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Semi-Experimental Equilibrium Structure Determinations by Employing B3LYP/SNSD Anharmonic Force Fields: Validation and Application to Semirigid Organic Molecules

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Abstract

This work aims at extending the semi-experimental (SE) approach for deriving accurate equilibrium structures to large molecular systems of organic and biological interest. SE equilibrium structures are derived by a least-squares fit of the structural parameters to the experimental ground-state rotational constants of several isotopic species corrected by vibrational contributions computed by quantum mechanical (QM) methods. A systematic benchmark study on 21 small molecules (CCse set) is carried

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out to evaluate the performance of hybrid density functionals (in particular B3LYP) in the derivation of vibrational corrections to rotational constants. The resulting SE equilibrium structures show a very good agreement with the corresponding geometries obtained employing post-Hartree-Fock vibrational corrections. The use of B3LYP in conjunction with the double- ζ SNSD basis set strongly reduces the computational costs, thus allowing for the evaluation of accurate SE equilibrium structures for medium-sized molecular systems. On these grounds, an additional set of 26 SE equilibrium structures including the most common organic moieties has been set up by collecting the most accurate geometries available in the literature together with new determinations from the present work. The overall set of 47 SE equilibrium structures determined using B3LYP/SNSD vibrational corrections (B3se set) provides a high quality benchmark for validating the structural predictions of other experimental and/or computational approaches. Finally, we present a new strategy (referred to as template approach) to deal with the cases for which it is not possible to fit all geometrical parameters due to the lack of experimental data.

INTRODUCTION

The last decades have seen many efforts to determine accurate molecular structures for systems of increasing size and complexity.¹⁻¹⁴ Detailed knowledge of the equilibrium structures of isolated molecular systems of chemical, biological or technological interest is indeed a prerequisite for a deeper understanding of other physical-chemical properties, ranging from a precise evaluation of the electronic structure to the understanding and analysis of the dynamical and environmental effects affecting the molecular structures and properties.^{1,2,15-17} Moreover, the availability of reference molecular structures allows one to test the accuracy of different quantum mechanical (QM) approaches,^{2,18-22} and it is essential for a correct development of accurate force fields either of general applicability (e.g. for systems of biological interest)²³⁻²⁶ or specifically tailored for individual systems.²⁷⁻³⁰ Furthermore, robust and re-

liable computational approaches are of primary importance for conformational analysis and modeling of drugs and biomolecules,^{18,31} as well as for a deeper understanding of chemical reactivity in terms of transition state structures,³² which are not directly determinable from experiment. For a fruitful interplay of experiment and theory in the interpretation and quantification of molecular properties, and for validation purposes, it is hence desirable to have a large number of accurate equilibrium geometries at one disposal.

Nowadays, an increasing number of experimental data is available thanks to the growing interest in the field, but the structural parameters derived from experiment often depend on the chosen technique and can be biased by vibration and/or environmental conditions.^{2,15} For example, the vibrationally averaged r_0 and substitution r_s structures are obtained from microwave and/or rotationally resolved infrared investigations through the analysis of the vibrational ground-state rotational constants for different isotopologues, but without an explicit consideration of vibrational effects.³³ The dependence of the results on experimental conditions complicates both the comparison of structures obtained with different experimental techniques and the subsequent use of these empirical structures in the computation of molecular properties. In addition, all vibrationally averaged structures (r_0 , r_s , $r_{\alpha,T}$, $r_{g,T}$, etc.) depend on the isotopic species considered.^{33,34}

A way to avoid all these problems is to resort to equilibrium structures (r_e), which are defined as the geometries at the minimum of the Born-Oppenheimer (BO) potential energy surface.^{1,2} Although they are cumbersome to derive experimentally, and therefore generally available only for small molecules, this kind of structures is preferred as they exclude vibrational effects in a rigorous manner and, within the BO approximation,^{35,36} are independent of the considered isotopic species. Moreover, depending solely on the electronic structure of the molecular system, r_e structures are directly comparable with the results from QM calculations.

Reference equilibrium structures can be obtained from high-level QM calculations, for instance making use of the coupled-cluster (CC) singles and doubles approximation augmented

by a perturbative treatment of triple excitations, CCSD(T),³⁷ which is able to provide accurate structures, rivaling the best experimental results, provided that extrapolation to the complete basis-set limit and core correlation are taken into the proper account (see, for example, refs. 38–40). However, for medium-sized molecular systems such computations are still very challenging, due to the unfavourable scaling of highly correlated levels of theory with the number of basis functions.

An important step forward in this field has been provided by the introduction of the so-called semi-experimental (SE) equilibrium geometry (r_e^{SE}), which is obtained by a least-square fit of experimental rotational constants of different isotopologues corrected by computed vibrational contributions.^{1,2,41} Introduced by Pulay *et al.*,⁴¹ this method is nowadays considered the best approach to determine accurate equilibrium structures for isolated molecules.⁴² Such an interplay of theory and experiment paves the route toward the extension of accurate structural studies to systems larger than those treatable by experimental and QM methods separately.

From a computational point of view, the bottleneck of the SE protocol is the calculation of the cubic force field at a level of theory sufficiently accurate to give reliable vibrational corrections to rotational constants.⁴² Actually, CCSD(T) is considered the gold standard for this kind of determinations, but the computational cost restricts its applicability to systems of less than 10 atoms (see for example Refs. 43–45). Such a limitation needs to be overcome in order to set up a database of accurate molecular geometries to be used as references for benchmark QM calculations as well as for the validation of simpler models for larger systems, with special focus on biomolecule building blocks. Therefore, the setup and validation of a SE approach able to combine high accuracy and low computational cost is of great interest. In this view, we carried out a systematic study to demonstrate that the calculation of vibrational corrections from anharmonic force fields evaluated using the density functional theory (DFT) permits to obtain r_e^{SE} structures that agree well with the best equilibrium geometries reported in the literature, but with a significantly reduced computational effort. The key

point is here the fact that the relevant quantity to correct equilibrium rotational constants is the sum of the vibration-rotation interaction constants α_i^β , and not the individual constants. The advantage is that resonance-free equations can be obtained and that, thanks to error cancellation, it is much easier to get sufficiently accurate values for the sum than for individual terms.

In previous studies, we showed that the B3LYP hybrid functional performs remarkably well for vibrational properties, when coupled to basis sets of at least polarized double- ζ quality including diffuse functions.⁴⁶⁻⁴⁹ On these grounds, all DFT computations have been performed at the B3LYP level.

A first validation study was performed on 21 small molecules (hereafter CCse set) for which a sufficient number of experimental rotational constants is available and cubic CCSD(T) force fields with at least triple- ζ basis sets were computationally feasible or already known. These reference values were next compared with those issuing from B3LYP and MP2 cubic force fields. The remarkable accuracy of B3LYP/SNSD results allowed us to derive new SE equilibrium structures for an additional set of 26 medium-sized molecules characterized by the most representative bond patterns of organic systems, and including H, C, N, O, F, S and Cl atoms. The whole set of 47 SE equilibrium structures determined using B3LYP/SNSD vibrational corrections (hereafter referred to as B3se set) represents a high quality benchmark for structural studies and validation of computational models. In addition to the rigorous SE approach, theoretical and experimental data can also be combined in cases for which the lack of experimental information for a sufficient number of isotopologues prevents the derivation of a complete SE equilibrium structure. In these cases, fixing some geometrical parameters to reliable and accurate estimates allows for the determination of the remaining structural parameters for systems otherwise non-entirely characterizable (see for example Refs. 50-55). To this end, we introduced a new approach, denoted as template approach, that exploits the accurate SE results obtained for reference molecules in order to derive SE equilibrium structures for similar systems by avoiding highly expensive CC computations.

METHODOLOGY AND COMPUTATIONAL DETAILS

The so-called r_0 structure is obtained by a least-squares fit (LSF) of the molecular parameters to the experimental ground-state rotational constants $(B_0^\beta)^{\text{EXP}}$ of a set of isotopologues, or their corresponding moments of inertia $(I_0^\beta)^{\text{EXP}}$, where $\beta = x, y$ or z is one of the principal inertial axes in the molecule-fixed reference frame.

On the other hand, the mixed experimental-theoretical approach starts from the consideration that equilibrium rotational constants should be employed instead of the experimental ones, thus requiring vibrational and electronic contributions to be subtracted before the fitting procedure. The r_e^{SE} structure is then obtained by a LSF to the SE equilibrium rotational constants $(B_e^\beta)^{\text{SE}}$, or their corresponding moments of inertia $(I_e^\beta)^{\text{SE}}$, where $(B_e^\beta)^{\text{SE}}$ are calculated from $(B_0^\beta)^{\text{EXP}}$ as,

$$(B_e^\beta)^{\text{SE}} = (B_0^\beta)^{\text{EXP}} - (\Delta B_0^\beta)^{\text{QM}} \quad (1)$$

$(\Delta B_0^\beta)^{\text{QM}}$ is explicitly given by,

$$\begin{aligned} (\Delta B_0^\beta)^{\text{QM}} &= \frac{m_e}{M_p} g^{\beta\beta} B_e^\beta - \sum_i \frac{\alpha_i^\beta d_i}{2} \\ &= \Delta B_{\text{el}}^\beta + \Delta B_{\text{vib}}^\beta \end{aligned} \quad (2)$$

$\Delta B_{\text{el}}^\beta$ is an electronic contribution, evaluated from the rotational \mathbf{g} tensor and the ratio between electron (m_e) and proton (M_p) masses.⁵⁶⁻⁵⁸ Although this term is often negligible, it will be systematically included in our computations for the sake of completeness. Within the BO approximation and enforcing Eckart-Sayvetz conditions,^{35,36,59,60} the vibrational contribution $\Delta B_{\text{vib}}^\beta$ is obtained by applying second-order vibrational perturbation theory (VPT2) to the molecular ro-vibrational Hamiltonian expressed in normal coordinates.⁶¹⁻⁶³ In the summation of eq. 2, α_i^β are the vibration-rotation interaction constants, explicitly given in the Supplementary Information (SI), and d_i is the degeneracy of the i -th vibrational normal

mode.

In the present investigation, the cubic force fields required for the computation of the $\Delta B_{\text{vib}}^{\beta}$ term have been evaluated at the CCSD(T),^{37,64} second-order Møller-Plesset perturbation theory (MP2)^{65,66} and DFT⁶⁷ levels. The correlation-consistent polarized cc-p(wC)VnZ basis sets⁶⁸⁻⁷¹ have mainly been used in CCSD(T) and MP2 calculations, with $n = \text{T, Q}$ denoting the cardinal number of the corresponding basis set, shortly denoted as (wC)VnZ in the text. The frozen-core (fc) approximation has been adopted in conjunction with the VnZ sets, while all electrons (but 1s for second-row elements) have been correlated with wCVnZ. The hybrid B3LYP functional⁷²⁻⁷⁴ has been used in conjunction with the SNSD basis set,^{48,49,75} which represents an excellent compromise between accuracy and computational cost for vibrational studies.^{46,48,49,76} Possible effects of basis set extension have also been investigated by employing the aug-cc-pVTZ (hereafter AVTZ) basis set.^{69,77} In the specific case of CH₂CHF and *cis*-CHFCHCl, the cc-pVTZ (VTZ) basis set has been preferred, in view of the worsening in the vibrational frequencies coming from the inclusion of diffuse functions in the triple- ζ basis set for halo-ethylenes.⁴⁸

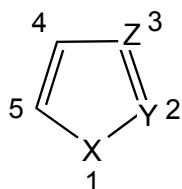
The CFOUR program package⁷⁸ has been employed for MP2 and CCSD(T) computations, while DFT calculations have been performed with the GAUSSIAN suite of programs.⁷⁹ For all computational levels, the harmonic part has been obtained using analytic second derivatives, whereas the corresponding cubic force field has been determined in a normal-coordinate representation via numerical differentiation of the analytically computed harmonic force constants.⁸⁰⁻⁸⁵ At the DFT level, the force field calculations have been carried out using very-tight criteria for the SCF and geometry optimization convergence, together with an ultra-fine grid for the numerical integration of the two-electron integrals and their derivatives. The numerical differentiations have been performed with the Gaussian default step of 0.01 Å.

The $\Delta B_{\text{el}}^{\beta}$ contributions have been evaluated by calculating the $g^{\beta\beta}$ constants at the B3LYP/AVTZ level of theory.

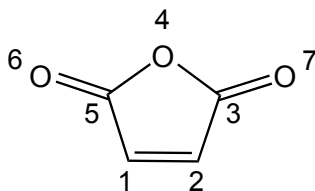
To obtain accurate reference equilibrium structures for pyridine, 2-fluoropyridine and 3-

fluoropyridine, we have performed geometry optimizations at the CCSD(T) level accounting for basis-set truncation errors and core-valence correlation effects by means of a composite approach.^{38,39} The corresponding r_e is denoted as CCSD(T)/CBS+CV.

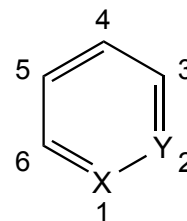
Figure 1: Sketch of the 36 asymmetric top molecules belonging to the B3se set (see also Tables 1, 4 and 5).



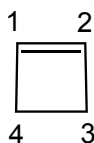
- (a) (X,Y,Z)
 (NH,CH,CH) pyrrole
 (NH,N,CH) pyrazole
 (NH,CH,N) imidazole
 (O,CH,CH) furan
 (S,CH,CH) thiophene



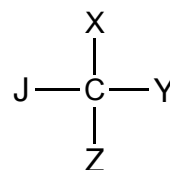
- (d) maleic anhydride



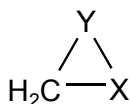
- (i) (X,Y)
 (N,CH) pyridine
 (N,N) pyridazine



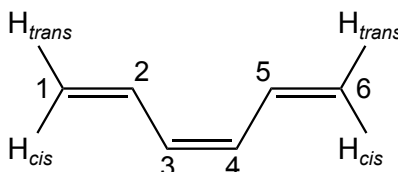
- (e) cyclobutene



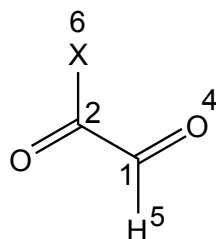
- (j) (X,Y,Z,J)
 (H,H,F,F) CH₂F₂
 (Cl,Cl,F,F) CCl₂F₂
 (H,H,Cl,Cl) CH₂Cl₂
 (H,Cl,F,F) CHClF₂
 (Cl,F,H,H) CH₂ClF



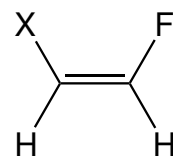
- (b) (X,Y)
 (NH,CH₂) aziridine
 (O,CH₂) oxirane
 (O,O) dioxirane



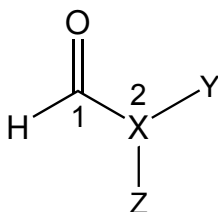
- (f) *cis*-hexatriene



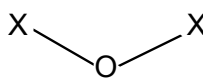
- (g) X=H *trans*-glyoxal
 X=OH glyoxylic acid



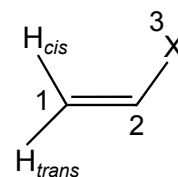
- (k) X=H CH₂CHF
 X=Cl *cis*-CHFCHCl



- (c) (X,Y,Z)
 (H,-,-) formaldehyde
 (CH₂,OH,-) glycolaldehyde
 (CH₂,CH₃,-) propanal
 (C,CH₂,H) *cis*-acrolein
 (C,H,CH₂) *trans*-acrolein
 (O,H,-) *cis*-formic acid
 (O,-,H) *trans*-formic acid
 (O,CH₃,-) *cis*-methyl formate



- (h) X=H water
 X=CH₃ dimethyl ether



- (l) X=H ethene
 X=OH ethenol
 X=CH₃ propene
 X=CHCH₂ butadiene

RESULTS AND DISCUSSION

All the asymmetric top molecules of the B3se set, and when needed, their atom numbering are sketched in Figure 1.

