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# Design of Low-Voltage Integrated Step-up Oscillators with Microtransformers for Energy Harvesting Applications

Enrico Macrelli, Aldo Romani, Rudi Paolo Paganelli, Antonio Camarda, and Marco Tartagni, *Member, IEEE*

**Abstract**—This paper describes the modeling of startup circuits in battery-less micropower energy harvesting systems and investigates the use of bond wire micromagnetics. The analysis focuses on step-up Meissner oscillators based on magnetic core transformers operating with input voltages down to  $\approx 100$  mV, e.g. from thermoelectric generators. As a key point, this paper examines the effect of core losses and leakage inductances on the startup requirements obtained with the classical Barkhausen criterion, and demonstrates the minimum transconductance for oscillations to occur. For validation purposes, a step-up oscillator IC is fabricated in a STMicroelectronics 0.32  $\mu\text{m}$  technology, and connected to two bond wire microtransformers, respectively, with a 1:38 MnZn ferrite core and with a 1:52 ferromagnetic low-temperature co-fired ceramic (LTCC) core. Coherently with the proposed model, experimental measurements show a minimum startup voltage of 228 mV for the MnZn ferrite core and of 104 mV for the LTCC core.

**Index Terms**—Bond wire magnetics, energy harvesting, integrated circuits, leakage inductances, magnetic losses, magnetic materials, step-up oscillators, transformers.

## I. INTRODUCTION

In energy harvesting (EH) applications, several types of energy transducers are used to convert environmental energy into electrical form [1]. Such energy is then managed to supply low-power and low-voltage circuits. Battery-powered systems are widespread in miniaturized electronics; however, batteries are not suitable for wireless sensor nodes (WSNs) or bio-implantable systems where periodic maintenance is difficult. For these applications, EH is the best choice for long-lasting power production and low maintenance. Among

the available types of energy transducers, thermoelectric generators (TEGs) may provide sufficient power for sustaining battery-less WSNs and, in general, for supplying fully autonomous systems. TEGs consist of arrays of thermocouples containing a p-type and n-type semiconductor connected electrically in series and thermally in parallel. Because of the Seebeck effect, the output voltage of a TEG is proportional to the number of thermocouples and to the temperature difference between cold and hot side [2]. TEGs with voltage outputs from 10 to 50 mV/K have been fabricated with microelectronic processes [3] with low series resistances typically lower than 1  $\Omega$ . For body-wearable applications, a temperature gradient of 5 K between body and environment is expected to generate an output voltage lower than 250 mV.

Under these conditions, when no initial energy is available, particular ultralow voltage step-up converters are required in order to kick-start battery-less systems from fully discharged states. Since in standard CMOS technologies the usual threshold voltage of a MOSFET is in the order of few hundreds of mV, self-starting designs from lower voltages would require a normally-ON device [4] [5] to allow current to circulate at the beginning. These circuits would then produce higher output voltages appropriate for standard CMOS circuits, so that a conventional power converter can be started and operated efficiently [6] [7]. We point out that the main design goal is to achieve the lowest possible activation voltage, rather than optimum efficiency, which will be guaranteed once the conventional power converter is started.

In the current state-of-the-art, several architectures of low-voltage step-up converters are implemented using TEGs. In [8] [9] various step-up converters based on a FET-tuned oscillator topology are reported. However, the startup of these circuits generally relies on a step-up transformer and a normally-ON MOSFET with a high ON-resistance, typically a few  $\Omega$ , compared to the source resistance, that restricts the achievable output power [5]. A first solution to overcome this problem is the realization of the startup circuit separated from the main power conversion block, so that classical high efficiency dc-dc converters can be used. Charge pumps are a common implementation of this approach [4], [10]-[12], but alternative solutions relying on mechanical vibrations have also been developed [13]. A second solution is to merge the startup circuit with the main dc-dc converter in order to decrease the number of devices and to improve the reliability. Synchronous and flyback boost converters are examples of

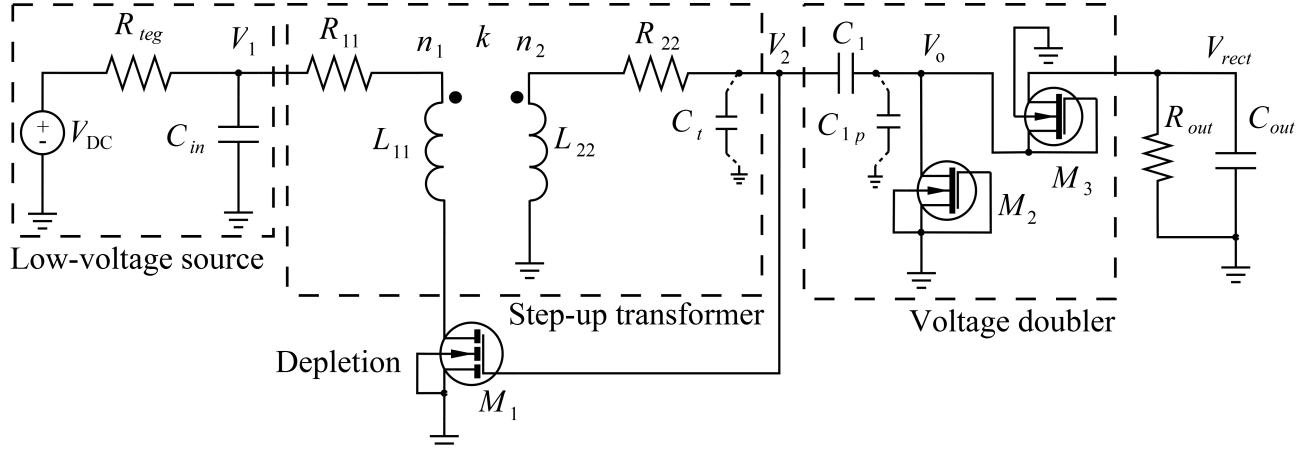
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**Fig. 1.** Schematic of the designed low-voltage step-up oscillator with a step-up transformer. Parasitic capacitances are also included.

merged architectures as in [14], where 0.6 V are required for the startup along with several off-chip components. Other examples of merged architectures are step-up oscillators based on transformers or cross-coupled inductors as in [5], [15]-[17]. Recently, several circuits operating at low-voltages have been reported in literature [18]-[26], and as commercial products [27] [28].

Toroidal micromagnetics are considered one of the best choices for implementing step-up oscillators based on transformers due to the good dc performance within a small footprint area. Nowadays, commercial miniature transformers for EH are available with high inductance and high turns ratio [29] [30], however with: (i) high dc resistance, i.e. 200  $\Omega$  at secondary for 1:50 turns, (ii) large dimensions, i.e.  $6.0 \times 6.0 \times 3.5 \text{ mm}^3$  ( $l \times w \times h$ ), (iii) high profile compared to micro-structures [31]. Besides this, literature reports toroidal microtransformers with bonding wires [32]-[34] with high quality-factor  $Q$ , small area and high turns ratio, which are features of paramount importance for low-voltage step-up oscillators [27]. The use of bonding wires allows in perspective die-level or in-package integration of the whole converter with the magnetics mounted on-top of the IC. In [32] and [33], transformers with NiZn and MnZn ferrite cores on a PCB substrate are reported with a turns ratio up to 1:38, a self-inductance up to 315  $\mu\text{H}$ , and a small-signal peak  $Q$ -factor up to 24.5 at 0.1 MHz. In [34], a 29  $\mu\text{H}$  1:50 transformer is described with a ferromagnetic low-temperature co-fired ceramic (LTCC) core on silicon, with a peak  $Q$ -factor of 11.6 at 1.3 MHz, and a maximum primary current of  $\approx 1$  A.

## II. DESCRIPTION OF WORK

An ideal transformer virtually presents zero winding and core losses, and unity coefficient of coupling. However, toroidal micromagnetics can exhibit large core losses due to eddy currents and hysteresis for increasing operating frequencies, depending on the core properties. In addition, these devices can experience lower coupling factors due to leakage inductances, depending on the winding structure and geometry, and on the core material. Both of these factors critically impact the performance of the step-up converter by increasing the minimum startup voltage. Currently, there is poor literature regarding this topic, thus it is very helpful to

analyze the effect of core losses and leakage inductances on the startup requirements in order to better design low-voltage step-up circuits in EH applications.

