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Having it all, for all: child-care subsidies and income distribution reconciled*

Francesca Barigozzi[†] Helmuth Cremer[‡] Kerstin Roeder[§]

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Abstract

We study the design of child-care policies when redistribution matters. Traditional mothers provide some informal child care, whereas career mothers purchase full time formal care. The sorting of women across career paths is endogenous and shaped by a social norm about gender roles in the family. Via this social norm traditional mothers' informal child care imposes an externality on career mothers, so that the market outcome is inefficient. Informal care is too large and the group of career mothers is too small so that inefficiency and gender inequality go hand in hand.

In a first-best world redistribution across couples and efficiency are separable. Redistribution is performed via lump-sum transfers and taxes which are designed to equalize utilities across all couples. The efficient allocation of child care is obtained by subsidizing formal care at a Pigouvian rate.

However, in a second-best setting, a trade-off between efficiency and redistribution emerges. The optimal uniform subsidy is lower than the "Pigouvian" level. Conversely, under a non-linear policy the first-best "Pigouvian" rule for the (marginal) subsidy on informal care is reestablished. While the share of high career mothers continues to be distorted downward for incentive reasons, this policy is effective in reconciling the objectives of reducing the child care related inefficiency and achieving a more equal income distribution across couples. Our results continue to hold when the norm is defined within the mothers' social group, rather than being based on the entire population.

JEL-Classification: D13, H23, J16, J22

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1 Introduction

While female labor force participation has been increasing steadily over the last decades (Goldin, 2006 and 2014b, Kleven and Landais, 2017) mothers continue to be the main providers of child care within the family (e.g., Paull, 2008; Ciccia and Verloo, 2012). Maternity leave and other child related career breaks or part-time work contribute in a significant way to the persistence of gender inequalities in the labor market. The so called “child penalty” appears to explain up to about 80% of the gender wage gap; see Kleven *et al.* (2018).¹

As a possible reason for the persistence of child-care compatible (part-time) work and child penalties, many studies point to social norms shaping women’s preferences over family and career (see Fortin 2015, Farré and Vella 2013, Bertrand *et al.* 2015, Bursztyn *et al.* 2017 and Kleven *et al.* 2018, among others). Social norms may contribute to the differential sorting of men and women across occupations with women entering low pay occupations that allow for shorter working days or more flexible working hours (see Goldin, 2014 and Card *et al.* 2016).

During the last five decades, most developed countries have put into practice multiple child policies with various declared goals, including gender equity, higher fertility, and child development. The policies who seem to have been the most effective in reducing gender disparities are child-care provision and subsidization. Evidence indicates that early childhood spending contributed substantially to enabling women to combine working life and motherhood, and to altering social norms regarding gender roles; see Olivetti and Petrongolo (2017).

Reducing gender disparities in the labor market is not the unique concern which is relevant for child-care policies. Redistribution across income levels has been *the* major issue for the design of tax and expenditures policies, it has lead to the emergence of the concept of “welfare state” which applies to all developed countries albeit to a different degree; see Boadway and Keen (1993). Unfortunately, the objective of reducing gender disparities in the labor market and redistributive concerns may be conflicting goals. Specifically, child-care provision and subsidization may be regressive if the parents who benefit more from the policy are the ones with relatively higher income. This is the case in most OECD countries, where very young children (aged 0-2) are more likely to use early childhood education and care services when they come from relatively advantaged socioeconomic backgrounds; see OECD (2017).² This evidence is confirmed by Krapf

¹The gender pay gap is the difference in average gross hourly earnings between women and men. Child penalty refers to the part of it that is determined by childbearing and family responsibilities. Specifically, child penalty is due to maternity leave and to leaves of absence and diminished hours of work for informal child care; see Blau and Kahn (2017); Kleven *et al.* (2019a) and (2019b).

²In Ireland, the participation rate for children in low-income families is, at about 20%, less than one-third of that for children from high-income families (66%). In Belgium, France and the Netherlands, participation rates for children from low-income backgrounds are generally a little higher (around 30–40%), but are still only about half those for children from the richest families (roughly 60-75%). Similarly, in a number of OECD countries children

(2014) and Petitsclerc *et al.* (2017) who document that low income and low maternal education is associated with reduced use of early child-care education in Sweden, Finland and Western Germany and in the UK, US, Netherlands and Canada, respectively.

Surprisingly, the interplay between child-care provision/subsidization and redistribution has so far to a large extent been ignored in the literature.³ We offer a fresh new look at this issue and propose a theoretical model whose crucial ingredient is an inefficient child penalty created by a gender norm. We then investigate the interaction between child penalties, child-care policies and redistribution. Our research questions are the following. To what extent reducing the child care related gender inequalities and achieving a more equal income distribution are conflicting objectives? How can this potential conflict be mitigated by an appropriate design of the child care policies?

We consider a model in which spouses' career prospects are perfectly correlated. However, while fathers always enter a high-career path, mothers can either enter the same high-career path or a low-career one. In the latter case mothers are "traditional" because they are able to provide some informal child care. "Career mothers" instead need to purchase full-time formal care in the market. The sorting of women across career paths is endogenous and shaped by a social norm about gender roles in the family. Via this social norm traditional mothers' informal care imposes an externality on career mothers, who feel guilt if they provide less informal care than the average amount provided by woman. Hence, in the *laissez faire* informal care is too large and the share of career mothers is too small. This translates in inefficiently high child penalties so that inefficiency and gender inequality go hand in hand. Furthermore, career choices exacerbate income inequalities (as measured for instance by the Gini coefficient) because higher incomes are concentrated on a smaller share of the population, which further decreases social welfare. We study the optimal design of linear and non-linear child-care policies when the government is concerned with both child-care related efficiency and redistribution.

In a recent paper, Barigozzi *et al.* (2018) have examined the interplay between social norms, career choices and child-care decisions. We build on their model but use a different specification

are also more likely to use early childhood education and care when their mother is educated to degree-level. In the United Kingdom, the participation rate for children with a mother that has attained tertiary education is at 41%, 17 percentage points higher than the rate for children with mothers that have not attained tertiary education (24%). In Switzerland, the gap is as large as 30 percentage points.

³Two exceptions are the literature on in-kind transfers and optimal taxation (Cremer and Pestieau 1996) and the literature on optimal taxation with endogenous fertility. In the latter, low-ability families may choose to 'specialize' in quantity, that is, to raise more children relative to higher-ability households. Child-related subsidies can, therefore, be used to enhance re-distribution: family size can be employed as an indicator for the earning capacity of the household (Cigno 1986). We totally depart from both strands of literature. We do not solve a model of optimal income taxation, we instead design non-linear child care subsidies. In addition, the number of children is exogenous in our model.

of the social norm. The research questions addressed in the two papers are completely different. Barigozzi *et al.* (2018) study whether eradicating or mitigating gender norms is socially optimal and how the design of specific policies (a uniform subsidy on child care, a women quota and parental leave) helps to achieve either one or the other objective. Redistribution is not a concern of the government in their model. In this paper we focus on the design of child-care subsidies when income redistribution is relevant.

We show that, in a first best, full information world efficiency and equity are separable. Redistribution is performed via lump-sum transfers and taxes which are designed to equalize utilities across all couples. Child-care policies, on the other hand, are designed to achieve the appropriate level of informal child care and the efficient share of high-career couples. Since the underlying problem is an externality, it is not surprising that the efficient policy involves a Pigouvian subsidy on market child care, which acts like a Pigouvian tax on informal care. And once child-care levels are efficient, the induced career choices are also efficient. However, since this policy taxes away all extra earnings of high-career couples, it is of course not incentive compatible and it cannot be implemented when the spouses' earning opportunities in the high-career path are not observable. Before moving to the study of feasible second-best policies, in Section 5 we present results from a numerical example useful to understand the relationship between the magnitude of the Pigouvian subsidy and the cost of the social norm.

We consider two types of second-best settings. First, we study a linear subsidy and we show that it involves a trade-off between efficiency and redistributive considerations. Consequently, the optimal subsidy is lower than the Pigouvian level which applies when efficiency is the only social concerns.

More interestingly, we then show that this trade-off depends on the linearity of the policy. To see that we characterize the optimal incentive compatible policy, that is the non-linear policy constrained by the information structure. We show that this policy reestablishes the first-best "Pigouvian" rule for the (marginal) subsidy on informal care. In other words there is no longer a trade-off between child-care subsidies and income redistribution. High-career couples enjoy positive rents and their share has to be reduced (compared to the first best) to mitigate these rents. Consequently the outcome remains second best. Still the policy is effective in reconciling the objectives of efficiency and income redistribution across couples. Note that the subsidy on formal care can be implicit in the case where child care is provided in kind.

The information requirement to implement this policy is rather minimal. It is sufficient that career paths *or* levels of formal child care are publicly observable. Amongst these the first one appears to be the least restrictive. When consumption of formal child care is observable for each couple, "topping-up" of child care provided in kind can be prevented, which in practice may appear difficult. But our analysis shows that when career paths are observable, topping up, is

not a problem anyway. High-career couples will then receive full time care (in kind or subject to a non linear subsidy) and they do not want to supplement this level by care paid at full market prices anyway. And due to the implicit or explicit subsidy, low-career couples consume already more formal care than they would at market prices.

From a practical perspective, the non linearity of the policy introduces a measure of means-testing into our policies because child-care fees effectively differ across income levels. Because of the information limitations, means-testing remains quite basic and couples within a given career path cannot be distinguished. Still even this basic screening device has a rather dramatic impact in reconciling redistribution and child-care policies (see also Sections 9 and 10 on this point). The child-care subsidy is according to the first-best Pigouvian rule. Unlike in the linear case, there is no need to set it at a lower level for redistributive reasons.

In Section 8, we examine the robustness of our results with respect to the specification of the gender norm. We study the case where the norm is determined by the social group of the mother. In other words, social comparisons defining the norm are restricted to the specific group a mother belongs to, rather than being based on the entire population. For example, career mothers may feel guilt if they provide less informal care than women they interact with on a daily basis in their neighborhood. This definition of the norm appears to be more realistic. It also raises new interesting issues because now policies have to address income redistribution both across and within social groups. We show that our main message continues to hold: with a linear policy the trade-off between efficiency and redistributive considerations persists whereas with a nonlinear policy the conflict basically disappears.

Finally, Section 9 examines how our results relate to real-world child policies and can provide guidance for policy design and reforms.

2 The model

Consider a population of couples with children, the size of which is normalized to one. Each couple consists of a mother ‘ f ’, a father ‘ m ’, and a given number of children. Couples choose their career-path, the mode of child care, and their consumption.⁴

There exist two types of career-paths (indexed by j). First, a full engaging high-career path, $j = h$, where individuals who take up this career path have to work an entire working day which we normalize to one. This constraint can be due to high peer pressure to work hard and to be fully committed, or to the obligation to spend the whole working day at the workplace—think

⁴In our model all individuals live in couples and all couples have the same number of children. They differ only in their socioeconomic background. This simplification implies that we neglect possible redistribution across families with a different number of children (or with grown up children) and between couples with children and single parents and/or singles without children.

for instance about a lawyer aiming to become a partner of the law firm.

Second, there is a less demanding low-career path, $j = \ell$, offering flexible working hours. Examples include most low qualified job but also some positions for college graduates like middle and high school teacher. The time not spent at work can be used for child care c_i , where $i = m, f$. Both jobs pay the wage rate y , but the high-career path comes with an earnings bonus q_i . We let $q_m \in [0, Q]$ and $q_f = \alpha q_m \in [0, \alpha Q]$, with $\alpha \in (0, 1]$. An $\alpha < 1$ captures pure discrimination: unequal pay for equally qualified workers, as it continues to be documented in nearly all developed countries.⁵ Observe that while $\alpha < 1$ adds a measure of realism to the descriptive part of our model, it will not be essential for our results that all continue to hold when $\alpha = 1$. In particular, as shown in Section 2.2 below, gender inequalities as measured by the GWG continue to exist even when $\alpha = 1$.

The bonus q_m is distributed according to the density function $f(\cdot)$, with the cumulative distribution being $F(\cdot)$. Potential bonuses are perfectly correlated in a couple. Consequently, there is a single level of q_f associated with each level of q_m .⁶

Care for children provided by the partner(s) is denoted by c_i ($i = m, f$), while that bought in the private market is denoted by c_p . The latter costs p per unit of time. We let $p = y$, meaning that the current salary of one member in the couple exactly covers the costs of buying full-time child care on the private market.⁷ The children must be taken care of for the entire working day, implying $c_m + c_f + c_p = 1$. Couples in which both parents choose the high-career path thus have to fully rely on private child care. When parents enter a flexible job their salary decreases proportionally to the time devoted to care. Informal and private care constitute a family public good and its value to the parents is given by:

$$G(c_m, c_f, c_p) = v(c_m + c_f) + \beta v(c_p),$$

where v satisfies the usual Inada conditions, including $v' > 0$ $v'' < 0$, $v(0) = 0$ and $v'(0) \rightarrow \infty$. Care provided by the father and mother are thus perfect substitutes while informal and private care are perceived by the parents as imperfect substitutes, with $0 < \beta \leq 1$. We thus rule out the case where $\beta > 1$, but allow $\beta = 1$, meaning that private care is (weakly) less welfare-enhancing

⁵The parameter α generates the unexplained component in the Oaxaca-Blinder decomposition of the GWG; see Blinder (1973) and Oaxaca (1973). Equation (4) below presents the decomposition of the GWG obtained in our model.

