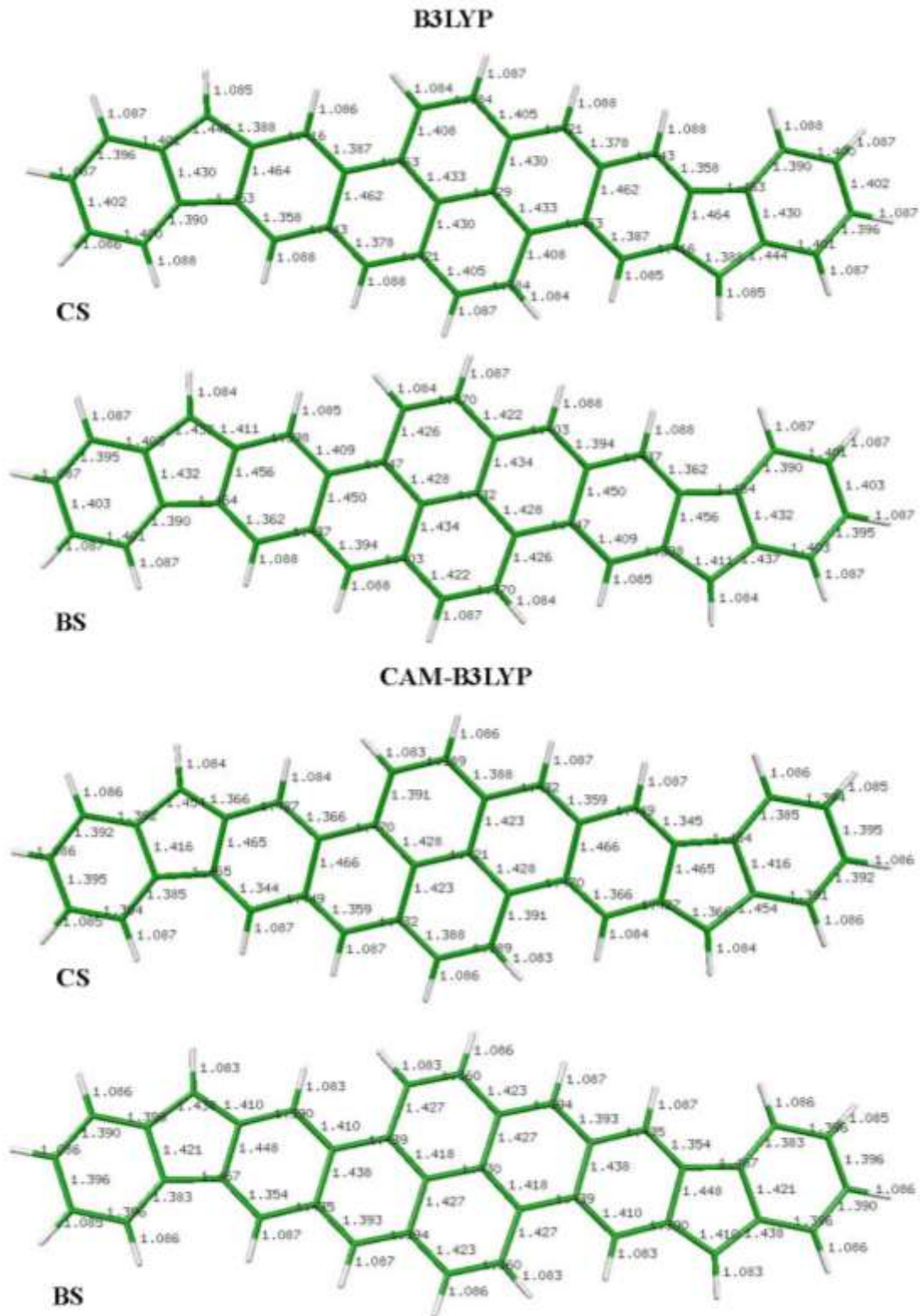


Figure S3. FP: (top) CS and BS equilibrium structures from B3LYP/6-31G* calculations, (bottom) CS and BS equilibrium structures from CAM-B3LYP/6-31G* calculations

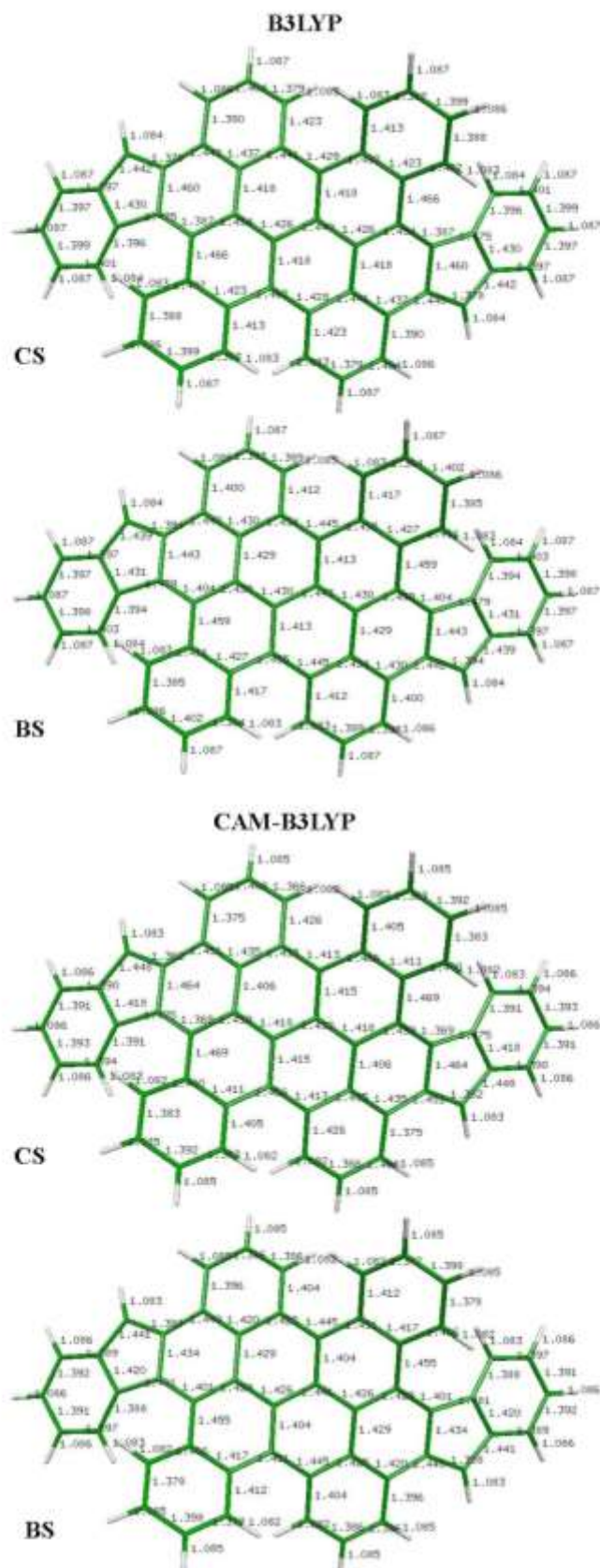


Figure S4. DFB: (top) CS and BS equilibrium structures from B3LYP/6-31G* calculations, (bottom) CS and BS equilibrium structures from CAM-B3LYP/6-31G* calculations