This paper presents the design of a step-up oscillator circuit acting as a voltage booster from discharged states for use in battery-less systems, and suitable for operation with low-voltage sources such as TEGs. The circuit also takes advantage of miniaturized bond wire transformers with magnetic cores. The proposed circuit analysis includes the effects of core losses and leakage inductances on the startup requirements, and identifies the minimum active device transconductance necessary for oscillations to occur with a potential lossy and loosely coupled microtransformer. Additionally, given a specific transformer, circuit parameters can be optimized, and the minimum requirements can be found. Similarly, if circuit parameters are constrained, the model contributes to define the requirements of the magnetic component, thus allowing to explore the design space. Experimental results obtained with two bond wire transformers with ferrite and magnetic LTCC cores validate circuit analysis by confirming the low-voltage startup capability of the designed oscillator circuit.

The paper is structured as follows. Section III introduces a circuit analysis of low-voltage step-up oscillators for EH and recalls the main properties of the used bond wire microtransformers. Section IV discusses the modeling results together with the experimental results. Finally, the conclusions are presented in Section V.

## III. LOW-VOLTAGE STEP-UP OSCILLATOR FOR ENERGY HARVESTING APPLICATIONS

This section presents the large and the small-signal analyses of the step-up converter. The analytical study also evaluates the startup capability of the converter and predicts the minimum transconductance which permits oscillations. Finally, the properties of the bond wire microtransformers used during validation are summarized.

### A. Circuit Description

The designed step-up converter is based on a FET-tuned oscillator similar to that described in [18] and [27] with self-startup capability from very low voltage. The circuit relies on a Meissner-type oscillator, a modified version of the standard

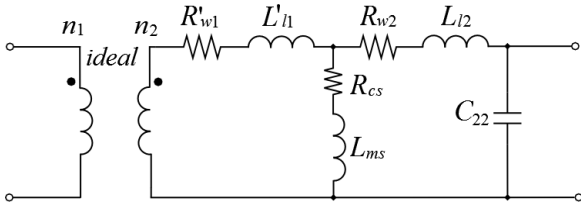


Fig. 2. Exact equivalent circuit of the step-up transformer referred at the secondary side with core losses and leakage inductances.

Hartley-type oscillator [26] [35]. Fig. 1 shows the schematic of the low-voltage step-up converter. The oscillator is composed of the step-up transformer and a depletion n-type MOSFET. A voltage doubler is also included. An integrated circuit (IC) including the MOSFET and the voltage doubler is realized in a STMicroelectronics 0.32  $\mu\text{m}$  technology.

The energy source is modeled with a dc voltage  $V_{\text{DC}} = V_{\text{teg}}$  and a series resistor  $R_{\text{teg}}$ , chosen to match the properties of a CP14 module from Laird Technologies [36]. The depletion n-type MOSFET  $M_1$  is chosen due to its normally-ON state at the considered low voltages because of its negative threshold voltage  $V_{m1}$ . The step-up transformer has a toroidal structure with  $n_1$  turns at the primary coil and  $n_2$  turns at the secondary coil. The transformer model shown in Fig. 1 includes [37]: the coupling coefficient  $k$ , the self-inductances  $L_{11}$  and  $L_{22}$ , the series resistances  $R_{11}$  and  $R_{22}$ , and the turns ratio  $n_{12} = n_2 / n_1$ . Besides, several capacitances are included in the analysis. The total capacitance is  $C_t = C_{22} + C_{\text{gs}1} + C_{\text{par}}$ , where  $C_{22}$  is the secondary parasitic capacitance of the transformer,  $C_{\text{gs}1}$  is the gate-source capacitance of  $M_1$ , and  $C_{\text{par}}$  is the total parasitic capacitance of IC pads and oscilloscope probes.  $C_1$  is an integrated poly-poly capacitor, with an associated additional parasitic capacitance  $C_{1p}$  between its minus terminal and ground, whereas we neglect the parasitic capacitance between its plus terminal and ground and the capacitance between the coils. An external filter capacitor  $C_m$  acts as energy buffer.

### B. Circuit Analysis

The circuit analysis presented herein is generic and independent on the chosen microelectronic process. Initially, the converter is connected to the energy source  $V_{\text{DC}}$  that imposes the current  $I_1$  through the primary winding and the normally-ON depletion MOSFET. Hence, this current induces a positive voltage  $V_2$  at the secondary coil ( $V_2 > 0$  V) which increases the gate-source voltage  $V_{\text{gs}1} = V_2$  of  $M_1$  and thus  $I_1$ . Once  $I_1$  reaches the core saturation, the voltage  $V_2$  starts to drop, which lowers the drain current  $I_1$ , thus decreasing again  $V_2$  below zero, by a loop until  $M_1$  is driven near its off-state ( $V_2 < 0$  V) leading to  $I_1 \approx 0$ . Preliminary current is delivered by the weak-inverted  $M_1$ , thus providing an increase of  $I_1$ , and thus, through the coupling of the coils, a further increase in  $V_2$  causing  $M_1$  to become more conductive again ( $V_2 \approx 0$  V), so that the oscillation process starts [5]. The depletion-mode n-type MOSFET acts as a controlled resistor switched between the ON-state (low ON-resistance) and OFF-state (high ON-resistance), which modulates the current  $I_1$ . The last stage is a voltage doubler composed by the pump capacitor  $C_1$  and the two diode-connected n-type enhancement MOSFETs  $M_2$  and  $M_3$ . Finally, the load is composed of a storage capacitor  $C_{\text{out}}$  and a resistor  $R_{\text{out}}$ .

The behavior of the converter in Fig. 1 is influenced by the step-up transformer's performance such as coupling, winding resistances and core losses. In order to assess the oscillation mechanism at small-signals, the transformer's parameters are referred at the secondary side. The series resistances  $R_{11}$  and  $R_{22}$  are expressed as:

$$R_{11} = R_{w1} + R_c \quad (1)$$

$$R_{22} = R_{w2} + R_{cs},$$

where  $R_c$  is the core equivalent series resistance (ESR) and  $R_{cs} = R_c n_{12}^2$  is the core ESR at secondary, whereas  $R_{w1}$  and  $R_{w2}$  are the winding resistances. The self-inductances  $L_{11}$  and  $L_{22}$  are expressed as:

$$L_{11} = L_{l1} + L_m \quad (2)$$

$$L_{22} = L_{l2} + L_{ms},$$

where  $L_{l1}$  and  $L_{l2}$  are the leakage inductances at primary and secondary, and  $L_m$  and  $L_{ms}$  are, respectively, the magnetizing inductances at primary and secondary. The latter quantities can be expressed as:

$$L_m = k L_{11} \quad (3)$$

$$L_{ms} = k L_{22} = L_m n_{12}^2.$$

It descends from (2) and (3) that:

$$L_{l1} = L_{11}(1-k) = L_m(1-k)/k \quad (4)$$

$$L_{l2} = L_{22}(1-k) = L_{ms}(1-k)/k.$$

Fig. 2 shows the exact equivalent circuit of the step-up transformer reported at the secondary side where:

$$R'_{w1} = R_{w1} n_{12}^2 \quad (5)$$

$$L'_{l1} = L_{l1} n_{12}^2 \approx L_{l2},$$

obtained by reporting the parameters at the secondary.