⁶Chiappori *et al.* (2017) find that the preference for partners of the same education has significantly increased, particularly for the highly educated, in the past decades in the US. Other authors document a considerable rise in educational assortative mating at the lowest education levels across Western nations; see for example Eika *et al.* (2014). We make the simplifying assumption that the positive correlation between the two spouses' socioeconomic status is *perfect*.

⁷This assumption is of no relevance to our results. Without it we would obtain a term proportional to $(p - y)$ in the first-order conditions with respect to child care. This would affect the equilibrium levels of child care but otherwise all other results are not affected.

than informal care; see our discussion in the Conclusion. Apart from child care, each parent derives utility from consumption of a numeraire commodity x .

Following Akerlof and Kranton (2000; 2010), individuals may suffer a disutility by deviating from the social categories that are associated with their identity (that is, an individual’s sense of self), which causes behavior to conform toward those norms. We assume that mothers try to conform to the behavior of their peers. They feel guilt if they provide less informal care than the average level provided by women in the society.⁸ “Mother’s guilt” is well documented in the psychology literature which points out that social norms on gender roles may cause mothers who work full-time to feel a sentiment of discomfort when delegating the care of their children to others; see, Guendouzi (2006), Rotkirch and Janhunen (2010) and Rose (2017), among others. The relevance of “mother’s guilt” in modern societies is (indirectly) documented by data from the World Value Survey and the International Social Survey Program about the persistence of gender roles in the family. As Kleven *et al.* (2019b, page 6) put it: “Two striking insights emerge: one is that gender attitudes are still quite traditional — essentially that women should work full-time before having children and after the children have left home, while they should work only part-time or not at all when they have children living at home—and the other is that different countries are very similar in holding this view.”⁹

Given our assumption on the flexibility associated with the two available career paths, the social norm for mothers corresponds to the utility loss associate with the full-time job and given by $\gamma(\max\{0; \bar{c}_f - c_f\})$, where \bar{c}_f is the average time spent with children by mothers in the society. The parameter $\gamma \in [0, 1]$ reflects the costs of norm deviations. In Section 8 we extend the model to that case where social comparisons defining the norm are restricted to the specific group a mother belongs to rather than being based on the entire women population. Mothers then suffer a disutility by deviating from the “restricted” social categories that are “strongly” associated with their identity. For example, they could refer to family members or to women they regularly interact with in their neighborhood. We show that our main results continue to hold under this alternative specification of the social norm.

⁸The model does not consider the possibility that a person’s identity might derive from his or her job (see Solow 1998). In other words, we disregard that the high career path can be, *per se*, a source of utility for the female population. This is in line with the evidence reported in the remainder of this paragraph which indicates that a negative attitude towards full-time working mothers is still pervasive in modern societies or that “job identity” is not equally spread in the male and female population.

⁹Studying child penalties, Kleven *et al.* (2019a and 2019b) report data on gender norms from the International Social Survey Programme (ISSP), waves 1988, 1994, 2002 and 2012, for six countries (Denmark, Sweden, Germany, Austria, United Kingdom and United States). They focus on the question: “Do you think that women should work outside the home full-time, part-time or not at all when there is a child under school age?” The share of respondents agreeing with the fact that women should work outside the home part-time or not at all when there is a child under school age is well above the 80% also in more egalitarian countries like Sweden and Denmark.

The timing of couples' decisions is as follows: first, parents choose their career path and then, in the second stage, they choose consumption and the amount of formal and informal child care. Parents act cooperatively and maximize the sum of their utilities:

$$W = x_f + x_m + G(c_f, c_m, c_p) - \gamma(\max\{0; \bar{c}_f - c_f\}). \quad (1)$$

Note that while we assume a unitary couple à la Becker, a collective couple as considered in an extensive literature following Chiappori (1988) would also choose an efficient solution and, for the issues we are dealing with, it would yield similar results. A collective model would be relevant to deal with problems like whether child support should be paid to mothers or to fathers. In our setting the two policies are equivalent whereas they are not in a collective model; see in particular Lundberg and Pollak (1993).¹⁰

2.1 Couple's optimization

We first analyze the choice of child-care activities for a given career path. Then, by proceeding backward, we consider the choice of career path made by the couple. This allows us to determine the average child care provided in the society and thus to define the cost of the social norm for mothers. We consider only decisions made at the second stage by the couples that turn out to be relevant for our analysis, namely the couples where (i) only the father enters the high-career path while the mother enters the flexible job market (traditional couples), and those where (ii) both parents take up the high-career path; see Appendix A.1 for the dominated couples' decisions.¹¹

Traditional couple. Denote welfare of this couple by $W_{h\ell}$, where the first subscript refers to the father's career choice and the second subscript refers to the mother's career choice. Since the father took up the high-career path he is not able to take care of the children, and $c_m^* = 0$. Noting that $c_f + c_p = 1$, the couple chooses formal care to maximize (1) where $x_{h\ell} = x_f + x_m = y + q$ because $p = y$.¹² The optimal level of formal child care is implicitly determined by

$$\beta v'(c_p^*) = v'(1 - c_p^*). \quad (2)$$

First-order condition (2) indicates that traditional mothers purchase formal care, c_p^* , in the market up to the point where marginal utility from formal care equals the marginal benefit from informal care, $1 - c_p^*$.

¹⁰Grossbard-Shechtman (1984) considers endogenous matching and it is not clear what the appropriate definition of efficiency would be. There is also some literature on the so-called non-cooperative couple (see for instance Meier and Rainer, 2015) but the mainstream approach appears to be based on cooperative solutions.

¹¹Only the mother in the high-career path is dominated by having both parents entering the high-career path which involves higher future benefits. Similarly, having both parents entering the low-career path can never be optimal since then the couple forgoes future benefits q_m .

¹²Spouses' labor income, net of formal child-care expenditures, is $x_{h\ell} = y + q + (1 - c_f)y - pc_p = y + q + c_p y - pc_p$.

The marginal norm cost for traditional mothers, γ , does not enter the FOC (2). To explain this, denote $c_{h\ell}^*$ and c_{hh} informal care provided by traditional parents and career parents, respectively. Traditional mothers do not suffer any norm cost because by definition we have $c_{hh} = 0$ so that $c_{h\ell}^* = 1 - c_p^* > \bar{c} > c_{hh}^* = 0$.

The indirect utility of this $h\ell$ -couple as a function of private child care c_p^* writes:

$$W_{h\ell}^* = y + q + v(1 - c_p^*) + \beta v(c_p^*)$$

High-career couple. High-career couples have no child-care decision to make; they have to buy the full amount of private care on the market. High-career mothers suffer the cost from deviating from the norm and the couple's welfare amounts to:

$$W_{hh}^* = y + q(1 + \alpha) + \beta v(1) - \gamma \bar{c}.$$

Note that high-career couples who exclusively have to rely on private child care are those with higher consumption levels, that is $x_{h\ell}^* = y + q < x_{hh}^* = y + q(1 + \alpha)$.

We are now in the position to analyze the couple's decision about the two partners' career paths. Families have to choose whether to be a high-career hh -couple fully relying of formal child care, or to be a traditional $h\ell$ -couple where the mother provides some informal care. A couple will become a high-career couple if it is beneficiary to do so, that is if $W_{hh}^* \geq W_{h\ell}^*$, or if

$$q \geq \hat{q}^* \equiv \frac{1}{\alpha} [v(1 - c_p^*) + \beta v(c_p^*) - \beta v(1) + \gamma \bar{c}].$$

The marginal couple \hat{q}^* is the couple where parents are indifferent between belonging to a traditional and to a career couple. Given \hat{q}^* we can now define average informal child care in society:

$$\bar{c} = \int_0^{\hat{q}^*} c_{h\ell}^* f(q) dq = F(\hat{q}^*) c_{h\ell}^* = F(\hat{q}^*) (1 - c_p^*).$$

Note that by assuming a quasi-linear welfare function we consider the least favorable scenario for our argument. Indeed, considering a concave $u(x_f + x_m)$ would imply that formal care expenditures are increasing in q in traditional families. This would exacerbate the regressive effect of child-care subsidies.¹³

2.2 Market outcome

An allocation is given by the identity of the marginal couple and by the amount of formal care purchased by traditional couples. We first characterize the *laissez-faire* allocation. We use this

¹³To see why one can derive $\frac{dc_p}{dq} = \frac{pu''(x_m + x_f)}{SOC}$, where:

$$SOC = pu''(2y + q - pc_p) + v''(1 - c_p) + \beta v''(c_p) < 0.$$

Hence formal child care would be strictly increasing in household labor income for $q \leq \hat{q}^*$.

terminology for conciseness even though it is effectively a “partial” *laissez faire* in the sense that it is the outcome absent of any of the policies considered in this paper—thus taking implicitly all other fiscal and regulatory policies as given. The following proposition characterizes this allocation.

Proposition 1 (Characterization of the *laissez faire*) *When mothers who do not provide child care suffer from deviating from the social norm, i.e. $\gamma > 0$, and/or the job market suffers from gender discrimination, $\alpha < 1$, then:*

(i) *it is never optimal for fathers to take up the low-career path;*

(ii) *the marginal couple is given by*

$$\hat{q}^* = \frac{1}{\alpha} [v(1 - c_p^*) + \beta [v(c_p^*) - v(1)] + \gamma F(\hat{q}^*)(1 - c_p^*)], \quad (3)$$

couples with high-career bonuses larger or equal to the threshold \hat{q}^ choose the high-career path for both parents;*

(iii) *private care purchased by traditional couples, c_p^* , satisfies equation (2).*

There are both traditional and career couples in the economy if $\hat{q}^* \in (0, Q)$.¹⁴ This is the most interesting case as it implies that the social norm persists as it is the case in most current societies, albeit to a different extent in different countries. We concentrate on this case, even though other outcomes are possible, depending on the parameters of the model and the distribution $F(q)$.¹⁵

From (3), an interior solution requires that \hat{q}^* exists such that $\hat{q}^* = (1/\alpha)[v(1 - c_p^*) + \beta [v(c_p^*) - v(1)] + \gamma F(\hat{q}^*)(1 - c_p^*)] < Q$. Due to the concavity of $v(\cdot)$, $v(1 - c_p^*) + \beta [v(c_p^*) - v(1)] > 0$ holds so that the previous inequality is always met provided that Q is sufficiently large and $F(\hat{q})$ is concave, which we assume in the remainder of the paper. This also ensures that the marginal couple \hat{q}^* is unique.

¹⁴Our model thus predicts that high-income mothers are employed in full-time jobs and purchase full-time formal child care. Recall however that our time unit corresponds to a full-time working day. Hence, this result does not imply that high-income mothers provide less informal care than low-income ones over the full day and including weekends. Indeed, a growing evidence based on Time Use Data indicates that better educated women, who typically have better paying jobs, both work more and spend more basic and especially quality time with their children; see, among others, Guryan *et al.* (2008) and, for a recent paper based on Italian data, Barigozzi *et al.* (2019).

¹⁵Corner solution at $\hat{q}^* = Q$ with only traditional couples or at $\hat{q}^* = 0$ with only career couples are possible. However, none of these cases appears to be empirically relevant.

The gender wage gap (GWG) is defined as the *difference in average income earned by mothers and fathers* in equilibrium and is given by:

$$\begin{aligned}
GWG &= \int_0^Q [y + q]f(q)dq - \left[F(\hat{q}^*)yc_p^* + \int_{\hat{q}^*}^Q [y + \alpha q]f(q)dq \right] \\
&= \underbrace{F(\hat{q}^*) (1 - c_p^*) y}_{\text{child penalty}} + \underbrace{\int_0^{\hat{q}^*} qf(q)dq}_{\text{adverse sorting}} + \underbrace{\int_{\hat{q}^*}^Q (1 - \alpha)qf(q)dq}_{\text{plain discrimination}} \tag{4}
\end{aligned}$$

The GWG decomposes in the gap between the hours worked because of family duties, and in the different return to labor supplied in sectors where man and women are employed. The first term in (4) thus represents “child penalty” (see Blau and Kahn, 2017; Kleven *et al.*, 2018): mothers in traditional couples do not work full time, but spend part of their time to provide informal child care. Child penalty thus depends on average informal care, $\bar{c} = F(\hat{q}^*) (1 - c_p^*)$, provided by traditional mothers. The second term accounts for the fact that women forego the extra earning opportunities associated with the high-career path. Interestingly, both child penalty and “adverse sorting” are affected by social norms and child-care decision through \hat{q}^* . They decrease when the share of career mothers in the society increases. The model thus offers a clean explanation of how social pressure determines women sorting and thus their low participation in leading positions together with lower wages. Finally, the last term in (4) captures the unexplained component of the GWG of the Oaxaca–Blinder decomposition, or the plain discrimination part; it vanishes when $\alpha = 1$.

Before turning to the design of child-care policies, we define the social planner’s objective function and the optimal allocation.

3 The optimal allocation

The social planner is interested both in efficiency and in redistribution. Specifically, the social welfare function is assumed to be a concave transformation, $\Psi(\cdot)$, of the families’ welfare functions in order to capture inter-family inequality aversion.¹⁶ Thus, a first-best (*fb*) allocation is defined by aggregate consumption levels $x_{hl}^{fb}(q)$ and $x_{hh}^{fb}(q)$, by the indifferent couple, \hat{q}^{fb} (which determines the share of female participation in the high-career path), and by the level of formal child care chosen by traditional couples, $c_p^{fb}(q)$ for $q < \hat{q}^{fb}$ (recall that, by definition, $c_p^{fb}(q) = 1$ for $q \geq \hat{q}^{fb}$).