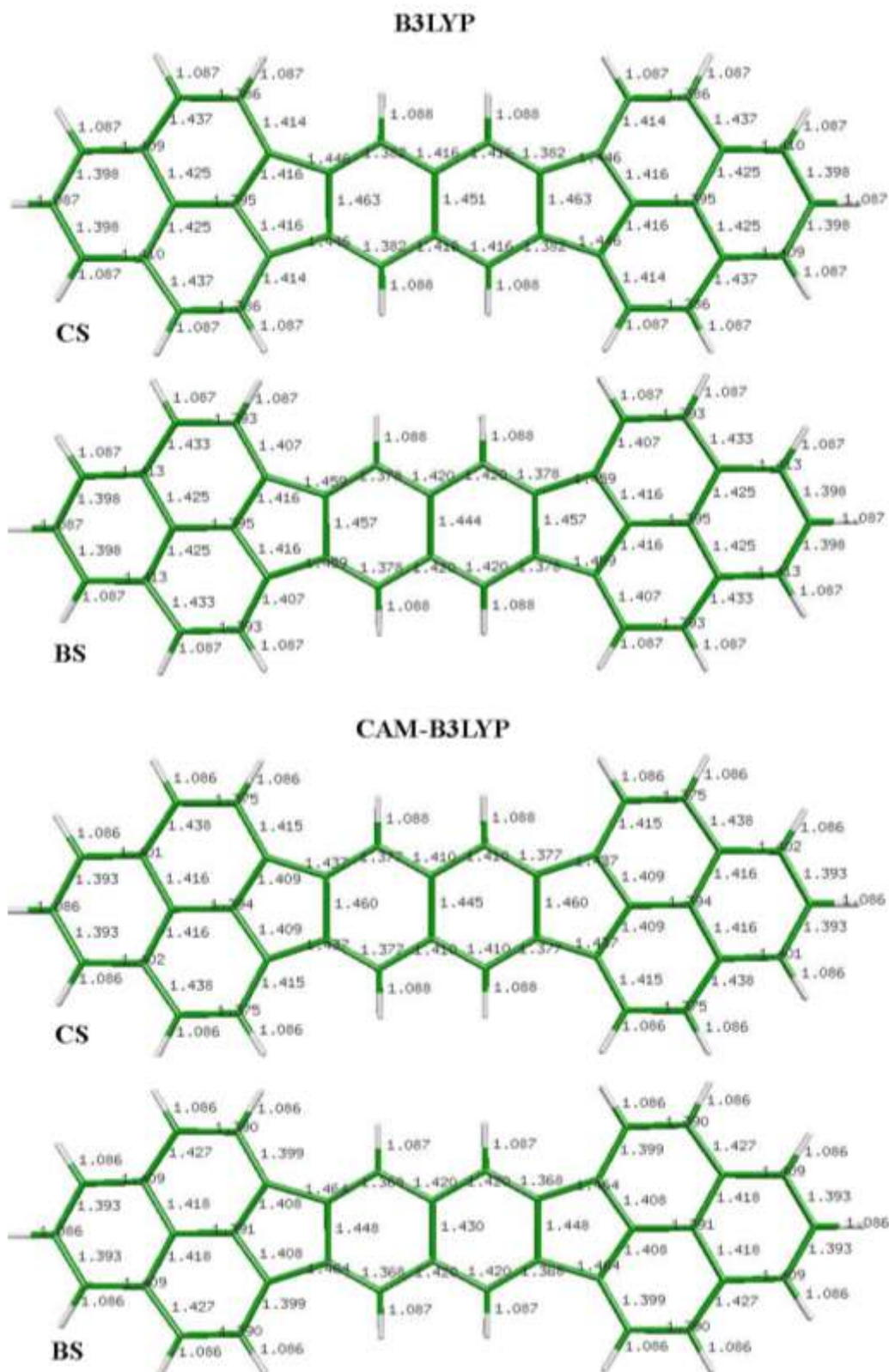
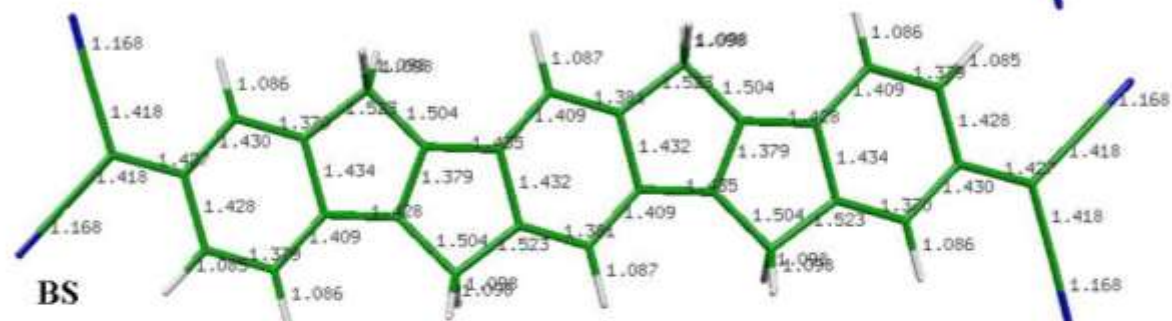
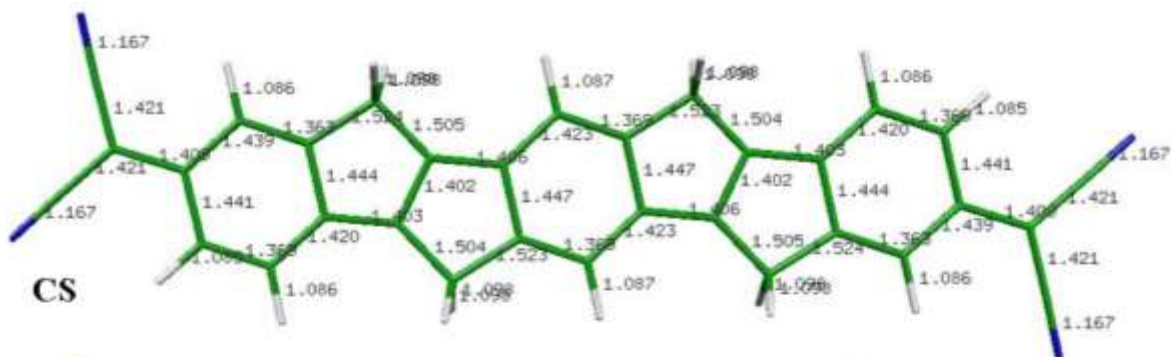


Figure S5. BISPHE: (top) CS and BS equilibrium structures from B3LYP/6-31G* calculations, (bottom) CS and BS equilibrium structures from CAM-B3LYP/6-31G* calculations