Let us now recall that  $V_{m1}$  and  $V_{\text{teg}}$  are, respectively, the negative threshold voltage of the MOSFET  $M_1$  and the open-circuit voltage of the TEG. From Fig. 1, since  $M_1$  is connected in series with the primary coil, the drain-source voltage  $V_{\text{ds}1}$  has small values compared to  $V_{\text{gs}1} - V_{m1}$ , thus forcing  $M_1$  to operate always in triode mode (linear region) as a controlled resistor for low values of the source voltage  $V_{\text{teg}}$ . The drain current  $I_{\text{ds}1}$  in linear region is defined as:

$$I_{\text{ds}1} = \beta_{n1} \left( V_{\text{gs}1} - V_{m1} - \frac{V_{\text{ds}1}}{2} \right) V_{\text{ds}1}, \quad (6)$$

where  $\beta_{n1} = \mu_n C_{\text{ox}} W_1 / L$  is the gain factor of  $M_1$ ,  $\mu_n$  is the electron mobility,  $W_1 / L$  is the form factor of  $M_1$ ,  $C_{\text{ox}} = \epsilon_{\text{ox}} / t_{\text{ox}}$  is the gate-oxide capacitance per unit area, with  $\epsilon_{\text{ox}} = \epsilon_0 \epsilon_r$ ,  $\epsilon_r = 3.9$  for silicon dioxide, and  $t_{\text{ox}}$  as the gate-oxide thickness. In triode mode, the gate-to-channel capacitance of  $M_1$  is due to the equal gate-source and gate-drain capacitances, which can be assumed to be in parallel under the assumption that  $V_{\text{ds}1}$  is small, as is the case in this application. Then, the overall capacitance is  $C_{\text{gs}1} = C_{\text{ox}} W_1 L$ .

The transconductance  $g_{m1}$  of  $M_1$  is computed from (6):

$$g_{m1} = \beta_{n1} V_{\text{ds}1} \approx \beta_{n1} \frac{V_{\text{teg}}}{1 - R_{\text{eq}} \beta_{n1} V_{m1}}, \quad (7)$$

where  $R_{eq} = R_{teg} + R_{l1} + R_{con1}$ , with  $R_{con1}$  as the parasitic resistance of connections at primary. The approximation in (7) is obtained for  $V_{gs1} \approx 0$  by considering the DC voltage across  $L_{l1}$  negligible, and by neglecting the quadratic term  $V_{ds1}^2$  in (6) considering that  $|V_{m1}| \gg V_{ds1}/2$  since we target ultra-low voltages of tens of mV. In order to maximize  $g_{m1}$ ,  $V_{teg}$  together with  $\beta_{n1}$  should be increased, whereas  $R_{eq}$  and  $|V_{m1}|$  should be reduced. The output conductance  $g_{ds1}$  of  $M_1$  is computed from (6):

$$g_{ds1} = \beta_{n1} (V_{gs1} - V_{m1} - V_{ds1}) \approx \beta_{n1} \frac{R_{eq} \beta_{n1} V_{m1}^2 - V_{teg} - V_{m1}}{1 - R_{eq} \beta_{n1} V_{m1}}, \quad (8)$$

where the same approximations of (7) hold. The ON-resistance of  $M_1$  is  $r_{ds} = 1/g_{ds1}$ , and can be referred to the secondary as  $r'_{ds} = r_{ds} n_{12}^2$ . Fig. 3 shows the resulting small-signal circuit. The total primary resistance referred at the secondary is  $R'_{wt1} = (R_{teg} + R_{w1} + R_{con1}) n_{12}^2$ , whereas the total secondary resistance is  $R_{wt2} = R_{w2} + R_{con2}$ , with  $R_{con2}$  as the parasitic resistance of connections at secondary. From Fig. 3, the equivalent capacitance at secondary is  $C_{eq} = C_t + (C_1 C_{1p}) / (C_1 + C_{1p})$ .

The startup requirements are calculated by the Barkhausen criterion, which implies that the loop gain  $A(f_0) \beta(f_0)$  at the oscillation frequency  $f_0$ , must be greater than unity, i.e.  $A(f_0) \beta(f_0) \geq 1$ , for oscillations to occur [35]. In this context,  $A(f_0)$  represents the transconductance of  $M_1$  seen from the secondary, while  $\beta(f_0)$  is the transfer function of the linear feedback network. This further means that the magnitude of  $A\beta$  must be greater than unity, i.e.  $|A(f_0) \beta(f_0)| \geq 1$ , while its phase shift must be equal to  $0^\circ$  or a multiple of  $360^\circ$ , i.e.  $\arg(A(f_0) \beta(f_0)) = 0^\circ$ . Since the current over the secondary winding is  $I_2 \cong I_1 / n_{12}$ , we observe from Fig. 3 that  $I_1 \cong g_{m1} V_{gs1}$ , thus  $I_2 \cong (g_{m1} V_{gs1}) / n_{12}$ . In order to extract the startup condition we can open the loop by virtually disconnecting the feedback network from  $M_1$ . In this case, we consider for the active part  $A = g_{m0} / n_{12}$ , where  $g_{m0}$  is the minimum transconductance of  $M_1$  that guarantees the trigger condition, whereas for the passive part  $\beta = V_{gs1} / I_2$ . From the analysis of the small-signal circuit in Fig. 3, we obtain:

$$\beta = \frac{V_{gs1}}{I_2} = \frac{I_{wt2}}{sC_{eq} I_2} = \frac{1}{sC_{eq}} \frac{I_{wt2}}{I_{wt1}} \frac{I_{wt1}}{I_2}, \quad (9)$$

$$\frac{I_{wt2}}{I_{wt1}} = \frac{sL_{ms} + R_{cs}}{s(L_{ms} + L_{l2}) + (R_{cs} + R_{wt2}) + 1/sC_{eq}}, \quad (10)$$

$$\frac{I_{wt1}}{I_2} = \frac{r'_{ds}}{sL'_{l1} + r'_{ds} + R'_{wt1} + \frac{(sL_{ms} + R_{cs})(sL_{l2} + R_{wt2} + 1/sC_{eq})}{s(L_{ms} + L_{l2}) + (R_{cs} + R_{wt2}) + 1/sC_{eq}}}, \quad (11)$$

where  $I_{wt2}$  is the current through  $R_{wt2}$  and  $I_{wt1}$  is the current through  $R'_{wt1}$ . After replacing (10) and (11) in (9), we can rationalize and switch to the frequency domain:

$$\beta = \frac{r'_{ds} (i\omega L_{ms} + R_{cs})(a(\omega) - ib(\omega))}{a^2(\omega) + b^2(\omega)}, \quad (12)$$

where  $a$  and  $b$  are the real and imaginary parts of the denominator of  $\beta$ , which are given by:

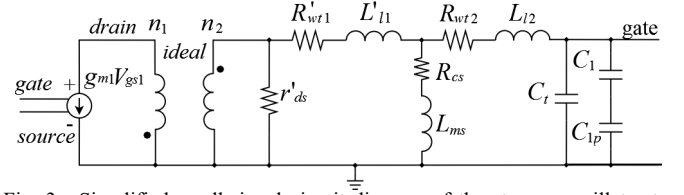


Fig. 3. Simplified small-signal circuit diagram of the step-up oscillator to investigate the mechanism of oscillation at the startup.

$$a(\omega) = -\omega^2 C_{eq} [(r'_{ds} + R'_{wt1})(L_{ms} + L_{l2}) + R_{wt2} L_{ms} + R_{cs} L_{l2} + (R_{wt2} + R_{cs}) L'_{l1}] + r'_{ds} + R'_{wt1} + R_{cs}, \quad (13)$$

$$b(\omega) = \omega C_{eq} [(r'_{ds} + R'_{wt1})(R_{wt2} + R_{cs}) + R_{wt2} R_{cs} - \omega^2 L_{ms} L_{l2} - \omega^2 (L_{ms} + L_{l2}) L'_{l1}] + \omega (L_{ms} + L'_{l1}), \quad (14)$$

where  $\omega = 2\pi f$ . In order to determine the frequency of oscillation  $f_0$ , we extract the frequency at which the imaginary part of the numerator of (12) is zero [35], which means that:

$$2\pi f_0 L_{ms} a(\omega_0) = R_{cs} b(\omega_0). \quad (15)$$

Hence, by solving (15) we get:

$$f_0 = \frac{1}{2\pi} \sqrt{\frac{1}{C_{eq}} \cdot \frac{L_{ms}(r'_{ds} + R'_{wt1}) - R_{cs}(L'_{l1} + C_{eq} R_T^2)}{L_{ms}^2(r'_{ds} + R'_{wt1} + R_{wt2}) + L_{l2} L_{ms}(r'_{ds} + R'_{wt1}) + L'_{l1} L_{ms} R_{wt2} - L'_{l1} L_{l2} R_{cs}}}, \quad (16)$$

where  $R_T^2$  ( $\Omega^2$ ) is given by:

$$R_T^2 = R_{cs} r'_{ds} + R_{wt2} r'_{ds} + R_{cs} R'_{wt1} + R_{wt2} R'_{wt1} + R_{wt2} R_{cs}. \quad (17)$$