Specifically, the social planner chooses $\{x_{hh}(q), x_{hl}(q), c_p(q), \hat{q}\}$ to maximize the following

¹⁶In Barigozzi *et al.* (2018), redistribution across income levels is not relevant because they use a straight utilitarian approach without applying a concave transformation to couples’ utilities.

welfare function:

$$\begin{aligned}
SW &= \int_0^{\hat{q}} \Psi(x_{hl}(q) + v(1 - c_p(q)) + \beta v(c_p(q))) f(q) dq \\
&\quad + \int_{\hat{q}}^Q \Psi(x_{hh}(q) + \beta v(1) - \gamma \bar{c}) f(q) dq
\end{aligned} \tag{5}$$

subject to the budget constraint:

$$y + \int_0^Q q f(q) dq + \int_{\hat{q}}^Q \alpha q f(q) dq = \int_0^{\hat{q}} x_{hl}(q) f(q) dq + \int_{\hat{q}}^Q x_{hh}(q) f(q) dq, \tag{6}$$

where $\bar{c} = \int_0^{\hat{q}} (1 - c_p(q)) f(q) dq$.

In Appendix A.2 we derive the optimal allocation that is characterized as follows. Welfare is constant irrespective of the couple's career path and their high-career bonuses:

$$W_{hl}^{fb}(q) = W_{hh}^{fb}(q) = W^{fb} \quad \forall q;$$

Formal child care is such that $c_p^{fb}(q) = c_p^{fb} \quad \forall q$ and is implicitly given by:

$$\beta v'(c_p^{fb}) + [1 - F(\hat{q}^{fb})] \gamma = v'(1 - c_p^{fb}). \tag{7}$$

The left-hand side denotes the social marginal benefit of formal child care while the right-hand side denotes the social marginal cost of informal care. Note that the above equation is independent of a traditional couple's q . Compared to the *laissez faire* described in (2), the marginal benefit contains an additional term $[1 - F(\hat{q}^{fb})] \gamma$ which reflects the negative externality of informal care provision on type- hh couples whose share is $1 - F(\hat{q}^{fb})$. Informal child care is thus inefficiently high in the *laissez faire*, which translates in underconsumption of formal care: $c_p^* < c_p^{fb}$. Not surprisingly c_p^{fb} and \hat{q}^{fb} do not depend on the social welfare function Ψ . This is due to the quasi-linearity of preferences. All Pareto-efficient allocations imply the same levels of c_p and \hat{q} , but *may* differ in consumption levels. But since we use a symmetric social welfare function any concave Ψ implies that in the first-best utility levels are equalized. However, the degree of concavity will matter in the second-best settings considered below.

Interestingly, $W_{hl}^{fb}(q) = W_{hh}^{fb}(q)$ and $c_p^{fb}(q) = c_p^{fb} \quad \forall q$ imply that the consumption of couples is constant in each career-path: $x_{hl}^{fb}(q) = x_{hl}^{fb}$ and $x_{hh}^{fb}(q) = x_{hh}^{fb} \quad \forall q$. This in turn implies that:

$$x_{hh}^{fb} - x_{hl}^{fb} = v(1 - c_p^{fb}) + \beta[v(c_p^{fb}) - v(1)] + \gamma F(\hat{q}^{fb})(1 - c_p^{fb}) > 0 \tag{8}$$

The above expression shows that high-career couples do not get higher consumption because of their higher q (as it was the case in the *laissez faire*), but because the government compensates them for their utility loss due to the cost of the social norm and to the purchase of full private

care (whose utility is mitigated by the parameter β). Finally, in Appendix A.2 we show that the FOC with respect to \hat{q} can be rewritten as:

$$\alpha \hat{q}^{fb} f(\hat{q}^{fb}) = f(\hat{q}^{fb})[v(1 - c_p^{fb}) + \beta(v(c_p^{fb}) - v(1)) + \gamma F(\hat{q}^{fb})(1 - c_p^{fb})] - \gamma[1 - F(\hat{q}^{fb})](1 - c_p^{fb})f(\hat{q}^{fb}) \quad (9)$$

so that

$$\hat{q}^{fb} \equiv \frac{1}{\alpha} \{ [v(1 - c_p^{fb}) + \beta(v(c_p^{fb}) - v(1))] + \gamma F(\hat{q}^{fb})(1 - c_p^{fb}) - \gamma[1 - F(\hat{q}^{fb})](1 - c_p^{fb}) \} \quad (10)$$

Comparing (3) and (10) and recalling that $c_p^* < c_p^{fb}$, we observe that $\hat{q}^* > \hat{q}^{fb}$, that is the share of high-career couples is inefficiently low in the *laissez faire*.

Expression (9) has a simple interpretation in terms of cost and benefits of *decreasing* \hat{q} (that is moving $f(\hat{q})$ couples from traditional to high-career). The LHS measures the marginal benefits arising from the high-career bonus. In the RHS, the first two terms in brackets represent the net lost utility from formal care and the norm cost, respectively. The last term is the Pigouvian term which is negative because the externality imposed on all high-career couples decreases because the average informal care falls. Formally, we have $\partial \bar{c} / \partial \hat{q} = (1 - c_p)f(\hat{q})$. Since a negative cost is effectively a benefit this term could have been moved to the LHS, but since the interpretation of (9) also shows that of (10) this presentation is more telling.¹⁷

Observe that \hat{q}^{fb} does not depend on Ψ ; it is the same in *all* Pareto efficient allocations. The first-best level \hat{q}^{fb} is set purely on efficiency grounds—to maximize the size of the cake which is then redistributed according to social preferences (which in our case involves equalization of utilities).

The following propositions characterizes the optimal allocation:

Proposition 2 (The optimal allocation) *The optimal allocation $\{x_{hh}^{fb}, x_{hl}^{fb}, c_p^{fb}, \hat{q}^{fb}\}$ maximizes the social welfare function (5) subject to the budget constraint (6) and is characterized as follows:*

- (i) *Couples' welfare does not depend on the career choice of the mother nor on the career bonus: $W_{hl}^{fb}(q) = W_{hh}^{fb}(q) \forall q$. High-career couples are compensated for their utility loss due to full private care and due to the cost of the social norm.*
- (ii) *Formal child care $c_p^{fb}(q) = c_p^{fb}$ is the same for all traditional couples and satisfies (7). It is chosen such that the negative externality induced by the social norm is fully internalized.*
- (iii) *The share of high-career couples is given by $1 - F(\hat{q}^{fb})$ where the marginal couple \hat{q}^{fb} is defined in (10).*

¹⁷Similarly, multiplying both sides of (9) by -1 , would be more in line with the original FOC, because it then measures the cost and benefits (reversed from the interpretation discussed) of increasing \hat{q} .

(iv) The optimal level of the GWG entails a child penalty and a sorting differential equivalent to $F(\hat{q}^{fb}) (1 - c_p^{fb}) y$ and $\int_0^{\hat{q}^{fb}} qf(q) dq$, respectively.

Point (iv) directly follows from substituting (c_p^{fb}, \hat{q}^{fb}) into equation (4).

3.1 Welfare analysis of the *laissez-faire* allocation

By comparing the optimal allocation and the market outcome we can establish in which sense the *laissez-faire* allocation is inefficient.

Proposition 3 (Welfare analysis of the *laissez faire*) *In the laissez-faire allocation:*

- (i) *Within each career path, welfare differs across couples; it increases with career prospect q .*
- (ii) *Formal child care, c_p^* , is inefficiently low and informal care, c_{hl}^* , is too high. This is due to the negative externality that informal care exerts on high-career mothers through the social norm.*
- (iii) *Female participation in the high-career path is inefficiently low, $\hat{q}^{fb} < \hat{q}^*$.*
- (iv) *In the GWG, both the child penalty and adverse sorting are inefficiently high.*

In the first best all couples receive the same welfare. Proposition 3(i) shows that, in the *laissez faire*, welfare is increasing in q both among traditional couples and among career couples. Thus, welfare is equalized neither across couples belonging to different career paths nor across couples within the same career path.

Point (ii) shows that the negative externality translates into under-consumption of formal child care by traditional couples in *laissez faire* ($c_p^* < c_p^{fb}$). Point (iii) concerns the share of women entering the high-career path which is inefficiently low in *laissez faire*. When the negative externality is internalized, formal child care increases and the cost of the social norm falls. As a result the high-career path is more attractive in first best, or $\hat{q}^* > \hat{q}^{fb}$.

Finally, point (iv) requires some explanations. For any given q , in the *laissez faire*, the female spouse's earnings are less than or equal to her first-best earnings. Indeed, child penalty is lower in the first best because women's labor income is higher due to the higher formal child care ($c_p^* < c_p^{fb}$). The optimal level of child penalty is thus obtained when the negative externality exerted by traditional mothers on career mothers is properly taken into account. This clarifies why, in the model, efficiency is reached via the appropriate reduction of child care related gender inequalities. Finally, adverse sorting is lower because more women enter the high-career path and benefit from the high-career bonus ($\hat{q}^* > \hat{q}^{fb}$).

Note that we follow the tradition of the optimal tax literature assuming that wages (which here include the q 's) are given because production technologies are linear. Consequently, accommodating the extra career-mothers ($F(\hat{q}^*) - F(\hat{q}^{fb})$) does not create a disequilibrium on the demand side of the labor market. This is of course a simplification. In reality a significant variation in the proportion of high-career couples would bring about a change in wages, which in turn would mitigate the increase in the share of high-career women. When this is accounted for the first-best share of high-career couples would be smaller but all the effects we describe would continue to be present.

4 Decentralizing the first-best allocation

Decentralization of the first-best solution requires a subsidy s on formal child care and individualized lump-sum taxes or transfers $T_{h\ell}(q)$ and $T_{hh}(q)$. When a subsidy s is in place, the net price of private child care is $p^n = p - s = y - s$, and a traditional couple's optimal child-care decision solves:

$$v'(1 - c_p) - s = \beta v'(c_p). \quad (11)$$

Comparing (11) with (7) shows that a subsidy of

$$s^{fb} = [1 - F(\hat{q}^{fb})]\gamma \quad (12)$$

implements the first-best level of child care. Since formal and informal care sum up to one, a subsidy on market care is effectively a tax on informal care. According to equation (12) s^{fb} corresponds to a Pigouvian *tax* on informal child care; it equals the marginal social cost of the externality informal care imposes on high-career couples.

The lump-sum transfers $T_{h\ell}(q)$ and $T_{hh}(q)$ must be chosen such that welfare levels between all couples are equalized, that is

$$\begin{aligned} W_{h\ell}(q) &= y + q + s^{fb}c_p^{fb} + v(1 - c_p^{fb}) + \beta v(c_p^{fb}) + T_{h\ell}(q) = W^{fb} \quad \text{when } q \leq \hat{q}^{fb}, \\ W_{hh}(q) &= y + (1 + \alpha)q + s^{fb} + \beta v(1) - \gamma\bar{c} + T_{hh}(q) = W^{fb} \quad \text{when } q \geq \hat{q}^{fb}. \end{aligned}$$

Decentralizing \hat{q}^{fb} further requires $T_{h\ell}(\hat{q}^{fb}) = T_{hh}(\hat{q}^{fb})$. To see this note that when $T_{h\ell}(\hat{q}) = T_{hh}(\hat{q})$ the marginal couple defined by $W_{h\ell}(\hat{q}) = W_{hh}(\hat{q})$ is determined by

$$\begin{aligned} &y + \hat{q} + s^{fb}c_p^{fb} + v(1 - c_p^{fb}) + \beta v(c_p^{fb}) \\ &= y + (1 + \alpha)\hat{q} + s^{fb} + \beta v(1) - \gamma\bar{c} \\ \Leftrightarrow \quad \hat{q} &= \frac{1}{\alpha}[v(1 - c_p^{fb}) + \beta(v(c_p^{fb}) - v(1))] + \gamma\bar{c} - s^{fb}(1 - c_p^{fb}) \end{aligned} \quad (13)$$

Using (12) together with $\gamma\bar{c} = \gamma F(\hat{q})(1 - c_p^{fb})$ shows that (13) and (10) coincide once formal child care is subsidized at the Pigouvian rate.

Hence, with sufficiently powerful instruments efficiency and redistribution can be addressed separately: the Pigouvian subsidy s^{fb} on private child care optimally reduces informal child-care provision (and thus child penalties) while the transfers $T_{hl}(q)$ and $T_{hh}(q)$ assure equal welfare to all couples. Note that the individualized transfers redistribute from high to low q couples but also compensate the high-career couples for their utility losses due to full private care and to their cost of the social norm.

Before turning to second-best policies we present a simple numerical example which illustrates the *laissez-faire* and first-best solutions.

5 Numerical illustration

The previous sections have shown that the marginal couple trades off the high-career bonus against the norm cost (and the decrease from child-care utility). An interesting question is then how large the norm cost has to be in order to generate a sizeable impact on the child-care policy? One can expect that the reply relies on the comparison between γ and q and some measure of its distribution like the average. The following example confirms this intuition.

Our model involves a number of normalizations so that absolute levels of γ , q and for that matter s are not very telling. The underlying specification and parameter values are explained in Appendix A.4. We consider levels of γ ranging from 0 to 0.9 while q is uniformly distributed over $[0, 1]$. When $\gamma = 0.5$, it is equal to the average q while, for $\gamma = 0.9$, it represents 90% or the top bonus. As explained in the Appendix, we interpreted \hat{q} as the share of employed women who work part-time and build the example in order to obtain empirically reasonable shares of low-career women: according to Eurostat, the share of women working part-time in the European countries is in the range [2%, 60%] with an average of 31.5%. Based on the *laissez-faire* equilibrium one can think about the high range of γ 's as Greece or Italy, while the low range represents Nordic countries, with France in the middle. Table 1 reports for each of the considered γ 's the marginal couple in the *laissez faire* and in the first best. The difference between these two levels is a possible measure of the significance of γ and not surprisingly this difference increases with γ . When γ is equal to the average level of q , the optimal policy involves a decrease in the share of traditional couples of about 15%.