Validation study: the performance of B3LYP force fields

As mentioned in the introduction, a set of 21 molecules, including linear (HCN, HNC, HCO⁺, HNCCN⁺, HCCH, HCCCCH), symmetric-top (H₂CCCH₂, SH₃⁺, NH₃) and asymmetric-top (H₂O, H₂CO, CH₂ClF, CH₂CHF, *cis*-CHFCHCl, oxirane, dioxirane, cyclobutene, *trans*-glyoxal, *cis* and *trans*-acrolein, pyridazine) molecules, has been selected to investigate the performance of the B3LYP hybrid functional in the computation of the vibrational contributions to experimental vibrational ground-state rotational constants $(B_0^\beta)^{\text{EXP}}$ subsequently used in the derivation of SE equilibrium geometries.

For all systems listed above, the experimental $(B_0^\beta)^{\text{EXP}}$ constants and the $\Delta B_{\text{vib}}^\beta$ contributions computed at the CCSD(T) and MP2 levels available in the literature have been collected, see Table 1 in the SI. When not available, MP2 and/or CCSD(T) vibrational contributions have been calculated in this work (see Table 1 for details), together with the $\Delta B_{\text{vib}}^\beta$ contributions computed at the DFT level. The $\Delta B_{\text{el}}^\beta$ contributions have also been taken into account. In particular, large $\Delta B_{\text{el}}^\beta$ values are found for H₂O (about from 7.6 to 0.7% of $(\Delta B_0^\beta)^{\text{QM}}$) and H₂CO (12.5-0.6%). Furthermore, the importance of taking into account the electronic contributions for *cis* and *trans*-acrolein and pyridazine is well known.⁸⁶⁻⁸⁸ For both isomers of acrolein, ΔB_{el}^A , ΔB_{el}^B and ΔB_{el}^C are about 3.0-4.5%, 0.5-0.6% and 0.05-0.07% of $(\Delta B_0^\beta)^{\text{QM}}$. For pyridazine, ΔB_{el}^A and ΔB_{el}^B are about 0.7-1.2% of $(\Delta B_0^\beta)^{\text{QM}}$, while ΔB_{el}^C is about 0.3%. All $\Delta B_{\text{vib}}^\beta$ and $\Delta B_{\text{el}}^\beta$ contributions are given in Table 1 in the SI.

In Figure 2, for all the considered molecules, we have displayed the $(\Delta B_0^\beta)^{\text{QM}}$ corrections for all isotopologues studied in terms of the percentage of the corresponding $(B_0^\beta)^{\text{EXP}}$. From this Figure, it is apparent that, as expected, the $(\Delta B_0^\beta)^{\text{QM}}$ are rather small contributions. They

vary from 2-3% of $(B_0^\beta)^{\text{EXP}}$, for systems like H_2O , to less than 1% in the case of HNCCN^+ and HCCCCCH . Negative $(\Delta B_0^\beta)^{\text{QM}}$ corrections are obtained for all molecules except for $(B_0^A)^{\text{EXP}}$ of H_2O . The different computational levels used for the calculation of $(\Delta B_0^\beta)^{\text{QM}}$ are discriminated by using different graphical symbols. This allows us to point out the very good agreement between the results obtained at the different levels of theory considered. Indeed, there is a generally good superposition of the graphical symbols for the various isotopologues: the discrepancies between the various methods and CCSD(T) are well within 1%. On these grounds, it is possible to estimate (see equation 13 of ref. 42) that the resulting SE geometrical parameters differ by at most 0.25% from those obtained with vibrational contributions at the CCSD(T) level.

In the following, the SE equilibrium structures derived using vibrational contributions from CCSD(T), MP2, B3LYP/SNSD and B3LYP/AVTZ force fields are referred to as CCSD(T) SE, MP2 SE, B3LYP/SNSD SE and B3LYP/AVTZ SE, respectively. The CCSD(T) and B3LYP/SNSD SE equilibrium structures are explicitly reported in Table 1, while the MP2 and B3LYP/AVTZ ones are given in Table 6 of the SI in terms of discrepancies with respect to the CCSD(T) SE geometrical parameters. In Table 1 the fully experimental r_0 structures are also collected together with the equilibrium geometries optimized at the B3LYP/SNSD level. The r_0 structures are reported to point out the non-negligible deviations that discourage their use even for establishing general trends. The B3LYP/SNSD equilibrium structures are shown in order to be easily accessible in view of the template approach presented later in the text. The root mean square (RMS) of the residuals in terms of equilibrium rotational constants (hereafter simply referred to as residuals), and for planar molecules, the mean inertial defects $\Delta_e = I^C - I^B - I^A$ are also given in Table 1 as indicators of the quality of the fits. Indeed, small values of the RMS residuals and Δ_e indicate a good quality of the fits and that $(\Delta B_0^\beta)^{\text{QM}}$ corrections lead to good SE equilibrium rotational constants, respectively.

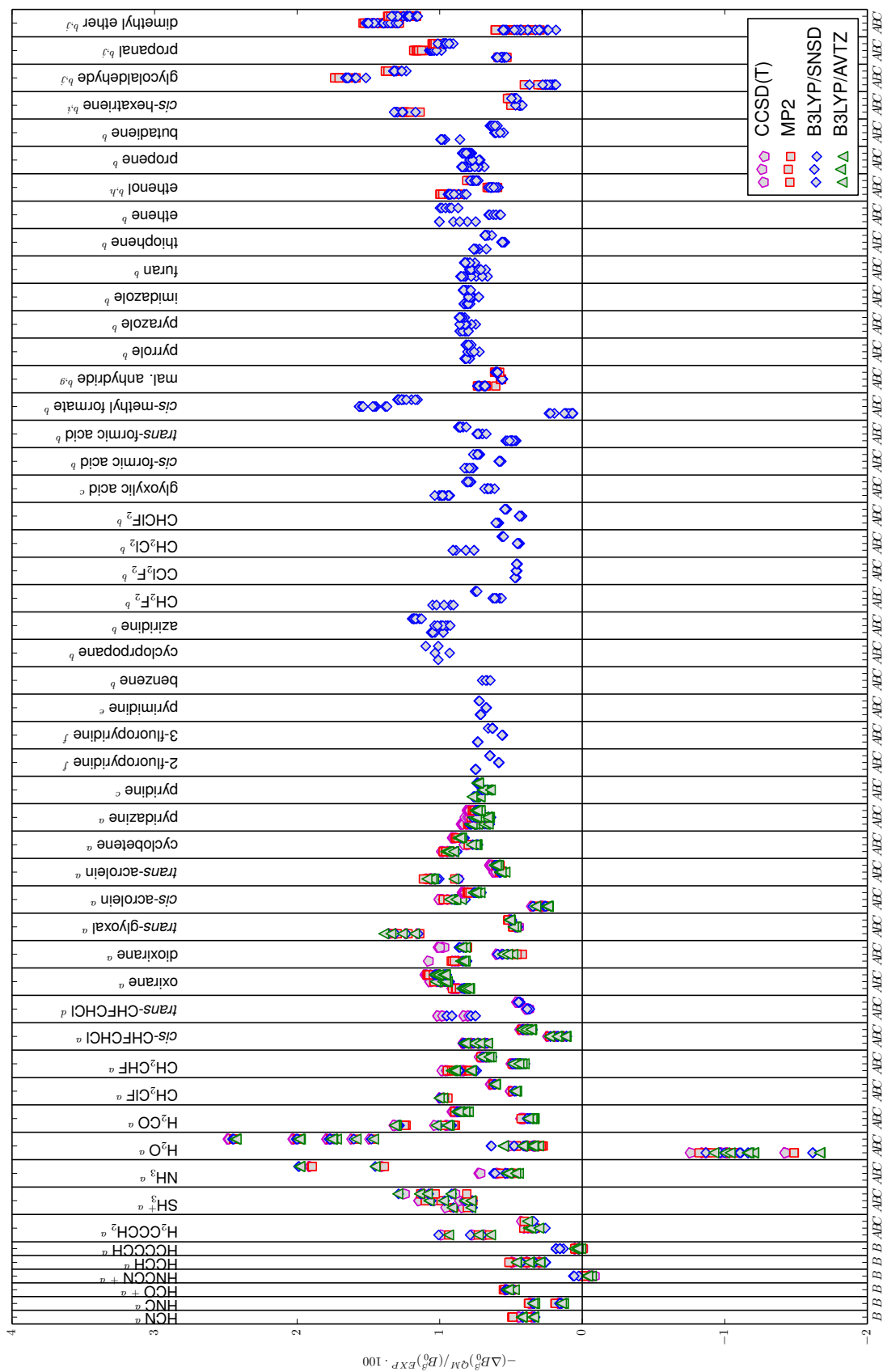
The differences in the geometrical parameters of the MP2, B3LYP/SNSD and B3LYP/AVTZ

SE equilibrium geometries with respect to the CCSD(T) SE equilibrium structures are graphically reported in Figure 3 (see also Table 6 in the SI). It is noteworthy that for the whole set of bond lengths the deviation of MP2 and B3LYP results from the CCSD(T) references never exceeds 0.0026 Å. The deviations show a nearly gaussian distribution with mean values close to zero and mean absolute errors (MAE) of 0.0004 Å, 0.0007 Å and 0.0005 Å for MP2, B3LYP/SNSD and B3LYP/AVTZ, respectively (see Table 2), thus pointing out the good accuracy of DFT vibrational contributions to rotational constants in evaluating SE equilibrium structures. The small standard deviations of MP2, B3LYP/SNSD and B3LYP/AVTZ can be considered fully satisfactory for geometrical parameter determinations. Focusing on specific bonds (see Figure 1 in the SI), it can be observed that the C-C bond lengths are those showing a quite large MAE with respect to the CH and CO bond lengths. A larger MAE (0.0056 Å) is obtained for r_0 structures, with a standard deviation of 0.0063 Å, a value significantly larger than the typical uncertainty affecting the SE methodology.

The deviations for angles are also very small, with MAE of 0.03, 0.06 and 0.06 degrees for MP2, B3LYP/SNSD and B3LYP/AVTZ, respectively. Similarly to bond lengths, these values correspond to accuracies comparable with the intrinsic errors of the SE fitting procedure. Also for angles, the deviations of r_0 structures are an order of magnitude larger than that of the various r_e^{SE} 's.

A linear least-square fit of the CCSD(T) r_e^{SE} values, expressed as a function of the corresponding MP2 and DFT ones (see Figure 2 in the SI), gives the parameters reported in Table 3. It is noteworthy that in all cases the angular coefficient is very close to 1 and the intercept never exceeds, in absolute value, 0.0025 Å for bond lengths and 0.06 degrees for angles. This confirms that using B3LYP corrections in the SE approach leads to results that reproduce very well the best SE equilibrium structures. In addition, the analysis of R^2 and standard deviation values of the linear regression does not point out any significant deviation from linearity.

Figure 2: $-(\Delta B_0^\beta)^{QM} / (B_0^\beta)^{EXP} \cdot 100$ for the isotopologues of all molecules considered in this work.



a) see Table 1 here and Table 1 in the SI. b) see Table 4 here and Table 2 in the SI. c) see Table 5 here and Table 2 in the SI. d) see Table 7 here and Table 4 in the SI. e) see Table 8 here and Table 5 in the SI. f) see Table 9 here and Table 3 in the SI. g) MP2/VTZ ΔB_{vib}^β from ref. 89. h) MP2/VQZ ΔB_{vib}^β from ref. 90. i) MP2/VTZ ΔB_{vib}^β from ref. 91. j) MP2/VTZ ΔB_{vib}^β from ref. 90.

Table 1: r_0 , r_e^{SE} and r_e geometries for the 21 molecules of the CCse set. Distances in Å, angles in degrees.

	r_0^a	$r_e^{\text{SE}^a}$		r_e
		CCSD(T)	B3LYP/SNSD	
– linear molecules –				
HCN^b				
r(H-C)	1.0624(2)	1.0651(1) ^{×,†}	1.0645(1) [†]	1.0707
r(C-N)	1.1568(1)	1.1533(1)	1.1536(1)	1.1551
Rms resid. [MHz]	0.0009	0.0001	0.0001	-
HNC^b				
r(H-N)	0.9863(2)	0.9954(1) ^{×,†}	0.9946(1) [†]	1.0022
r(N-C)	1.1725(1)	1.1685(1)	1.1688(1)	1.1739
Rms resid. [MHz]	0.0010	0.0001	0.0001	-
HCO⁺				
r(H-C)	1.0921(2)	1.0919(1) ^{×,†}	1.0916(1) [†]	1.0995
r(C-O)	1.1091(1)	1.1057(1)	1.1057(1)	1.1075
Rms resid. [MHz]	0.0011	0.0001	0.0001	-
HNCCN^{+c}				
r(H-N)	1.0058(4)	1.0133(1) ^{×,†}	1.0138(2) [†]	1.0191
r(N-C)	1.1400(8)	1.1406(1)	1.1392(4)	1.1455
r(C-C)	1.3762(9)	1.3724(1)	1.3735(4)	1.3686
r(C-N)	1.1584(7)	1.1634(1)	1.1607(3)	1.1628
Rms resid. [MHz]	0.0017	0.0002	0.0008	-
HCCH^d				
r(C≡C)	1.2084(1)	1.2030(1) ^{+,†}	1.2036(1) [†]	1.2060
r(C-H)	1.0572(2)	1.0617(1)	1.0611(1)	1.0676
Rms resid. [MHz]	0.0013	0.0001	0.0002	-
HCCCCH^e				
r(C≡C)	1.2079(3)	1.2084(3) ^{×,†}	1.2070(4) [†]	1.2123
r(C-C)	1.3751(4)	1.3727(4)	1.3726(6)	1.3685
r(C-H)	1.0561(1)	1.0615(1)	1.0610(1)	1.0667
Rms resid. [MHz]	0.0008	0.0008	0.0012	-
– symmetric top molecules –				
SH₃^{+f}				
r(S-H)	1.3563(2)	1.3500(1) ^{+,†}	1.3502(1) [†]	1.3683
a(H-S-H)	94.19(3)	94.15(1)	94.11(1)	94.30
Rms resid. [MHz]	0.0068	0.0010	0.0011	-
NH₃^b				
r(N-H)	1.0150(3)	1.0110(2) ^{×,†}	1.0111(2) [†]	1.0176
a(H-N-H)	107.52(4)	106.94(2)	106.87(3)	106.59
Rms resid. [MHz]	0.0055	0.0033	0.0036	-
H₂CCCH₂				
r(C=C)	1.3096(4)	1.3066(1) ^{÷,†}	1.3075(2) [†]	1.3077
r(C-H)	1.0833(9)	1.0807(1)	1.0800(4)	1.0874
a(H-C-H)	118.56(11)	118.26(1)	118.37(5)	117.41
Rms resid. [MHz]	0.0169	0.0011	0.0081	-
– asymmetric top molecules –				
H₂O^b				
r(O-H)	0.9567(1)	0.9573(1) ^{×,†}	0.9572(1) [†]	0.9644
a(H-O-H)	104.93(2)	104.53(1)	104.47(1)	104.60
Rms resid. [MHz]	0.0014	0.0004	0.0004	-
Mean Δ_e [uÅ ²]	0.06277	0.00506	0.00603	-