Expression (16) includes the leakage inductances  $L'_{l1}$ ,  $L_{l2}$  and the core losses  $R_{cs}$ , and gives the approximate onset oscillation frequency. However, the transformer parameters in (16) are generally frequency-dependent. Therefore, in order to predict the effective oscillation frequency we should include in (16) the approximate AC analytical models of  $L_{ms}$ ,  $R_{w1}$ ,  $R_{w2}$ , and  $R_{cs}$ , as shown in [32] and [37], which comprise eddy-current effects and the complex permeability model, together with an estimate (or measure) of the coupling  $k$  and of  $C_{22}$ . In section IV, equation (16) will be resolved numerically by finding the point at which the oscillation frequency equals the operating frequency of the microtransformer. Now, if we consider a lossy transformer with perfect coupling ( $L'_{l1} \approx 0$ ,  $L_{l2} \approx 0$ ), (16) can be simplified to:

$$f_0 \approx \frac{1}{2\pi} \sqrt{\frac{1}{C_{eq}} \cdot \frac{L_{ms}(r'_{ds} + R'_{wt1}) - R_{cs} C_{eq} R_T^2}{L_{ms}^2(r'_{ds} + R'_{wt1} + R_{wt2})}}. \quad (18)$$

Alternatively, if we consider a loosely coupled transformer without core losses ( $R_{cs} \approx 0$ ), (16) can be simplified to:

$$f_0 \approx \frac{1}{2\pi} \sqrt{\frac{1}{C_{eq}} \cdot \frac{r'_{ds} + R'_{wt1}}{L_{ms}(r'_{ds} + R'_{wt1} + R_{wt2}) + L_{l2}(r'_{ds} + R'_{wt1}) + L'_{l1} R_{wt2}}}. \quad (19)$$

If we neglect both leakage inductances ( $L'_{l1} \approx 0$ ,  $L_{l2} \approx 0$ ) and core losses ( $R_{cs} \approx 0$ ), i.e. loss-less and perfectly coupled transformer, (16) can be shortened to:

$$f_0 \approx \frac{1}{2\pi} \sqrt{\frac{1}{C_{eq}} \cdot \frac{r'_{ds} + R'_{wt1}}{L_{ms}(r'_{ds} + R'_{wt1} + R_{wt2})}}. \quad (20)$$

which leads to the general resonant frequency of LC-circuits [35], i.e.  $f_0 \cong 1 / [2\pi (C_{eq} L_{ms})^{1/2}]$  by considering  $R'_{wt1} \gg R_{wt2}$ .

Now, if we consider only the real part of (12) and we combine the findings of (15) at resonance, we have that:

$$\beta(f_0) = r'_{ds} \frac{R_{cs} a(f_0) + 2\pi f_0 L_{ms} b(f_0)}{a^2(f_0) + b^2(f_0)} = \frac{r'_{ds} R_{cs}}{a(f_0)} \quad (21)$$

In order to obtain the unity loop gain at resonance as  $A(f_0) \beta(f_0) = (g_{m0} / n_{12}) \beta(f_0) = 1$ , the minimum  $g_{m0}$  of  $M_1$  is:

$$g_{m0} = \frac{n_{12}}{\beta(f_0)} = \frac{n_{12} a(f_0)}{r'_{ds} R_{cs}}, \quad (22)$$

which results, after some algebraic steps, in:

$$g_{m0} \approx \frac{n_{12}}{r'_{ds}} \cdot \frac{L_{ms}^2 (r'_{ds} + R'_{wt1}) + L_{l2}^2 R_{cs}}{L_{ms} (L_{ms} + L_{l2}) (r'_{ds} + R'_{wt1}) - L_{l2}^2 R_{cs}} + \frac{C_{eq} R_T^2 [(L_{ms} + L_{l2}) (r'_{ds} + R'_{wt1}) + 2L_{l2} R_{cs}]}{L_{ms} (L_{ms} + L_{l2}) (r'_{ds} + R'_{wt1}) - L_{l2}^2 R_{cs}}. \quad (23)$$

Equation (23) is obtained by considering a step-up transformer with  $n_{12} \gg 1$ ,  $L'_{l1} \approx L_{l2}$  from (5),  $R'_{wt1} \gg R_{wt2}$ , and hence  $R_T^2 \approx R_{cs} (r'_{ds} + R'_{wt1})$ . Now, if we consider a loosely coupled transformer without core losses ( $R_{cs} \approx 0$ ), (23) can be simplified to:

$$g_{m0} \approx \frac{n_{12}}{r'_{ds}} \cdot \frac{L_{ms}}{L_{ms} + L_{l2}}. \quad (24)$$

Besides, if we consider a lossy transformer with perfect coupling ( $L'_{l1} \approx L_{l2} \approx 0$ ), (23) can be simplified as:

$$g_{m0} \approx \frac{n_{12}}{r'_{ds} L_{ms}} \cdot (C_{eq} R_T^2 + L_{ms}). \quad (25)$$

Finally, if we neglect both leakage inductances ( $L'_{l1} \approx L_{l2} \approx 0$ ) and core losses ( $R_{cs} \approx 0$ ), i.e. loss-less and perfectly coupled transformer, (23) can be reduced to:

$$g_{m0} \approx \frac{n_{12}}{r'_{ds}} = \frac{1}{r_{ds} n_{12}}. \quad (26)$$

Now, if we neglect  $V_{ds1}$  in (8) because of the small values of  $V_{teg}$  considered, we obtain that  $g_{ds1} \approx -\beta_{n1} V_{m1}$  and thus  $r_{ds} \approx 1 / (-\beta_{n1} V_{m1})$ . In this case, (26) becomes:

$$g_{m0} \approx -\frac{\beta_{n1} V_{m1}}{n_{12}}. \quad (27)$$

Additionally, we can extract the minimum source voltage  $V_{teg0}$  by inverting (7) and using  $g_{m0}$  instead of  $g_{m1}$  as follows:

$$V_{teg0} \approx \frac{g_{m0}}{\beta_{n1}} \cdot (1 - R_{eq} \beta_{n1} V_{m1}). \quad (28)$$

Now, by substituting (27) in (28) we obtain:

$$V_{teg0} \approx -\frac{V_{m1}}{n_{12}} \cdot (1 - R_{eq} \beta_{n1} V_{m1}). \quad (29)$$

In order to minimize the first factor in (29), the step-up transformer should have a large  $n_{12}$ , while the n-type MOSFET should have a small  $|V_{m1}|$ . In order to minimize the second factor  $(1 - R_{eq} \beta_{n1} V_{m1})$ , we should reduce again  $|V_{m1}|$  together with  $R_{eq}$  and  $\beta_{n1}$ . In Section IV this design

optimization will be discussed in depth. Finally, the Barkhausen criterion is fulfilled if  $g_{m1}$  is greater than the  $g_{m0}$  given in (22)-(27), or if  $V_{teg}$  is greater than the  $V_{teg0}$  given in (28)-(29), as:

$$g_{m1} \geq g_{m0} \quad \text{or} \quad V_{teg} \geq V_{teg0}. \quad (30)$$

Equation (30) sets the startup condition in order for oscillations to occur. Since few and mainly qualitative analyses are present in literature [18] [26] for this kind of circuits, relationships (16), (18)-(20), (22)-(27), and (28)-(29) represent new analytical expressions for calculating respectively  $f_0$ ,  $g_{m0}$ , and  $V_{teg0}$ , in a Meissner-type oscillator topology with a potential lossy and loosely coupled step-up microtransformer.

