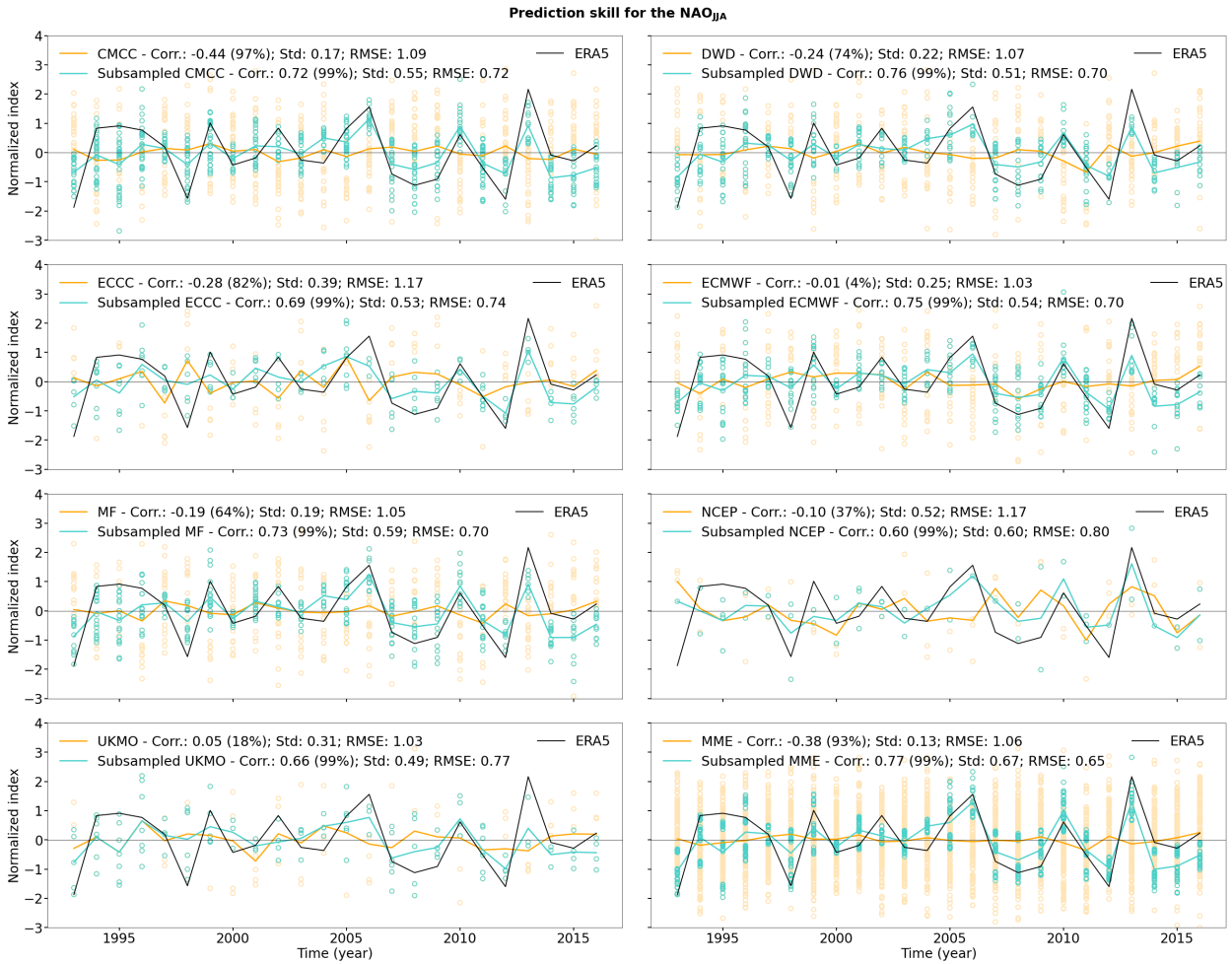
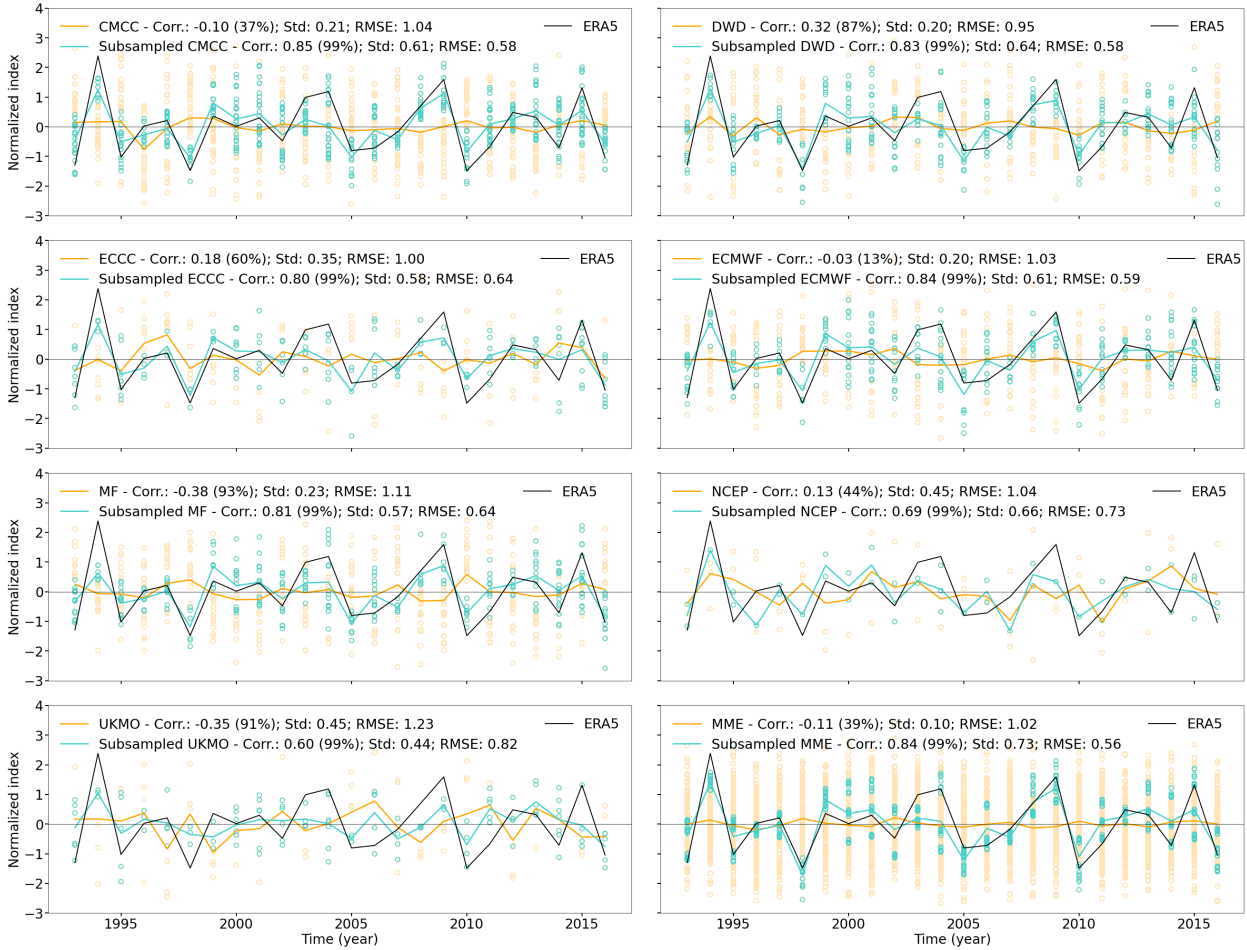