H₂CO^b				
r(C-O)	1.2095(2)	1.2047(1) ^{×,†}	1.2051(1) [†]	1.2052
r(C-H)	1.1064(4)	1.1003(1)	1.1002(1)	1.1099
a(H-C-O)	121.66(3)	121.65(1)	121.62(1)	121.84
Rms resid. [MHz]	0.0028	0.0003	0.0003	-
Mean Δ_e [uÅ ²]	0.06455	0.00297	0.00223	-
CH₂ClF^g				
r(C-H)	1.0891(13)	1.0840(1) ^{‡,†}	1.0842(1) [†]	1.0896
r(C-F)	1.3706(9)	1.3594(1)	1.3591(1)	1.3682
r(C-Cl)	1.7613(6)	1.7641(1)	1.7645(1)	1.7998
a(H-C-Cl)	109.34(38)	107.96(1)	107.93(1)	107.61
a(H-C-H)	110.21(14)	112.57(1)	112.55(1)	113.23
a(F-C-Cl)	110.18(99)	110.02(1)	110.02(2)	110.15
Rms resid. [MHz]	0.0008	0.0001	0.0001	-
CH₂CHF				
r(C1-F)	1.3574(29)	1.3424(2) ^{‡,†}	1.3412(5) [†]	1.3528
r(C1-H)	1.0921(18)	1.0792(1)	1.0784(4)	1.0856
r(C1-C2)	1.3169(31)	1.3213(2)	1.3234(6)	1.3247
r(C2-H _{trans})	1.0774(21)	1.0772(1)	1.0768(4)	1.0839
r(C2-H _{cis})	1.0854(14)	1.0785(1)	1.0782(3)	1.0848
a(F-C1-H)	107.70(62)	112.10(6)	112.36(19)	111.62
a(F-C1-C2)	121.57(3)	121.72(1)	121.68(1)	121.90
a(C1-C2-H _{trans})	118.83(21)	118.95(1)	118.94(4)	119.25
a(C1-C2-H _{cis})	121.02(19)	121.32(1)	121.29(3)	121.72
Rms resid. [MHz]	0.0023	0.0001	0.0004	-
Mean Δ_e [uÅ ²]	0.09356	0.00281	0.00162	-
cis-CHFCHCl^h				
r(C1-Cl)	1.7271(19)	1.7129(2) ^{‡,†}	1.7124(14) [†]	1.7404
r(C1-H)	1.1109(19)	1.0795(2)	1.0795(14)	1.0818
r(C1=C2)	1.3162(26)	1.3244(2)	1.3266(19)	1.3278
r(C2-F)	1.3363(21)	1.3313(2)	1.3306(16)	1.3416
r(C2-H)	1.0858(16)	1.0796(1)	1.0776(13)	1.0849
a(Cl-C1=C2)	123.13(14)	123.08(1)	123.08(13)	123.74
a(H-C1=C2)	126.88(23)	121.08(2)	121.06(19)	120.91
a(F-C2=C1)	122.27(20)	122.56(2)	122.47(15)	123.10
a(H-C2=C1)	124.16(21)	123.49(2)	123.33(16)	123.45
Rms resid. [MHz]	0.0026	0.0002	0.0020	-
Mean Δ_e [uÅ ²]	0.19860	0.00712	0.01604	-
oxiraneⁱ				
r(C-C)	1.4719(4)	1.4609(2) ^{‡,†}	1.4615(2) [†]	1.4674
r(C-O)	1.4357(2)	1.4274(1)	1.4281(1)	1.4324
r(C-H)	1.0823(3)	1.0816(2)	1.0814(2)	1.0889
a(C-O-C)	61.67(2)	61.56(1)	61.55(1)	61.63
a(H-C-H)	116.63(4)	116.25(2)	116.33(2)	115.75
a(H-C-O)	114.75(5)	114.87(3)	114.82(3)	115.04
Rms resid. [MHz]	0.0031	0.0015	0.0015	-
dioxirane^j				
r(C-O)	1.3914(4)	1.3846(5) [‡]	1.3850(1) [†]	1.3901
r(O-O)	1.5192(1)	1.5133(5)	1.5140(1)	1.5006
r(C-H)	1.0837(11)	1.0853(15)	1.0850(1)	1.0919
a(H-C-H)	116.70(13)	117.03(20)	117.06(1)	116.96
Rms resid. [MHz]	0.0065	0.25	0.0006	-

trans-glyoxal^k

r(C=O)	1.2135(10)	1.2046(1) ^{÷,†}	1.2051(1) [†]	1.2069
r(C-C)	1.5155(15)	1.5157(1)	1.5149(2)	1.5262
r(C-H)	1.1031(6)	1.1006(1)	1.1006(1)	1.1093
a(H-C-C)	115.42(9)	115.23(1)	115.37(1)	115.14
a(O=C-H)	123.80(8)	123.60(1)	123.45(1)	123.45
Rms resid. [MHz]	0.0019	0.0001	0.0002	-

cis-acrolein

r(C1-C2)	1.4884(13)	1.4806(1) ^{÷,†}	1.4809(3) [†]	1.4840
r(C2-C3)	1.3389(12)	1.3350(1)	1.3368(2)	1.3377
r(C1-O)	1.2124(10)	1.2108(1)	1.2102(2)	1.2145
r(C1-H)	1.1047(10)	1.1024(1)	1.1021(2)	1.1113
r(C2-H)	1.0864(9)	1.0824(1)	1.0807(2)	1.0885
r(C3-H _{cis})	1.0984(14)	1.0808(1)	1.0800(3)	1.0868
r(C3-H _{trans})	1.0796(10)	1.0797(1)	1.0786(2)	1.0857
a(C1-C2-C3)	121.39(10)	121.21(1)	121.33(2)	122.28
a(O-C1-C2)	124.06(10)	123.96(1)	123.88(2)	124.66
a(C2-C1-H)	115.33(11)	115.83(1)	115.81(2)	115.24
a(C3-C2-H)	121.32(12)	121.57(1)	121.63(2)	121.21
a(C2-C3-H _{cis})	118.59(10)	119.85(1)	119.86(2)	120.35
a(C2-C3-H _{trans})	121.49(17)	121.61(1)	121.66(4)	121.73
Rms resid. [MHz]	0.0014	0.0001	0.0003	-
Mean Δ_e [uÅ ²]	-0.02202	0.01311	0.01346	-

trans-acrolein

r(C1-C2)	1.4803(10)	1.4702(1) ^{÷,†}	1.4703(1) [†]	1.4735
r(C2-C3)	1.3393(14)	1.3354(1)	1.3355(1)	1.3384
r(C1-O)	1.2122(12)	1.2103(1)	1.2109(1)	1.2142
r(C1-H)	1.1096(17)	1.1048(1)	1.1044(1)	1.1133
r(C2-H)	1.0809(14)	1.0814(1)	1.0817(1)	1.0876
r(C3-H _{cis})	1.0872(15)	1.0825(1)	1.0826(1)	1.0883
r(C3-H _{trans})	1.0833(14)	1.0795(1)	1.0792(1)	1.0856
a(C1-C2-C3)	120.18(8)	120.18(1)	120.21(1)	121.02
a(O-C1-C2)	123.66(13)	124.02(1)	123.97(1)	124.21
a(C2-C1-H)	114.70(12)	115.08(1)	115.11(1)	115.02
a(C3-C2-H)	122.79(15)	122.78(1)	122.85(1)	122.41
a(C2-C3-H _{cis})	119.91(11)	120.46(1)	120.44(1)	120.89
a(C2-C3-H _{trans})	121.71(18)	122.10(1)	122.07(1)	122.22
Rms resid. [MHz]	0.0013	0.0001	0.0001	-
Mean Δ_e [uÅ ²]	-0.01588	-0.00527	-0.00845	-

cyclobutene

r(C1=C2)	1.3478(7)	1.3406(1) ^{÷,†}	1.3409(1) [†]	1.3420
r(C2-C3)	1.5210(2)	1.5141(1)	1.5149(1)	1.5193
r(C3-C4)	1.5727(15)	1.5639(1)	1.5646(2)	1.5736
r(C1-H)	1.0807(5)	1.0805(1)	1.0801(1)	1.0867
r(C3-H)	1.0923(3)	1.0894(1)	1.0892(1)	1.0961
r(C1-C2-C3)	94.24(4)	94.23(1)	94.23(1)	94.37
r(C1-C2-H)	133.59(7)	133.42(1)	133.47(1)	133.47
a(C4-C3-H)	114.57(5)	114.64(1)	114.60(1)	114.78
a(H-C3-H)	109.22(3)	109.09(1)	109.19(1)	108.59
Rms resid. [MHz]	0.0011	0.0001	0.0001	-

pyridazine^l				
r(N2-C3)	1.3395(100)	1.3302(12) ^{80,†}	1.3324(24) [†]	1.3366
r(C3-C4)	1.3948(96)	1.3938(12)	1.3926(23)	1.3971
r(C4-C5)	1.3865(70)	1.3761(16)	1.3778(16)	1.3829
r(C4-H)	1.0797(23)	1.0802(4)	1.0791(5)	1.0858
r(C3-H)	1.0822(15)	1.0810(3)	1.0804(4)	1.0871
a(C3-C4-C5)	116.85(18)	116.85(3)	116.86(4)	116.88
a(N2-C3-C4)	123.91(22)	123.86(4)	123.87(5)	123.67
a(C4-C3-H)	121.50(46)	121.35(6)	121.39(11)	121.43
a(C5-C4-H)	122.26(29)	122.37(4)	122.32(7)	122.25
Rms resid. [MHz]	0.0054	-	0.0013	-
Mean Δ_e [$\text{u}\text{\AA}^2$]	0.03281	-	-0.00103	-

All computations have been performed in this work except where otherwise indicated.

a) Graphical symbols denote the basis sets used in the calculations of $\Delta B_{\text{vib}}^{\beta}$ contributions: \div VTZ; \ddagger CVTZ; \asymp VQZ; \times CVQZ; $+$ wCVQZ, $\aleph 0$ ANO0. \dagger denotes the inclusion of $\Delta B_{\text{el}}^{\beta}$. For all the structures calculated in this work, the uncertainties on the geometrical parameters are reported within parentheses, rounded to $1 \cdot 10^{-4}$ \AA for lengths and $1 \cdot 10^{-2}$ degrees for angles if smaller than these values.

$\Delta_e = I^C - I^B - I^A$ is the inertial defect.

b) CCSD(T) $\Delta B_{\text{vib}}^{\beta}$ from ref. 92.

c) CCSD(T) $\Delta B_{\text{vib}}^{\beta}$ from ref. 93.

d) CCSD(T) $\Delta B_{\text{vib}}^{\beta}$ from ref. 94.

e) CCSD(T) $\Delta B_{\text{vib}}^{\beta}$ from ref. 95.

f) CCSD(T) $\Delta B_{\text{vib}}^{\beta}$ from ref. 96.

g) CCSD(T) $\Delta B_{\text{vib}}^{\beta}$ from ref. 97.

h) CCSD(T) $\Delta B_{\text{vib}}^{\beta}$ from ref. 98.

i) CCSD(T) $\Delta B_{\text{vib}}^{\beta}$ from ref. 99.

j) CCSD(T) r_e^{SE} from ref. 85.

k) CCSD(T) $\Delta B_{\text{vib}}^{\beta}$ from ref. 100.

l) CCSD(T) r_e^{SE} from ref. 88.

Figure 3: Statistical distributions of the MP2, B3LYP/SNSD and B3LYP/AVTZ deviations from CCSD(T) SE equilibrium parameters for the molecules belonging to the CCse set (see Table 1 and Table 6 in the SI).

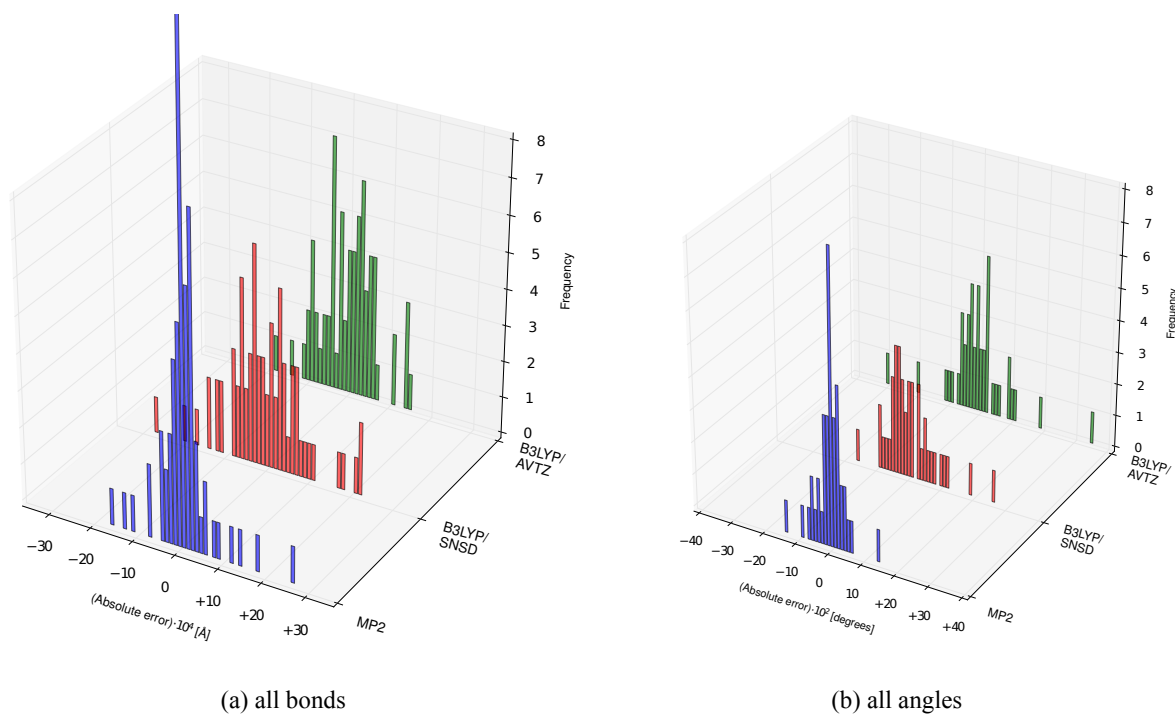


Table 2: Mean, standard deviation, and mean absolute error (MAE) for the MP2, B3LYP/SNSD and B3LYP/AVTZ deviations from CCSD(T) SE equilibrium parameters for the molecules belonging to the CCse set (see Table 1 and Table 6 in the SI). For the different types of bonds, only the sets having at least 7 items have been considered.

	MP2 ^a	B3LYP/SNSD	B3LYP/AVTZ
All bonds (68 items)			
Mean	+0.0001	-0.0001	+0.0000
St. Dev.	0.0006	0.0009	0.0007
MAE	0.0004	0.0007	0.0005
CH bonds (27 items)			
Mean	+0.0002	-0.0005	-0.0005
St. Dev.	0.0003	0.0005	0.0005
MAE	0.0002	0.0006	0.0006
CC bonds (18 items)			
Mean	+0.0001	+0.0006	+0.0004
St. Dev.	0.0007	0.0010	0.0007
MAE	0.0005	0.0009	0.0007
CO bonds (7 items)			
Mean	+0.0001	+0.0004	+0.0003
St. Dev.	0.0002	0.0005	0.0002
MAE	0.0001	0.0005	0.0003
All angles (42 items)			
Mean	+0.00	+0.00	-0.01
St. Dev.	0.04	0.08	0.10
MAE	0.03	0.06	0.06

a) all MP2 calculations have been performed with basis sets of at least triple- ζ quality, Table 6 in the SI for details.

Table 3: Parameters for linear regressions of the CCSD(T) r_e^{SE} parameters versus the MP2, B3LYP/SNSD and B3LYP/AVTZ r_e^{SE} ones for the molecules belonging to the CCse set (see Table 1 and Table 6 in the SI).

	MP2 ^a	B3LYP/SNSD	B3LYP/AVTZ
All bonds			
<i>A</i>	0.999740	0.998023	1.001581
<i>B</i>	0.000186	0.002475	-0.001953
R^2	0.999989	0.999976	0.999988
St. Dev.	0.000405	0.000582	0.000421
All angles			
<i>A</i>	1.000144	1.000004	1.000561
<i>B</i>	-0.012640	-0.005008	-0.058692
R^2	0.999985	0.999956	0.999928
St. Dev.	0.000609	0.001049	0.001347
$r_e^{\text{SE}}(\text{CCSD(T)}) = A \cdot r_e^{\text{SE}}(\text{MP2 or B3LYP}) + B$			

a) all MP2 calculations have been performed with basis sets of at least triple- ζ quality, Table 6 in the SI for details.