B3LYP



CAM-B3LYP

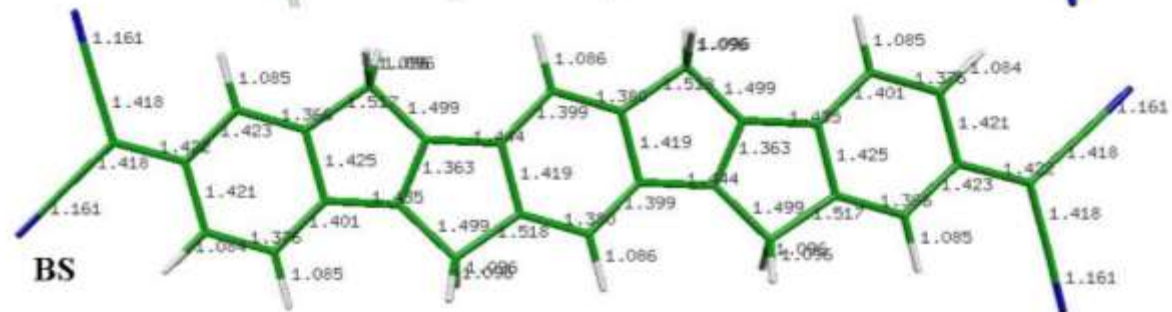
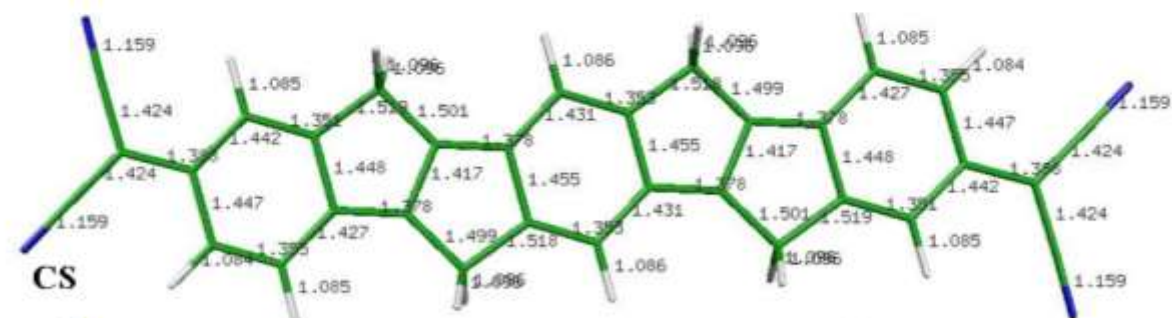


Figure S6. TPQ (top) CS and BS equilibrium structures from B3LYP/6-31G* calculations, (bottom) CS and BS equilibrium structures from CAM-B3LYP/6-31G* calculations

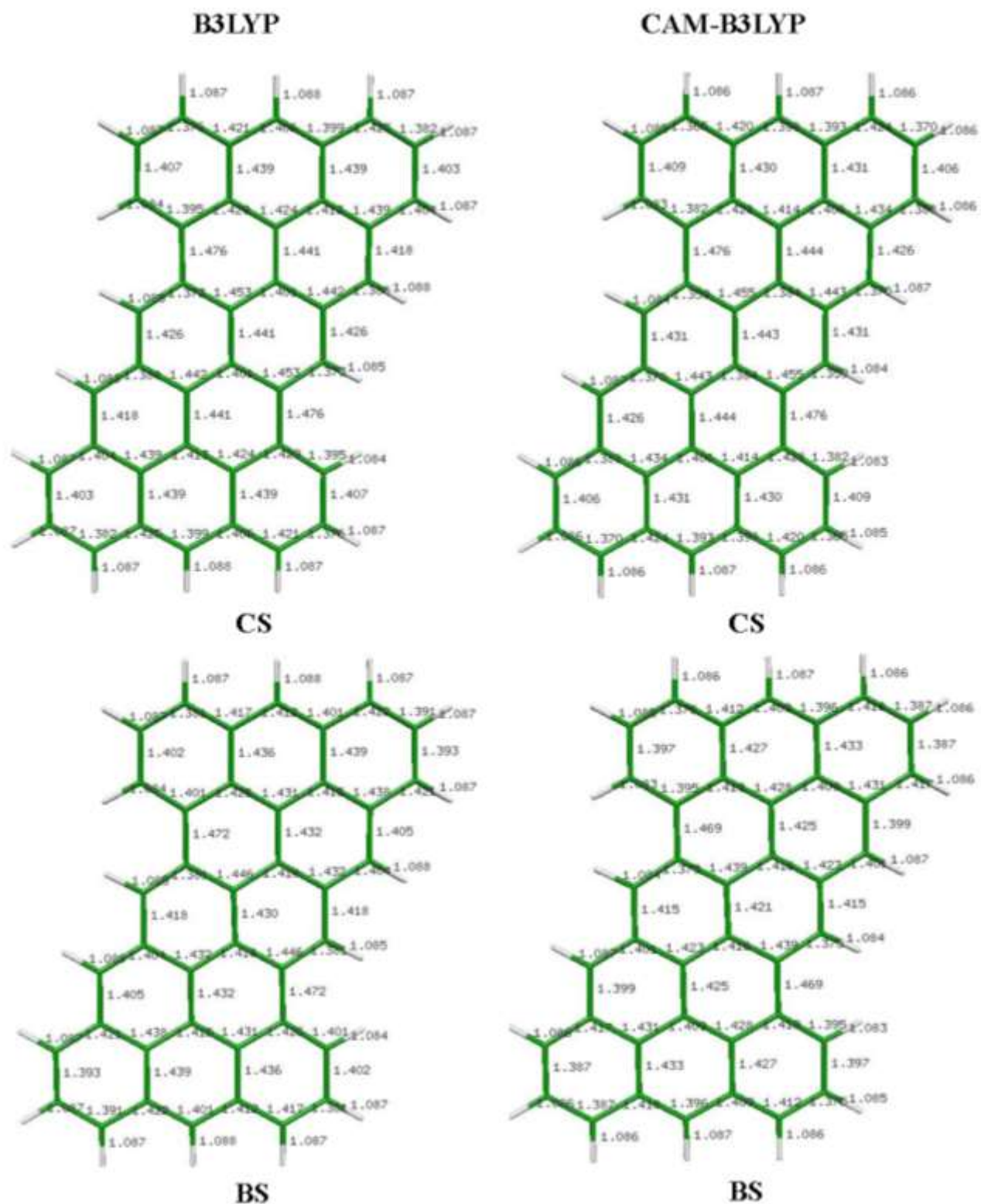


Figure S7. SHZ: (left) CS and BS equilibrium structures from B3LYP/6-31G* calculations, (right) CS and BS equilibrium structures from CAM-B3LYP/6-31G* calculations