8 FIG. S1. a) Summer (JJA) Atlantic Ridge pattern, calculated as the third EOF of summer Z500 over the North  
 9 Atlantic sector (25°–80°N, 90°W–40°E) in ERA5. The variance of the summer low-frequency atmospheric  
 10 variability explained by the Atlantic Ridge is shown on the top right of the subplot. b) As a) but in the C3S  
 11 MME. Refer to section 2 for more details about the EOF analysis applied to the C3S MME. The results about  
 12 the C3S MME are represented as MME mean. Hatched areas represent the regions with consistent sign in Z500  
 13 anomalies associated with the Atlantic Ridge across all SPSs. c) The summer Atlantic Ridge index in ERA5  
 14 (black) and in the C3S MME (orange). The correlation between the summer Atlantic Ridge index in ERA5 and  
 15 the corresponding index as ensemble mean of the MME is presented on the top right of the subplot, along with  
 16 its confidence level enclosed in parentheses.

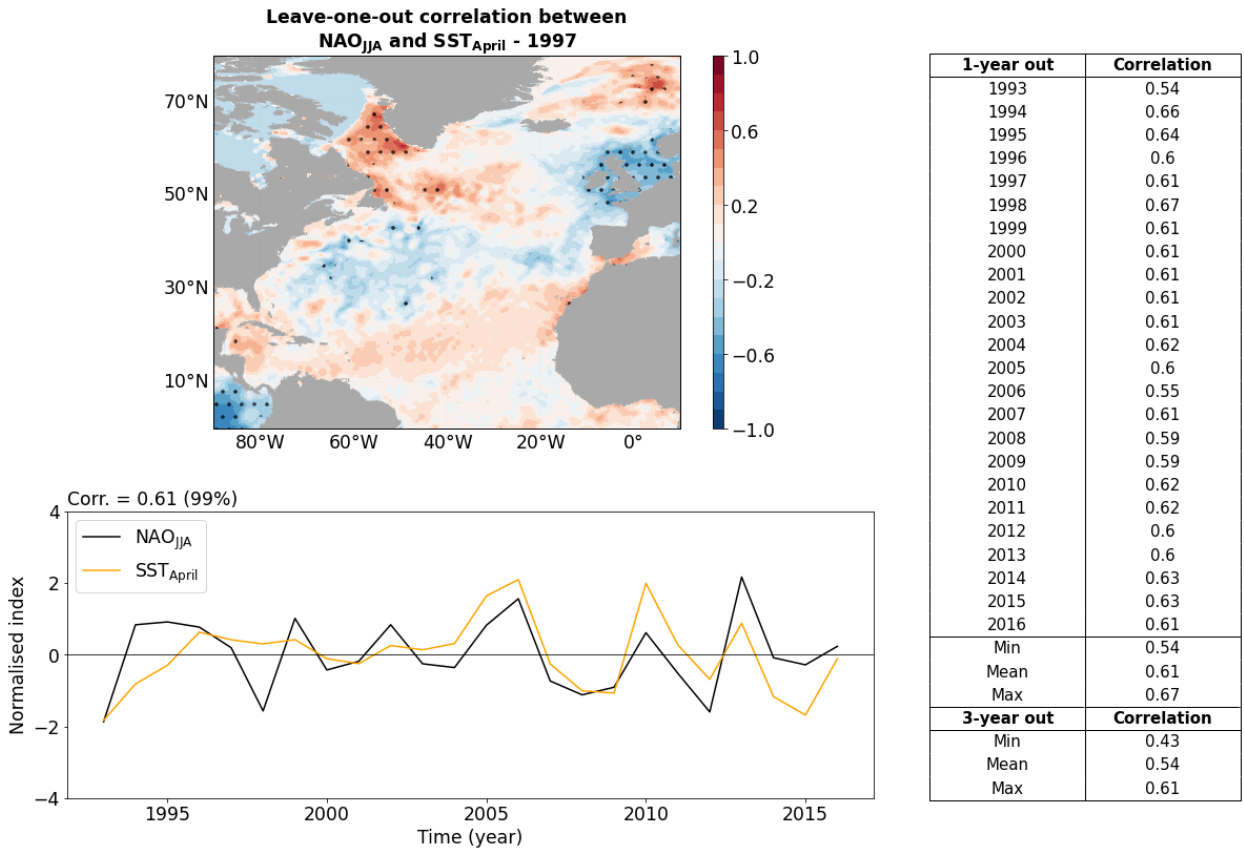


17 FIG. S2. The summer NAO index in ERA5 (black) and in the individual full (orange) and subsampled (azul)  
 18 C3S SPS ensembles. The orange (azul) circles represent each members of the individual full (subsamped) C3S  
 19 SPS ensemble. The orange (azul) solid lines represents the ensemble mean of the full (subsamped) C3S SPS  
 20 ensemble. The subsampling of the individual SPS ensembles is performed using all the April NAO predictors.  
 21 Specifically, 10, 7, 3, 6, 6, 1, and 5 members are selected for every predictor for the CMCC, DWD, ECCC,  
 22 ECMWF, MF, NCEP and UKMO SPSs, respectively. The correlation between the summer NAO index in ERA5  
 23 and the corresponding index as ensemble mean in the full and subsampled SPS ensemble is presented in the  
 24 legend, along with its confidence level enclosed in parentheses. The variability of the summer NAO index as  
 25 ensemble mean of the full and subsampled SPS ensemble is also shown in the legend as standard deviation (std).  
 26 Finally, the RMSE of the full and subsampled MME mean NAO index computed with respect to the summer  
 27 NAO index in ERA5 is shown at the end of the legend. The plot in the bottom right is the same as above, but for  
 28 the full and subsampled MME. In this case, the subsampling is performed selecting 10 members for every April  
 29 predictor.

Prediction skill for the EA<sub>JJA</sub>



30 FIG. S3. Same as Figure S2, but performing the subsampling of the individual SPS ensembles and MME using  
 31 all the April EA predictors.



32 FIG. S4. (top) Leave-one-out cross-validated correlation (shadings) between the summer NAO index and the  
 33 April sea surface temperature (SST) in the North Atlantic (90°W–10°E; 0°–80°N), using ERA5 data. The year  
 34 1997 is here shown as an example and it has been randomly selected within the time period 1993–2016. Black  
 35 dots denote correlations that are statistically significant at the 90% confidence level. (bottom) The summer NAO  
 36 (black) and April SST (orange) indices. Refer to section 2 in the manuscript for more details about the calculation  
 37 of the April NAO predictor index. The correlation between the two indices is provided in the top right corner,  
 38 along with its confidence level enclosed in parentheses. (left) Leave-one-out and leave-three-out cross-validated  
 39 correlation between the summer NAO and April SST indices.