From small to medium-large systems: B3LYP/SNSD semi-experimental structures

In the previous section we demonstrated that the SE equilibrium structures derived from $\Delta B_{\text{vib}}^{\beta}$ contributions calculated at the B3LYP level have an accuracy comparable to that obtained when using CCSD(T) corrections. In view of these results, and aiming at increasing the number of geometrical patterns considered, in this section B3LYP SE equilibrium structures are presented for 26 organic molecules containing H, C, N, O, F, S, Cl atoms. For the systems considered, to the best of our knowledge, SE equilibrium structures derived from CCSD(T) vibrational contributions are not available, but a sufficient number of isotopologues has been characterized experimentally to allow for a reliable determination of all geometrical parameters without any constraint and/or assumption. Focusing on the B3LYP/SNSD quantum mechanical model, which permits to keep the computational costs low, the new SE equilibrium structures are compared with both the most accurate determinations available in the literature and vibrationally averaged r_0 geometries. Together with the 21 molecules previously considered, a high-quality benchmark set, including a total of 47 molecules (hereafter referred to as B3se set), has been set up for validating structural predictions from other experimental and/or computational approaches.

The geometrical parameters for CH_2F_2 , CCl_2F_2 , CH_2Cl_2 , CHClF_2 , ethene, ethenol, propene, butadiene, *cis*-hexatriene, cyclopropane, aziridine, benzene, pyrrole, pyrazole, imidazole, furan, thiophene, maleic anhydride, dimethyl ether, *cis* and *trans*-formic acid, *cis*-methyl formate, glycolaldehyde, and propanal are collected in Table 4 and compared with the best r_e^{SE} equilibrium structures available in the literature. In Table 5, we present the SE equilibrium structures for two additional molecules (glyoxylic acid and pyridine), which are then compared with the best theoretical r_e structures available. For all these molecules, the $(B_0^{\beta})^{\text{EXP}}$, $\Delta B_{\text{vib}}^{\beta}$ and $\Delta B_{\text{el}}^{\beta}$ are summarized in Tables 2 of the SI. It is noteworthy that for most of the systems the RMS of the residuals for r_0 geometries is about one order of magnitude larger than the RMS of the residuals for SE equilibrium geometries. The small values for the latter,

less than 7 kHz for all systems, demonstrate the good quality of the fits.

In analogy with the CCse set, equilibrium geometries obtained at the B3LYP/SNSD level are reported in Tables 4 and 5 because of their subsequent use within the template approach presented in the next section.

Halomethanes

A systematic evaluation of the SE equilibrium structure for a series of chlorinated and fluorinated methanes has been carried out recently.¹⁰¹ In this work, in addition to the SE equilibrium structure of CH₂ClF reported in the previous section, CH₂F₂, CCl₂F₂, CH₂Cl₂, and CHClF₂ have been considered as models to investigate the C-X bond pattern, where X is a halogen atom and the C hybridization is *sp*³. CH₂F₂, CCl₂F₂ and CH₂Cl₂ have C_{2v} symmetry and are completely characterized by 5 geometrical parameters, while CHClF₂ belongs to the C_s symmetry group and has 6 unique structural parameters. In ref. 101, the $\Delta B_{\text{vib}}^{\beta}$ contributions have been calculated at the MP2/VTZ (with the modified V(T+d)Z for the chlorine atom¹⁰²) level of theory for the halomethanes considered, except for CCl₂F₂ (B3LYP/6-311+G(3df,2pd)). For all these systems, there is a good agreement between the SE equilibrium structures obtained employing B3LYP and MP2 vibrational contributions. The C-F bond length shows the largest variation with the number of hydrogens bonded to the C atom, i.e., it increases from 1.3286 Å for CCl₂F₂ (no H atoms) to 1.3363 Å for CHClF₂ (one H atom) and to 1.3533 Å/1.3594 Å for CH₂F₂/CH₂ClF (two H atoms). A similar trend is shown by the CCl bond length, which changes from 1.7641/1.7642 Å for CH₂ClF/CH₂Cl₂ to 1.7558 Å for CHClF₂ and to 1.7519 Å for CCl₂F₂. On the contrary, the CH bond length is only marginally affected by the number of halogen atoms bonded to the C atom (1.0810, 1.0840, 1.0849 and 1.0867 Å for CH₂Cl₂, CH₂ClF, CHClF₂, and CH₂F₂, respectively).

Substituted alkene compounds

Together with CH_2CHF and *cis*- CHFCHCl (presented in Table 1), ethene, ethenol, butadiene, *cis*-hexatriene and propene have been studied as representatives of the $\text{Y-C}=\text{C-X}$ bond pattern for non cyclic molecules, where C is sp^2 hybridized and X and Y are either halogens or C atoms.

Ethene and ethenol (or vinyl alcohol) are the simplest alkene and enol compound, respectively. A r_e^{SE} structure for ethene, which is defined by 3 internal parameters (D_{2h} symmetry), is available in the literature.¹⁰³ It corresponds to a weighted average of different r_e^{SE} geometries calculated by use of $\Delta B_{\text{vib}}^\beta$ at the MP2 and B3LYP levels, in conjunction with basis sets of at least triple- ζ quality, and where scaled quadratic force fields have been coupled with unscaled cubic force fields in the vibrational corrections calculations. The uncertainties of 0.0010 Å and 0.10 degrees on the parameters of the structure of ref. 103 (see Table 4) include both the uncertainties related to the SE methodology and those estimated from the parameter differences found using the different QM models in the $\Delta B_{\text{vib}}^\beta$ calculations. All the B3LYP/SNSD r_e^{SE} results, obtained by fitting the SE I_e^A and I_e^B moments of inertia, coincide with those of ref. 103 within the respective error bars.

The *syn* conformer of ethenol is fairly rigid and completely defined by 11 internal parameters (C_s symmetry). The SE equilibrium structure recently determined using $\Delta B_{\text{vib}}^\beta$ computed at the MP2/VQZ level⁹⁰ is given in Table 4 together with the B3LYP/SNSD r_e^{SE} results, obtained by fitting the SE I_e^A and I_e^C moments of inertia. The agreement is extremely good and the small RMS residual and uncertainties on the fitted parameters indicate that the B3LYP/SNSD SE equilibrium geometry is also accurate.

Propene is the simplest mono-methyl internal rotor, and it has been largely studied by infrared and microwave spectroscopy (see Refs. 104,105 and references therein). As a consequence, experimental rotational constants are available for a large number of isotopologues (20). The molecular structure of propene (C_s symmetry with a synperplanar arrangement of the $\text{C1}=\text{C2}-\text{C3}-\text{H}_{\text{plane}}$ moiety) is defined by 15 geometrical parameters, and has recently

been evaluated by means of the SE approach using $\Delta B_{\text{vib}}^{\beta}$ contributions at the MP2/VTZ(fc) level.¹⁰⁵ Some remarks on the fitting procedure need to be made. Due to large uncertainties affecting the $(B_0^A)^{\text{EXP}}$ of some isotopologues¹⁰⁶ that lead to ill-conditioned results, the fit has been performed on the SE equilibrium moments of inertia corresponding to the $(B_0^B)^{\text{EXP}}$ and $(B_0^C)^{\text{EXP}}$ rotational constants. Moreover, the CHD_{cis}=CDCH₃ and CH₂=¹³CHCH₃ isotopologues have been excluded from the fit because of the corresponding large residuals affecting the equilibrium rotational constants. In this framework, B3LYP/SNSD vibrational contributions lead to residuals with a very small RMS. Some fitted geometrical parameters defining the methyl hydrogen atoms lying outside the molecular C-C-C plane (in particular the C3-H_{out} bond length (1.0895 Å) and the C1=C2-C3-H_{out} dihedral angle (120.47 degrees)) are significantly smaller than the corresponding values obtained using MP2 vibrational contributions (1.0949 Å and 121.08 degrees). The latter values are closer to their r_0 counterparts (1.1036 Å and 121.07 degrees) than our equilibrium ones. In contrast to the B3LYP trend, the MP2 SE C3-H_{out} bond length differs significantly from the other C-H bonds, which range between 1.0805 and 1.0862 Å.

Butadiene and *cis*-hexatriene are planar C_{2h} and C_{2v} molecules, respectively, belonging to the class of polyenes, which are of great importance in biology and organic electronics due to a π -electron delocalization that increases as the C=C chain gets longer. In analogy with ethene, a r_e^{SE} structure for butadiene was obtained by Craig and coworkers from the average of different MP2 and B3LYP r_e^{SE} geometries. The B3LYP/SNSD r_e^{SE} parameters, obtained by fitting the SE I_e^A and I_e^C moments of inertia, agree with those of ref. 103 within the respective error bars.

The B3LYP/SNSD SE equilibrium structure of *cis*-hexatriene is in good agreement with that obtained using a MP2/VTZ force field.⁹¹ The largest discrepancy (about 0.0028 Å) is observed for the C3-H bond length. The r_0 structure shows consistently longer bond lengths, up to about 0.01 Å, again for the C3-H bond. Contrary to the molecules discussed above, in the case of *cis*-hexatriene the inclusion of the $(\Delta B_0^{\beta})^{\text{QM}}$ terms in the fitting procedure only

leads to a small reduction of the RMS residuals (1.7 kHz for r_e^{SE} with respect to 2.2 kHz for r_0).

It is noteworthy that the lengthening of the C=C double bonds as a consequence of π -electron delocalization is well reproduced: the C=C bond length is 1.3211/1.3245 Å in CH₂CHF/*cis*-CHFCHCl (a single C=C bonded to halogen atoms), 1.3326 Å in propene (a single C=C bond linked to a methyl group) and 1.3418/1.3509 Å in *cis*-hexatriene (three C=C groups). For the latter, the length of the central C=C bond (large conjugation) is 1.3509 Å and that of the terminal C=C one (lower conjugation) is 1.3418 Å, thus well reproducing the expected behaviour. It is also interesting to note that the C-C single bond length decreases from 1.4956 Å in propene ($sp^2 - sp^3$ type without any conjugation) to 1.4510 Å (conjugated $sp^2 - sp^2$ bond) in *cis*-hexatriene.

Cyclic and heterocyclic compounds

Cyclic and heterocyclic compounds are important building blocks of organic and biological molecules. Together with cyclobutene reported in Table 1, which is one of the smallest cycloalkenes, in this work we have studied cyclopropane and benzene (Table 4), which are among the simplest cycloalkanes and aromatic systems, and oxirane, dioxirane, pyridazine (Table 1), aziridine, pyrrole, pyrazole, imidazole, furan, thiophene, maleic anhydride (Table 4) and pyridine (Table 5), as prototypical heterocyclic compounds.

Cyclopropane belongs to the D_{3h} symmetry group and it is completely defined by 3 geometrical parameters: the C-C and C-H distances and the HCH angle. The SE equilibrium structure has been previously determined by using a SDQ-MBPT(4)/VTZ cubic force field.¹⁰⁷ Though two rotational constants of the parent species (B_0^B and B_0^C), B_0^B of C₃D₆ and B_0^A , B_0^B , B_0^C of C₃H₄D₂ have been experimentally determined, the inclusion of all of them in the fitting procedure leads to large residuals, as also noticed in ref. 107. The geometry reported in Table 4 has been obtained by using the SE equilibrium moments of inertia of C₃H₄D₂, together with the SE I_e^B of the parent species. Thanks to its high symmetry (D_{6h}), the

structure of benzene is defined by only 2 geometrical parameters: the C-H and C-C bond lengths. Its SE equilibrium structure has been determined for the first time by Stanton *et al.*¹⁰⁸ using vibrational contributions at the MP4(SDQ)/VTZ level. The B3LYP/SNSD SE equilibrium structures of cyclopropane and benzene show small uncertainties on the geometrical parameters and are in good agreement with the previous determinations.

Aziridine, also called ethylene imine, is one of the simplest non-aromatic N-heterocycles. Its equilibrium structure (C_s symmetry) is completely determined by 10 geometrical parameters, and is characterized by a high nitrogen inversion barrier. The rotational spectrum of aziridine has been studied in great detail because of its potential astrophysical interest.^{109–111} Very recently, a SE equilibrium structure has been determined by combining the experimental ground-state rotational constants with $\Delta B_{\text{vib}}^\beta$ contributions computed at the MP2/VTZ level.¹¹² The B3LYP/SNSD SE equilibrium structure has been derived by fitting SE equilibrium inertia moments, all equally weighted. The resulting SE equilibrium structure shows a very small RMS residual and a good agreement with the MP2/VTZ one.

Pyrazole and imidazole are two five-membered heteroaromatic rings, with adjacent and non-adjacent nitrogen atoms, respectively. Both molecules are completely characterized by 15 geometrical parameters, and have C_s symmetry. Pyrazole is used in the synthesis of many medical/organic molecules, while imidazole is present in important biological building-blocks, such as histidine and the related hormone histamine. The B3LYP/SNSD r_e^{SE} geometries shown in Table 4 have been obtained by fitting the SE I_e^B and I_e^C moments of inertia for pyrazole, and I_e^A and I_e^C for imidazole, all equally weighted.

For imidazole, the experimental rotational constants used were taken from ref. 113 without applying any corrections, while in ref. 112 the experimental values were corrected by the contribution of theoretical quartic distortion constants within the predicated method. In spite of these methodological differences, the B3LYP/SNSD r_e^{SE} parameters are in good agreement with the results of ref. 112.

Pyrrole, furan, and thiophene are three planar heterocyclic molecules belonging to the C_{2v}

point group, whose structures are completely defined by 9, 8 and 8 parameters, respectively. For pyrrole and furan, the best SE equilibrium structures reported in the literature were determined by correcting the vibrational ground-state rotational constants with $\Delta B_{\text{vib}}^{\beta}$ contributions calculated at the MP2/wCVTZ and MP2/VTZ levels, respectively.^{112,114} The best SE equilibrium geometry of thiophene was derived from a combined use of electron diffraction (ED), microwave spectroscopy (MW) and computed vibrational contributions at the B3LYP/6-311+G* level.¹¹⁵ The B3LYP/SNSD SE equilibrium geometries of pyrrole and furan are in good agreement with those already available. On the contrary, the B3LYP/SNSD SE equilibrium parameters of thiophene collected in Table 4 show relevant differences with respect to those previously determined. For example, the B3LYP/SNSD SE value for $r(\text{CS})$ is 0.0087 Å longer than that of ref. 115, while the B3LYP/SNSD SE C=C bond length is 0.0095 Å shorter than the corresponding value of ref. 115.

It is interesting to note how the C-C bond lengths change when both the H atoms linked with the C atom in α -position with respect to the O atom of the ring are substituted with two O atoms, that is, when moving from furan to maleic anhydride. To the best of our knowledge, the most accurate SE equilibrium structure available for maleic anhydride (C_{2v} symmetry) was derived using a MP2/VTZ cubic force field, also including the non negligible contribution due to $\Delta B_{\text{el}}^{\beta}$.⁸⁹ As a matter of fact, for B3LYP calculations the inclusion of the latter contributions reduces the RMS residual from 8.5 kHz to 0.4 kHz and the SE equilibrium inertial defect from a mean value of $-0.01634 \text{ u}\text{\AA}^2$ to $-0.00779 \text{ u}\text{\AA}^2$. For this molecule, the MP2 and B3LYP SE equilibrium structures agree very well one another. From Table 4 we note a significant decrease of the C3-C4 bond length when moving from furan to maleic anhydride (1.4344 Å in furan with respect to $r(\text{C1-C2})=1.3320$ Å in maleic anhydride, see Figure 1 d) and a contemporary increase of the C2-C3 bond length (1.3542 Å in furan with respect to 1.4857 Å in maleic anhydride), and of the ring C-O distance (from 1.3598 Å in furan to 1.3848 Å in maleic anhydride).