Turning to s , the absolute value reported (which is a per unit subsidy) is not in itself informative. However, one can relate it to the q and more interestingly to the level of $y = p$ which, as explained in the Appendix, is set at 1/2 in our example. Consequently, $s = 0.45$ corresponds to a subsidy rate of 95% while $s = 0.3$ corresponds to a 60% rate; these levels are reported in the last column of the table.

The example does manage to replicate “reasonable” shares of traditional mothers which reflect equilibrium levels roughly in line with those observed in a range of countries; see Appendix

γ	LF: \hat{q}^*	FB: \hat{q}^{fb}	s	s/p
0.9	0.667	0.5	0.45	0.9
0.8	0.6	0.468	0.425	0.85
0.7	0.545	0.438	0.393	0.79
0.6	0.5	0.413	0.352	0.7
0.5	0.461	0.391	0.305	0.61
0.4	0.429	0.373	0.251	0.5
0.3	0.4	0.358	0.193	0.39
0.2	0.375	0.346	0.131	0.26
0.1	0.352	0.338	0.06	0.12
0	0.333	0.333	0	0

Table 1: Numerical illustration with $v(c) = -0.6(1-c)^2$, $\beta = 1$, $\alpha = 0.9$, $Q = 1$, $y = p = 0.5$ and with a uniform distribution of q . We report the marginal couple at the *laissez-faire* (LF), first-best (FB) and the implementing subsidy and subsidy rate for a range of norm costs $\gamma \in [0, 1]$.

A.4 for more details. The specific definition of the “sizeable magnitude” is of course subject to debate but the table suggests that at least in countries with relatively large norm cost the distortion brought about by the norm cost is not trivial and calls for a rather significant subsidy on child care to achieve a more efficient balance of women’s career choices.

We now turn to the second-best policies.

6 Linear policy

First, we consider a simple policy under which instruments are restricted in an *ad hoc* way. In other words, we remain agnostic about the information structure. We assume that the instruments necessary to implement the first best are not available (specifically the individualized transfers) and consider a simple linear policy which represents a widely used benchmark in the public economics literature.

The considered policy consists of a uniform (linear) subsidy s on market child care, financed by a uniform lump-sum tax τ . The government’s budget constraint is then given by

$$\tau = sF(\hat{q}(p^n))c_p(p^n) + s[1 - F(\hat{q}(p^n))]. \quad (14)$$

Recall that $p^n = p - s = y - s$ is the net, after subsidy, price of market care. Let us denote $c_p^s = c_p(p^n)$ consumption of formal care under the linear subsidy s . As before it is implicitly determined by:

$$v'(1 - c_p^s) - s = \beta v'(c_p^s) \quad (15)$$

The social welfare function can be written as:

$$\begin{aligned}
SW(s, \tau) &= \int_0^{\hat{q}(p^n)} \Psi(y + q + sc_p(p^n) - \tau + v(1 - c_p(p^n)) + \beta v(c_p(p^n))) f(q) dq \\
&\quad + \int_{\hat{q}(p^n)}^Q \Psi(y + (1 + \alpha)q + s - \tau + \beta v(1 - \gamma \bar{c}(p^n))) f(q) dq,
\end{aligned} \tag{16}$$

where $\hat{q}^s = \hat{q}(p^n)$ and $\bar{c}(p^n) = F(\hat{q}^s)(1 - c_p(p^n))$. The FOC w.r.t. τ is given by:

$$\lambda = \int_0^Q \Psi'(q) f(q) dq \equiv E[\Psi'], \tag{17}$$

where λ is the Lagrangian multiplier of the budget constraint, E is the expectation operator and $\Psi(q)$ is defined as $\Psi(W_{h\ell}(q))$ for $h\ell$ couples and as $\Psi(W_{hh}(q))$ for hh couples. This equation has a familiar flavor from linear taxation models, in particular Sheshinski (1972). It states that the social marginal cost of raising an additional dollar, λ , should be equal to its social marginal benefit, $E[\Psi']$. Now define:

$$E_{h\ell}[\Psi'] \equiv \frac{\int_0^{\hat{q}^s} \Psi'(q) f(q) dq}{F(\hat{q}^*)} \quad \text{and} \quad E_{hh}[\Psi'] \equiv \frac{\int_{\hat{q}^s}^Q \Psi'(q) f(q) dq}{1 - F(\hat{q}^*)}, \tag{18}$$

which represent the average marginal utilities of income by traditional and high-career couples respectively.

Considering that $\partial p_n / \partial s = -1$, the FOC with respect to s can be written as:

$$\begin{aligned}
&F(\hat{q}^s) E_{h\ell}[\Psi'] c_p^s + (1 - F(\hat{q}^s)) E_{hh}[\Psi'] \left[1 - \gamma F(\hat{q}^s) \frac{dc_p^s}{dp^n} + \gamma(1 - c_p^s) f(\hat{q}^s) \frac{d\hat{q}^s}{dp^n} \right] \\
&- \lambda \left[F(\hat{q}^s) c_p^s - s F(\hat{q}^s) \frac{dc_p^s}{dp^n} + s(1 - c_p^s) f(\hat{q}^s) \frac{d\hat{q}^s}{dp^n} + 1 - F(\hat{q}^s) \right] = 0.
\end{aligned} \tag{19}$$

Noting that $E[c_p^s] = F(\hat{q}^s) c_p^s + 1 - F(\hat{q}^s)$ we show in Appendix A.5 that the optimal linear subsidy on formal child care, s^o , amounts to:

$$s^o = \gamma \frac{(1 - F(\hat{q}^s)) E_{hh}[\Psi']}{E[\Psi']} - \frac{\text{cov}[\Psi', c_p^s]}{E[\Psi'] \frac{\partial E[c_p^s]}{\partial p^n}} \tag{20}$$

The first expression is the Pigouvian term and the second term is the redistributive term. When $\Psi'' = 0$ so that social welfare is not concave and there is no concern for redistribution and the above expression reduces to $s^o = [1 - F(\hat{q}^s)]\gamma$, which is the first-best Pigouvian rule. From expression (13) this also yields $\hat{q} = \hat{q}^s$ so that we return to the first-best allocation. When the social welfare function is concave, we have $\text{cov}[\Psi', c_p^s] < 0$ since families with higher formal care have a higher welfare. In the Appendix we show that $\partial E[c_p^s] / \partial p^n < 0$ so that the second term on the RHS in expression (20) is negative (a positive fraction is preceded by a negative sign). Redistributive concerns thus decrease optimal child-care subsidies since it is mainly the high-career couples who profit from such subsidies. Furthermore, we have $E_{hh}[\Psi'] < E[\Psi']$

so that the Pigouvian term is also reduced compared to its first-best counterpart. This is because the externality affects high-career couples who, in the second best, have a lower social marginal utility. The marginal social damage of the externality is determined by converting their (marginal) utility into social (marginal) utility, which is achieved by the term $E_{hh}[\Psi']/E[\Psi']$.¹⁸ Consequently, we have $s^o < s^{fb}$; see Appendix A.5 for the formal proof.

Proposition 4 (Linear child care subsidy) *The optimal linear policy when redistribution is relevant ($\Psi'' > 0$) implies:*

- (i) $s^o < s^{fb}$ because it is mainly the high-career couples who profit from this policy. Thus, formal child care purchased by traditional couples, c_p^s , is inefficiently low ($c_p^{fb} > c_p^s$);
- (ii) and $\hat{q}^s > \hat{q}^{fb}$ so that there are more traditional couples in the second best than in the first best. The marginal couple is distorted upwards to reduce the share of high-career couples receiving the subsidy for full-time formal care which improves redistribution.
- (iii) In the GWG, both child penalties and adverse sorting are inefficiently high.

The intuition for (iii) is the same as for the corresponding point in Proposition 3. As expected, the linear subsidy mitigates the inefficiency of the *laissez-faire* informal care provision but does not fully restore efficiency. However, welfare is obviously higher with the linear policy than in the *laissez faire*.

7 Nonlinear policy

Now, we take a different approach and assume that the available policies are not restricted in an *ad hoc* way. Instead, we study the design of the best policy that is available *given the information structure*. This is not just a matter of theoretical interest. The important underlying practical question is whether the distortions characterized in the previous section are unavoidable once redistribution under asymmetric information is involved, or whether they are simply artifacts of the linearity of the considered policy.

Under full information this approach yields the first best, but this supposes that all relevant variables, including a couple's high-career earning opportunities q are publicly observable. We shall now assume that q is not publicly observable but that both the career path and the level of market care *are* observable at the individual (couple's) level. The government can then offer two contracts conditioned on the *reported* type \tilde{q} denoted by $\{J(\tilde{q}), c_p^g(\tilde{q}), T(\tilde{q})\}$, where $J \in \{hl, hh\}$ indicates the career path, T is the transfer that households have to pay and $c_p^g(\tilde{q})$ is the amount of formal child care provided by the government. Since $c_p^g(\tilde{q})$ is observable at the

¹⁸In the FB, utilities are equalized so that this term is equal to one.

couple's level, the distinction between in-kind provision and a nonlinear taxation of market care is not relevant; see Cremer and Gahvari (1997). To be more precise, this is simply a matter of practical implementation of the underlying optimal contract. This implies, in particular, that when $c_p^g(\tilde{q})$ is interpreted as in-kind provision, topping up is not possible.¹⁹ As usual we shall, without loss of generality, concentrate on incentive compatible contracts.

Given that no topping up is possible it must be $c_p^g(q) = 1$ for all hh couples. In addition, given that, conditional on the career path, all families have the same preferences for child care, it is impossible to separate families according to q once the career path has been assigned. Hence, the government offers only two contracts: $\{T_{hl}, c_p^g\}$ for hl -couples and $\{T_{hh}, 1\}$ for hh -couples. In other words, all traditional couples consume the same level of market care and face the same tax or transfer. The same is true for all high-career couples.²⁰

The average informal care provided by traditional mothers now is $\bar{c} = F(\hat{q}^g)(1 - c_p^g)$, where \hat{q}^g denotes the marginal couple, whose welfare is the same in the two career paths, $W_{hh}(\hat{q}^g) = W_{hl}(\hat{q}^g)$.

The government maximizes the following welfare function:

$$\begin{aligned} \max_{T_{hl}, c_p^g, T_{hh}, \hat{q}^g} SW = & \int_0^{\hat{q}^g} \underbrace{\Psi(y + q + c_p^g y - T_{hl} + v(1 - c_p^g) + \beta v(c_p^g))}_{W_{hl}} f(q) dq \\ & + \int_{\hat{q}^g}^Q \underbrace{\Psi(2y + (1 + \alpha)q - T_{hh} + \beta v(1) - \gamma F(\hat{q}^g)(1 - c_p^g))}_{W_{hh}} f(q) dq \end{aligned} \quad (21)$$

subject to the budget constraint

$$F(\hat{q}^g)T_{hl} + [1 - F(\hat{q}^g)]T_{hh} - p[F(\hat{q}^g)c_p^g + 1 - F(\hat{q}^g)] \geq 0, \quad (22)$$

and subject to the following incentive constraint:

$$\begin{aligned} & 2y + (1 + \alpha)\hat{q}^g - T_{hh} + \beta v(1) - \gamma F(\hat{q}^g)(1 - c_p^g) \\ & - (y + \hat{q}^g + c_p^g y - T_{hl} + v(1 - c_p^g) + \beta v(c_p^g)) = 0. \end{aligned} \quad (23)$$

Since there is pooling in both groups, incentive compatibility requires simply that \hat{q}^g is indifferent between the two career paths. This follows because $\partial W_{hh}(q)/\partial q = 1 + \alpha > \partial W_{hl}(q)/\partial q = 1$ so that W_{hh} increases faster in q than W_{hl} . Consequently, condition (23) ensures that no high-career couple with $q \geq \hat{q}^g$ should have an incentive to mimic a traditional couple, that is $W_{hh}(q) \geq W_{hl}(q) \forall q \in [\hat{q}^g, Q]$. Similarly, it implies that no traditional couple wants to mimic a high-career couple.

¹⁹With the considered information structure it can be prevented and nothing can be gained by allowing it.

²⁰This is a well known property in contract theory and we skip the proof. To establish the results formally one has to maximize social welfare subject to the budget and incentive constraints. A simple first-order approach will show that the solution involves pooling within each career group.