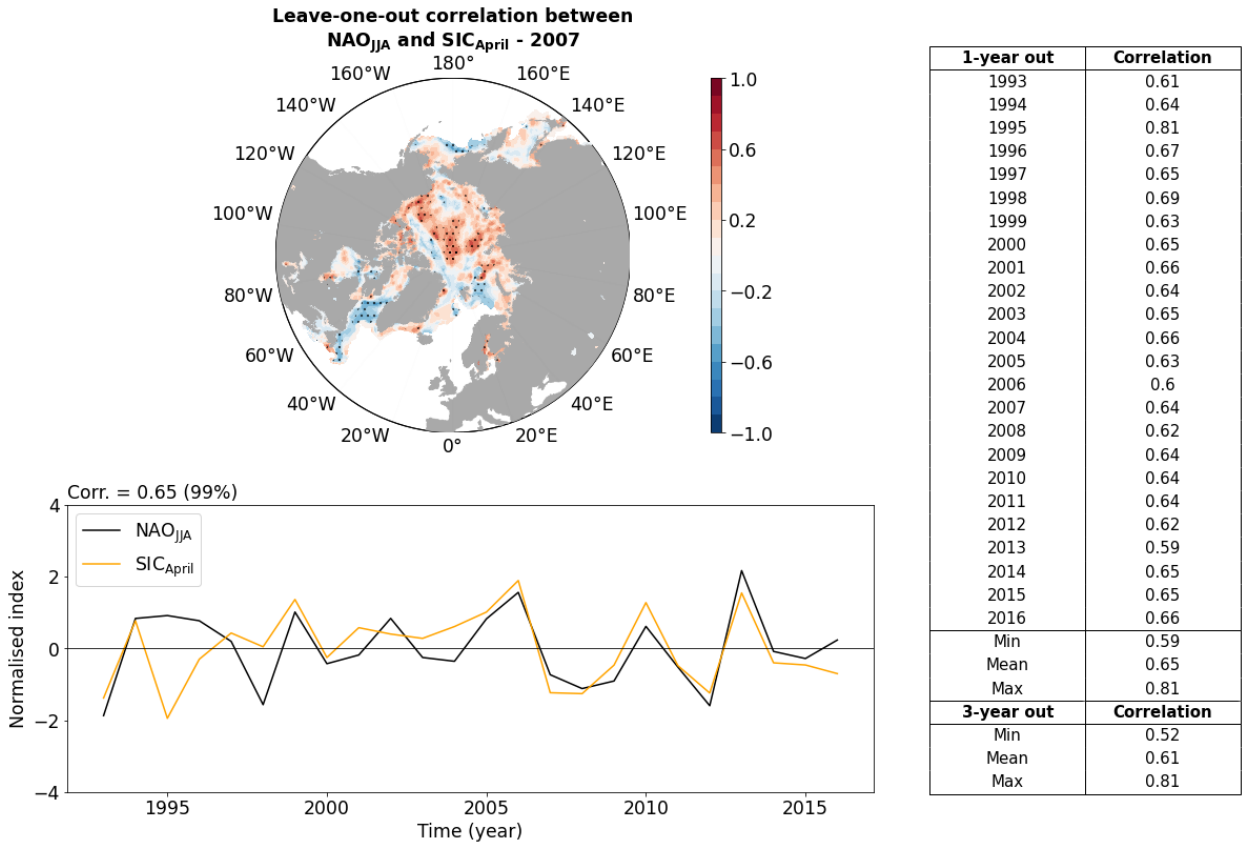


FIG. S5. Same as Figure S4, but for the sea-ice concentration (SIC) in the Northern Hemisphere (north of 40°N).