Thanks to the large number of isotopologues experimentally investigated^{116,117} (see Table 2

in SI) and to the limited number of independent geometrical parameters (10), it is possible to determine a full SE equilibrium structure for pyridine (C_{2v} symmetry). The r_e^{SE} structure given in Table 5 has been obtained by fitting the SE I_e^A and I_e^C moments of inertia derived from the experimental rotational constants corrected by $\Delta B_{\text{vib}}^\beta$ contributions calculated at the B3LYP/SNSD level. Even in this case, the inclusion of the $\Delta B_{\text{el}}^\beta$ terms leads to a considerable improvement of the inertial defects. The CCSD(T)/CBS+CV and B3LYP/SNSD structures determined in this work are reported in Table 5 for comparison purposes and a subsequent use within the template approach (see next section). The CCSD(T)/CBS+CV and B3LYP SE equilibrium structures remarkably agree one to other and also with the r_e^{SE} determined in ref.¹¹² using B3LYP/6-311+G(3df,2pd) vibrational corrections and the so-called predicate approach. It is worthwhile noting that the SE equilibrium structures of benzene and pyridine derived using B3LYP/SNSD vibrational contributions show quite different C-C bond lengths: 1.3919 Å in benzene versus 1.3907 Å for the bond directly connected to the C-N bond and 1.3888 Å for the furthest bond in pyridine.

Ethers, aldehydes, esters and carboxylic acids

In addition to *trans*-glyoxal, *cis*- and *trans*-acrolein (see Table 1), dimethyl ether, glycolaldehyde, propanal, formic and glyoxylic acids as well as methyl formate have been investigated as models for the most significant oxygen-containing moieties.

Dimethyl ether, the simplest molecule with two internal rotors, has been studied in great detail as an interstellar molecule and because of the interest in its rotational-torsional spectrum.^{118–120} Its equilibrium structure has C_{2v} symmetry (characterized by antiperiplanar arrangement of both the C-O-C- H_{plane} moieties) and is completely defined by 7 geometrical parameters. The SE equilibrium structure determined using B3LYP/SNSD vibrational contributions is in remarkable agreement with that obtained in ref.⁹⁰ using an MP2/VTZ cubic force field (see Table 4).

Formic acid (C_s symmetry) can be considered the prototype of carboxylic acids and presents

two rotamers, the *cis* and *trans* forms. The SE equilibrium structures of both forms have been previously obtained by combining the experimental ground-state rotational constants of several isotopologues (11 and 7 for the *cis* and *trans* form, respectively) with $\Delta B_{\text{vib}}^{\beta}$ calculated from a MP2/VTZ cubic force field.¹²¹ As shown in Table 4, for both conformers, the SE equilibrium structures issuing from B3LYP vibrational contributions are in very good agreement with the reference SE results.

cis-methyl formate is an important interstellar molecule and is considered the prototype system for studying the internal rotation of a methyl group.¹²² At equilibrium, *cis*-methyl formate possesses a symmetry plane with one pair of equivalent out-of-plane hydrogen atoms (C_s symmetry) and $d(\text{C-O-C}_m\text{-H}_{\text{plane}}) = 180.00$ degrees, where H_{plane} is the methyl hydrogen on the symmetry plane. In ref. 122, $\Delta B_{\text{vib}}^{\beta}$ contributions derived from a MP2/VTZ cubic force field were combined with the available experimental rotational constants. The agreement between the MP2/VTZ and B3LYP/SNSD results is good for all parameters that are not related to the H_{plane} atom. In fact, quite large discrepancies are found for both the $\text{C}_m\text{-H}_{\text{plane}}$ bond length (about 0.0052 Å) and the $\text{O-C}_m\text{-H}_{\text{plane}}$ angles (about 0.69 Å). As noted for propene, the B3LYP/SNSD r_e^{SE} shows a smaller difference between the $\text{C}_m\text{-H}_{\text{plane}}$ and $\text{C}_m\text{-H}_{\text{out}}$ bond lengths than the MP2 SE equilibrium structure.

Glycolaldehyde can be considered the simplest sugar. Only the *syn* conformer, which is stabilized by an intramolecular hydrogen bond, has been observed by microwave spectroscopy.^{123–127} It has C_s symmetry and is completely defined by 12 geometrical parameters. Recently, a SE equilibrium structure was determined by combining the ground-state experimental rotational constants with $\Delta B_{\text{vib}}^{\beta}$ contributions at the MP2/VTZ level.⁹⁰ The agreement with the new B3LYP/SNSD SE equilibrium structure is generally good, except for some small discrepancies on $r(\text{C1-C2})$ (1.5014 versus 1.5003 Å), $r(\text{O-H})$ (0.9618 versus 0.9593 Å), and $a(\text{C1-C2-H})$ (107.80 versus 108.11 degrees). It is noteworthy that the B3LYP/SNSD r_e^{SE} is in remarkable agreement with the high level fully theoretical r_e (referred to as r_e^{BO} in Table 6 of ref. 90): $r(\text{C1-C2})=1.5016$ Å, $r(\text{O-H})=0.9653$ Å and $a(\text{C1-C2-H})=107.794$ Å.

The *syn* conformer of propanal, or propionaldehyde, which is significantly more stable than its *gauche* counterpart, has C_s symmetry (with $d(\text{C1-C2-C-H}_{plane}) = 180.00$ degrees) and is completely defined by 15 geometrical parameters. Once again, Table 4 shows that MP2/VTZ⁹⁰ and B3LYP/SNSD cubic force fields lead to very similar SE equilibrium structures.

Finally, in Table 5 we report the first determination of the SE equilibrium structure of glyoxylic acid (C_s symmetry), which is the simplest α -oxoacid and is completely determined by 11 geometrical parameters. The B3LYP/SNSD SE equilibrium structure has been obtained by fitting the SE I_e^B and I_e^C moments of inertia of 8 out of 9 experimentally observed isotopologues (see Table 2), where the $\text{H}^{13}\text{COCOOH}$ isotopologue has been excluded from the fit because of the large residuals shown by the fitted equilibrium rotational constants. In Table 5, the B3LYP SE equilibrium structure is compared with the theoretical r_e equilibrium geometry optimized at the CCSD(T)/VQZ level, taken from ref. 128. The agreement between these two structures is remarkable.

Table 4: r_0 , r_e^{SE} and r_e geometries of CH_2F_2 , CCl_2F_2 , CH_2Cl_2 , CHClF_2 , ethene, ethenol, propene, butadiene, *cis*-hexatriene, cyclopropane, aziridine, benzene, pyrrole, pyrazole, imidazole, furan, thiophene, maleic anhydride, dimethyl ether, *cis* and *trans*-formic acid, *cis*-methyl formate, glycolaldehyde and propanal. Distances in Å, angles in degrees.

	r_0^a	$r_e^{\text{SE}^a}$		r_e
		Literature	B3LYP/SNSD	B3LYP/SNSD
– halomethanes –				
CH_2F_2^b				
r(C-F)	1.3596(4)	1.35323(1) [†]	1.3533(1) [†]	1.3668
r(C-H)	1.0871(11)	1.08703(3)	1.0867(2)	1.0935
a(F-C-F)	108.06(3)	108.282(2)	108.29(1)	108.44
a(H-C-H)	113.42(13)	113.442(9)	113.48(2)	113.74
a(H-C-F)	108.81(5)	108.750(2)	108.74(1)	108.64
Rms resid. [MHz]	0.0082	-	0.0013	-
CCl_2F_2^c				
r(C-F)	1.3511(59)	1.3287(8) [†]	1.3286(7) [†]	1.3372
r(C-Cl)	1.7395(50)	1.7519(7)	1.7519(6)	1.7857
a(F-C-F)	105.57(47)	107.75(9)	107.77(6)	108.04
a(Cl-C-Cl)	113.22(35)	111.62(7)	111.61(4)	111.83
a(Cl-C-F)	109.44(20)	109.35(1)	109.34(3)	109.22
Rms resid. [MHz]	0.0060	-	0.0008	-
CH_2Cl_2^d				
r(C-H)	1.0743(15)	1.0816(2) [†]	1.0810(8) [†]	1.0862
r(C-Cl)	1.7711(4)	1.76425(3)	1.7642(2)	1.7956
a(H-C-H)	111.34(16)	111.772(4)	111.79(9)	112.48
a(Cl-C-Cl)	111.92(3)	112.166(3)	112.18(2)	112.85
a(Cl-C-H)	108.40(6)	108.237(10)	108.23(3)	107.90
Rms resid. [MHz]	0.0122	-	0.0069	-
CHClF_2^d				
r(C-H)	1.0953(6)	1.0850(11)	1.0849(2) [†]	1.0901
r(C-F)	1.3450(11)	1.3363(5)	1.3363(4)	1.3466
a(C-Cl)	1.7465(20)	1.7560(9)	1.7558(8)	1.7915
a(H-C-F)	109.14(11)	109.97(4)	110.02(4)	110.14
a(H-C-Cl)	110.41(23)	109.60(6)	109.45(9)	109.16
a(F-C-Cl)	110.25(6)	109.62(4)	109.63(2)	109.58
a(F-C-F)	107.59(9)	108.06(6)	108.06(3)	108.23
Rms resid. [MHz]	0.0017	-	0.0006	-
– substituted alkene compounds –				
ethene^e				
r(C=C)	1.3373(3)	1.3305(10)	1.3317(1) [†]	1.3322
r(C-H)	1.0836(3)	1.0805(10)	1.0805(1)	1.0870
a(C=C-H)	121.26(2)	121.45(10)	121.40(1)	121.71
a(H-C-H)	117.49(3)	117.10(10)	117.19(1)	116.58
Rms resid. [MHz]	0.0024	-	0.0002	-
Mean Δ_e [$\text{u}\text{Å}^2$]	0.06148	-	0.00119	-

ethanol^f

r(O-H)	0.9595(17)	0.9604(2) [†]	0.9605(1) [†]	0.9668
r(C2-O)	1.3708(20)	1.3594(8)	1.3598(1)	1.3638
r(C2-H)	1.0893(17)	1.0794(4)	1.0789(1)	1.0860
r(C1=C2)	1.3333(21)	1.3312(9)	1.3316(1)	1.3344
r(C1-H _{cis})	1.0882(13)	1.0816(2)	1.0812(1)	1.0873
r(C1-H _{trans})	1.0762(14)	1.0772(4)	1.0770(1)	1.0831
a(C2-O-H)	108.51(14)	108.81(4)	108.70(1)	109.41
a(C1=C2-H)	127.14(73)	122.65(32)	122.58(8)	122.74
a(C1=C2-O)	126.11(4)	126.297(5)	126.26(1)	126.84
a(C2-C1-H _{cis})	121.37(13)	121.90(4)	121.87(1)	122.29
a(C2-C1-H _{trans})	119.62(19)	119.59(2)	119.58(1)	119.86
Rms resid. [MHz]	0.0022	-	0.0001	-
Mean Δ_e [$\text{u}\text{\AA}^2$]	0.04867	-0.00424	-0.00206	-

propene^g

r(C1=C2)	1.3408(16)	1.3310(7) [†]	1.3326(2) [†]	1.3340
r(C2-C3)	1.5042(15)	1.4956(7)	1.4956(2)	1.5004
r(C1-H _{cis})	1.0920(17)	1.0834(6)	1.0818(2)	1.0882
r(C1-H _{trans})	1.0789(21)	1.0805(12)	1.0804(2)	1.0862
r(C2-H)	1.0874(13)	1.0857(4)	1.0841(2)	1.0909
r(C3-H _{plane})	1.0823(30)	1.0862(8)	1.0880(4)	1.0947
r(C3-H _{out})	1.1036(56)	1.0949(9)	1.0895(7)	1.0976
a(C1=C2-C3)	124.11(6)	124.47(2)	124.43(1)	125.29
a(C2-C1-H _{cis})	120.42(13)	121.08(5)	121.13(2)	121.56
a(C2-C1-H _{trans})	121.53(26)	121.55(14)	121.31(3)	121.59
a(C1=C2-H)	118.50(29)	118.75(13)	118.84(4)	118.68
a(C2=C3-H _{plane})	111.24(12)	111.10(4)	111.07(2)	111.55
a(C2-C3-H _{out})	110.00(54)	110.53(11)	111.02(7)	111.03
d(C1=C2-C3-H _{out})	121.07(59)	121.08(14)	120.47(8)	120.80
Rms resid. [MHz]	0.0017	-	0.0002	-

butadiene^e

r(C1=C2)	1.3450(12)	1.3376(10)	1.3386(1) [†]	1.3411
r(C2-C3)	1.4603(17)	1.4539(10)	1.4543(2)	1.4561
r(C1-H _{cis})	1.0847(8)	1.0819(10)	1.0815(1)	1.0876
r(C1-H _{trans})	1.0822(10)	1.0793(10)	1.0793(1)	1.0854
r(C2-H)	1.0848(8)	1.0847(10)	1.0839(1)	1.0903
a(C1=C2-C3)	123.32(4)	123.62(10)	123.53(1)	124.29
a(C1=C2-H)	119.91(12)	119.91(10)	119.76(1)	119.34
a(C2=C1-H _{cis})	120.49(6)	120.97(10)	120.94(1)	121.41
a(C2=C1-H _{trans})	121.22(7)	121.47(10)	121.43(1)	121.63
Rms resid. [MHz]	0.0023	-	0.0002	-
Mean Δ_e [$\text{u}\text{\AA}^2$]	0.02434	-	-0.00790	-

cis-hexatriene^h

r(C1=C2)	1.3421(10)	1.33993(28) [†]	1.3418(8) [†]	1.3437
r(C2-C3)	1.4599(23)	1.45041(38)	1.4510(17)	1.4510
r(C3=C4)	1.3507(32)	1.34997(87)	1.3509(24)	1.3550
r(C1-H _{cis})	1.0808(29)	1.08255(35)	1.0815(22)	1.0876
r(C1-H _{trans})	1.0809(24)	1.07982(28)	1.0800(18)	1.0853
r(C2-H)	1.1107(25)	1.08788(37)	1.0866(19)	1.0881
r(C3-H)	1.0916(14)	1.08417(28)	1.0813(10)	1.0895
a(C1=C2-C3)	122.85(28)	122.755(38)	122.59(21)	123.61
a(C2-C3=C4)	126.21(9)	126.273(19)	126.23(6)	127.04
a(C2=C1-H _{cis})	121.03(29)	121.017(34)	121.05(22)	121.42
a(C2=C1-H _{trans})	121.43(30)	121.456(37)	121.38(23)	121.60
a(C1-C2-H)	120.38(29)	119.320(37)	119.51(22)	118.45
a(C4=C3-H)	119.67(18)	118.035(27)	117.48(14)	117.47
Rms resid. [MHz]	0.0022	-	0.0017	-
Mean Δ_e [$\text{u}\text{\AA}^2$]	-0.17124	-0.005	-0.01153	-