### C. Properties of the Bond Wire Microtransformers

Two 1:n<sub>2</sub> bond wire transformers on a PCB substrate were used (Fig. 4). The first is the 1:38 turns toroidal MnZn 75 ferrite core reported in [32], with a  $\cong 24$  mm<sup>2</sup> area and inductance per unit area of 12.8  $\mu$ H/mm<sup>2</sup> up to 0.3 MHz. The second is a 1:52 toroidal race-track shaped 40011 ferromagnetic LTCC core similar to that shown in [34], with a  $\cong 28$  mm<sup>2</sup> area and 1.1  $\mu$ H/mm<sup>2</sup> up to several MHz. Since the oscillation frequency  $f_0$  described in (16), (18)-(20) depends mainly on  $L_{ms}$  and  $C_{eq}$ , in order to limit high-frequency effects the transformer should have a large  $L_{22}$  along with a good coupling  $k$  to reduce  $f_0$  with a fixed  $C_{eq}$ . Besides, a high turns ratio  $n_{12}$ , i.e. high  $L_{22} / L_{11}$ , is further required as shown in (28)-(29) to allow lower startup voltages. On the other hand, integrated capacitors have limited values which impose restrictions on  $C_{eq}$ , and thus on the minimum achievable  $f_0$ .

The ferrite core outer  $D_o$  and inner  $D_i$  diameters are 3.95 mm and 2.15 mm, whereas the thickness is 0.45 mm. Since two pairs of bonding wires were found to be short-circuited, the actual turns ratio of the MnZn 75 device is 1:36. The LTCC core size is  $7.0 \times 3.0 \times 0.4$  mm<sup>3</sup> ( $l \times w \times h$ ), with a 1 mm core width. The LTCC core device is assembled with 25  $\mu$ m gold bonding wires on a PCB substrate with copper metallizations with 90  $\mu$ m width, 60  $\mu$ m minimum spacing, and 16  $\mu$ m thickness. The one-turn mean metal and wire length are respectively 1.7 and 2.1 mm, the bond pad pitch is 150  $\mu$ m, and the outer-inner pad distances from the core are respectively 450 and 225  $\mu$ m. The LTCC core has relative permeability  $\mu_{rc} \approx 200$ , resistivity  $\rho_c > 10^8$   $\Omega$ ·cm, saturation flux density  $B_s \approx 300$  mT, mean magnetic path length  $l_c \approx 14.3$  mm, and cross-section  $A_c \approx 0.40$  mm<sup>2</sup>. The -3dB frequency and bandwidth of the inductive  $\mu'_{rs}$  and resistive  $\mu''_{rs}$  relative permeabilities, respectively, are estimated to be  $f_H \approx 9.6$  MHz and  $\Delta f \approx 1.0$  MHz, as discussed in [32] [37].

The MnZn 75 core [32] has a higher permeability compared to the ferromagnetic LTCC core thus ensuring higher self-inductances but nevertheless high series resistances due to greater eddy currents in both windings and core. Besides this, the LTCC core [38]-[40] has a lower permeability and a higher resistivity which allow to reduce the high-frequency effects while providing lower self-inductances.

## IV. EXPERIMENTAL RESULTS AND MODEL VALIDATION

This section illustrates the modeling results and the startup measurements obtained with both bond wire transformers.

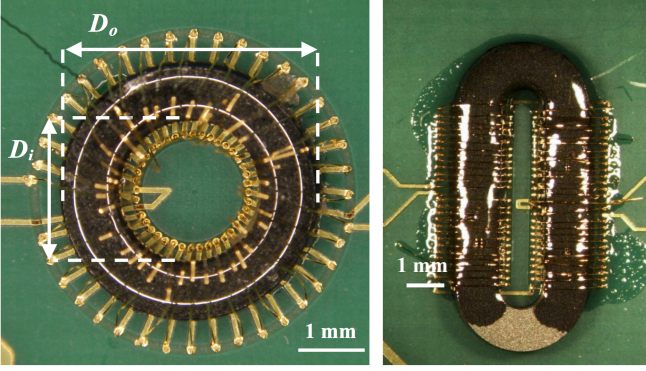


Fig. 4. The bond wire microtransformers used for validation: 1:38 turns with MnZn 75 core (left), and 1:52 turns with 40011 ferromagnetic LTCC core (right).

The energy source voltage  $V_{ieg}$  is assumed to be in the 50-250 mV range by assuming the 10 mV/K Seebeck coefficient of the CP14 module [36] and a 5-25 K temperature gradient between cold and hot side. These are typical values for wearable or industrial applications. Fig. 5 shows a microphotograph of the IC with the top metal pads compatible with bond wire micromagnetics. The die area is  $15 \text{ mm}^2$ , and the area of the sole step-up oscillator in Fig. 1, composed by the active (i.e.  $M_1, M_2, M_3$ ) and passive (i.e. capacitors) parts, is about  $0.6 \text{ mm}^2$ . The remaining area contains a series of unused integrated capacitors and MOSFETs that can be optionally connected. Besides, the measured parasitic resistances of connections are  $R_{con1} \approx 2.35 \Omega$  and  $R_{con2} \approx 1.93 \Omega$  for the primary and secondary side. For  $M_1$ , we have  $\beta_{n1} = 0.3157 \text{ A/V}^2$ , and  $C_{gs1} \approx 3.0 \text{ pF}$ . The values used in the experiment (see Fig. 1) are:  $R_{ieg} = 0.43 \Omega$  [36],  $C_{in} = 390 \text{ nF}$ ,  $C_{out} = 100 \text{ nF}$ , and  $R_{out} = 10 \text{ M}\Omega$ . The latter is chosen to represent the typical current drawn by a supervisor circuit whose duty is the activation of the conventional power converter once the step-up oscillator has made the minimum supply voltage available.

#### A. Startup with Ferrite Core Microtransformer

The MnZn 75 core has a higher permeability ( $\mu_{rc} \approx 5000$ ) and a lower resistivity ( $\rho_c = 3 \cdot 10^2 \Omega \cdot \text{cm}$ ) than the LTCC core. This enhances  $L_{11}, L_{22}$  at the expense of higher  $R_{11}, R_{22}$  due to higher core losses. However, this device has a very good  $k$ . By combining into (16) the approximate AC analytical model (extrapolated from core material and impedance measurements in [32]) of the 1:36 turns MnZn 75 device, we can determine numerically the effective oscillation frequency.

Let us now recall that  $r'_{ds} = n_{12}^2 / g_{ds1}$ , with  $g_{ds1} \approx -\beta_{n1} V_{m1}$  since  $|V_{m1}| \gg V_{ds1}$ , as previously discussed. Fig. 6 shows the expression of  $f_0$  in (16) as a function of frequency obtained with  $C_{22} < 1 \text{ pF}$  (estimated from [37]),  $C_{par} \approx 25 \text{ pF}$ , and thus  $C_t \approx C_{22} + C_{gs1} + C_{par} \approx 29 \text{ pF}$ ,  $C_1 = 150 \text{ pF}$ ,  $C_{1p} = 10 \text{ pF}$ , and thus  $C_{eq} = C_t + (C_1 C_{1p}) / (C_1 + C_{1p}) = 39 \text{ pF}$ .

TABLE I  
MICROTRANSFORMER PARAMETERS.

| Core | $L_m$ (nH) | $L_{ms}$ ( $\mu\text{H}$ ) | $L_{11}$ (nH) | $L_{12}$ ( $\mu\text{H}$ ) | $R_{w1}$ ( $\Omega$ ) | $R_{w2}$ ( $\Omega$ ) | $R_{cs}$ ( $\Omega$ ) | $k$  |
|------|------------|----------------------------|---------------|----------------------------|-----------------------|-----------------------|-----------------------|------|
| MnZn | 130        | 165                        | 14.4          | 18.3                       | 0.2                   | 5.5                   | 1260                  | 0.9  |
| LTCC | 6.8        | 18.4                       | 5.3           | 14.5                       | 0.15                  | 8.1                   | 10.7                  | 0.56 |

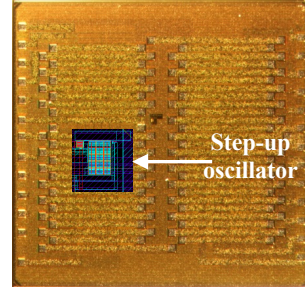


Fig. 5. Microphotograph of the IC designed in a STMicroelectronics  $0.32 \mu\text{m}$  BCD technology. The step-up converter layout is shown inside.