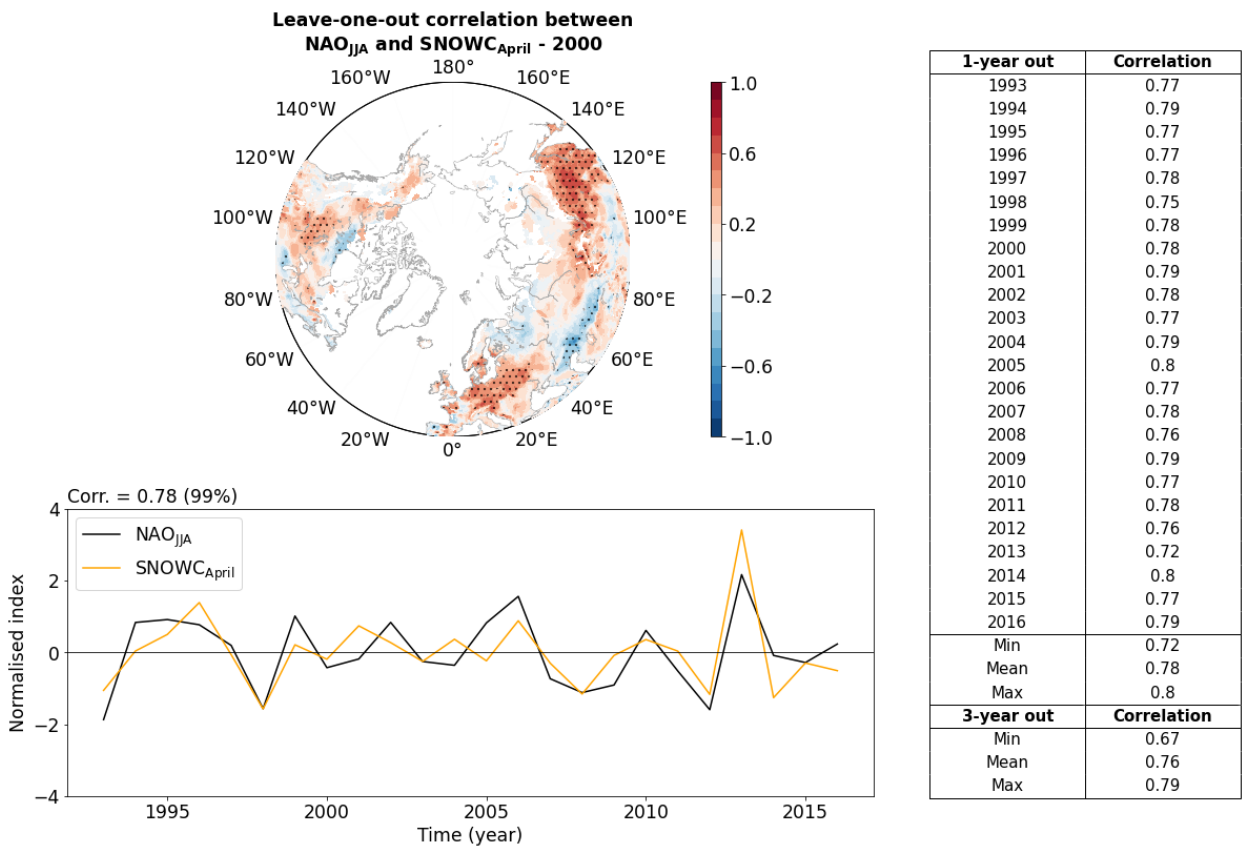
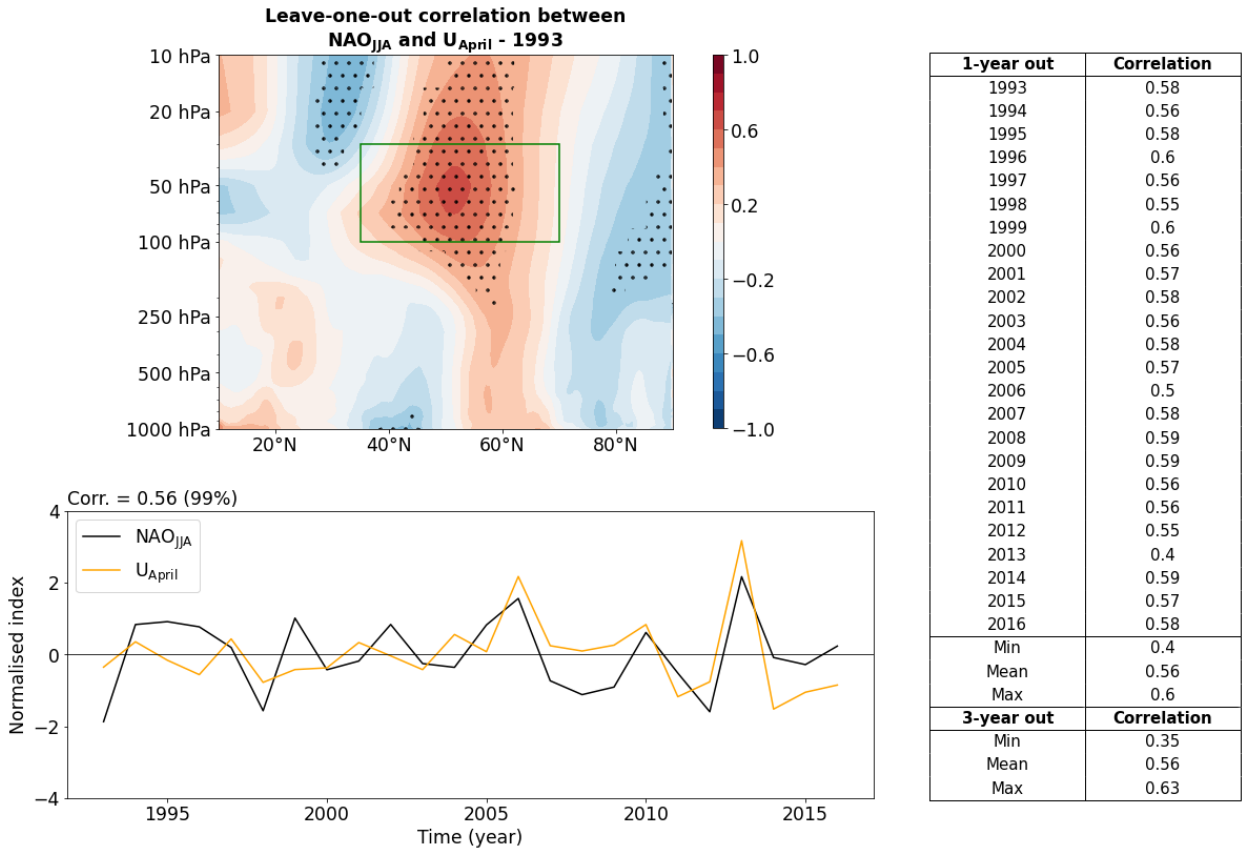