– cyclic and heterocyclic compounds –

cyclopropaneⁱ

r(C-C)	1.5144(2)	1.5030(10)	1.5031(1) [†]	1.5094
r(C-H)	1.0790(4)	1.0786(10)	1.0787(2)	1.0856
a(H-C-H)	115.38(4)	114.97(10)	114.94(2)	114.25
Rms resid. [MHz]	0.0036	-	0.0022	-

aziridine^j

r(C-N)	1.4800(4)	1.47013(6) [†]	1.4714(1) [†]	1.4740
r(C-C)	1.4800(4)	1.47703(8)	1.4777(1)	1.4845
r(N-H)	1.0118(8)	1.01279(13)	1.0126(1)	1.0180
r(C-H _{cis})	1.0821(7)	1.08099(13)	1.0805(1)	1.0877
r(C-H _{trans})	1.0803(7)	1.07971(13)	1.0791(1)	1.0866
a(C-N-H)	109.36(5)	109.376(9)	109.16(1)	110.03
a(C-N-C)	60.42(2)	60.311(6)	60.28(1)	60.47
a(N-C-C)	59.79(1)	59.845(3)	59.86(1)	59.77
a(N-C-H _{cis})	118.47(9)	118.28(2)	118.19(1)	118.61
a(N-C-H _{trans})	114.49(10)	114.46(2)	114.38(1)	114.66
a(C-C-H _{cis})	117.52(9)	117.829(14)	117.81(1)	117.99
a(C-C-H _{trans})	119.15(7)	119.538(14)	119.49(1)	119.85
Rms resid. [MHz]	0.0017	-	0.0001	-

benzene^k

r(C-C)	1.3970(2)	1.3914(10)	1.3919(1) [†]	1.3961
r(C-H)	1.0807(12)	1.0802(20)	1.0795(1)	1.0865
Rms resid. [MHz]	0.0266	-	0.0016	-
Mean Δ_e [$\text{u}\text{\AA}^2$]	-	-	-	-

pyrrole^l

r(C-N)	1.3766(6)	1.36940(17) [†]	1.3694(1) [†]	1.3755
r(C2-C3)	1.3792(7)	1.3723(2)	1.3732(1)	1.3794
r(C3-C4)	1.4275(23)	1.4231(4)	1.4228(2)	1.4256
r(N-H)	0.9936(5)	1.00086(14)	1.0007(1)	1.0081
r(C2-H)	1.0741(4)	1.07532(13)	1.0744(1)	1.0801
a(C3-H)	1.0751(5)	1.07527(16)	1.0745(1)	1.0810
a(H-N-C2)	125.21(3)	125.096(8)	125.09(1)	125.08
a(C5-N-C2)	109.58(4)	109.809(16)	109.82(1)	109.85
a(N-C2-C3)	107.87(5)	107.762(15)	107.76(1)	107.66
a(C2-C3-C4)	107.34(8)	107.334(12)	107.33(1)	107.42
a(N-C2-H)	121.89(22)	120.99(7)	121.12(2)	121.16
a(C2-C3-H)	125.43(19)	125.94(6)	125.88(2)	125.70
Rms resid. [MHz]	0.0009	-	0.0001	-
Mean Δ_e [$\mu\text{\AA}^2$]	0.01545	-	0.00018	-

pyrazole^m

r(N1-N2)	1.3530(40)	1.3431(6) [†]	1.3441(1) [†]	1.3486
r(N2=C3)	1.3302(46)	1.3286(7)	1.3289(1)	1.3329
r(C3-C4)	1.4190(571)	1.4093(6)	1.4090(11)	1.4144
r(C4=C5)	1.3794(49)	1.3771(8)	1.3765(1)	1.3817
r(C5-N1)	1.3611(33)	1.3523(6)	1.3519(1)	1.3587
r(N1-H)	0.9947(23)	1.0014(4)	1.0014(1)	1.0092
r(C3-H)	1.0768(23)	1.0755(4)	1.0757(1)	1.0817
r(C4-H)	1.0747(24)	1.0736(4)	1.0739(1)	1.0797
r(C5-H)	1.0754(35)	1.0740(5)	1.0745(1)	1.0805
a(N1-N2-C3)	103.92(18)	104.18(3)	104.11(1)	104.23
a(N2-C3-C4)	112.20(99)	111.90(5)	111.93(2)	111.88
a(C3-C4-C5)	104.38(78)	104.46(4)	104.46(2)	104.53
a(C4-C5-N1)	106.22(22)	106.23(4)	106.26(1)	106.19
a(C5-N1-N2)	113.27(1.60)	113.24(5)	113.24(3)	113.18
a(N2-N1-H)	121.17(1.09)	118.97(11)	118.95(2)	119.06
a(N2-C3-H)	123.12(1.41)	119.49(14)	119.51(3)	119.49
a(C3-C4-H)	126.94(1.45)	128.32(13)	128.18(3)	128.22
a(N1-C5-H)	121.03(1.09)	121.84(11)	121.75(2)	121.82
Rms resid. [MHz]	0.0042	-	0.0001	-
Mean Δ_e [$\mu\text{\AA}^2$]	0.03139	-	0.00120	-

imidazoleⁿ

r(N1-C2)	1.3700(40)	1.3612(9) [†]	1.3616(7) [†]	1.3671
r(C2=N3)	1.3141(36)	1.3111(8)	1.3103(6)	1.3161
r(N3-C4)	1.3865(33)	1.3797(8)	1.3794(5)	1.3789
r(C4=C5)	1.3670(252)	1.3627(8)	1.3627(41)	1.3731
r(C5-N1)	1.3824(32)	1.3738(9)	1.3743(5)	1.3802
r(N1-H)	0.9942(22)	1.0008(5)	1.0011(3)	1.0096
r(C2-H)	1.0769(21)	1.0759(6)	1.0770(3)	1.0817
r(C4-H)	1.0768(25)	1.0747(6)	1.0752(4)	1.0809
r(C5-H)	1.0765(25)	1.0764(5)	1.0764(4)	1.0793
a(N1-C2-N3)	111.98(22)	111.91(6)	111.93(4)	111.56
a(C2-N3-C4)	105.07(26)	105.02(5)	105.03(4)	105.43
a(N3-C4-C5)	110.63(51)	110.60(6)	110.62(8)	110.61
a(C4-C5-N1)	105.50(1.27)	105.45(6)	105.43(21)	105.12
a(C5-N1-C2)	106.81(98)	107.02(5)	106.99(16)	107.29
a(C2-N1-H)	125.50(68)	126.23(16)	126.15(11)	126.41
a(N1-C2-H)	122.56(52)	122.53(12)	122.37(9)	122.43
a(N3-C4-H)	120.70(54)	121.51(11)	121.45(9)	121.40
a(N1-C5-H)	121.51(56)	121.92(12)	121.90(9)	122.22
Rms resid. [MHz]	0.0040	-	0.0006	-
Mean Δ_e [$\text{u}\text{\AA}^2$]	0.02737	-	0.00096	-

furan^o

r(C2-O)	1.3670(11)	1.3594(7) [†]	1.3598(4) [†]	1.3647
r(C2=C3)	1.3570(18)	1.3552(8)	1.3542(4)	1.3611
r(C3-C4)	1.4459(176)	1.432(2)	1.4344(19)	1.4357
r(C2-H)	1.0740(8)	1.0735(7)	1.0739(3)	1.0790
r(C3-H)	1.0729(7)	1.0753(6)	1.0743(3)	1.0806
a(C2-O-C5)	106.43(10)	106.63(6)	106.50(3)	106.89
a(O-C2-C3)	110.88(8)	110.66(9)	110.79(4)	110.42
a(C2-C3-C4)	105.91(59)	106.03(7)	105.96(6)	106.14
r(H-C2-O)	115.11(12)	115.88(6)	115.82(3)	115.85
a(H-C3-C4)	127.49(6)	127.66(5)	127.61(3)	127.46
Rms resid. [MHz]	0.0092	-	0.0010	-
Mean Δ_e [$\text{u}\text{\AA}^2$]	0.04728	-	0.00116	-

thiophene^p

r(S-C2)	1.7196(10)	1.704(2)	1.7127(5) [†]	1.7404
r(C2=C3)	1.3663(18)	1.372(3)	1.3625(9)	1.3678
r(C3-C4)	1.4307(44)	1.421(4)	1.4233(21)	1.4289
r(C2-H)	1.0763(10)	1.085(5)	1.0772(5)	1.0811
r(C3-H)	1.0783(6)	1.088	1.0792(3)	1.0844
a(C2-S-C5)	91.90(8)	92.4(2)	91.88(4)	91.32
a(S-C2-C3)	111.65(7)	111.6	111.66(3)	111.53
a(C2=C3-C4)	112.40(15)	112.2	112.40(7)	112.81
a(H-C2-S)	119.76(20)	119.9(3)	120.06(10)	119.84
a(H-C3-C4)	124.12(5)	124.4(4)	124.14(3)	123.92
Rms resid. [MHz]	0.0020	-	0.0010	-
Mean Δ_e [$\text{u}\text{\AA}^2$]	0.06604	-	0.00340	-

maleic anhydride^q

r(C1=C2)	1.3406(52)	1.3324(5) [†]	1.3320(10) [†]	1.3355
r(C2-C3)	1.4870(18)	1.4849(5)	1.4857(3)	1.4895
r(C3-O4)	1.3907(11)	1.3848(3)	1.3843(2)	1.3941
r(C3=O7)	1.1943(8)	1.1894(2)	1.1896(2)	1.1948
r(C1-H)	1.0747(7)	1.0765(2)	1.0761(1)	1.0822
a(C1=C2-C3)	107.88(17)	107.96(1)	107.94(3)	108.15
a(C2-C3=O7)	129.75(12)	129.67(3)	129.59(2)	129.85
a(C1=C2-H)	129.91(6)	129.90(1)	129.93(1)	129.84
a(C2-C3-O4)	108.01(8)	107.78(2)	107.79(2)	107.59
a(C3-O4-C5)	108.22(10)	108.52(3)	108.53(2)	108.53
a(O4-C5=O6)	122.24(15)	122.55(4)	122.61(3)	122.56
Rms resid. [MHz]	0.0023	-	0.0004	-
Mean Δ_e [$\text{u}\text{\AA}^2$]	-0.00800	-0.00057	-0.00779	-

- ethers, aldehydes, esters and carboxylic acids -**dimethyl ether^r**

r(C-O)	1.4160(1)	1.40660(2) [†]	1.4074(1) [†]	1.4139
r(C-H _{plane})	1.0843(10)	1.0865(2)	1.0855(2)	1.0924
r(C-H _{out})	1.0999(4)	1.09506(7)	1.0949(1)	1.1014
r(C-O-C)	111.71(2)	111.100(3)	111.06(1)	112.55
r(O-C-H _{plane})	107.17(8)	107.515(14)	107.50(2)	107.34
r(O-C-H _{out})	110.70(2)	111.191(3)	111.12(1)	111.40
d(C-O-C-H _{out})	60.20(4)	60.542(6)	60.52(1)	60.67
Rms resid. [MHz]	0.0021	-	0.0005	-

cis-formic acid^s

r(C-H)	1.1005(12)	1.0976(4) [†]	1.0985(3) [†]	1.1063
r(C=O)	1.1980(18)	1.1920(4)	1.1910(3)	1.1960
r(C-O)	1.3518(17)	1.3472(4)	1.3485(3)	1.3540
r(O-H)	0.9575(16)	0.9610(4)	0.9619(2)	0.9680
a(H-C=O)	121.51(88)	123.26(22)	124.21(18)	123.99
a(O-C=O)	122.23(3)	122.28(1)	122.30(1)	122.41
a(C-O-H)	109.29(15)	109.28(3)	109.00(2)	109.71
Rms resid. [MHz]	0.0023	-	0.0003	-
Mean Δ_e [$\text{u}\text{\AA}^2$]	0.06366	-	-0.00067	-

trans-formic acid^s

r(C-H)	1.0944(7)	1.0920(1) [†]	1.0918(3) [†]	1.0000
r(C=O)	1.2048(15)	1.1980(1)	1.1973(5)	1.2026
r(C-O)	1.3442(16)	1.3406(1)	1.3417(5)	1.3469
r(O-H)	0.9712(12)	0.9662(1)	0.9656(4)	0.9729
a(H-C=O)	123.67(66)	125.04(1)	125.38(22)	125.15
a(O-C=O)	124.98(3)	124.83(1)	124.78(1)	125.05
a(C-O-H)	106.37(8)	106.97(1)	106.78(2)	107.37
Rms resid. [MHz]	0.0019	-	0.0005	-
Mean Δ_e [$\text{u}\text{\AA}^2$]	0.08253	-	0.00057	-

***cis*-methyl formate^t**

r(C _m -O)	1.4378(40)	1.4341(5) [†]	1.4358(16) [†]	1.4440
r(C-O)	1.3444(40)	1.3345(4)	1.3343(15)	1.3411
r(C _m -H _{plane})	1.0526(63)	1.0793(10)	1.0845(30)	1.0893
r(C _m -H _{out})	1.0935(20)	1.0871(3)	1.0875(8)	1.0924
r(C-H)	1.0952(46)	1.0930(5)	1.0925(18)	1.1006
r(C=O)	1.2051(46)	1.2005(5)	1.2001(17)	1.2049
a(C _m -O-C)	114.99(34)	114.32(4)	114.26(13)	115.77
a(O-C _m -H _{plane})	108.01(98)	106.05(16)	105.35(42)	105.46
a(O-C _m -H _{out})	109.76(14)	110.19(2)	110.07(5)	110.24
a(O-C-H)	109.74(44)	109.96(5)	109.54(17)	109.24
a(O-C=O)	125.37(43)	125.50(5)	125.50(16)	125.81
d(H _{out} -C-O-C)	58.98(21)	-60.28(3)	-60.36(8)	-60.37
Rms resid. [MHz]	0.0067	-	0.0025	-

glycolaldehyde^r

r(C1=O)	1.2138(23)	1.2086(4) [†]	1.2083(5) [†]	1.2115
r(C1-H)	1.0946(18)	1.1015(3)	1.1011(4)	1.1096
r(C1-C2)	1.5166(19)	1.5003(3)	1.5014(4)	1.5065
r(C2-H)	1.1029(11)	1.0969(2)	1.0964(2)	1.1033
r(C2-O)	1.3946(20)	1.3962(3)	1.3970(4)	1.4014
r(O-H)	1.0410(35)	0.9593(5)	0.9618(6)	0.9721
a(C2-C1=O)	121.22(19)	121.65 ^u	121.68(4)	122.05
a(C2-C1-H)	116.80(24)	116.91 ^u	116.85(5)	116.47
a(C1-C2-H)	107.68(13)	108.11(2)	107.80(3)	107.79
a(C1-C2-O)	112.47(17)	111.75(3)	111.72(3)	112.63
a(C2-O-H)	103.07(13)	106.28(2)	106.14(3)	106.53
d(H-C2-C1=O)	122.90(12)	122.35(2)	122.27(2)	122.82
Rms resid. [MHz]	0.0067	-	0.0006	-

propanal^r				
r(C1-C2)	1.5130(20)	1.5023(6) [†]	1.5037(4) [†]	1.5087
r(C2-C3)	1.5236(22)	1.5164(4)	1.5165(4)	1.5260
r(C3-H _{plane})	1.0759(18)	1.0884(3)	1.0879(3)	1.0943
r(C3-H _{out})	1.0944(10)	1.0883(2)	1.0888(2)	1.0938
r(C2-H)	1.0991(11)	1.0949(2)	1.0946(2)	1.1012
r(C1=O)	1.2093(22)	1.2074(4)	1.2075(4)	1.2099
r(C1-H)	1.1059(18)	1.1056(3)	1.1040(3)	1.1145
a(C2-C3-H _{plane})	111.37(29)	110.66(4)	110.52(6)	110.62
a(C2-C3-H _{out})	110.24(7)	110.72(2)	110.68(1)	111.02
a(C1-C2-C3)	113.89(17)	113.60(2)	113.65(3)	114.84
a(C1-C2-H)	107.11(14)	106.95(3)	106.75(3)	106.63
a(C2-C1-O)	124.24(19)	124.38(3)	124.34(4)	124.98
a(C2-C1-H)	115.16(23)	115.44(3)	115.34(4)	114.91
d(O-C1-C2-H)	123.91(12)	123.77(2)	123.78(2)	124.39
d(C1-C2-C3-H _{out})	58.90(10)	59.46(2)	59.42(2)	59.64
Rms resid. [MHz]	0.0067	-	0.0004	-

a) All fits have been performed on moments of inertia. For all structures evaluated in this work, the uncertainties on the geometrical parameters are reported within parentheses, rounded to $1 \cdot 10^{-4}$ Å for lengths and $1 \cdot 10^{-2}$ degrees for angles if smaller than these values. $\Delta_e = I^C - I^B - I^A$ is the inertial defect. † denotes the inclusion of ΔB_{el}^β .

b) MP2/VTZ r_e^{SE} from ref. 101.

c) B3LYP/6-311+G(3df,2pd) r_e^{SE} from ref. 101.

d) MP2/V(T+d)Z r_e^{SE} from ref. 101.

e) literature r_e^{SE} obtained as average of different MP2 and B3LYP r_e^{SE} , with basis sets of at least triple- ζ quality, where the ΔB_{vib}^β are derived coupling scaled quadratic force fields with unscaled cubic force fields, from ref. 103.

f) MP2/VQZ r_e^{SE} from ref. 90.

g) MP2/VTZ r_e^{SE} from ref. 105.

h) MP2/VTZ r_e^{SE} from ref. 91.

i) SDQ-MBPT(4)/VTZ r_e^{SE} from ref. 107.

j) MP2/VTZ r_e^{SE} from ref. 112.

k) SDQ-MBPT(4)/VTZ r_e^{SE} from ref. 108.

l) MP2(AE)/wCVTZ r_e^{SE} from ref. 112.

m) B3LYP/6-311+G(3df,2pd) r_e^{SE} from ref. 112.

n) B3LYP/6-311+G(3df,2pd) r_e^{SE} from ref. 112, where the experimental ground-state rotational constants were corrected within the predicates method.

o) MP2/VTZ r_e^{SE} from ref. 114.

p) SE structure ED + MW + vibSP(B3LYP/6-311+G* force field), see ref. 115.

q) MP2/VTZ r_e^{SE} from ref. 89.

r) MP2/VTZ r_e^{SE} from ref. 90.

s) MP2/VTZ r_e^{SE} from ref. 121.

t) MP2/VTZ r_e^{SE} from ref. 122.

u) values calculated as $121.65 = 180.00 - 58.35$ and $116.91 = 180.00 - 63.09$, where 58.35 and 63.09 are taken from Table 6 of ref. 90.