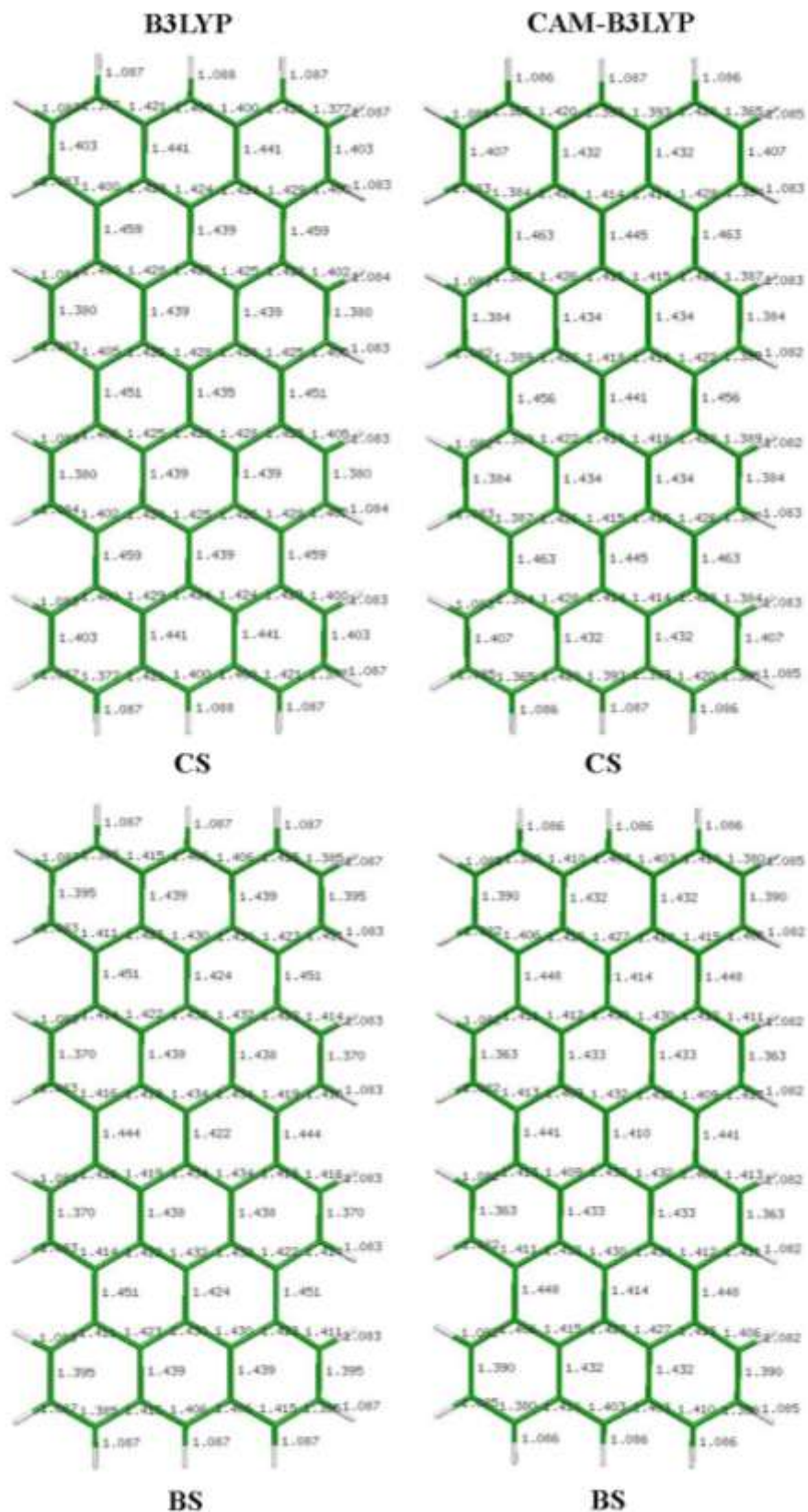


Figure S8. QANTHENE: (left) CS and BS equilibrium structures from B3LYP/6-31G* calculations, (right) CS and BS equilibrium structures from CAM-B3LYP/6-31G* calculations

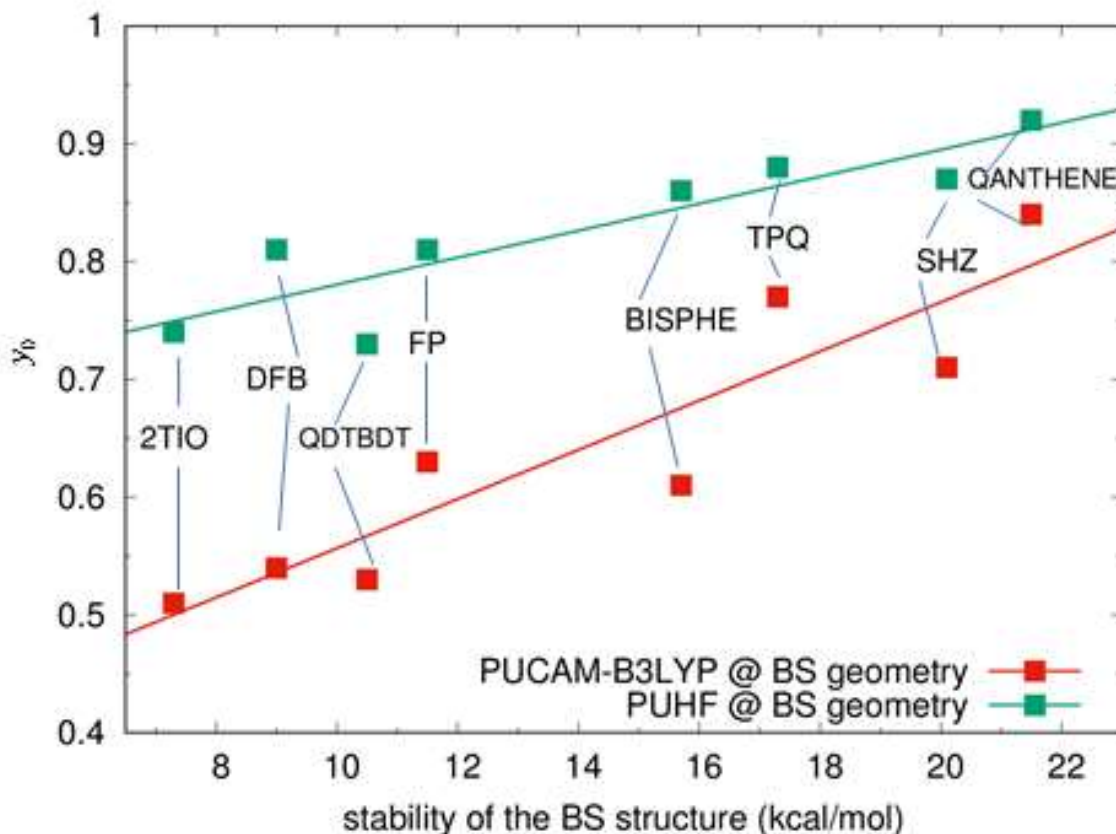


Figure S9. Correlation between the y_0 value computed at PUHF (green squares) or PUCAM-B3LYP (red squares) level and the computed stabilization of the BS structure with respect to the CS structure, both optimized at CAM-B3LYP/6-31G* level.