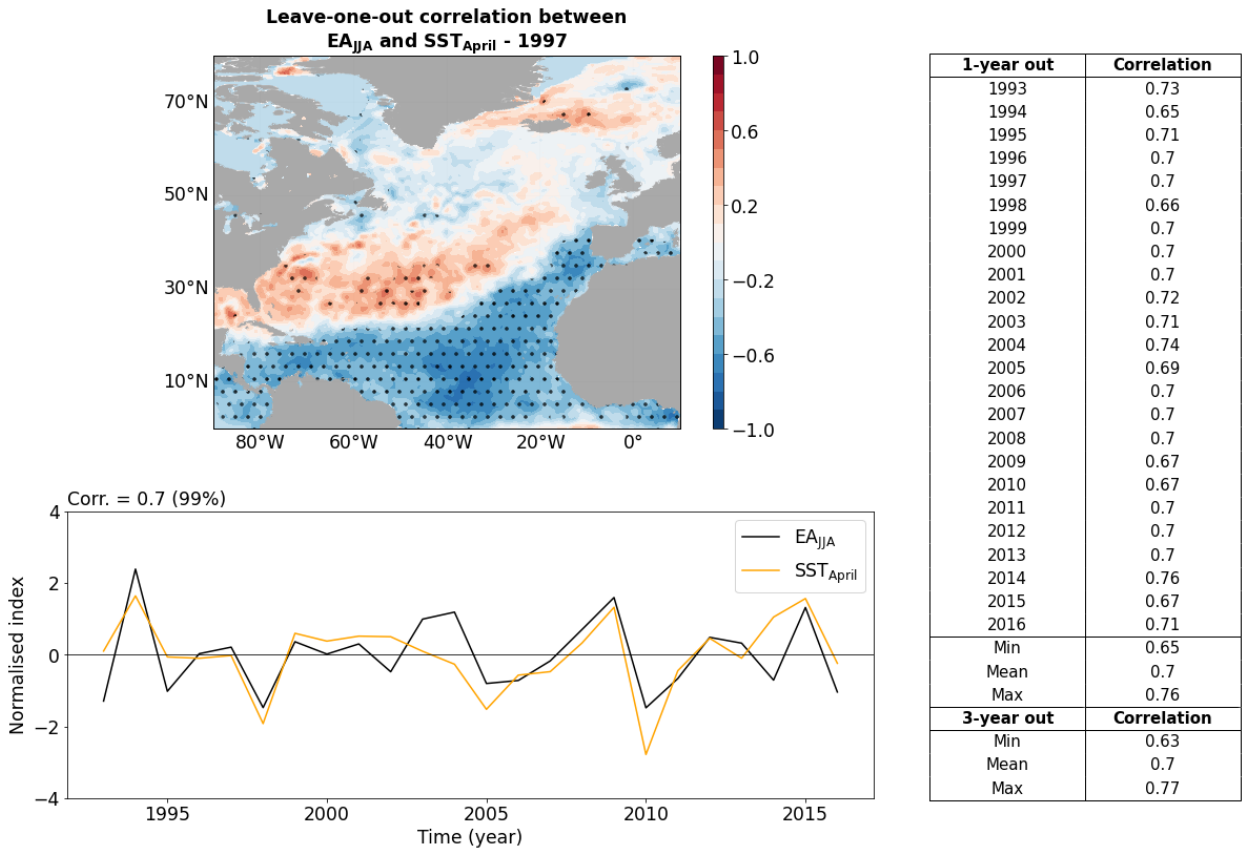