Table 5: r_0 , r_e^{SE} and r_e geometries for glyoxylic acid and pyridine. Distances in Å, angles in degrees.

	r_0^a	$r_e^{\text{SE}^a}$	r_e	
		B3LYP/SNSD	CCSD(T)	B3LYP/SNSD
glyoxylic acid				
r(C1-C2)	1.5361(29)	1.5211(3) [†]	1.5256 ^b	1.5345
r(C1-H)	1.0959(28)	1.0964(3)	1.0963	1.1045
r(C1=O)	1.2063(30)	1.2067(3)	1.2087	1.2080
r(C2=O)	1.2039(30)	1.1994(3)	1.1977	1.2034
r(C2-O)	1.3310(33)	1.3325(3)	1.3317	1.3373
r(O-H)	0.9552(44)	0.9692(4)	0.9697	0.9764
r(C2-C1-H)	115.36(21)	115.59(2)	115.41	115.13
r(C2-C1=O)	120.54(27)	120.60(3)	120.66	121.03
r(C1-C2=O)	120.97(25)	121.95(3)	121.90	121.74
r(C1-C2-O)	113.95(29)	113.70(3)	113.35	113.78
r(C-O-H)	107.15(23)	106.84(2)	106.74	107.67
Rms resid. [MHz]	0.0030	0.0003	-	-
Mean Δ_e [$\text{u}\text{\AA}^2$]	0.06291	-0.01110	-	-
pyridine				
r(C2-C3)	1.3950(15)	1.3907(18) [†]	1.3898 ^c	1.3954
r(C3-C4)	1.3949(12)	1.3888(13)	1.3876	1.3930
r(N-C2)	1.3414(35)	1.3358(40)	1.3346	1.3391
r(C2-H)	1.0841(11)	1.0818(12)	1.0824	1.0887
r(C3-H)	1.0800(10)	1.0796(11)	1.0801	1.0858
r(C4-H)	1.0819(12)	1.0802(13)	1.0808	1.0865
a(C6-N-C2)	117.01(16)	116.93(18)	117.01	117.19
a(N-C2-C3)	123.75(18)	123.79(21)	123.73	123.64
a(C2-C3-C4)	118.50(9)	118.53(11)	118.54	118.50
a(C3-C4-C5)	118.49(9)	118.44(10)	118.44	118.54
a(N-C2-H)	115.49(24)	115.97(28)	115.97	116.00
a(C3-C2-H)	120.76(16)	120.25(18)	120.30	120.36
a(C2-C3-H)	120.73(16)	120.10(18)	120.14	120.22
a(C3-C4-H)	120.76(6)	120.78(7)	120.78	120.73
Rms resid. [MHz]	0.0028	0.0031	-	-
Mean Δ_e [$\text{u}\text{\AA}^2$]	0.03958	0.00392	-	-

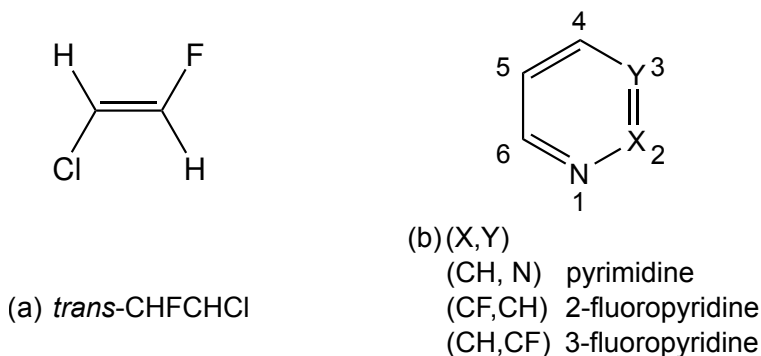
a) The fits have been performed using SE I_e^B and I_e^C moments of inertia for glyoxylic acid and I_e^A and I_e^C ones for pyridine. The digits within parentheses are the uncertainties on the geometrical parameters.

$\Delta_e = I^C - I^B - I^A$ is the inertial defect. † denotes the inclusion of $\Delta B_{\text{el}}^\beta$.

b) r_e optimized at the CCSD(T)/VQZ level, from ref. 128.

c) r_e optimized at the CCSD(T)/CBS+CV level, from this work.

Figure 4: Sketch of the 4 molecules determined within the template approach.



Toward larger systems: the template approach

In all cases presented above, a large number of experimental data, coupled with a limited number of molecular parameters, permitted the complete determination of the molecular structure. This is often not possible when the molecular size and topological complexity increase because of the large number of isotopologues then required. In these cases, the strategy widely adopted in the literature consists of fixing in the fitting procedure some parameters to the corresponding computed values,^{50,52-54} or allowing some internal coordinates (called predicates) to vary from reference values within given uncertainties.¹²⁹

Although, as shown above, $\Delta B_{\text{vib}}^{\beta}$ and ΔB_{el} contributions calculated at the B3LYP level leads to very good r_e^{SE} results, the fixed parameters (or reference values within predicated methodology) need to be estimated at much higher levels of theory to achieve good accuracy. An example is provided by the case of glycine Ip, for which the differences between the CCSD(T)/VTZ and CCSD(T)/CBS+CV equilibrium structures are significant.¹³⁰ Since CCSD(T)/CBS+CV calculations for large systems are computationally very expensive, they are not always feasible.

In the following, we present a new approach to deal with medium-large systems and a series of test cases that allow us to point out its reliability. When one is interested in the determination of the r_e^{SE} structure of a molecule for which high-level computations are too expensive, it is possible to use a similar molecule (e.g., an isomer or substituted system), for

which an accurate r_e^{SE} structure is available, as a template for deriving the parameters to be fixed in the fitting procedure. These parameters can be obtained as

$$r_e(\text{fixed}) = r_e + \Delta\text{TM} \quad (3)$$

where ΔTM is defined as

$$\Delta\text{TM} = r_e^{\text{SE}}(\text{TM}) - r_e(\text{TM}) \quad (4)$$

r_e is the geometrical parameter of interest calculated at the same level for both the molecule under consideration and that chosen as reference, denoted as template-molecule (TM). In the following, some examples of application of this new approach are given and the reachable accuracy is addressed.

***trans*-1-chloro-2-fluoroethylene**

The first system analyzed is *trans*-1-chloro-2-fluoroethylene, for which the lack of experimental rotational constants for the ^{13}C -containing isotopologues does not allow the determination of the C=C bond length. As discussed above, a possible solution is to fix this parameter at a value obtained at a very high level of theory, as done in ref. 98. CCSD(T)/CBS+CV equilibrium geometries are available for both *cis* and *trans* isomers (see ref. 98 and Table 6) together with a complete r_e^{SE} equilibrium structure for the *cis* species (see Table 1). As a consequence, the *cis*-1-chloro-2-fluoroethylene can be used as a template for the estimation of the ΔTM correction for $r(\text{CC})$ of the *trans* isomer. According to eq. 4, the difference between the SE and theoretical values of $r(\text{CC})$ in *cis*-chlorofluoroethylene has been employed to correct the theoretical value of the C=C bond length of *trans*-chlorofluoroethylene, obtained at the same level of theory. Subsequently, the corrected $r(\text{CC})$ has been kept fixed in the fits performed, the corresponding results being reported in Table 7. In all cases, the $\Delta B_{\text{vib}}^\beta$ terms have been calculated at the B3LYP/SNSD level, and the B3LYP/AVTZ $\Delta B_{\text{el}}^\beta$ contributions have also been included. The fits have been performed on the SE I_e^A

and I_e^B moments of inertia, with 20 and 1 as relative weights, since I_e^B is about 20 times larger than I_e^A . The four fits differ for the level of theory used in the evaluation of r_e^{SE} of the template molecule and of r_e : $r_e^{\text{SE}}(\text{C}=\text{C})$ has been taken from SE equilibrium structure of *cis*-chlorofluoroethylene calculated with either CCSD(T)/VTZ $\Delta B_{\text{vib}}^\beta$ contributions, fits 1 and 2, or B3LYP/SNSD $\Delta B_{\text{vib}}^\beta$ contributions, fits 3 and 4, while the theoretical $r_e(\text{C}=\text{C})$ value at the CCSD(T)/CBS+CV level has been used for fits 1 and 3, and that at the B3LYP/SNSD level for fits 2 and 4. Table 7 shows that the results of fits 1 and 2 are similar to one another, and this is also the case for fits 3 and 4.

This suggests that the accuracy of the template approach is rather independent from the chosen theoretical method used in r_e estimation, and only limited by the accuracy of the template-molecule SE equilibrium structure considered. It is noteworthy that fit 4 allowed us to obtain a SE equilibrium structure completely independent from high-level (extremely expensive) computational results. This is particularly appealing in the treatment of medium-large systems, for which structural determinations at highly-correlated levels become computationally too expensive.

Table 6: r_e equilibrium geometries of *cis*- and *trans*-1-chloro-2-fluoroethylene. Distances in Å, angles in degrees.

	<i>cis</i> -CHFCHCl		<i>trans</i> -CHFCHCl	
	CBS+CV ^a	B3LYP/SNSD	CBS+CV ^a	B3LYP/SNSD
r(C1-Cl)	1.7107	1.7404	1.7163	1.7495
r(C1-H)	1.0764	1.0818	1.0775	1.0825
r(C1=C2)	1.3249	1.3278	1.3240	1.3266
r(C2-F)	1.3310	1.3416	1.3376	1.3499
r(C2-H)	1.0787	1.0849	1.0785	1.0840
a(Cl-C1=C2)	123.10	123.74	120.63	121.11
a(H-C1-C2)	120.43	120.91	122.95	123.62
a(F-C2=C1)	122.53	123.10	120.14	120.10
a(H-C2=C1)	123.43	123.45	125.82	126.50

a) CCSD(T)/CBS+CV r_e equilibrium geometry from ref. 98.

Table 7: r_e^{SE} equilibrium geometries of *trans*-1-chloro-2-fluoroethylene. Distances in Å, angles in degrees.

<i>trans</i> -chloro fluoroethylene	$r_e^{\text{SE}^a}$			
	Fit 1 ^b	Fit 2 ^c	Fit 3 ^d	Fit 4 ^e
r(C1-Cl)	1.7188(9)	1.7190(9)	1.7178(9)	1.7179(9)
r(C1-H)	1.0775(21)	1.0774(21)	1.0780(21)	1.0779(21)
r(C1=C2)	1.3236 [√]	1.3233 [√]	1.3257 [√]	1.3254 [√]
r(C2-F)	1.3395(20)	1.3398(20)	1.3376(20)	1.3379(20)
r(C2-H)	1.0792(27)	1.0792(27)	1.0790(27)	1.0790(27)
a(Cl-C1=C2)	120.46(6)	120.45(6)	120.54(6)	120.53(6)
a(H-C1-C2)	122.60(15)	122.62(15)	122.47(15)	122.49(15)
a(F-C2=C1)	120.17(21)	120.16(21)	120.18(21)	120.18(21)
a(H-C2=C1)	125.86(5)	125.89(5)	125.69(5)	125.71(5)
Rms resid. [MHz]	0.0011	0.0011	0.0011	0.0011
Mean Δ_e [$\text{u}\text{\AA}^2$]	0.00308	0.00308	0.00308	0.00308

- a) All fits have been performed on SE I_e^A and I_e^B moments of inertia, with 20 and 1 as weights, respectively, derived from $(B_0^\beta)^{\text{exp}}$ constants corrected by B3LYP/SNSD $\Delta B_{\text{vib}}^\beta$ and B3LYP/AVTZ $\Delta B_{\text{el}}^\beta$ contributions. The digits within parentheses are the uncertainties on the geometrical parameters, while $\sqrt{}$ denotes the parameter kept fixed, obtained using *cis*-chlorofluoroethylene as TM (see text). $\Delta_e = I^C - I^B - I^A$ is the inertial defect.
- b) $r_e(\text{fixed}) = r_e(\text{CBS+CV}) + \Delta\text{TM}$; $\Delta\text{TM} = r_e^{\text{SE}}(\text{CCSD(T)}/\text{VTZ}) - r_e(\text{CBS+CV})$.
- c) $r_e(\text{fixed}) = r_e(\text{B3LYP/SNSD}) + \Delta\text{TM}$; $\Delta\text{TM} = r_e^{\text{SE}}(\text{CCSD(T)}/\text{VTZ}) - r_e(\text{B3LYP/SNSD})$.
- d) $r_e(\text{fixed}) = r_e(\text{CBS+CV}) + \Delta\text{TM}$; $\Delta\text{TM} = r_e^{\text{SE}}(\text{B3LYP/SNSD}) - r_e(\text{CBS+CV})$.
- e) $r_e(\text{fixed}) = r_e(\text{B3LYP/SNSD}) + \Delta\text{TM}$; $\Delta\text{TM} = r_e^{\text{SE}}(\text{B3LYP/SNSD}) - r_e(\text{B3LYP/SNSD})$.

Pyrimidine

Analogously to the case of *trans*-chlorofluoroethylene, the limited number of isotopologues experimentally investigated (7) makes the derivation of all geometrical parameters of pyrimidine not possible. In particular, no deuterated species have been studied experimentally, thus preventing the derivation of the C-H bond lengths and of the corresponding angles. In Table 8, three different fits for the SE equilibrium structure of pyrimidine are reported, all obtained by correcting the experimental rotational constants with $\Delta B_{\text{vib}}^\beta$ contributions at the B3LYP/SNSD level and fitting on the I_e^A and I_e^C moments of inertia, with the inclusion of $\Delta B_{\text{el}}^\beta$ (see Table 8). To evaluate the non-determinable parameters, pyridine has been used as TM (fit 1 in Table 8). The ΔTM corrections have been derived from the B3LYP/SNSD

results of pyridine (Table 5). In particular, the N3-C4-H angle of pyrimidine has been estimated by using the Δ TM correction evaluated for the N-C2-H angle of pyridine; the Δ TM corrections for $r(\text{C2-H})$ and $r(\text{C4-H})$ have been based on the values for the C2-H distance of pyridine (these three parameters have in common the N-C-H pattern), while for the C5-H distance in pyrimidine the Δ TM correction has been calculated from $r(\text{C3-H})$ of pyridine (these two parameters shares a N-CH-C-H pattern). For the SE equilibrium structure of pyrimidine obtained following this procedure (fit 1 in Table 8), we expect an accuracy similar to that of a full SE equilibrium structure obtained with B3LYP/SNSD $\Delta B_{\text{vib}}^{\beta}$ contributions.