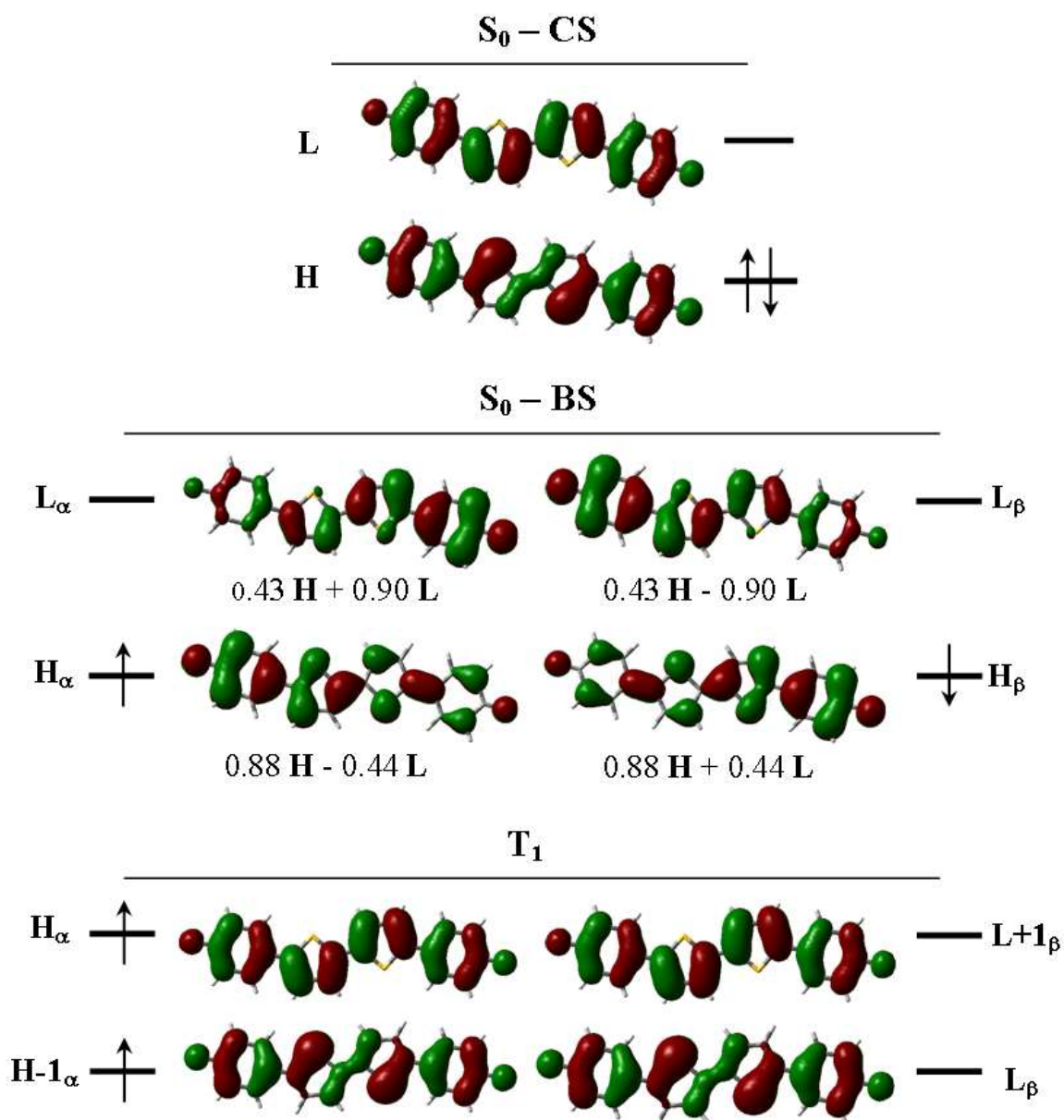


Figure S10. Frontier molecular orbitals of 2TIO computed with (top) a CS singlet reference configuration, (middle) a BS singlet open-shell configuration and (bottom) a triplet configuration, at the optimized BS UB3LYP geometry of the singlet ground state ($y_0(\text{PUHF}) = 0.67$). Each localized orbital (BS) is also expressed as a linear combination of the delocalized (CS) orbitals.