FIG. S6. Same as Figure S4, but for the snow cover (SNOWC) in the Northern Hemisphere (north of 40°N).

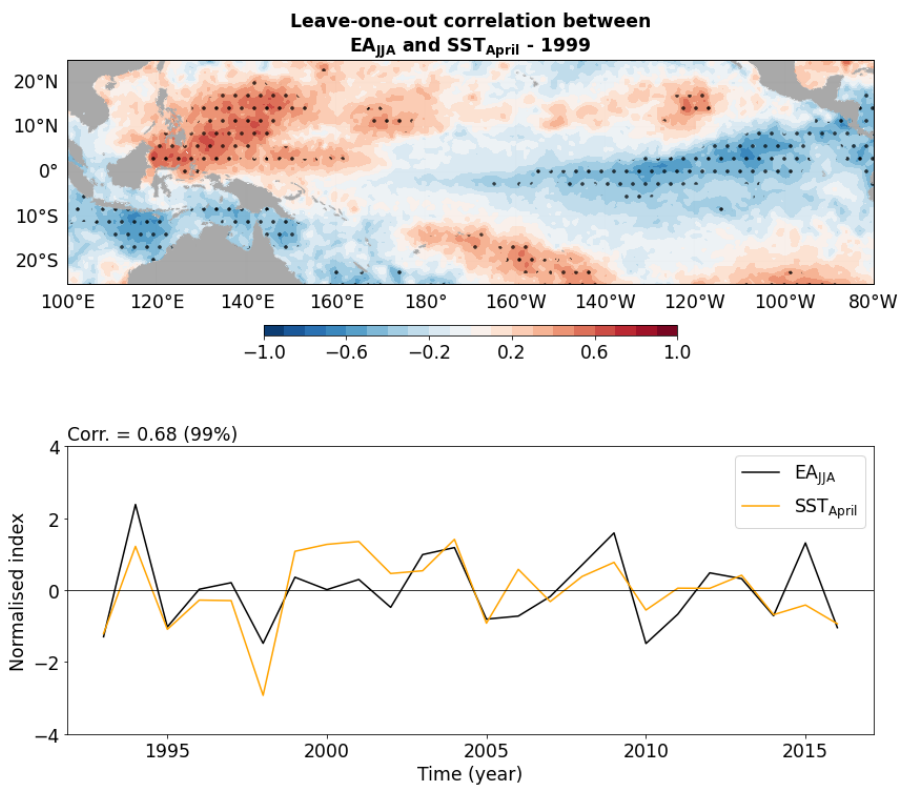


40 FIG. S7. Same as Figure S4, but for the zonal wind (U). The zonal wind is zonally-averaged over the longitudinal  
 41 range of the North Atlantic sector as in Wang and Ting (2022) (75°W–15°E). The green box represents the part  
 42 of the lower stratosphere where the zonally-averaged zonal wind is averaged to define the April U index shown  
 43 in the plot on the bottom (orange line; 30 hPa–100 hPa; 35°N–70°N).