Fit 2 and 3 in Table 8 show that it is possible to obtain very similar results using pyridazine (see Table 1) as TM instead of pyridine. This finding points out another interesting feature of the template approach, that is, the choice of TM is rather flexible: it is sufficient to find a molecule in which the parameter of interest, for example the C4-H bond length in pyrimidine, is present and involved in a similar bond pattern, a N-C-H bond chain for the case under consideration. The comparison of the results for fits 2 and 3 demonstrates that the SE equilibrium structure obtained with the TM approach does not change significantly if the r_e^{SE} (TM) parameter is taken from the best SE equilibrium structure available (CCSD(T)/ANO0 vibrational contributions in this case) or from the B3LYP/SNSD r_e^{SE} . A r_e^{SE} equilibrium structure of pyrimidine has been recently determined using a B3LYP/6-311+G(3df,2pd) cubic force field and the so-called predicate approach based on a CCSD(T) equilibrium geometry.¹¹² The remarkable agreement between the “template” and the “predicate” r_e^{SE} equilibrium geometries (see Table 8) gives further support to the template strategy, which has the advantage of avoiding any expensive CCSD(T) computation.

Table 8: r_e and r_e^{SE} equilibrium geometries for pyrimidine. Distances in Å, angles in degrees.

pyrimidine	$r_e^{\text{SE}^a}$				r_e	
	Fit 1 ^b	Fit 2 ^c	Fit 3 ^d	Literature ^e	Literature ^f	B3LYP/SNSD
r(C2-N3)	1.3334(1)	1.3334(1)	1.3334(1)	1.3331(3)	1.3339	1.3374
r(N3-C4)	1.3355(1)	1.3355(1)	1.3358(1)	1.3349(6)	1.3349	1.3385
r(C4-C5)	1.3868(4)	1.3867(3)	1.3866(4)	1.3874(4)	1.3874	1.3921
r(C2-H)	1.0814 [√]	1.0822 [√]	1.0816 [√]	1.0820(23)	1.0819	1.0883
r(C4-H)	1.0819 [√]	1.0826 [√]	1.0820 [√]	1.0843(17)	1.0824	1.0887
r(C5-H)	1.0789 [√]	1.0795 [√]	1.0784 [√]	1.0799(23)	1.0793	1.0851
a(C2-N3-C4)	115.69(1)	115.69(1)	115.68(1)	115.712(21)	115.656	115.91
a(N3-C4-C5)	122.27(2)	122.27(2)	122.27(2)	122.276(19)	122.332	122.25
a(C4-C5-C6)	116.72(1)	116.72(1)	116.72(2)	116.661(36)	116.632	116.61
a(N1-C2-H)	116.31(1)	116.31(1)	116.31(1)	116.318(19)	116.303	116.46
a(N3-C4-H)	116.45 [√]	116.37 [√]	116.32 [√]	116.48(20)	116.461	116.48
a(C4-C5-H)	121.64(1)	121.64(1)	121.64(1)	121.670(18)	121.684	121.70
Rms resid. [MHz]	0.0004	0.0003	0.0004	-	-	-
Mean Δ_e [uÅ ²]	-0.00133	-0.00133	-0.00133	-	-	-

a) All fits have been performed on SE I_e^A and I_e^C moments of inertia, derived from the $(B_0^\beta)^{\text{EXP}}$ constants corrected by B3LYP/SNSD $\Delta B_{\text{vib}}^\beta$ and B3LYP/AVTZ $\Delta B_{\text{el}}^\beta$ contributions. The digits within parentheses are the uncertainties on the geometrical parameters, while [√] denotes the parameters kept fixed. $\Delta_e = I^C - I^B - I^A$ is the inertial defect.

b) $r_e(\text{fixed}) = r_e(\text{B3LYP/SNSD}) + \Delta\text{TM}$; $\Delta\text{TM} = r_e^{\text{SE}}(\text{B3LYP/SNSD}) - r_e(\text{B3LYP/SNSD})$, with pyrimidine as TM: r(C2-H) and r(C4-H) from r(C2-H), r(C5-H) from r(C3-H), a(N3-C4-H) from a(N-C2-H), see text.

c) $r_e(\text{fixed}) = r_e(\text{B3LYP/SNSD}) + \Delta\text{TM}$; $\Delta\text{TM} = r_e^{\text{SE}}(\text{CCSD(T)/ANO0}) - r_e(\text{B3LYP/SNSD})$, with pyridazine as TM: r(C2-H) and r(C4-H) from r(C3-H), r(C5-H) from r(C4-H), a(N3-C4-H) from a(N2-C3-H), see text.

d) $r_e(\text{fixed}) = r_e(\text{B3LYP/SNSD}) + \Delta\text{TM}$; $\Delta\text{TM} = r_e^{\text{SE}}(\text{B3LYP/SNSD}) - r_e(\text{B3LYP/SNSD})$, with pyridazine as TM: r(C2-H) and r(C4-H) from r(C3-H), r(C5-H) from r(C4-H), a(N3-C4-H) from a(N2-C3-H), see text.

e) r_e^{SE} structure determined using B3LYP/6-311+G(3df,2pd) $\Delta B_{\text{vib}}^\beta$ and the predicate approach, from ref. 112.

f) $r_e^{\text{BO}}(\text{II})$ in Table 9 of ref. 112.

Fluoropyridines

The first determinations of the SE equilibrium structure of 2- and 3-fluoropyridine are reported in Tables 9 and 10, respectively. Fluorine substitution reduces the molecular symmetry from C_{2v} to C_s , with the consequent increase of the number of unique internal parameters from 10 to 18. Because of the limited number of available experimental data, for

these molecules it is not possible to evaluate all structural parameters. Therefore, some parameters have been fixed using the template approach.

Because of the lack of rotational data for deuterated species, only the parameters defining the C-C ring and the C-F bond length have been considered as free parameters for 2-fluoropyridine. On the other hand, for 3-fluoropyridine also the C-F bond length has been kept fixed in order to converge the fitting procedure.

Starting from the assumption that the substitution of a hydrogen atom with fluorine does not affect significantly the structure of the ring, we used pyridine as TM for 2-fluoropyridine. The best results have been obtained by fitting the SE I_e^A and I_e^C moments of inertia. In fit 1, the Δ TM corrections have been estimated by considering the CCSD(T)/CBS+CV level for r_e , while in fit 2, r_e has been calculated at the B3LYP/SNSD level. Even in this case, the values in Table 5 confirm that the resulting SE structures are negligibly affected by the level of theory chosen for r_e .

For 3-fluoropyridine, we proceeded analogously to 2-fluoropyridine for what concerns the C-H bonds, while for the C-F distance and the corresponding C3-C2-F angle, 2-fluoropyridine has been employed as TM. This is consistent with what discussed above for pyrimidine, namely that the choice of the TM molecule is quite flexible, thus allowing the simultaneous use of more than one TM in the determination of the parameters to be fixed. As in 2-fluoropyridine, we have used the B3LYP/SNSD r_e^{SE} of pyridine combined with both CCSD(T)/CBS+CV (fit 1) and B3LYP/SNSD (fit 2) structures as r_e in the calculation of Δ TM.

Table 9: r_e and r_e^{SE} equilibrium geometries for 2-fluoropyridine. Distances in Å, angles in degrees.

2-fluoropyridine	$r_e^{\text{SE}^a}$		r_e	
	Fit 1 ^b	Fit 2 ^c	CBS+CV	B3LYP/SNSD
r(N-C2)	1.3138(10)	1.3135(10)	1.3063	1.3120
r(N-C6)	1.3402(5)	1.3402(5)	1.3410	1.3438
r(C2-C3)	1.3838(14)	1.3840(14)	1.3898	1.3935
r(C3-C4)	1.3837(3)	1.3837(3)	1.3836	1.3898
r(C4-C5)	1.3949(4)	1.3948(4)	1.3933	1.3972
r(C5-C6)	1.3836(4)	1.3836(4)	1.3844	1.3909
r(C2-F)	1.3357(2)	1.3358(2)	1.3344	1.3483
r(C3-H)	1.0781 [√]	1.0775 [√]	1.0787	1.0839
r(C4-H)	1.0801 [√]	1.0796 [√]	1.0807	1.0860
r(C5-H)	1.0788 [√]	1.0783 [√]	1.0794	1.0848
r(C6-H)	1.0809 [√]	1.0811 [√]	1.0815	1.0876
a(C6-N-C2)	116.24(6)	116.24(6)	116.42	116.61
a(N-C2-C3)	126.17(7)	126.17(7)	126.17	126.08
a(C2-C3-C4)	116.73(3)	116.72(3)	116.59	116.53
a(C3-C4-C5)	119.06(1)	119.06(1)	119.09	119.21
a(C4-C5-C6)	118.37(0)	118.37(0)	118.39	118.33
a(C5-C6-N)	123.44(2)	123.44(2)	123.35	123.25
a(C3-C2-F)	118.43(12)	118.41(12)	117.87	117.98
a(C2-C3-H)	120.38 [√]	120.48 [√]	120.42	120.60
a(C3-C4-H)	120.33(1)	120.33(1)	120.34	120.10
a(C6-C5-H)	120.26 [√]	120.25 [√]	120.30	120.37
a(C5-C6-H)	120.86 [√]	120.86 [√]	120.91	120.97
Rms resid. [MHz]	0.0001	0.0001	-	-
Mean Δ_e [uÅ ²]	-0.00180	-0.00180	-	-

a) The fits have been performed on the SE I_e^A and I_e^C moments of inertia. The $(B_0^\beta)^{\text{EXP}}$ constants have been corrected by B3LYP/SNSD $\Delta B_{\text{vib}}^\beta$ and B3LYP/AVTZ $\Delta B_{\text{el}}^\beta$ contributions. The digits within parentheses are the uncertainties on the geometrical parameters, while [√] denotes the parameters kept fixed obtained using pyridine as TM, see text. $\Delta_e = I^C - I^B - I^A$ is the inertial defect.

b) $r_e(\text{fixed}) = r_e(\text{CBS+CV}) + \Delta\text{TM}$; $\Delta\text{TM} = r_e^{\text{SE}}(\text{B3LYP/SNSD}) - r_e(\text{CBS+CV})$.

c) $r_e(\text{fixed}) = r_e(\text{B3LYP/SNSD}) + \Delta\text{TM}$; $\Delta\text{TM} = r_e^{\text{SE}}(\text{B3LYP/SNSD}) - r_e(\text{B3LYP/SNSD})$.

Table 10: r_e and r_e^{SE} equilibrium geometries for 3-fluoropyridine. Distances in Å, angles in degrees.

3-fluoropyridine	$r_e^{\text{SE}^a}$		r_e	
	Fit 1 ^b	Fit 2 ^c	CBS+CV	B3LYP/SNSD
r(N-C2)	1.3346(9)	1.3352(9)	1.3323	1.3368
r(C2-C3)	1.3931(5)	1.3888(6)	1.3859	1.3904
r(C3-C4)	1.3714(6)	1.3757(6)	1.3786	1.3850
r(C4-C5)	1.3895(8)	1.3901(9)	1.3894	1.3933
r(C5-C6)	1.3940(5)	1.3926(5)	1.3888	1.3955
r(C6-N)	1.3314(9)	1.3326(10)	1.3337	1.3389
r(C2-H)	1.0811 [√]	1.0813 [√]	1.0817	1.0877
r(C3-F)	1.3406 [√]	1.3398 [√]	1.3393	1.3523
r(C4-H)	1.0791 [√]	1.0787 [√]	1.0797	1.0852
r(C5-H)	1.0794 [√]	1.0791 [√]	1.0800	1.0856
r(C6-H)	1.0808 [√]	1.0812 [√]	1.0814	1.0877
a(C6-N-C2)	117.68(6)	117.65(6)	117.73	117.88
a(N-C2-C3)	121.75(6)	121.85(6)	122.09	121.79
a(C2-C3-C4)	121.07(3)	121.07(3)	120.83	121.04
a(C3-C4-C5)	117.04(2)	116.94(2)	116.84	116.91
a(C4-C5-C6)	118.88(2)	118.91(2)	119.18	118.94
a(C5-C6-N)	123.58(5)	123.58(5)	123.33	123.43
a(C3-C2-H)	119.90 [√]	120.12 [√]	119.95	120.23
a(C4-C3-F)	120.59 [√]	120.19 [√]	119.14	119.76
a(C3-C4-H)	121.88(1)	121.97(1)	121.96	120.52
a(C6-C5-H)	120.24 [√]	120.25 [√]	120.28	120.37
a(C5-C6-H)	120.48 [√]	120.36 [√]	120.53	120.47
Rms resid. [MHz]	0.0004	0.0004	-	-
Mean Δ_e [uÅ ²]	-0.00180	-0.00180	-	-

a) The fits have been performed on the SE I_e^A and I_e^B moments of inertia. The $(B_0^\beta)^{\text{EXP}}$ constants have been corrected by B3LYP/SNSD $\Delta B_{\text{vib}}^\beta$ and B3LYP/AVTZ $\Delta B_{\text{el}}^\beta$ contributions. The digits within parentheses are the uncertainties on the geometrical parameters, while [√] denotes the parameters kept fixed obtained using pyridine and 2-fluoropyridine as TM, see text. $\Delta_e = I^C - I^B - I^A$ is the inertial defect.

b) $r_e(\text{fixed}) = r_e(\text{CBS+CV}) + \Delta\text{TM}$; $\Delta\text{TM} = r_e^{\text{SE}}(\text{B3LYP/SNSD}) - r_e(\text{CBS+CV})$.

c) $r_e(\text{fixed}) = r_e(\text{B3LYP/SNSD}) + \Delta\text{TM}$; $\Delta\text{TM} = r_e^{\text{SE}}(\text{B3LYP/SNSD}) - r_e(\text{B3LYP/SNSD})$.

CONCLUSIONS

The present paper is devoted to a thorough investigation on the determination of accurate equilibrium structures by means of a semi-experimental approach, avoiding as much as pos-

sible the use of expensive CC calculations. In the first part, 21 small molecules for which accurate SE structures determined using CCSD(T) vibrational contributions are available have been selected (CCse set) and used to demonstrate that the $\Delta B_{\text{vib}}^{\beta}$ contributions derived from cubic force fields at the DFT level lead to results with an accuracy comparable to that obtainable at higher levels of theory (MP2 and, especially, CCSD(T)). In the second part, it has been shown that the B3LYP/SNSD model represents a very good compromise between accuracy and computational cost in the calculation of $\Delta B_{\text{vib}}^{\beta}$ contributions, thus making the accurate determination of molecular structures for medium and large systems feasible. Within this context, new SE equilibrium structures have been determined for a set of 26 molecules, mostly including building blocks of biomolecules. These structures together with the SE equilibrium structures of the previous 21 molecules determined using B3LYP/SNSD vibrational contributions provide a set of 47 accurate equilibrium structures (referred to as the B3se set) which can be recommended as reference data for the investigation of molecular properties, as well as for parameterisations and validation of QM models. Finally, a new method, denoted template approach, has been proposed to deal with molecules for which there is a lack of experimental data and it is thus necessary to fix some geometrical parameters in the fitting procedure. This approach further extends the size of molecular systems amenable to highly accurate molecular structure determinations. The whole B3se set is available (in graphical interactive form) on our website dreams.sns.it.

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Figure 5: TOC graphics



Supporting Information Available

Supporting Information Available: expressions of the vibration-rotation interaction constants; $(B_0^\beta)^{\text{EXP}}$, $\Delta B_{\text{vib}}^\beta$ and $\Delta B_{\text{el}}^\beta$ results for all the molecules studied in the paper (Tables 1-5); the comparison between the r_0 and r_e^{SE} geometries estimated using $\Delta B_{\text{vib}}^\beta$ from CCSD(T), MP2, B3LYP/SNSD and B3LYP/AVTZ cubic force fields (Table 6); the statistical distributions of the deviations from CCSD(T) SE equilibrium parameters for CH, CC and CO bonds of the molecules belonging to the CCse set (Figure 1); the plots of the CCSD(T) r_e^{SE} versus the MP2 and B3LYP ones for the molecules belonging to the CCse set (Figures 2).

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