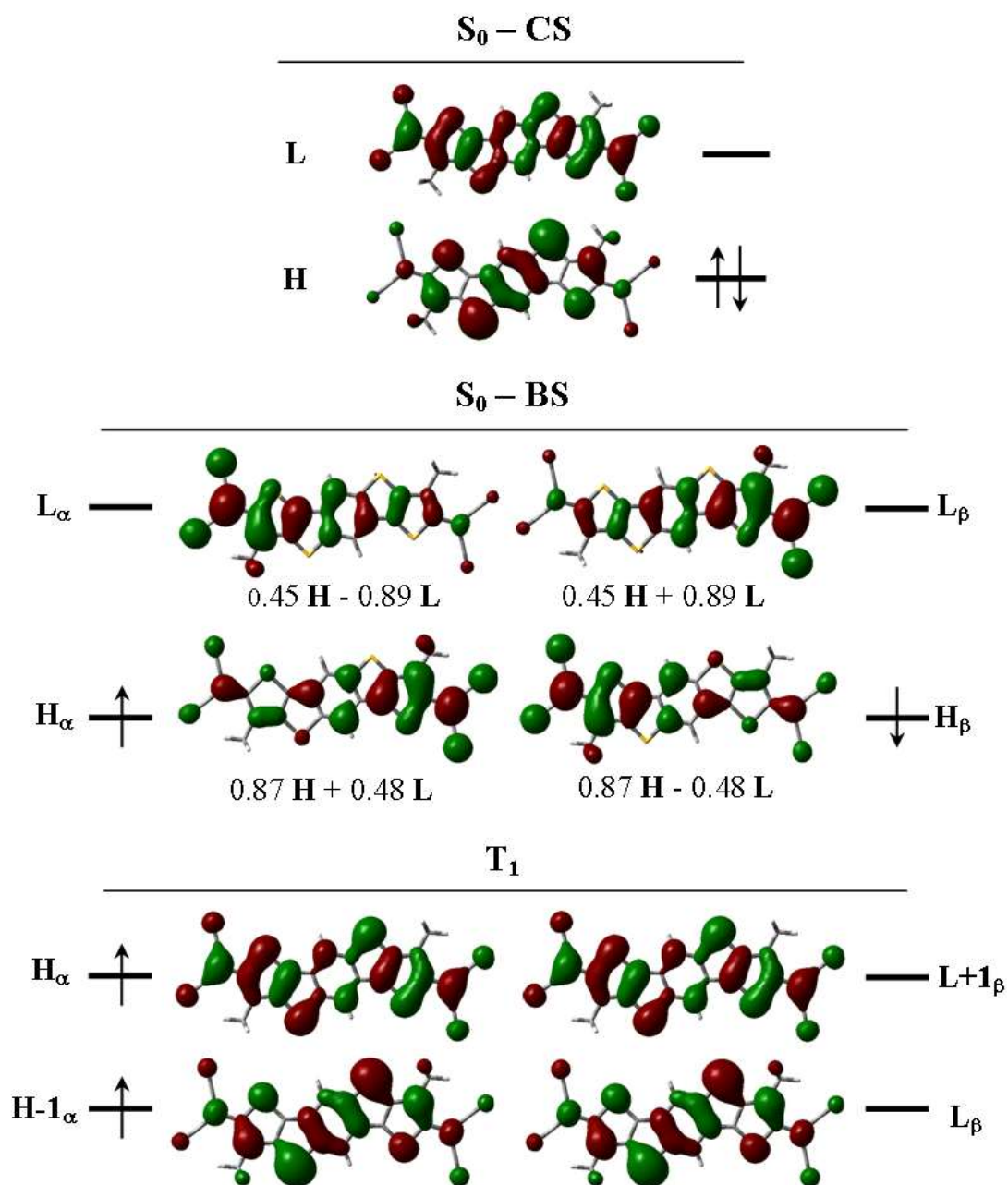


Figure S11. Frontier molecular orbitals of QDTBDT computed with (top) a CS singlet reference configuration, (middle) a BS singlet open-shell configuration and (bottom) a triplet configuration, at the optimized BS UB3LYP geometry of the singlet ground state ($y_0(PUHF) = 0.71$). Each localized orbital (BS) is also expressed as a linear combination of the delocalized (CS) orbitals.

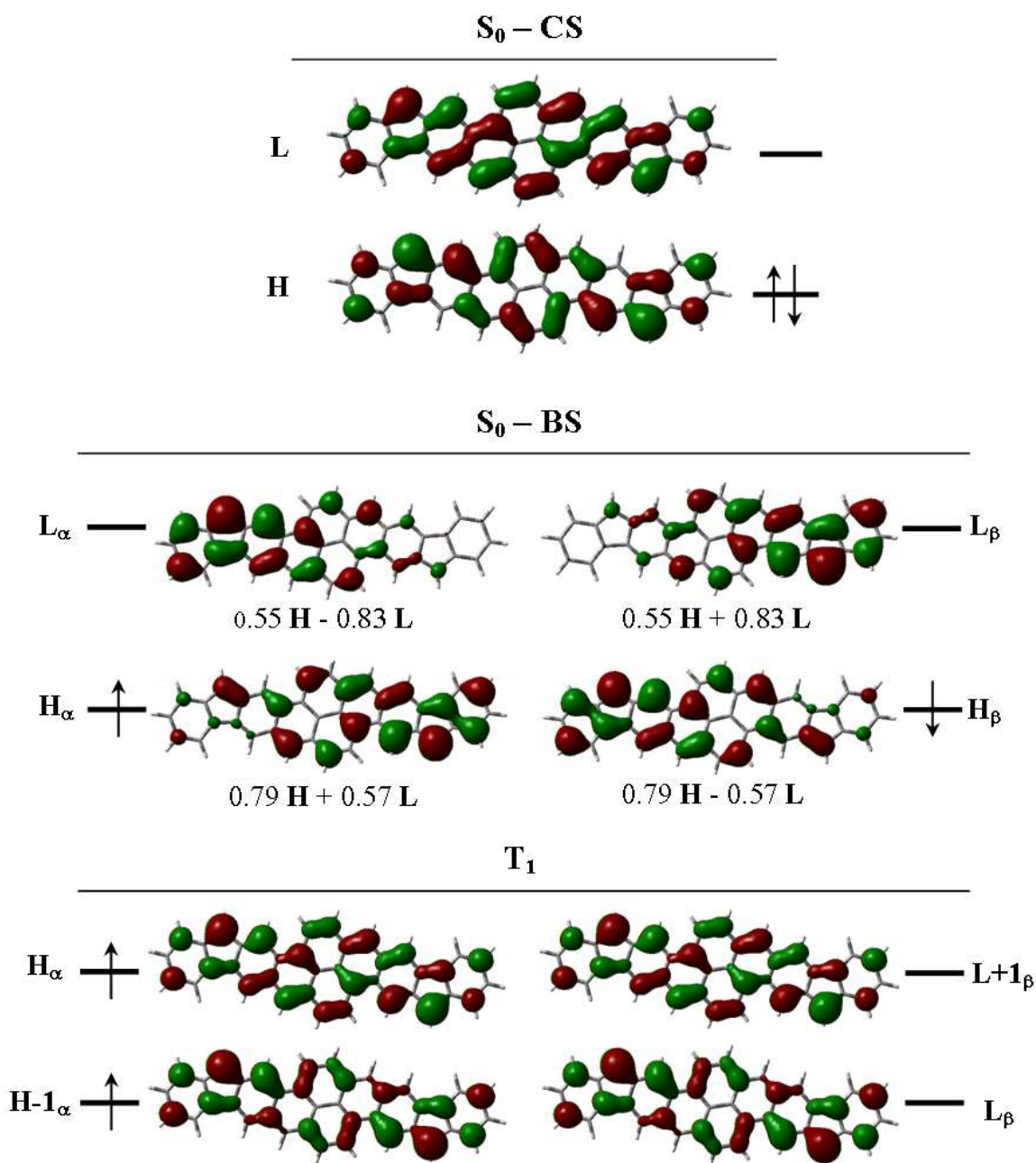


Figure S12. Frontier molecular orbitals of FP computed with (top) a CS singlet reference configuration, (middle) a BS singlet open-shell configuration and (bottom) a triplet configuration, at the optimized BS UB3LYP geometry of the singlet ground state ($y_0(\text{PUHF}) = 0.80$). Each localized orbital (BS) is also expressed as a linear combination of the delocalized (CS) orbitals.