The effective oscillation frequency (denoted as  $f_0$ ) is the point where the frequencies in the xy-axes match ( $f_0 \approx 1.45 \text{ MHz}$ ). Hence, the transformer parameters at  $f_0$  from [32] are summarized in Table I.

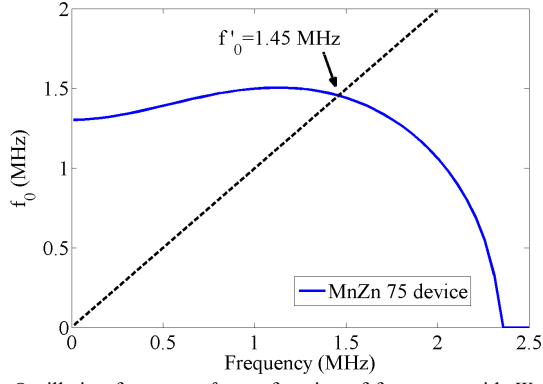
In order for oscillations to occur, we must design  $M_1$  or set external conditions so that  $g_{m1} \geq g_{m0}$  or  $V_{ieg} \geq V_{ieg0}$  as stated in (30). Fig. 7 shows the transconductances  $g_{m1}$  in (7) and  $g_{m0}$  in (22) versus  $V_{ieg}$ , and demonstrates that the converter starts to oscillate when  $g_{m1} \geq g_{m0}$  which happens at  $V_{ieg0} \approx 200 \text{ mV}$  with  $g_{m1} = g_{m0} \approx 28 \text{ mS}$ . Fig. 8 shows on the top the same  $g_{m0}$  and  $g_{m1}$  (with  $V_{ieg} = 200 \text{ mV}, 220 \text{ mV}$ ) versus  $\beta_{n1}$ , and explains that the startup condition  $g_{m1} \geq g_{m0}$  happens for  $0.1 \text{ A/V}^2 \leq \beta_{n1} \leq 4.5 \text{ A/V}^2$  with  $V_{ieg} = 220 \text{ mV}$ , whereas the useful range of  $\beta_{n1}$  shrinks with  $V_{ieg} = 200 \text{ mV}$ . Hence, the chosen value  $\beta_{n1} = 0.3157 \text{ A/V}^2$  represents a good compromise for oscillations to occur. Furthermore, Fig. 8 illustrates on the bottom the strong dependence of  $f_0$  on the gain  $\beta_{n1}$ . Hence, as a general rule we can deduce that reducing  $\beta_{n1}$  implies dropping the startup and MOSFET transconductances, i.e. reducing the minimum source voltage, at the cost of higher oscillation frequencies and thus of higher core losses. The main parameters of the small-signal analysis are shown in Table II.

Fig. 9 shows on the top  $g_{m0}$  and  $g_{m1}$  versus  $V_{m1}$  with the chosen  $\beta_{n1}$  and  $V_{ieg} = 200 \text{ mV}$ , whereas on the bottom the dependence of  $f_0$  on  $V_{m1}$  is depicted. We can assess that decreasing  $|V_{m1}|$  allows to increase  $g_{m1}$  and to decrease  $g_{m0}$ , however at the cost of higher oscillation frequencies. Fig. 10 shows further the contour plot of  $g_{m0}$  with  $V_{ieg} = 200 \text{ mV}$  as a function of  $V_{m1}$  and  $\beta_{n1}$ .

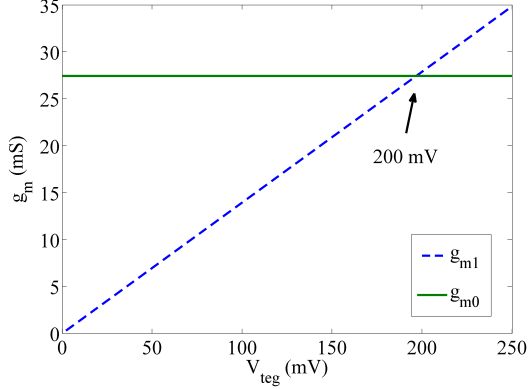
In order to set-up the startup conditions, Fig. 11 plots the starting isosurface as a function of  $(V_{m1}, \beta_{n1}, V_{ieg})$  obtained by evaluating if  $g_{m1} \geq g_{m0}$  is verified: if this is true, the point is located on or above the isosurface. The combinations below the isosurface do not permit oscillations. We see that the minimum allowable  $V_{ieg} = V_{ieg0}$  for which oscillations occur is  $\approx 25 \text{ mV}$ , and can be potentially obtained if  $(V_{m1}, \beta_{n1}) = (-0.1 \text{ V}, 6 \text{ A/V}^2)$ . We remark that the plots from Fig. 8 to Fig. 11 assume that the transformer parameters remain constant.

An Agilent E3631 power supply is used for emulating the voltage source. Experimental tests are performed on the startup converter with the 1:36 turns MnZn 75 device. The circuit starts oscillating and increasing the output voltage from input source voltages down to  $V_{ieg} \approx 228 \text{ mV}$ . If  $V_{ieg} \approx 260 \text{ mV}$ , the steady-state rectified output voltage is  $V_{rect} \approx 0.7 \text{ V}$ , which is sufficient to start a standard boost

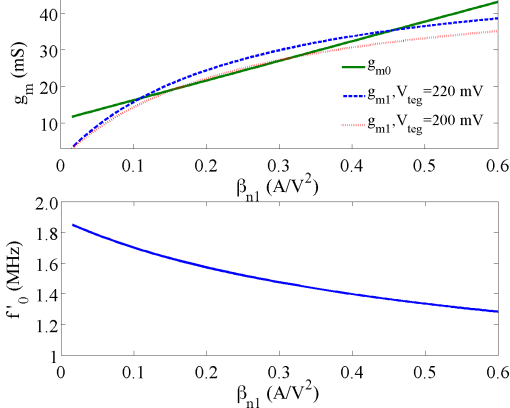




**Fig. 6.** Oscillation frequency  $f_0$  as a function of frequency with  $W_1 = 2$  mm for the step-up oscillator with the 1:36 turns MnZn 75 core transformer. The dashed black line is the bisector of the graph.

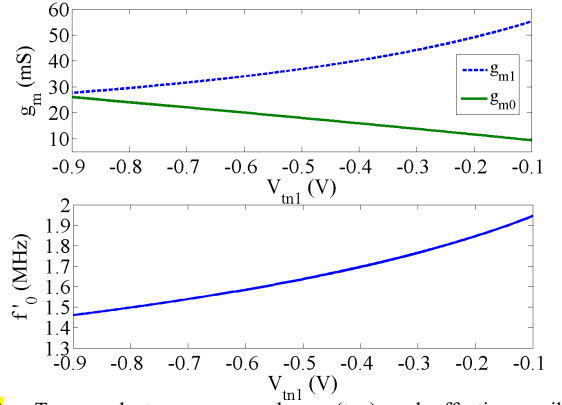


**Fig. 7.** Transconductances  $g_{m1}$  and  $g_{m0}$  versus source voltage  $V_{teg}$  with the chosen  $\beta_{n1}$  and with the 1:36 turns MnZn 75 core transformer.