44 FIG. S8. (top) Leave-one-out cross-validated correlation (shadings) between the summer EA index and the  
 45 April sea surface temperature (SST) in the North Atlantic (90°W–10°E; 0°–80°N), using ERA5 data. The year  
 46 1997 is here shown as an example and it has been randomly selected within the time period 1993–2016. Black  
 47 dots denote correlations that are statistically significant at the 90% confidence level. (bottom) The summer EA  
 48 (black) and April SST (orange) indices. Refer to section 2 in the manuscript for more details about the calculation  
 49 of the April EA predictor index. The correlation between the two indices is provided in the top right corner,  
 50 along with its confidence level enclosed in parentheses. (left) Leave-one-out and leave-three-out cross-validated  
 51 correlation between the summer EA and April SST indices.



<b>1-year out</b>	<b>Correlation</b>
1993	0.66
1994	0.66
1995	0.67
1996	0.68
1997	0.69
1998	0.66
1999	0.68
2000	0.71
2001	0.69
2002	0.7
2003	0.68
2004	0.66
2005	0.67
2006	0.71
2007	0.68
2008	0.68
2009	0.68
2010	0.68
2011	0.69
2012	0.68
2013	0.68
2014	0.68
2015	0.74
2016	0.67
Min	0.66
Mean	0.68
Max	0.74
<b>3-year out</b>	<b>Correlation</b>
Min	0.62
Mean	0.69
Max	0.75

FIG. S9. Same as Figure S8, but for the SST in the tropical Pacific (100°E–80°W; 25°S–25°N).