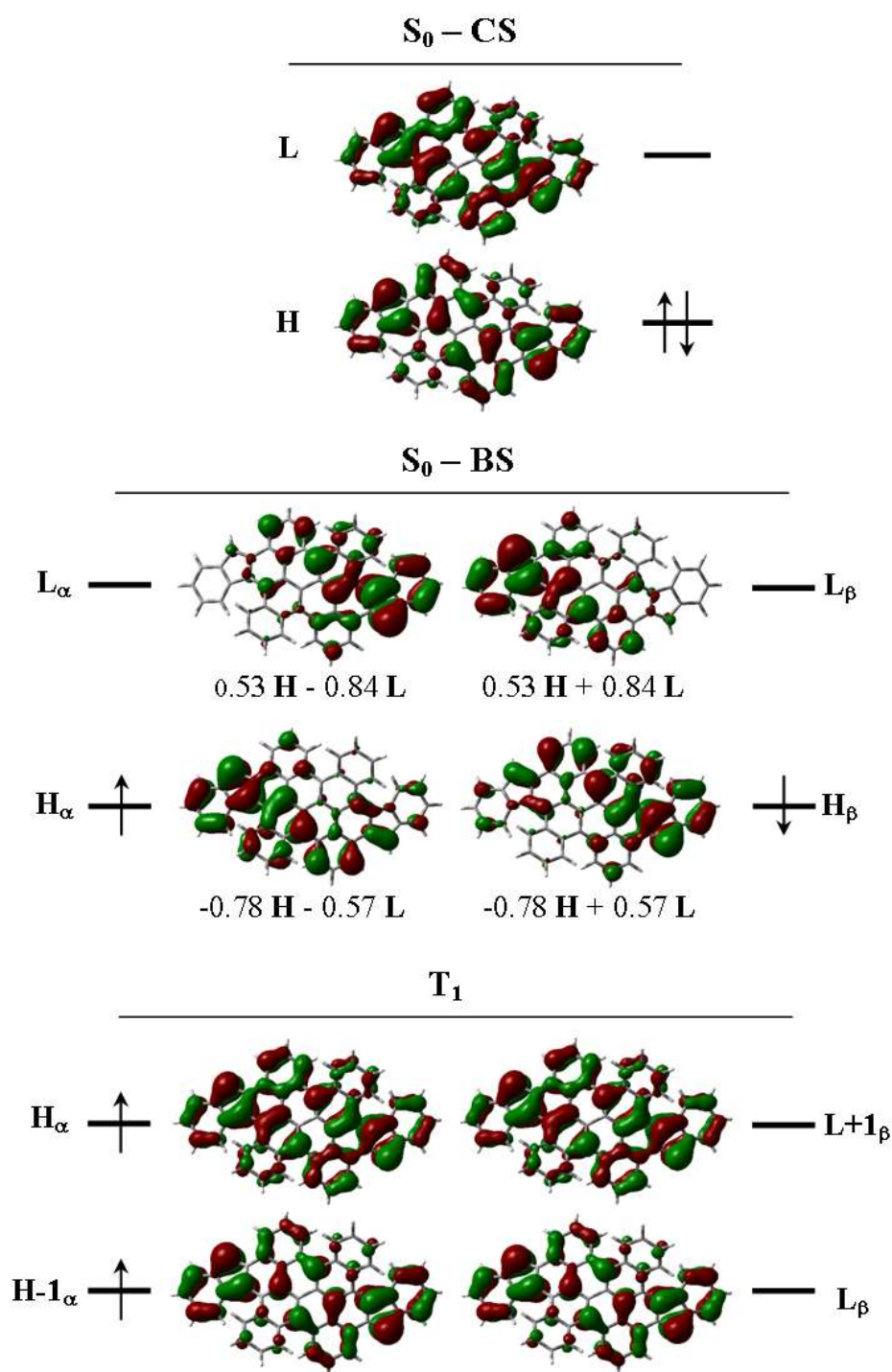


Figure S13. Frontier molecular orbitals of DFB computed with (top) a CS singlet reference configuration, (middle) a BS singlet open-shell configuration and (bottom) a triplet configuration, at the optimized BS UB3LYP geometry of the singlet ground state ($\gamma_0(PUHF) = 0.80$). Each localized orbital (BS) is also expressed as a linear combination of the delocalized (CS) orbitals.

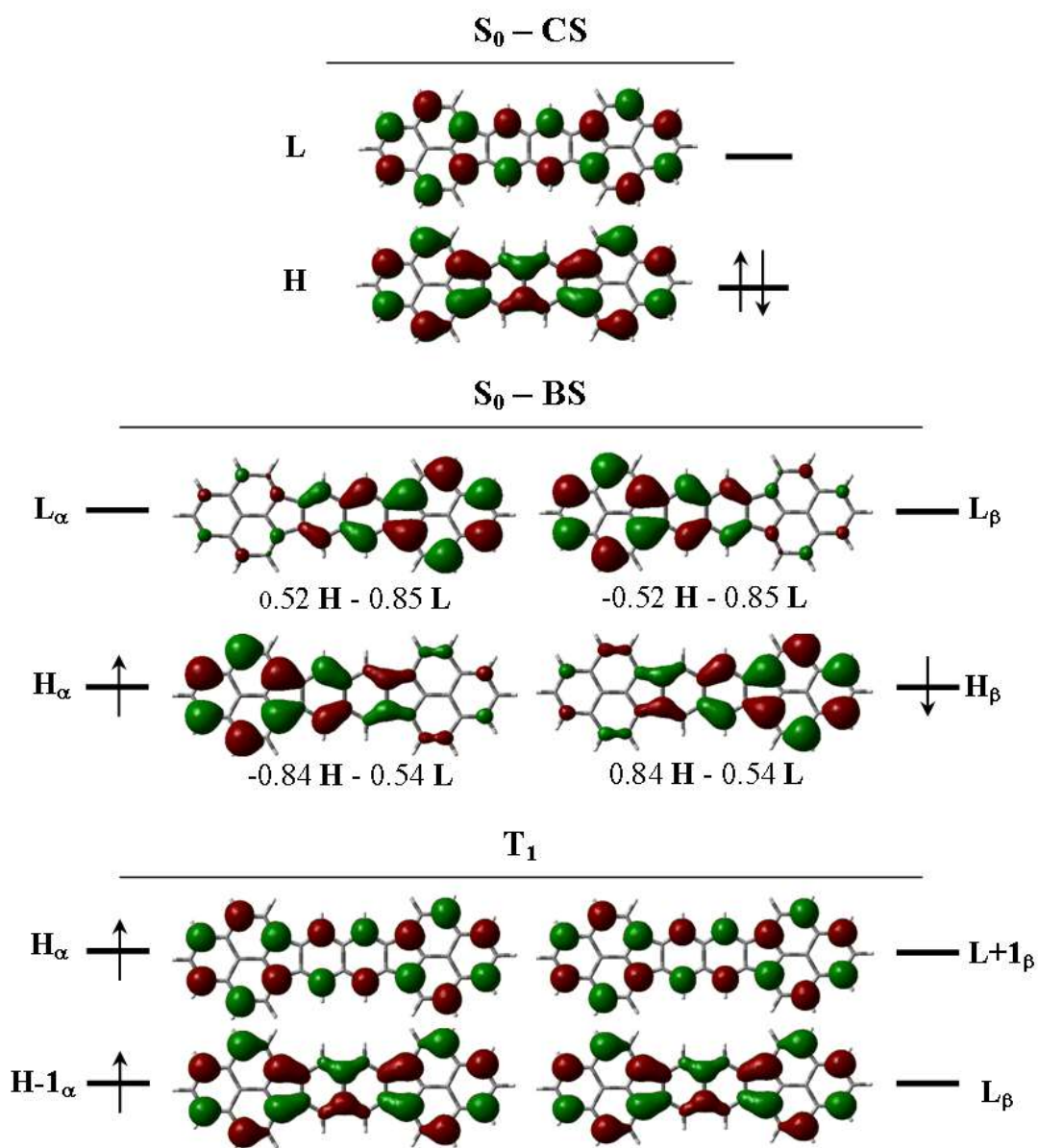


Figure S14. Frontier molecular orbitals of BISPHE computed with (top) a CS singlet reference configuration, (middle) a BS singlet open-shell configuration and (bottom) a triplet configuration, at the optimized BS UB3LYP geometry of the singlet ground state ($\gamma_0(PUHF) = 0.85$). Each localized orbital (BS) is also expressed as a linear combination of the delocalized (CS) orbitals.