We denote the Lagrangian multipliers associated with the budget constraint and the incentive constraint $\widehat{\lambda}$ and μ respectively. Using the expectation operators defined in (18) we can write the FOCs with respect to the transfers $T_{h\ell}$ and T_{hh} as:

$$- E_{h\ell}[\Psi']F(\widehat{q}^g) + \mu + \widehat{\lambda}F(\widehat{q}^g) = 0 \quad (24)$$

$$- E_{hh}[\Psi'][1 - F(\widehat{q}^g)] - \mu + \widehat{\lambda}[1 - F(\widehat{q}^g)] = 0 \quad (25)$$

Combining (24) and (25) and rearranging yields:

$$\widehat{\lambda} = \int_0^{\widehat{q}^g} \Psi'(\cdot) f(q) dq + \int_{\widehat{q}^g}^Q \Psi'(\cdot) f(q) dq = E[\Psi'] . \quad (26)$$

This equation simply states that the marginal cost of raising additional revenue, $\widehat{\lambda}$, must be equal to its marginal social benefit, $E[\Psi']$. The FOC with respect to formal child care for traditional couples, c_p^g , is given by:

$$\begin{aligned} & \int_0^{\widehat{q}^g} \Psi'(\cdot) [y - v'(1 - c_p^g) + \beta v'(c_p^g)] f(q) dq + \int_{\widehat{q}^g}^Q \Psi'(\cdot) \gamma F(\widehat{q}^g) f(q) dq \\ & - \widehat{\lambda} p F(\widehat{q}^g) + \mu [\gamma F(\widehat{q}^g) - y + v'(1 - c_p^g) - \beta v'(c_p^g)] = 0 \end{aligned} \quad (27)$$

In Appendix A.6 we show that by using (25) and (26) the (27) reduces to:

$$v'(1 - c_p^g) + \beta v(c_p^g) = [1 - F(\widehat{q}^g)]\gamma. \quad (28)$$

Comparing this expression to (11) shows that the level of child care c_p^g can be decentralized by a subsidy on market care given by:

$$s^g = [1 - F(\widehat{q}^g)]\gamma. \quad (29)$$

Consequently, the public provision of c_p^g corresponds to an implicit subsidy on market care which is set according to the Pigouvian *rule* defined by (12). In other words, it reflects the marginal social damage which is here measured by the extra norm cost imposed on all career couples. This is an interesting result because it implies that the downward distortion on s implied by the redistributive bias obtained in the previous section indeed appears to be an artifact of the *ad hoc* restrictions imposed on the policy, namely its simple linear specification. When the policy is constrained only by the information structure this distortion vanishes. Intuitively, with the nonlinear subsidy a distortion in child care does not relax the incentive constraint and there is no reason to deviate from the Pigouvian rule. This simple intuition also explains why this result is very robust and does not depend on the specification of the norm cost; see Appendix A.10 for more details.

However, while s^g is set according to the first-best Pigouvian *rule*, its actual *level* will differ from s^{fb} , unless $\widehat{q}^g = \widehat{q}^{fb}$. This brings us to the next question namely the comparison between \widehat{q}^g

and \hat{q}^{fb} . This amounts to studying whether the solution under asymmetric information involves a distortion on the marginal couple and if yes in which direction.

The FOC with respect to \hat{q}^g can be written as:

$$\begin{aligned} & \Psi(W_{hl}(\hat{q}^g)) - \Psi(W_{hh}(\hat{q}^g)) - \gamma f(\hat{q}^g)(1 - c_p^g)(1 - F(\hat{q}^g))E_{hh}[\Psi'] \\ & + \hat{\lambda} [f(\hat{q}^g)(T_{hl} - T_{hh}) + pf(\hat{q}^g)(1 - c_p^g)] + \mu [\alpha - \gamma f(\hat{q}^g)(1 - c_p^g)] = 0, \end{aligned} \quad (30)$$

where the first two terms vanish because of the incentive constraint.

The approach is to evaluate the FOC for \hat{q}^g at \hat{q}^{fb} while adjusting all the other endogenous variables according to their respective FOCs.²¹ When $\hat{q}^g = \hat{q}^{fb}$ we have from (28) that $c_p^g = c_p^{fb}$. In Appendix A.7 we show that

$$T_{hl} - T_{hh} = \gamma[1 - F(\hat{q}^{fb})](1 - c_p^g) - y(1 - c_p^g). \quad (31)$$

Solving (25) for μ and inserting (31) in (30), we have:

$$\begin{aligned} \frac{\partial \mathcal{L}}{\partial \hat{q}^g} \Big|_{\hat{q}^g = \hat{q}^{fb}} &= -E_{hh}[\Psi'](1 - F(\hat{q}^g))\gamma f(\hat{q}^{fb})(1 - c_p^g) \\ &+ E[\Psi'] \left[f(\hat{q}^{fb})(-y(1 - c_p^g) + \gamma(1 - F(\hat{q}^{fb}))(1 - c_p^g)) + f(\hat{q}^{fb})y(1 - c_p^g) \right] \\ &+ [-E_{hh}[\Psi'](1 - F(\hat{q}^g)) + E[\Psi'](1 - F(\hat{q}^{fb}))][\alpha - \gamma f(\hat{q}^{fb})(1 - c_p^g)] \\ &= (1 - F(\hat{q}^{fb}))(E[\Psi'] - E_{hh}[\Psi'])\alpha > 0. \end{aligned} \quad (32)$$

So that we have $\hat{q}^g > \hat{q}^{fb}$. In words, the second-best solution implies an upward distortion of the marginal couple \hat{q}^g . Consequently, there are more traditional couples in the second-best solution than in the first-best one.

To understand this expression note that a couple with $q \geq \hat{q}$ enjoys an informational rent of $\alpha(q - \hat{q}) = W_{hh}(q) - W_{hh}(\hat{q})$. Total rents are thus given by:

$$R = \int_{\hat{q}}^Q \alpha(q - \hat{q})f(q)dq$$

and we have:²²

$$\frac{\partial R}{\partial \hat{q}} = -\alpha \int_{\hat{q}}^Q f(q)dq = -\alpha[1 - F(\hat{q})].$$

Under full information these rents can be extracted and redistributed. Under asymmetric information they cannot because of the incentive constraint. As \hat{q} increases the extra amount

²¹If the other variables were held constant the sign of the derivative would be inconclusive. However, adjusting all the other variables in an optimal way reduces the problem to a single dimension so that the derivative is informative. As an example, consider the maximization of $f(x, y)$ and denote the solution (x^*, y^*) . Showing that at any given point (x, y) , $\partial f/\partial x > 0$ is not enough to prove that $x > x^*$. However, by using the FOC for y we reduce the problem to the maximization of $f(x, y^*(x))$ and the derivative of this expression allows us to compare x and x^* , as long as the problem is concave which we have to assume anyway.

²²Note that the derivative wrt the lower bound is zero.

$\alpha[1 - F(\hat{q})]$ can be extracted and redistributed which implies a social benefit of $(E[\Psi'] - E_{hh}[\Psi'])\alpha(1 - F(\hat{q}^{fb}))$. In words, the second-best solution involves an upward distortion in the marginal couple in order to reduce “informational rents” of the high-career couples. This means that by increasing the level of q of the marginal couple more tax revenue can be extracted from the high-career couple and redistributed to the traditional couples with lower income, so that welfare increases.

We can now also return to the *levels* of the implicit subsidy implied by the policy. Equation (12) and (29) together with $\hat{q}^g > \hat{q}^{fb}$ imply $s^g < s^{fb}$, so that asymmetric information leads to a lower implicit subsidy on formal care. Intuitively, the strict Pigouvian rule applies in both cases but with $\hat{q}^g > \hat{q}^{fb}$ the group of high-career couples affected by the externality is smaller so that its marginal social damage is also smaller. Consequently, using (11) we'll also have $c_p^g < c_p^{fb}$. As in the linear case all these results emerge as long as $\Psi'' < 0$ so that social welfare is concave and there is a concern for redistribution. When $\Psi'' = 0$ we return to the first-best solution.

To sum up, while the nonlinear policy brings us back to the first-best Pigouvian rule for the marginal subsidy, it continues to imply a downward distortion on formal care and there will be more traditional couples than efficient. Consequently, the potential conflict between child-care provision and redistribution does not completely disappear with nonlinear instruments but it is significantly mitigated.

Finally, let us revisit the underlying information structure. We have assumed for simplicity that a couple's formal care and career path are observable. We have made this assumption for the ease of exposition, but the arguments and results we presented make clear that the observability of the career path is effectively not necessary. The policy we characterize here can be implemented as long as a couple's level of formal care is observable. This is because high-career couples need full-time care so that their choice of child care would reveal any attempt to mimic a traditional couple. Similarly, a traditional couple mimicking a high-career one would have to choose full-time day care so that mimicking involves the same consumption bundle with or without observable career paths.

The main results of this section are summarized in the following proposition.

Proposition 5 *Assume that couples' formal child care is observable and can be provided publicly at level $c_p^g(q)$ or subject to a nonlinear tax or subsidy. The optimal incentive compatible policy when redistribution is relevant ($\Psi'' < 0$) implies:*

- (i) *that there is pooling within the traditional and the high-career couples groups: all traditional couples receive the same level of formal care and pay the same tax and similarly for all high-career couples.*
- (ii) *that high-career couples receive full-time formal care, while the level of c_p^g implies an implicit*

marginal subsidy which is determined by the Pigouvian rule: it equals $s^g = [1 - F(\hat{q}^g)]\gamma$ which reflects the marginal social damage represented by the norm cost imposed on the high-career couples.

(iii) $\hat{q}^g > \hat{q}^{fb}$ so that there are more traditional couples in the second best than in the first best. The marginal couple is distorted upwards to reduce the high-career couples' informational rents which improves redistribution.

(iv) $s^g < s^{fb}$; while both levels are set according to the Pigouvian rule, the inequality follows because there are less high-career couples in the second best so that the marginal social damage of the norm cost is smaller.

(v) that, in the GWG, both child penalties and adverse sorting are inefficiently high.

The intuition for (v) is the same as for the corresponding part in Propositions 3 and 4. Again, the policy mitigates the inefficiency of the *laissez-faire* informal care provision but, while welfare is obviously higher with the nonlinear policy than with the linear one, first-best efficiency is not restored.

8 Social comparisons among peers

In this section we consider a more sophisticated norm based on (local) social comparisons among peers. In other words, the norm that is relevant to any given mother is not determined by the informal average child care in the whole population but by that in her social group. For instance, mothers could refer to the average behavior of female family members or to the behavior of the women they interact with in their everyday life. Groups could also be defined on a geographical basis such as North vs. Southern Italy, where women are exposed to different social environments.²³

Let us assume that there are two social groups, indexed A and B . The groups may differ in their distribution of q , $F^A(q)$ and $F^B(q)$ and in the norm costs γ^A and γ^B . For simplicity and without loss of generality we assume that the two groups have equal size. Preferences are the same as in a one-group model and (apart from the norm cost) are the same for all individuals. Consequently, for $k = A, B$, we have

$$W_{hl}^k(q) = y + q + c_p^k y - T_{hl}^k + v(1 - c_p^k) + \beta v(c_p^k),$$

$$W_{hh}^k(q) = 2y + (1 + \alpha)q - T_{hh}^k + \beta v(1) - \gamma^k F(\hat{q}^k)(1 - c_p^k).$$

²³Social norms on gender roles are much stronger and the gender wage gap is higher in the South of Italy than in the North (Piazzalunga 2018), while policies are the same all over the country.

The optimal allocation is obtained exactly like in Section 3, except that the objective is redefined as $SW = SW^A + SW^B$, where the term pertaining to each group is obtained from (5) by adding the superscript to the relevant variables. Similarly the budget constraint is the sum of expressions in (6). Note that the budget constraint is “global” so that redistribution may occur both within and between groups. We skip all the straightforward algebra but explain the derivation of some expressions which involve some more rearrangements in Appendix (A.8) and (A.9). The FB levels of c_p^k ($k = A, B$) continue to be given by expression (7) and we have

$$\beta v'(c_p^{fb,k}) + [1 - F^k(\hat{q}^{fb,k})]\gamma^k = v'(1 - c_p^{fb,k}),$$

which are group specific and, if individualized lump-sum transfers $T_{hh}^k(q)$ and $T_{hl}^k(q)$ were available, could be implemented by the Pigouvian subsidy s^k given by

$$s^{fb,k} = [1 - F^k(\hat{q}^{fb,k})]\gamma^k.$$

To study second best policies and the robustness of our results we have to distinguish between policies with and without “tagging”. Tagging, as defined in the optimal taxation literature, means that the policy (linear or non linear) can be conditioned on the couple’s group, which is an exogenous variable.²⁴ In that case it directly follows that all of our results continue to apply. Specifically, in the linear case we have

$$s^{ok} = \gamma^k \frac{(1 - F^k(\hat{q}^{sk}))E_{hh}^k[\Psi']}{E[\Psi']} - \frac{\text{cov}^k[\Psi', c_p^{sk}]}{E[\Psi'] \frac{\partial E^k[c_p^{sk}]}{\partial p^a}}$$

which, except for the superscripts is the same as (20) and we have $s^{ok} < s^{fb}$ as with a single group.²⁵

Under nonlinear policies we have,

$$s^{gk} = [1 - F^k(\hat{q}^{gk})]\gamma^k.$$

and the Pigouvian rule applies again. To sum up, the main message of our paper continues to hold when there are several groups and when tagging is possible.

However, tagging is admittedly a strong assumption. In the linear case it is at odds with the assumption that the policy is uniform. More fundamentally, in both the linear and nonlinear cases it requires that groups are observable *and* that it is politically acceptable to use this information to design a policy. In the optimal tax literature tagging is typically considered as problematic (except in special cases) because it may be considered as arbitrary discrimination and violate “horizontal equity” requirements. A more meaningful, and demanding, test for the robustness of the results is thus the case without tagging to which we now turn.

²⁴See for instance Cremer *et al.* (2010).

²⁵We can say this for sure as long as $E_{hh}^k[\Psi'] < E[\Psi']$; since the latter is not indexed (the budget constraint is global) this might be violated under some assumptions on F^k . But this is just a sufficient condition given that the covariance term is necessarily negative.