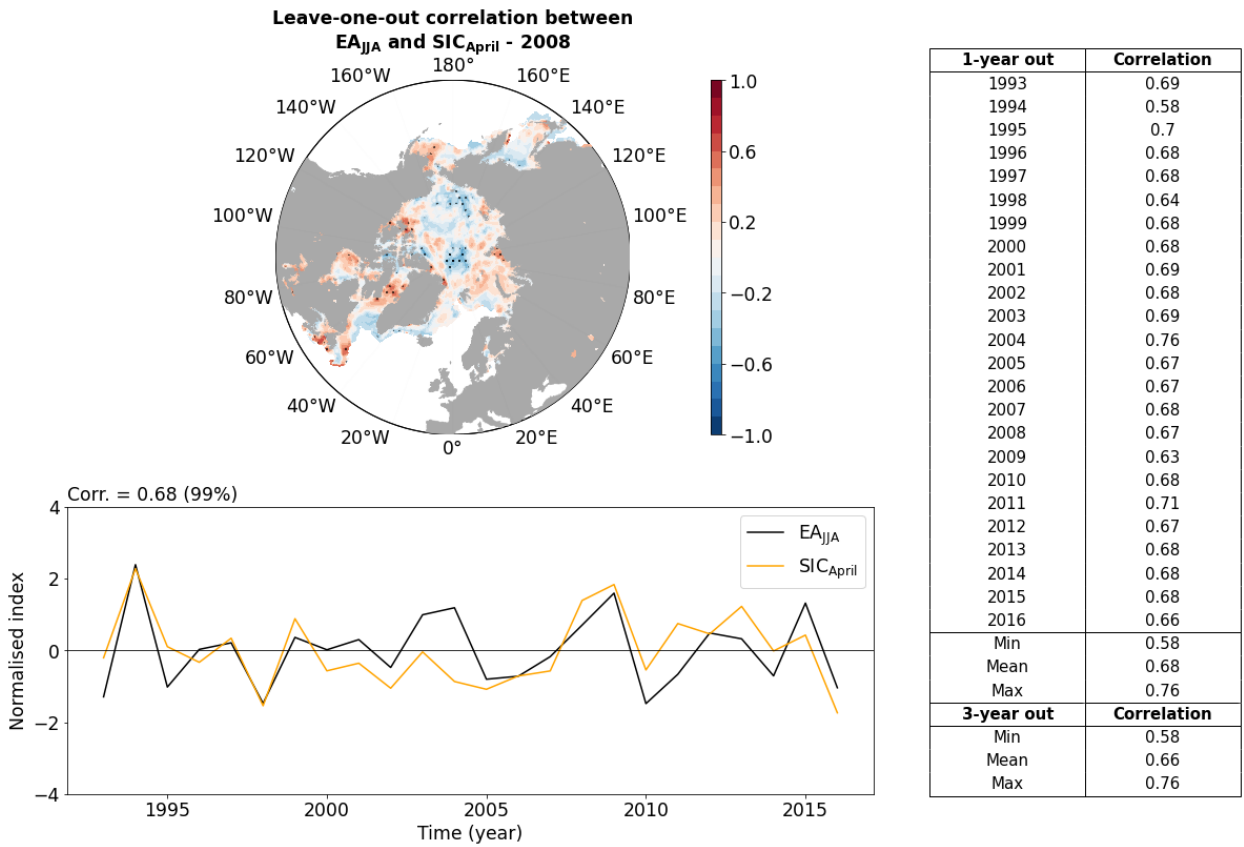
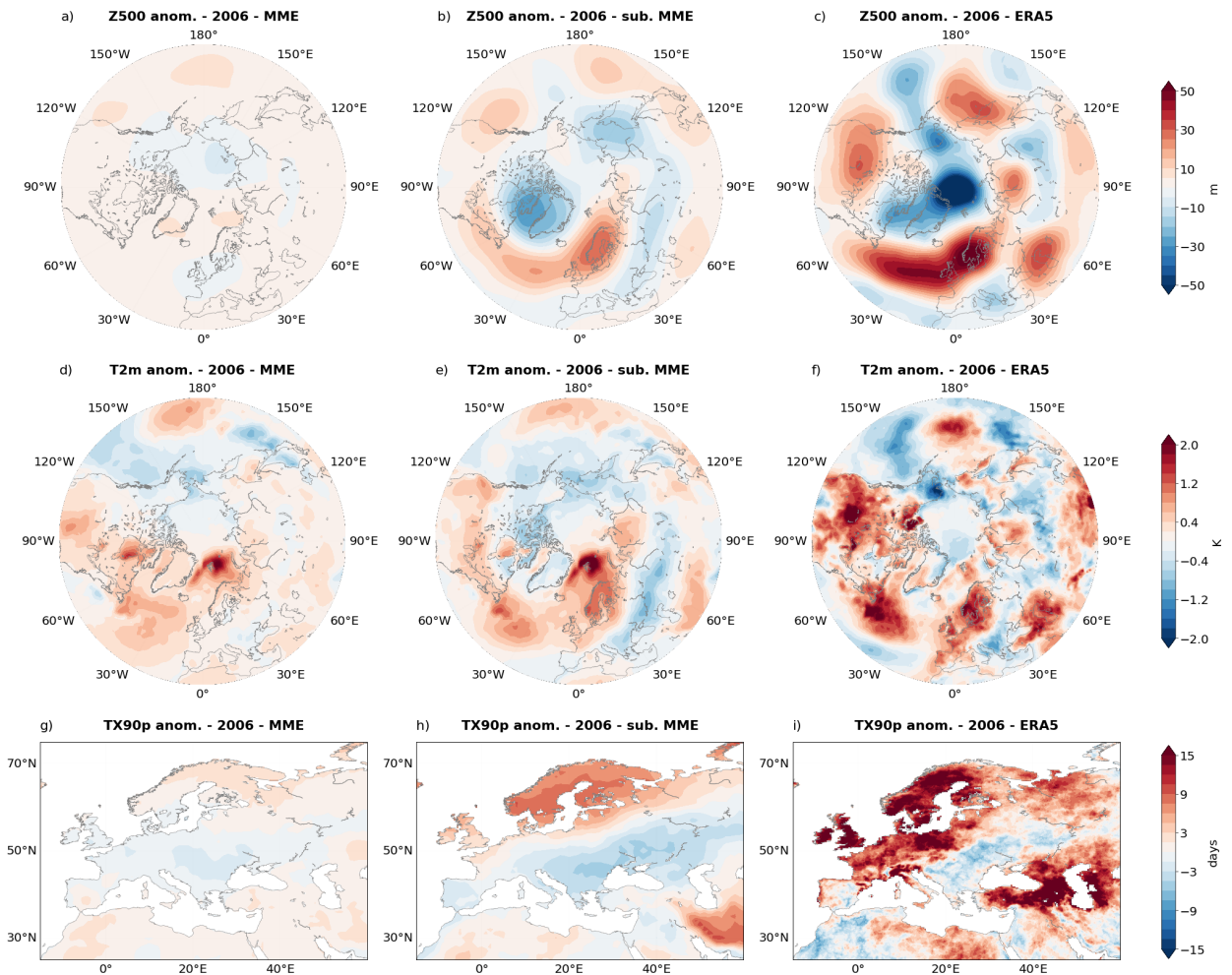


FIG. S10. Same as Figure S8, but for the SIC in the Northern Hemisphere (north of 40°N).



52 FIG. S11. a) Z500 anomalies (m) for the full C3S MME mean during summer 2006. b) As a) but for the  
 53 subsampled C3S MME mean. The subsampling of the MME is performed using all the April EA predictors  
 54 computed with the leave-three out cross-validation procedure and selecting 10 members for every predictor. c)  
 55 As a) but for ERA5. d, e, f) As a, b, c) but for T2m (K). g, h, i) As a, b, c) but for TX90p (days).

56 **References**

- 57 Wang, L., and M. Ting, 2022: Stratosphere-Troposphere Coupling Leading to Extended Seasonal  
58 Predictability of Summer North Atlantic Oscillation and Boreal Climate. *Geophysical Research*  
59 *Letters*, **49** (2), e2021GL096362.