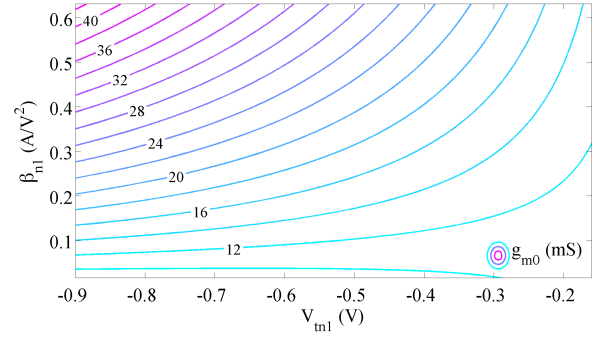


**Fig. 8.** Transconductances  $g_{m1}$  and  $g_{m0}$  (top) and effective oscillation frequency  $f'_0$  (bottom) versus gain  $\beta_{n1}$  for the step-up oscillator with the 1:36 turns MnZn 75 core transformer.

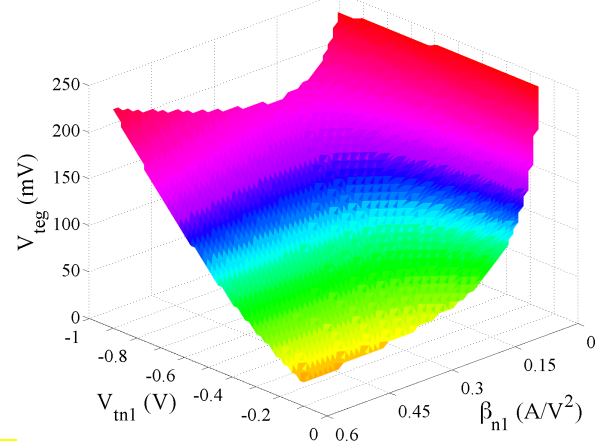
converter or a charge pump with reasonable efficiency. This is in good agreement with the analytical results described previously, which report  $V_{teg0} \approx 200$  mV. Fig. 12 displays the experimental startup waveforms obtained by increasing  $V_{teg}$ , while Fig. 13 depicts the steady-state oscillating waveforms associated to Fig. 12 for time  $t \geq 25$  s with a measured oscillation frequency of  $\approx 1.36$  MHz, which is very close to the expected  $f'_0 \approx 1.45$  MHz. The data in Figs. 12 and 13 are acquired through a digital sampling oscilloscope Tektronix MSO 2024.



**Fig. 9.** Transconductances  $g_{m1}$  and  $g_{m0}$  (top) and effective oscillation frequency  $f'_0$  (bottom) versus  $M_1$  threshold voltage  $V_{tn1}$  with the chosen  $\beta_{n1}$ ,  $V_{teg} = 200$  mV, and the 1:36 turns MnZn 75 core transformer.



**Fig. 10.** Contour plot of  $g_{m0}$  as a function of  $M_1$  threshold voltage  $V_{tn1}$  and gain  $\beta_{n1}$  with  $V_{teg} = 200$  mV and the 1:36 turns MnZn 75 core transformer.



**Fig. 11.** Starting isosurface of the step-up oscillator as a function of  $M_1$  threshold voltage  $V_{tn1}$ , gain  $\beta_{n1}$ , and source voltage  $V_{teg}$  with the 1:36 turns MnZn 75 core transformer. The points  $(V_{tn1}, \beta_{n1}, V_{teg})$  under the isosurface do not allow oscillation, whereas the combinations on or above the isosurface permit oscillations.

### B. Startup with Magnetic LTCC Core Microtransformer

The 40011 magnetic LTCC core has a lower permeability ( $\mu_{rc} \approx 200$ ) and a higher resistivity ( $\rho_c > 10^8 \Omega \cdot \text{cm}$ ) than the MnZn 75 core. This reduces  $L_{11}$ ,  $L_{22}$  with the benefit of lower  $R_{11}$ ,  $R_{22}$ , i.e. lower core losses, due to the higher resistivity. However, the transformer is loosely coupled, i.e. it has lower  $k$  than the MnZn 75 device. As before, by joining into (16) the approximate AC analytical model of the 1:52 turns 40011 LTCC device based on [34], we can determine numerically  $f'_0$ .

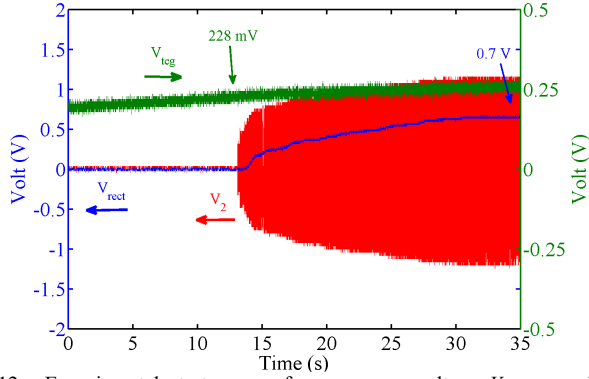


Fig. 12. Experimental startup waveforms: source voltage  $V_{teg}$ , secondary voltage  $V_2$ , and rectified output voltage  $V_{rect}$  for the step-up oscillator with the 1:36 turns MnZn 75 core transformer.  $V_2$  and  $V_{rect}$  are referred to the left y-axis and  $V_{teg}$  to the right y-axis.

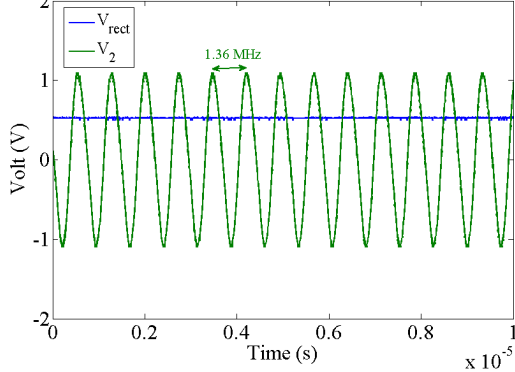


Fig. 13. Experimental oscillating waveforms: secondary voltage  $V_2$ , and rectified output voltage  $V_{rect}$  for the step-up oscillator with the 1:36 turns MnZn 75 core transformer.

TABLE II

MAIN TRANSFORMER AND DIFFERENTIAL PARAMETERS.

| Core | $n_{12}$      | $L'_{l1}$ ( $\mu\text{H}$ ) | $R'_{w1}$ ( $\text{k}\Omega$ ) | $R_{w2}$ ( $\Omega$ ) | $R_{eq}$ ( $\Omega$ ) |
|------|---------------|-----------------------------|--------------------------------|-----------------------|-----------------------|
| MnZn | 36            | 18.7                        | 3.86                           | 7.43                  | 4.48                  |
| LTCC | 52            | 14.4                        | 7.92                           | 10                    | 2.93                  |
| Core | $C_{eq}$ (pF) | $g_{m1}$ (mS)               | $g_{m0}$ (mS)                  | $f_0$ (MHz)           | $V_{teg0}$ (mV)       |
| MnZn | 39            | 30.6                        | 28                             | 1.45                  | 200                   |
| LTCC | 84            | 15.5                        | 12.1                           | 3.03                  | 71                    |

Fig. 14 plots on the top the expression of  $f_0$  in (16) as a function of frequency obtained with  $C_{22} < 1$  pF (estimated from [37]),  $C_{par} \approx 40$  pF, and thus  $C_t \approx C_{22} + C_{gs1} + C_{par} \approx 44$  pF,  $C_1 = 600$  pF,  $C_{1p} = 40$  pF, and thus  $C_{eq} = C_t + (C_1 C_{1p}) / (C_1 + C_{1p}) = 84$  pF. The effective oscillation frequency is located at  $f'_0 \approx 3.03$  MHz. The values of the transformer parameters at  $f'_0$  are summarized in Table I. Fig. 14 on the bottom shows the transconductances  $g_{m1}$  in (7) and  $g_{m0}$  in (22) versus  $V_{teg}$  with the chosen  $\beta_{n1}$ , and proves that the converter starts to oscillate at  $V_{teg0} \approx 71$  mV with  $g_{m1} = g_{m0} \approx 12.1$  mS. Fig. 15 displays on the top the same  $g_{m0}$  and  $g_{m1}$  (with  $V_{teg} = 71$  mV, 90 mV) as a function of  $\beta_{n1}$ , and clarifies that the startup condition  $g_{m1} \geq g_{m0}$  occurs for  $0.1 \text{ A/V}^2 \leq \beta_{n1} \leq 0.7 \text{ A/V}^2$  with  $V_{teg} = 90$  mV. Besides,  $f_0$  does not change significantly with  $\beta_{n1}$ . Reducing  $\beta_{n1}$  involves reducing the startup and MOSFET transconductances, i.e.