8.1 Uniform policy, no tagging

The problem is essentially the same as the linear case with tagging except that we now impose $s^A = s^B = s$ and similarly for τ . Roughly speaking the FOCs are then simply the sum of the FOCs under tagging. We show in Appendix A.8 that the optimal uniform level of s is given by

$$s^o = \gamma^A \frac{(1 - F^A(\hat{q}^{sA}))E_{hh}^A[\Psi']}{E[\Psi']} \delta^A + \gamma^B \frac{(1 - F^B(\hat{q}^{sB}))E_{hh}^B[\Psi']}{E[\Psi']} (1 - \delta^A) - \frac{\text{cov}[\Psi', c_p^s]}{E[\Psi'] \left(\frac{\partial E^A[c_p^s]}{\partial p^n} + \frac{\partial E^B[c_p^s]}{\partial p^n} \right)}, \quad (33)$$

where

$$\delta^A = \frac{\frac{\partial E^A[c_p^s]}{\partial p^n}}{\frac{\partial E^A[c_p^s]}{\partial p^n} + \frac{\partial E^B[c_p^s]}{\partial p^n}}, \quad (34)$$

so that $0 < \delta^A < 1$. Note that $E[\Psi']$ is defined over both groups; as in Section 6 it is equal to the multiplier associated with the budget constraint which, as explained above, is “global”. Note that the amount of formal care purchased by traditional couples is the same in the two groups and satisfies $v'(1 - c_p^s) - s^o = \beta v'(c_p^s)$. However, the *average* amount of formal care differ in the two groups via the distribution $F^k(q)$.

To interpret expression (33) it is better to start with the case where $\Psi'' = 0$ so that redistribution is not a concern. Expression (33) then reduces to

$$s^o = \gamma^A ((1 - F^A(\hat{q}^{*A}))\delta^A + \gamma^B ((1 - F^B(\hat{q}^{*B}))(1 - \delta^A)). \quad (35)$$

When there was a single group (or under tagging), absent redistribution concerns, a linear subsidy set at the (group-specific) Pigouvian level was sufficient to reestablish efficiency. However, with two (or more) groups this is no longer possible because the subsidy must be uniform across groups. The optimal uniform policy then strikes a compromise between the two relevant Pigouvian levels; s^o is set at a weighted average of the group-specific levels.

This effect continues to be present when redistribution matters, as we can see by comparing the first two terms of (33) to the first term of (20). Most significantly from our perspective, the redistributive concern continues to decrease the optimal uniform subsidy. For the reasons explained in Section 6 the covariance term in (33) is still negative and the two first terms in this expressions are smaller than their counterparts in (35) as long as $E_{hh}^k[\Psi'] < E[\Psi']$, for $k = A, B$ so that the average social marginal utility of income is smaller in both high-career groups than in the entire population.

This shows that the trade-off between efficiency and redistributive considerations persists with local social comparisons: the optimal subsidy s^o is lower than the Pigouvian level which applies when efficiency is the only social concerns.

8.2 Nonlinear policy, no tagging

When tagging is not possible the optimal policy has to rely on self-selection. The same menu of contracts has to be offered to everyone but the incentive constraints ensure that all couples choose the package $\{T_{hl}, c_p^g\}$ designed for them. The menu includes four contracts, $\{T_{hl}^A, c_p^{gA}\}$ and $\{T_{hl}^B, c_p^{gB}\}$ for hl -couples and $\{T_{hh}^A, 1\}$ and $\{T_{hh}^B, 1\}$ for hh -couples. Since high-career couples of both groups must benefit from full-time child care they cannot be separated and incentive compatibility requires $T_{hh}^A = T_{hh}^B = T_{hh}$. The incentive constraint for low-career couples requires

$$y + c_p^{gA}y - T_{hl}^A + v(1 - c_p^{gA}) + \beta v(c_p^{gA}) = y + c_p^{gB}y - T_{hl}^B + v(1 - c_p^{gB}) + \beta v(c_p^{gB}). \quad (36)$$

In words, low-career couples of any given q must receive the same utility in both groups. They may receive different levels of child care but the T^k must be adjusted so that they are on the same indifference curve. Note that norm costs are of no relevance for low-career couples. In addition the counterpart to equation (23) must be satisfied within each group so that high-career couples do not want to mimic low-career couples of any of the groups. With (36), this requires, for $k = A, B$,

$$\begin{aligned} & 2y + (1 + \alpha)\hat{q}^{gk} - T_{hh} + \beta v(1) - \gamma^k F^k(\hat{q}^{gk}) \left(1 - c_p^{gk}\right) \\ & - \left(y + \hat{q}^{gk} + c_p^{gk}y - T_{hl} + v(1 - c_p^{gk}) + \beta v(c_p^{gk})\right) = 0. \end{aligned} \quad (37)$$

We show in Appendix A.9 that maximizing $SW = SW^A + SW^B$ subject to the global budget constraint and the incentive constraints (36) and (37) yields²⁶

$$v' \left(1 - c_p^{gk}\right) - \beta v' \left(c_p^{gk}\right) = (1 - F(\hat{q}^{gk}))\gamma^k + \gamma^k \frac{E^k[\Psi'] - E[\Psi']}{E[\Psi']}, \quad k = A, B. \quad (38)$$

In words, within each group we obtain the Pigouvian rule modified to account for redistribution between groups. Note that with tagging we would have $E^A[\Psi'] = E^B[\Psi'] = E[\Psi']$ so that average marginal social utilities of income would be equalized across groups. In that case the expressions would reduce to the simple Pigouvian rule, as mentioned when tagging was discussed.

Absent of tagging we must have $T_{hh}^A = T_{hh}^B = T_{hh}$ which limits the possibility of redistribution between groups and the solution implies in general different levels of $E^k[\Psi']$. While utilities of low and high-career couples for any given q are equalized across groups, the marginal couples differ because of the norm costs and the distribution which are group-specific. Hence, the regressive within group effect of public child care is not relevant. This major message obtained in the one group case is thus robust.

To further interpret expression (38) assume for instance that $E^A[\Psi'] > E[\Psi'] > E^B[\Psi']$ so that group A is ‘‘poorer’’. This yields $c_p^{gA} > c_p^{fb} > c_p^{gB}$ and $s^{gA} > s^{fb} > s^{gB}$. The level of

²⁶ As part of the proof we show that the Lagrange multiplier associated with (36) is equal to zero. In other words, utility level of low career couples are equalized anyway, even when this is not imposed as extra constraint.

formal child care (and thus the marginal subsidy) is larger than the Pigouvian level in the poor group and lower than this level in the more wealthy group. Thus, child-care provision becomes progressive when it comes to redistribution between groups because traditional couples in the poorer group receive a larger level of child care than those in the richer group.

To sum up, with a nonlinear policy there is no conflict between efficient child-care provision and redistribution among income levels.

9 Policy discussion

Elizabeth Warren (a democratic candidate for the US presidential elections) has included “universal child care” as a main pillar in her electoral platform. Similarly, in recent Bavarian elections a new “Free voters of Bavaria” movement managed to unsettle the traditional Christian Democratic majority in the regional parliament with a program aiming at offering free child care to all families. Whether or not these are realistic policy options or utopian visions that are impossible to finance (and mainly a boon for well off couples) remains to be seen. But these two examples (which could be completed by many others) show how significant these issues are in practice. Policy choices that are made in the coming years may affect gender roles (and even fertility decisions) for many decades to come.

In most countries the current situation is not the *laissez faire* allocation used as reference in our analysis. Various policies already provide child care and early childhood education. In the majority of countries, education now begins for most well before 5 years old: 71.5% of young children aged 3 and 4 years are enrolled in education across OECD countries as a whole, and this rises to 79.8% in the OECD countries that are part of the European Union.²⁷ Publicly-funded pre-primary provision tends to be more strongly developed in the European than in the non-European countries of the OECD. In Europe, the concept of universal access of 3- to 6-year-olds is generally accepted. Most European countries provide all children with at least two years of free, publicly-funded provision before they begin primary school provision. Public expenditure on early childhood and educational care, in cash or in kind, represents today on average 0.8 percent of GDP in OECD countries.²⁸

Typically, neither the nursery school nor the primary school provide a form of child care which fully covers the daily needs of full-time working parents.²⁹ In addition, apart from Scandinavian

²⁷Enrollment rates for early childhood education at this age range from over 90% in Belgium, Denmark, France, Germany, Iceland, Italy, New Zealand, Norway, Spain, Sweden and the United Kingdom, at one end of the spectrum, to less than a third in Australia, Greece, Korea, Switzerland and Turkey.

²⁸It attains 2 percent in Denmark, and is above 1 percent in the rest of Scandinavia, the United Kingdom, and France. North American and Southern EU countries have the lowest rates of early childhood public spending. In the United States, early childhood public spending is 0.4 percent of GDP; see OECD (2014).

²⁹Average hours in early childhood education and care differ substantially across countries. In most OECD

countries, the demand for day-care centers is significantly larger than the available capacity, even in countries with long parental leave. In countries where public funding for such provision is limited, most working parents must either seek (complementary or alternative) solutions in the private market, where ability to pay significantly influences accessibility to quality services, or else rely on informal arrangements with family, friends and neighbors; see OECD (2010).

Fees charged to parents for publicly provided early child-care are often high. Parents in Ireland, the Netherlands, Switzerland and the United Kingdom face some of the highest out-of-pocket costs for center-based care in Europe. Even though all countries except Ireland provide additional financial support for families on very low incomes, net fees often remain high in absolute terms.³⁰ This contributes to the fact that children are more likely to use early childhood education and care services when they come from relatively advantaged socioeconomic backgrounds; see OECD (2017), Petitclerc *et al.* (2017) and Krapf (2014).

To sum up, currently most child-care systems are not designed in such a way to accommodate working parents' needs. The supply of day-care facilities is rationed in terms of spots available, opening hours are generally too short and fees tend to be quite high for children of 0–3 years of age. As long as this remains the case, child-care policies notwithstanding, the current situation suffers from the same deficiencies as the *laissez faire* in our model. The policies we present, though only second-best, would represent a step in the right direction.

Our model shows that a “free for all” approach would be neither efficient nor fair. This would be overshooting in the opposite direction. Our analysis also suggests that attendance can be used as a device to screen high- and low-income families because the number of hours children spend in day-care represents a proxy for the family's income. This is in line with the evidence reported by Capizzano and Main (2005). They analyze data from the most recent National Survey of America's Families (i.e. the 2002 NSAF survey) and report that children from higher-income families spend more hours per day in child care than children from low-income families. This shows that results from our model are consistent with parents' behavior and confirms that, as suggested by the model, fees contingent on the time children spend in the facility can be efficiency enhancing. However, in OECD countries, day-care fees are generally based on enrollment and possibly on family's size and income but to a much lower extent on hours of attendance; see OECD (2017). In addition, information about hours of attendance is

countries, children in early childhood education and care (0-2-year-olds) use it for an average between 25 and 35 hours during a usual week, with the OECD average just under 30 hours per week. However, in some countries (e.g. Iceland, Latvia and Portugal) average hours approach 40 hours during a usual week. In others, such as the Netherlands and the United Kingdom, 0-2 years old in early education centers are there for an average of less than 20 hours during a usual week.

³⁰In the Netherlands and the United Kingdom the out-of-pocket cost of full-time center-based care for two children (aged 2 and 3) in a low-earning dual-earner family works out at around 20% of family disposable income, and at 35% in Ireland.

typically easier to collect than information about family income or wealth and is not falsifiable. Which again points at children’s hours of attendance as a practical screening instrument.

10 Conclusion

We have studied the design of child-care policies when women’s career choices are endogenous. High-career mothers suffer from a norm cost caused by “mothers’ guilt”. Through their child-care choices low-career mothers create a negative externality via the norm cost. Consequently, the *laissez-faire* solution is inefficient; it implies too much informal child care and a share of high-career mothers which is too low.

Child-care policies are effective in enhancing efficiency and reducing gender inequalities. However, since they provide larger benefits to high-income couples, they tend to be regressive. Under full information, this effect can be offset by lump-sum transfers associated with a Pigouvian subsidy on formal child care. A uniform subsidy, on the other hand, involves a trade-off between efficiency and redistribution across couples and should be set below the Pigouvian level. Under a nonlinear policy the first-best “Pigouvian” rule for the (marginal) subsidy on formal care is reestablished. While the share of high-career mothers continues to be distorted downward for incentive reasons, this policy is effective in reconciling the objectives of reducing the inefficiency in informal care provision and achieving a more equal income distribution across couples.

Our message is robust to a more sophisticated specification of the social norm such that “mother’s guilt” emerges only when women compare their informal care provision to the one of mothers belonging to their reference group. In this case, policies have to address income redistribution both within and across social groups and a linear policy may become even more regressive than in the case of a less sophisticated social norm. Specifically, the group with the larger share of career mothers is likely to be richer and to benefit relatively more from a linear subsidy. With a nonlinear policy instead we obtain the Pigouvian rule within each group modified to account for redistribution between groups. Hence, we show that with a nonlinear policy there is no conflict between efficient formal care provision in each group and redistribution among income levels within and across groups.

From a practical perspective a nonlinear policy can be implemented through in-kind provision of child care, at different levels, depending on the mothers’ career path, and financed with nonlinear taxes. Alternatively nonlinear subsidies on market care can be used.³¹ Either way,

³¹See also Cremer and Gahvari (1997) who show that when individual consumption levels are observable, in-kind transfers and nonlinear subsidies are equivalent. This information structure also differentiates our model from the extensive literature on in-kind transfers of which child care is a prime example (see Blomquist and Chirstiansen, 1995, or Blomquist *et al.*, 2010, among others).

day care fees should be contingent on the amount of time children spend in the facility. More generally, our model indicates that providing “free child care to all” is problematic. While universal provision of preschool child care is desirable, free access is never optimal because it represents a too regressive policy.