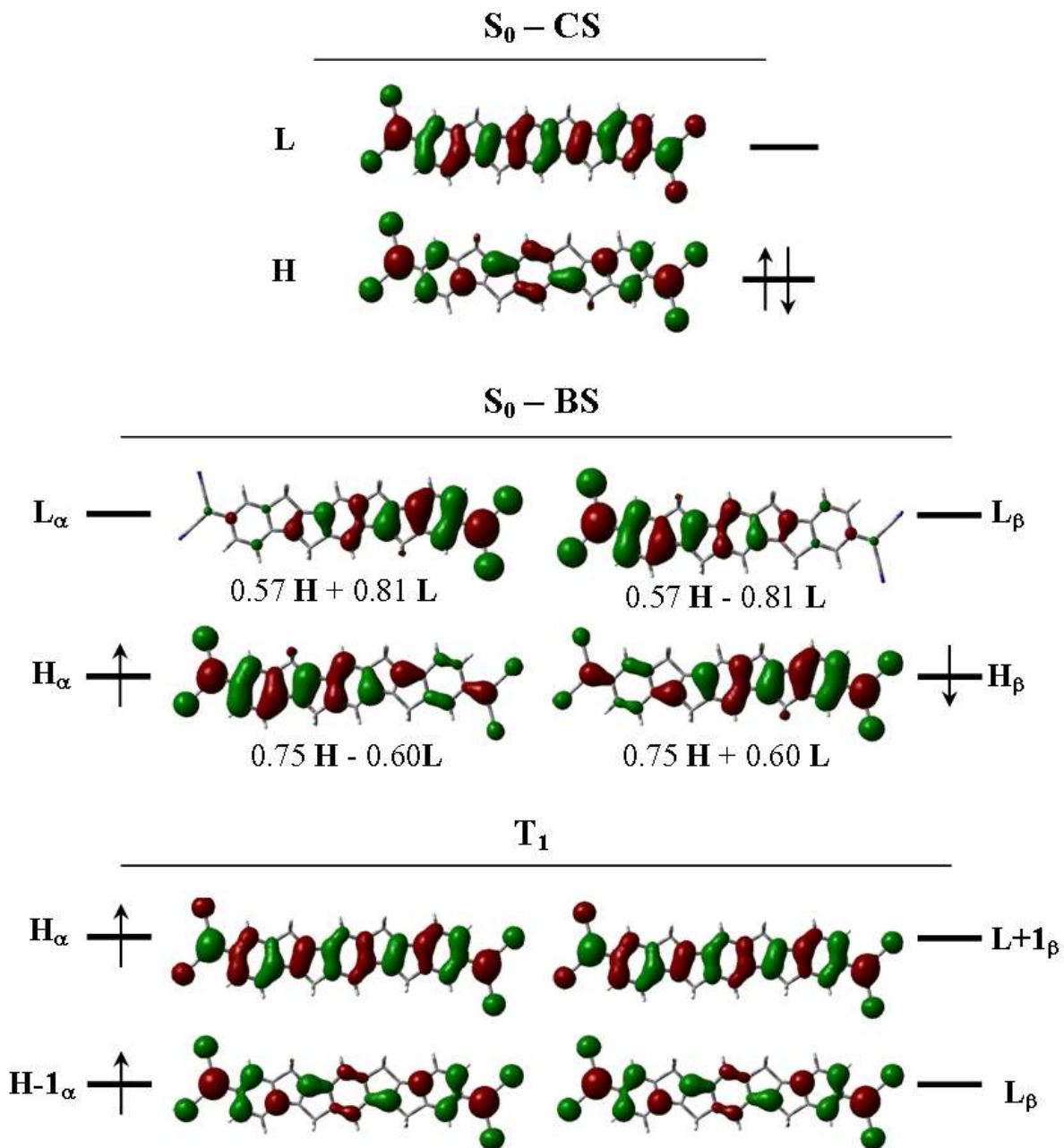


Figure S15. Frontier molecular orbitals of TPQ computed with (top) a CS singlet reference configuration, (middle) a BS singlet open-shell configuration and (bottom) a triplet configuration, at the optimized BS UB3LYP geometry of the singlet ground state ($y_0(PUHF) = 0.86$). Each localized orbital (BS) is also expressed as a linear combination of the delocalized (CS) orbitals.

References

- 1 S. Di Motta, F. Negri, D. Fazzi, C. Castiglioni and E. V. Canesi, “Biradicaloid and Polyenic Character of Quinoidal Oligothiophenes Revealed by the Presence of a Low-Lying Double-Exciton State”, *J. Phys. Chem. Lett.* 2010, **1**, 3334-3339.
- 2 J. Li, X. Qiao, Y. Xiong, H. Li and D. Zhu, “Five-Ring Fused Tetracyanothienoquinoids as High-Performance and Solution-Processable n-Channel Organic Semiconductors: Effect of the Branching Position of Alkyl Chains”, *Chem. Mater.*, 2014, **26**, 5782-5788.
- 3 P. Hu, S. Lee, T. S. Heng, N. Aratani, T. P. Gonçalves, Q. Qi, X. Shi, H. Yamada, K.-W. Huang, J. Ding, D. Kim and J. Wu, “Toward Tetraradicaloid: The Effect of Fusion Mode on Radical Character and Chemical Reactivity”, *J. Am. Chem. Soc.*, 2016, **138**, 1065–1077.
- 4 J. Ma, J. Liu, M. Baumgarten, Y. Fu, Y-Z. Tan, K. S. Schellhammer, F. Ortmann, G. Cuniberti, H. Komber, R. Berger, K. Müllen and X. Feng, “A Stable Saddle-Shaped Polycyclic Hydrocarbon with an Open-Shell Singlet Ground State”, *Angew. Chem. Int. Ed.*, 2017, **129**, 3328-3332.
- 5 K. Kamada, K. Ohta, A. Shimizu, T. Kubo, R. Kishi, H. Takahashi, E. Botek, B. Champagne and M. Nakano, “Singlet Diradical Character from Experiment”, *J. Phys. Chem. Lett.* 2010, **1**, 937-940.
- 6 X. Zhu, H. Tsuji, K. Nakabayashi, S.-i Ohkoshi and E. Nakamura, “Air- and Heat-Stable Planar Tri-*p*-quinodimethane with Distinct Biradical Characteristics”, *J. Am. Chem. Soc.* 2011, **133**, 16342-16345.
- 7 W. Zeng, Z. Sun, T. S. Heng, T. P. Gonçalves, T. Y. Gopalakrishna, K.-W. Huang, J. Ding and J. Wu, “Super-heptazethrene”, *Angew. Chem. Int. Ed.*, 2016, **55**, 8615-8619.
- 8 A. Konishi, Y. Hirao, K. Matsumoto, H. Kurata, R. Kishi, Y. Shigeta, M. Nakano, K. Tokunaga, K. Kamada and T. Kubo, “Synthesis and Characterization of Quarteranthene: Elucidating the Characteristics of the Edge State of Graphene Nanoribbons at the Molecular Level”, *J. Am. Chem. Soc.* 2013, **135**, 1430-1437.