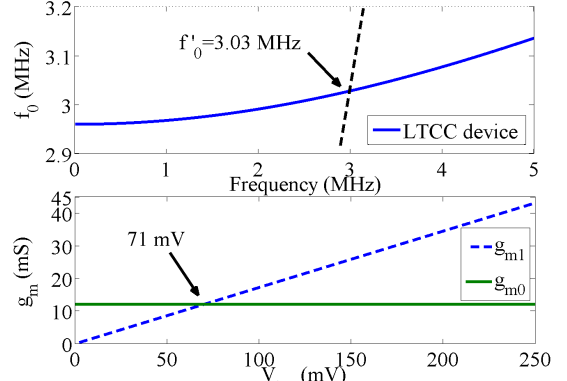


Fig. 14. Oscillation frequency  $f_0$  as a function of frequency (top) and transconductances  $g_{m1}$  and  $g_{m0}$  (bottom) versus source voltage  $V_{teg}$  with  $W_1 = 2$  mm for the step-up oscillator with the 1:52 turns 40011 LTCC core transformer.

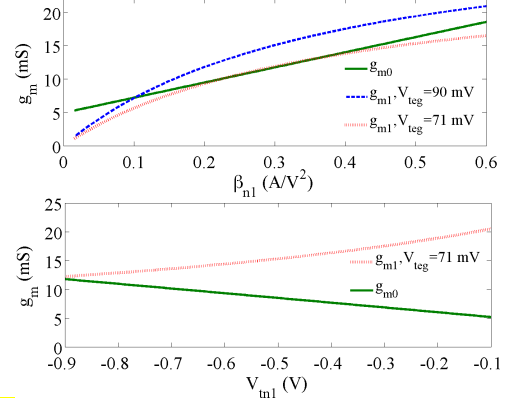


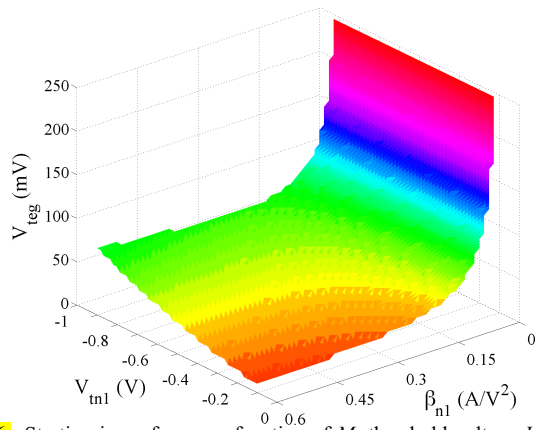
Fig. 15. Transconductances  $g_{m1}$  and  $g_{m0}$  versus  $M_1$  gain  $\beta_{n1}$  (top), and threshold voltage  $V_{m1}$  with the chosen  $\beta_{n1}$  (bottom), with the 1:52 turns LTCC core transformer.

reducing the minimum source voltage, without substantial drawbacks. The main parameters of the small-signal analysis with  $V_{teg} = 90$  mV are reported in Table II.

Let us now set  $r'_{ds} = n_{12}^2 / g_{ds1}$ , where  $g_{ds1}$  is derived from (8). Fig. 15 illustrates on the bottom  $g_{m0}$  and  $g_{m1}$  versus  $V_{m1}$  with the chosen  $\beta_{n1}$  and  $V_{teg} = 71$  mV. Decreasing  $|V_{m1}|$  increases  $g_{m1}$  and decreases  $g_{m0}$ , without significant changes of  $f_0$ .

Fig. 16 plots the starting isosurface as a function of  $(V_{m1}, \beta_{n1}, V_{teg})$ . The minimum  $V_{teg} = V_{teg0}$  for which oscillations might happen is  $\approx 10$  mV, obtained in case  $(V_{m1}, \beta_{n1}) = (-0.1 \text{ V}, 0.6 \text{ A/V}^2)$ . The plots in Figs. 15 and 16 assume constant transformer parameters, which is reasonably true because  $f_0$  is quite insensitive from  $\beta_{n1}$  and  $V_{m1}$ .

Experimental tests are performed on the startup converter with the 1:52 turns 40011 LTCC device achieving oscillations with input voltages down to  $V_{teg} \approx 104$  mV. When  $V_{teg} \approx 152$  mV, a steady-state rectified output  $V_{rect} \approx 0.7$  V is provided. This is in satisfactory agreement with the analytical results illustrated before, which report  $V_{teg0} \approx 71$  mV. Fig. 17 shows the experimental startup waveforms obtained by increasing  $V_{teg}$  up to 104 mV and above. At steady-state we obtain a measured oscillation frequency of  $\approx 2.88$  MHz, which is reasonably close to the effective  $f'_0 \approx 3.03$  MHz. The same equipment is used for the stimulus and for acquiring the data.



**Fig. 16.** Starting isosurface as a function of  $M_1$  threshold voltage  $V_{m1}$ , gain  $\beta_{n1}$ , and source voltage  $V_{reg}$  with the 1:52 turns 40011 LTCC core transformer. Oscillations occur for points  $(V_{m1}, \beta_{n1}, V_{reg})$  above the surface.

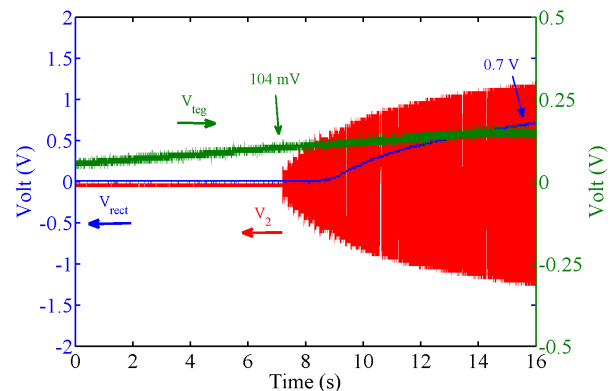
## V. CONCLUSIONS

This work achieves a measured minimum startup voltage of  $\approx 100$  mV obtained by coupling the low-voltage oscillator IC and an LTCC core bond wire transformer. As a new element, with respect to Meissner-type oscillators presented in literature, this work has investigated the effects of core losses and leakage inductances on the startup requirements, and has provided a complete analytical model of the whole circuit with lossy microtransformers. The analysis highlights the trade-offs between MOSFET design and technological parameters, i.e.  $\beta_{n1}$  and  $V_{m1}$ , and the microtransformer parameters, i.e.  $L_{ms}$ ,  $k$ , and  $n_{12}$ , in order to reduce the minimum transconductance  $g_{m0}$  and the minimum startup voltage  $V_{reg0}$ .

As an additional key point, the step-up oscillator IC validates the proposed model. We also remark that literature reports lower activation voltages based on mechanical switches [13], and on off-chip or SMD transformers [18] [19] [24]-[26]. The circuits in [18] and [27] start respectively from 40 mV and 20 mV, and rely on larger better-coupled off-chip transformers with higher inductances and turns-ratios of 1:60 and 1:100. In addition, the amplifier FET in [18] has a very favorable threshold voltage of -15 mV. However, the proposed approach based on bond wire magnetics allows direct die-level integration of the magnetic part, as in [34]. Lower startup voltages can be achieved, e.g. down to  $\approx 10$  mV, by tuning design parameters, or by using more efficient microtransformers.

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**Fig. 17.** Experimental startup waveforms: source voltage  $V_{reg}$ , secondary voltage  $V_2$ , and rectified output voltage  $V_{rect}$  for the step-up oscillator with the 1:52 turns 40011 LTCC core transformer.

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