Some of our assumptions are admittedly debatable. For instance we have assumed that the norm cost is determined by the *average* levels of informal care. In our earlier paper we have considered first the *median* and added an appendix dealing with a general specification of the norm, which includes *average* and *median* as special cases. We have used the *average* in this paper because, with that specification, a (Pigouvian) linear subsidy is sufficient to achieve the FB when only efficiency matters. This makes a clear benchmark against which we can assess the impact of redistributive considerations. In our earlier paper where only efficiency matters, we have shown that with a norm based on the *median*, the optimal linear subsidy is already below the Pigouvian level. Hence, using the *median* norm in our current analysis would imply that redistributive concerns exacerbate distortions already existing when only efficiency matters. This would make the expressions less transparent, while the main point, namely that in the linear case redistribution reduces the subsidy, continues to go through. We consider a more general specification of the norm which encompasses the *average* and the *median* in Appendix A.10. Most significantly we show there that a nonlinear policy brings us back to the Pigouvian rule for the child-care subsidy irrespective of the specification of the norm.

Similarly a caveat about the Social Welfare Function is in order. We confess that our utilitarian (consequentialist) approach is debatable on philosophical grounds. The alternative would have been to consider a paternalistic (non welfarist) approach excluding the norm cost from social welfare. In that case (i) informal child care under *laissez-faire* would be optimal because the externality does not matter but (ii), the share of career couples would be too low in *laissez faire* because career couples are wrongly discouraged by the norm. In other words, under the paternalistic approach, the results would be less rich than they currently are, because informal child care would always be optimal in *laissez faire*. So the paternalistic approach would provide less sophisticated results in the sense that some of the effects which contribute to the explanation of the source of gender inequalities would be “brushed under the carpet”. Furthermore the paternalistic approach would of course come at the price that the considered “optimum” is not Pareto efficient.

The issue of welfare relevant externalities (and the appropriate “laundering of preference”) is extensively discussed for instance by Harsanyi (1982) who indeed argues that not all externalities can be considered as policy relevant. However, as we discuss in Section 2 the phenomenon of “mother’s guilt” and more generally the societal perception of traditional gender roles are indeed well documented in the empirical literature and appear to be sufficiently significant to consider

them as policy relevant.

Our model has ignored a certain number of important aspects. For instance, we do not consider the welfare of children and the impact of early education on their human capital. There is now ample evidence that high quality formal child care yields better outcome for the children than informal care by less advantaged mothers (see Duncan and Sojourner, 2013, Cornelissen *et al.*, 2018). This is likely to call for an even more generous child-care policy and tend to increase subsidies. We have also ignored the fact that family policies may be intended to foster fertility. In the political debate this argument is used both to enhance child care or, at the opposite, to pay mothers who stay home. Anyway fertility would add another layer of complexity. To our knowledge, it is not clear from the empirical literature which type of family policy is best for fertility nor even if any has a significant impact. For instance Gauthier (2007, page 323) in the abstract of her paper draws the following inventory of the state of the literature: “As to the empirical evidence, studies provide mixed conclusions as to the effect of policies on fertility. While a small positive effect of policies on fertility is found in numerous studies, no statistically significant effect is found in others. Moreover, some studies suggest that the effect of policies tends to be on the timing of births rather than on completed fertility.”

We have also not considered the issue of explicit means testing. This would require a more complex information structure to keep the problem interesting. In essence we would have to combine our approach with a more traditional optimal tax model inspired, for instance, by Casarico *et al.* (2015). These and further extensions are on our research agenda.

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Appendix

A.1 Couples’ optimization

Below we study couples’ decisions focusing on parents’ informal care provision. In the main text we focused instead on the complementary choice of formal care purchase.

A.1.1 Only the mother enters the high-career path

Since the mother is in the high-career path, she is not able to take care of the children and suffers the cost of not conforming to the norm. Welfare of the couple is denoted by $W_{\ell h}$ and informal care provided by the father by $c_m = c_{\ell h}$. Noting that $c_{\ell h} + c_p = 1$ and $p = y$, the couple chooses $c_{\ell h}$ to maximize:

$$\max_{c_{\ell h}} W_{\ell h} = y + \alpha q + v(c_{\ell h}) + \beta v(1 - c_{\ell h}) - \gamma \bar{c}_f.$$

Optimal child-care provision, $c_{\ell h}^*$, is implicitly determined by:

$$v'(c_{\ell h}^*) = \beta v'(1 - c_{\ell h}^*).$$

Indirect welfare $W_{\ell h}^*$ writes:

$$W_{\ell h}^* = y + \alpha q + v(c_{\ell h}^*) + \beta v(1 - c_{\ell h}^*) - \gamma \bar{c}_f.$$

A.1.2 Both couples enter the low-career path

Here both parents may provide informal care. The social norm for the mother is potentially binding. Welfare of this couple is denoted by $W_{\ell \ell}$ and total informal care provided by the parents

is $c_{\ell\ell} = c_f + c_m$. Noting that $c_f + c_m + c_p = c_{\ell\ell} + c_p = 1$ and $p = y$, the couple chooses $c_{\ell\ell}$ to maximize:

$$\begin{aligned} \max_{c_f; c_m} \quad & W_{\ell\ell} = (1 - c_m) y + (1 - c_f) y - p(1 - c_{\ell\ell}) \\ & + v(c_{\ell\ell}) + \beta v(1 - c_{\ell\ell}) - \gamma(\max\{0; \bar{c}_f - c_f\}) \\ = & y + v(c_{\ell\ell}) + \beta v(1 - c_{\ell\ell}) - \gamma(\max\{0; \bar{c}_f - c_f\}) \end{aligned}$$

Optimal child-care provision, $c_{\ell\ell}^* = c_f^* + c_m^*$, is implicitly determined by the two conditions:

$$\begin{aligned} v'(c_m^*) &\leq \beta v'(1 - c_{\ell\ell}^*) \\ v'(c_f^*) &\leq \beta v'(1 - c_{\ell\ell}^*) + I\gamma, \end{aligned}$$

where I is an indicator function which takes value 1 when the social norm for mothers is binding, namely when $\bar{c}_f - c_f > 0$, and 0 otherwise. Welfare $W_{\ell\ell}^*$ now is:

$$W_{\ell\ell}^* = y + v(c_{\ell\ell}^*) + \beta v(1 - c_{\ell\ell}^*) - \gamma(\max\{0; \bar{c}_f - c_f^*\}).$$

A.2 The optimal allocation

Denoting λ the Lagrangean multiplier with respect to the budget constraint, the FOCs of (5) with respect to the couples' consumption levels can be rewritten as:

$$\begin{aligned} \frac{\partial SW}{\partial x_{h\ell}(q)} &= \Psi'(W_{h\ell}(q))f(q) - \lambda f(q) = 0 \quad \forall q \leq \hat{q} \\ \frac{\partial SW}{\partial x_{hh}(q)} &= \Psi'(W_{hh}(q))f(q) - \lambda f(q) = 0 \quad \forall q > \hat{q}. \end{aligned}$$

so that:

$$\Psi'(W_{hh}^{fb}(q)) = \Psi'(W_{h\ell}^{fb}(q)) = \lambda \quad \Leftrightarrow \quad W_{h\ell}^{fb}(q) = W_{hh}^{fb}(q) \quad \forall q.$$

Equalizing welfare levels across career paths, we can write:

$$x_{h\ell}^{fb}(q) + v(1 - c_p^{fb}(q)) + \beta v(c_p^{fb}(q)) = x_{hh}^{fb}(q) + \beta v(1) - \gamma F(\hat{q}^{fb})(1 - c_p^{fb}(q)) \quad \forall q. \quad (\text{A.1})$$

We now consider the point-by-point derivative of the social welfare with respect to $c_p(q)$. Given that $c_p(q)$ exerts a negative effect on all hh -couples we have:

$$\Psi'(W_{h\ell}^{fb}(c_p^{fb}(q))) \frac{-\partial W_{h\ell}^{fb}(c_p^{fb}(q))}{\partial c_p^{fb}(q)} f(q) + \int_{\hat{q}}^Q \Psi'(W_{hh}^{fb}(\varepsilon)) \frac{\partial W_{hh}^{fb}(\varepsilon)}{\partial \bar{c}} \frac{-\partial \bar{c}}{\partial c_p^{fb}(q)} f(\varepsilon) d\varepsilon = 0$$

which gives:

$$\Psi'(W_{h\ell}^{fb}) \left[v'(1 - c_p^{fb}(q)) - \beta v'(c_p^{fb}(q)) \right] f(q) + \int_{\hat{q}}^Q \Psi'(W_{hh}^{fb}) (-\gamma f(q)) f(\varepsilon) d\varepsilon = 0$$

Considering that $W_{h\ell}^{fb} = W_{hh}^{fb}$, we can simplify the previous equation as follows:

$$v'(1 - c_p^{fb}(q)) - \beta v'(c_p^{fb}(q)) - \gamma \int_{\hat{q}}^Q f(\varepsilon) d\varepsilon = 0$$

showing that it must be $c_p^{fb}(q) = c_p^{fb} \forall q$. Rearranging, the above equation we obtain (27) in the main text.

Taking the derivative of the social welfare function with respect to the marginal couple \hat{q} and rearranging, yields:

$$\alpha \hat{q} f(\hat{q}^{fb}) = f(\hat{q}^{fb}) \left[x_{hh}^{fb}(\hat{q}^{fb}) - x_{hl}^{fb}(\hat{q}^{fb}) - \gamma[1 - F(\hat{q}^{fb})](1 - c_p^{fb}) \right]. \quad (\text{A.2})$$

Given that $c_p(q) = c_p \forall q$, we observe that $x_{hl}^{fb}(q) = x_{hl}^{fb}$ and $x_{hh}^{fb}(q) = x_{hh}^{fb} \forall q$. Hence, equation (A.1) can be rewritten as:

$$x_{hh}^{fb} - x_{hl}^{fb} = v(1 - c_p^{fb}) + \beta[v(c_p^{fb}) - v(1)] + \gamma F(\hat{q}^{fb})(1 - c_p^{fb}) > 0 \quad (\text{A.3})$$

With (A.3) we can rewrite (A.2) as (9) in the main text.

A.3 Comparative statics

Child care, c_p , and the marginal couple, \hat{q} , are implicitly determined by the following two equations:

$$f_1(c_p, \hat{q}, p^n) \equiv y - p^n - v'(1 - c_p) + \beta v'(c_p) = 0$$

$$f_2(c_p, \hat{q}, p^n) \equiv y - \alpha \hat{q} + c_p y + p^n(1 - c_p) + v(1 - c_p) + \beta[v(c_p) - v(1)] + \gamma f(\hat{q})(1 - c_p)$$

When we want to know the effect in price changes of formal child care, we have to solve:

$$\begin{bmatrix} \frac{\partial f_1}{\partial c_p} & \frac{\partial f_1}{\partial \hat{q}} \\ \frac{\partial f_2}{\partial c_p} & \frac{\partial f_2}{\partial \hat{q}} \end{bmatrix} \begin{bmatrix} dc_p \\ d\hat{q} \end{bmatrix} = - \begin{bmatrix} \frac{\partial f_1}{\partial p^n} \\ \frac{\partial f_2}{\partial p^n} \end{bmatrix} dp^n.$$

Inserting the derivatives and inverting the first matrix, we have:

$$\begin{bmatrix} dc_p \\ d\hat{q} \end{bmatrix} = \frac{1}{D} \begin{bmatrix} -\alpha + \gamma f(\hat{q})(1 - c_p) & 0 \\ \gamma F(\hat{q}) & v''(1 - c_p) + \beta v''(c_p) \end{bmatrix} \begin{bmatrix} 1 \\ -(1 - c_p) \end{bmatrix} dp^n,$$

where $D = [-\alpha + \gamma f(\hat{q})(1 - c_p)][v''(1 - c_p) + \beta v''(c_p)] > 0$. We thus have:

$$\frac{dc_p}{dp^n} = \frac{1}{v''(1 - c_p) + \beta v''(c_p)} < 0 \quad (\text{A.4})$$

$$\frac{d\hat{q}}{dp^n} = \frac{-[v''(1 - c_p) + \beta v''(c_p)](1 - c_p) + \gamma F(\hat{q})}{[-\alpha + \gamma f(\hat{q})(1 - c_p)][v''(1 - c_p) + \beta v''(c_p)]} > 0 \quad (\text{A.5})$$

A.4 Numerical example: specification and calibration

Our model involves a number of normalizations so that absolute levels of γ , q and for that matter s are not very telling. To make meaningful comparisons we have to look at relative levels. Another difficulty is that with the normalization $y = p$ these two variables do not directly affect the results and in particular are not relevant for the *laissez faire* and the first best. This makes it difficult to assess the importance of s . In this example we have tried to overcome these difficulties by a number of shortcuts which are admittedly rough approximations but they do lead to rather intuitive results which are in line with our conjecture.

We use a quadratic utility of (formal and informal) child care c so that $v(c) = -0.6(1 - c)^2$ and set $\beta = 1$. This means that the relevant part in the couple's utility is given by

$$-0.6(1 - c_f)^2 - 0.6(1 - c_p)^2 + sc_p = -0.6(c_p)^2 - 0.6(1 - c_p)^2 + sc_p;$$

where the s is zero in the *laissez faire* while in the first best (or rather its decentralization) it is given by the Pigouvian level (which in turn depends on the norm cost both directly and indirectly via the \hat{q}). The bonus q is uniformly distributed over $[0, 1]$ and its average is 0.5; while we assume that $\alpha = 0.9$. We consider levels of γ ranging from 0 to 0.9. When $\gamma = 0.5$ it is equal to the average q while, for $\gamma = 0.9$, it represents 90% of the top bonus. The parameter 0.6 in the v function is set to yield (roughly) empirically reasonable shares of low-career women, i.e. shares in the range [2%, 60%]. Indeed, in the model, low-career women are employed women who, basically, work part-time. Looking at Eurostat data we observe that the share of women working part-time in European countries is on average 31.5% but it is above 50% in Mediterranean countries and it reaches the 60% in Italy and the 66% in Greece; see the report by the European Commission "Women in the labour market" available at https://ec.europa.eu/info/sites/info/files/european-semester_thematic-factsheet_labour-force-participation-women_en_0.pdf

Based on the *laissez faire* equilibrium one can thus think about the high range of γ 's as Greece or Italy, while the low range represents Nordic countries, with France ($\hat{q} = 40\%$) in the middle. Table 1 reports for each of the considered γ 's the marginal couple in the *laissez faire* and in first best. The difference between these two levels is a possible measure of the significance of γ and not surprisingly this difference increases with γ . When γ is equal to the average level of q , the optimal policy involves a decrease in the share of traditional couples of about 15%.

Turning to s , the absolute value reported (which is a per unit subsidy) is not in itself informative. However, one can relate it to the q and more interestingly to the $y = p$. As mentioned above $y = p$ cannot be directly identified from the results. However, recall that y represents (average) wages in the low-career path. A very minimalist assumption would be that the average wage in the high-career path ($y + E[q]$) is at least twice as large as that in the low-career path (y). For instance the Bureau of Labor Statistics in the US estimates an average (hourly) wage of about \$28 for teachers as opposed to about \$62 for executives in management positions. From this we can then calibrate a hypothetical level of $y = p$ of 0.5 (so the average high-career wage is 1). From that perspective $s = 0.45$ then corresponds to a subsidy rate of 95% while $s = 0.3$ corresponds to a 60% rate.

A.5 Uniform subsidies

The FOC wrt s can be written as

$$\begin{aligned} E[\Psi'c_p^s] + (1 - F(\hat{q}^s))E_{hh}[\Psi']\gamma \left[F(\hat{q}^s)\frac{dc_p^s}{dp^n} - (1 - c_p^s)f(\hat{q}^s)\frac{d\hat{q}^s}{dp^n} \right] - E[\Psi']E[c_p^s] \\ - E[\Psi']s \left[-F(\hat{q}^s)\frac{dc_p^s}{dp^n} + (1 - c_p^s)f(\hat{q}^s)\frac{d\hat{q}^s}{dp^n} \right] = 0, \end{aligned}$$

where $E[c_p^s] = F(\hat{q}(p^n))c_p(p^n) + 1 - F(\hat{q}(p^n))$. Noting that

$$\frac{\partial E[c_p^s]}{\partial p^n} = F(\hat{q}^s)\frac{dc_p^s}{dp^n} - (1 - c_p^s)f(\hat{q}^s)\frac{d\hat{q}^s}{dp^n} < 0 \quad (\text{A.6})$$

and $\text{cov}[\Psi', c_p^s] = E[\Psi' c_p^s] - E[\Psi']E[c_p^s]$, we can write

$$\frac{\partial SW}{\partial s} = \text{cov}[\Psi', c_p^s] - (1 - F(\hat{q}^s))E_{hh}[\Psi']\gamma \frac{\partial E[c_p^s]}{\partial p^n} + E[\Psi']s \frac{\partial E[c_p^s]}{\partial p^n}. \quad (\text{A.7})$$

Setting this expression equal to zero and solving for s yields equation (20). Further evaluating (A.7) at the Pigouvian level $s^{fb} = [1 - F(\hat{q}^{fb})]\gamma_f$, which from (13) implies $\hat{q}^* = \hat{q}^{fb}$ yields

$$\left. \frac{\partial SW}{\partial s} \right|_{s=s^{fb}} = \text{cov}[\Psi', c_p^s] - (1 - F(\hat{q}^{fb}))E_{hh}[\Psi']\gamma \frac{\partial E[c_p^s]}{\partial p^n} + E[\Psi'] [1 - F(\hat{q}^{fb})]\gamma_f \frac{\partial E[c_p^s]}{\partial p^n} = \text{cov}[\Psi', c_p^s] < 0 \quad (\text{A.8})$$

so that assuming concavity we must have $s^o < s^{fb}$.

A.6 Proof of equation (28)

The FOC wrt c_p^g is given by:

$$\int_0^{\hat{q}^g} \Psi'(\cdot) [y - v'(1 - c_p^g) + \beta v'(c_p^g)] f(q) dq + \int_{\hat{q}^g}^Q \Psi'(\cdot) \gamma F(\hat{q}^g) f(q) dq - \hat{\lambda}_p F(\hat{q}^g) + \mu [\gamma F(\hat{q}^g) - y + v'(1 - c_p^g) - \beta v'(c_p^g)] = 0.$$

With equations (25) and (26) and the following definitions:

$$E_{hl}[\Psi'] = \frac{\int_0^{\hat{q}^g} \Psi'(\cdot) f(q) dq}{F(\hat{q}^g)} \quad \text{and} \quad E_{hh}[\Psi'] = \frac{\int_{\hat{q}^g}^Q \Psi'(\cdot) f(q) dq}{1 - F(\hat{q}^g)}$$

we can rewrite the above FOC as:

$$E_{hl}[\Psi'] F(\hat{q}^g) [y - v'(1 - c_p^g) + \beta v'(c_p^g)] + \gamma F(\hat{q}^g) E_{hh}[\Psi'] (1 - F(\hat{q}^g)) - E[\Psi'] y F(\hat{q}^g) + [-E_{hh}[\Psi'] (1 - F(\hat{q}^g)) + E[\Psi'] (1 - F(\hat{q}^g))] [\gamma F(\hat{q}^g) - y + v'(1 - c_p^g) - \beta v'(c_p^g)] = 0. \quad (\text{A.9})$$

Noting that $E_{hl}[\Psi'] F(\hat{q}^g) + E_{hh}[\Psi'] (1 - F(\hat{q}^g)) = E[\Psi']$, we can write:

$$E[\Psi'] [y - v'(1 - c_p^g) + \beta v'(c_p^g)] - E[\Psi'] y F(\hat{q}^g) + E[\Psi'] (1 - F(\hat{q}^g)) [\gamma F(\hat{q}^g) - y + v'(1 - c_p^g) - \beta v'(c_p^g)] = 0$$

which reduces to:

$$[1 - F(\hat{q}^g)]\gamma - v'(1 - c_p^g) + \beta v'(c_p^g) = 0.$$

A.7 Proof of equation (31)

Solving the IC constraint for $T_{hl} - T_{hh}$ yields

$$T_{hl} - T_{hh} = -y - \alpha \hat{q}^g - \beta v(1) + \gamma F(\hat{q}^g) (1 - c_p^g) + c_p^g y + v(1 - c_p^g) + \beta v(c_p^g)$$

From (13) we have the first-best marginal couple:

$$\hat{q}^{fb} \equiv \frac{1}{\alpha} \left[v(1 - c_p^{fb}) + \beta v(c_p^{fb}) - \beta v(1) + \gamma F(\hat{q}^{fb})(1 - c_p^{fb}) - \gamma [1 - F(\hat{q}^{fb})](1 - c_p^{fb}) \right]$$

We now substitute $c_p^g = c_p^{fb}$ and $\hat{q}^g = \hat{q}^{fb}$:

$$\begin{aligned} T_{hl} - T_{hh} &= -y - v(1 - c_p^g) - \beta v(c_p^g) + \beta v(1) - \gamma F(\hat{q}^{fb})(1 - c_p^g) + \gamma[1 - F(\hat{q}^{fb})](1 - c_p^g) \\ &\quad - \beta v(1) + \gamma F(\hat{q}^{fb})(1 - c_p^g) + c_p^g y + v(1 - c_p^g) + \beta v(c_p^g). \end{aligned}$$

The above equation simplifies to:

$$T_{hl} - T_{hh} = \gamma[1 - F(\hat{q}^{fb})](1 - c_p^g) - y(1 - c_p^g).$$

A.8 Proof of equation (33)

The objective function is obtained from (16) by indexing all the group-specific variables and summing over $k = A, B$. Similarly, the budget constraint is³²

$$2\tau = \sum_{k=A}^B \left\{ sF(\hat{q}^{sk}(p^n))c_p(p^n) + s[1 - F(\hat{q}^{sk}(p^n))] \right\}. \quad (\text{A.10})$$

The FOC with respect to s is then given by

$$\begin{aligned} &\sum_{k=A}^B \left\{ F(\hat{q}^{sk})E_{hl}^k[\Psi']c_p^s + (1 - F(\hat{q}^{sk}))E_{hh}^k[\Psi'] \left[1 - \gamma^k F(\hat{q}^{sk}) \frac{dc_p^s}{dp^n} + \gamma^k (1 - c_p^s) f(\hat{q}^{sk}) \frac{d\hat{q}^{sk}}{dp^n} \right] \right\} \\ &- \lambda \sum_{k=A}^B \left[F(\hat{q}^{sk})c_p^s - sF(\hat{q}^{sk}) \frac{dc_p^s}{dp^n} + s(1 - c_p^s) f(\hat{q}^{sk}) \frac{d\hat{q}^{sk}}{dp^n} + 1 - F(\hat{q}^{sk}) \right] = 0. \end{aligned} \quad (\text{A.11})$$

The FOC with respect to τ is given by³³

$$2\lambda = \sum_{k=A}^B \int_0^{Q^k} \Psi'(q) f^k(q) dq \equiv 2E[\Psi'], \quad (\text{A.12})$$

Proceeding like in Appendix A.5, and making use of (A.12) we can rewrite (A.11)

$$\begin{aligned} &E[\Psi', c_p^s] + \sum_{k=A}^B (1 - F^k(\hat{q}^{sk})) E_{hh}^k[\Psi'] \gamma^k \left[F^k(\hat{q}^{sk}) \frac{dc_p^s}{dp^n} - (1 - c_p^s) f^k(\hat{q}^{sk}) \frac{d\hat{q}^{sk}}{dp^n} \right] - E[\Psi'] E[c_p^s] \\ &- E[\Psi'] s \sum_{k=A}^B \left[-F^k(\hat{q}^{sk}) \frac{dc_p^s}{dp^n} + (1 - c_p^s) f^k(\hat{q}^{sk}) \frac{d\hat{q}^{sk}}{dp^n} \right] = 0, \end{aligned} \quad (\text{A.13})$$

³²To keep the model (and the expressions) as close as possible to the one group case, we assume that population “size” in each group is one. Consequently, all the within group expectations defined above remain valid. Total population size is then 2 and the global expectation and covariance is obtained by dividing the usual integral by 2.

³³Total population size is now equal to 2 so that

$$E[\Psi'] = \frac{1}{2} \sum_{k=A}^B \int_0^{Q^k} \Psi'(q) f^k(q) dq.$$

The expectations $E[\Psi', c_p^s]$ and $E[c_p^s]$ are redefined in the same way.

where $E[c_p^s] = \sum_{k=A}^B E^k[c_p^s]/2 = \sum_{k=A}^B [F^k(\hat{q}^{sk}(p^n))c_p(p^n) + 1 - F^k(\hat{q}^{sk}(p^n))]/2$. So that equation (A.6) becomes

$$\frac{\partial E^k[c_p^s]}{\partial p^n} = F^k(\hat{q}^{sk}) \frac{dc_p^s}{dp^n} - (1 - c_p^s) f^k(\hat{q}^{sk}) \frac{d\hat{q}^{sk}}{dp^n} < 0 \quad (\text{A.14})$$

and (A.13) can be written as

$$\text{cov}[\Psi', c_p^s] - \sum_{k=A}^B (1 - F^k(\hat{q}^{sk})) E_{hh}^k[\Psi'] \gamma^k \frac{\partial E^k[c_p^s]}{\partial p^n} + E[\Psi']_s \sum_{k=A}^B \frac{\partial E^k[c_p^s]}{\partial p^n} = 0. \quad (\text{A.15})$$

Solving for s and rearranging then yields expression (33).

A.9 Proof of expression (38)

First, observe that equation (36) does not impose any extra restriction. This is because when the constraint (36) is *not* imposed the solution implies that utilities of the low-career couples are equal across groups for any given q . In other words the constraint is redundant. To see this assume, by contrast, that the solution implies for instance $W_{h\ell}^A(q) < W_{h\ell}^B(q)$. Then, $W_{h\ell}^A(q)$ is not relevant for the *IC* constraint of any of the high-career couples; when an *hh* couple mimics a *h\ell* couples it will always claim to be of type *B*. But then we can slightly decrease the tax by *h\ell* couples in group *A* and increase the taxes equally in all other groups to maintain budget balance. This will not affect the incentive constraints and since *h\ell* couples in group *A* are the ones with the lowest utility, it is plain that social welfare increases.

Proceeding like in Appendix A.6 we can show that the FOC with respect to c_p^{gk} is given by

$$\int_0^{\hat{q}^{gk}} \Psi'(\cdot) \left[y - v'(1 - c_p^{gk}) + \beta v'(c_p^{gk}) \right] f^k(q) dq + \int_{\hat{q}^{gk}}^{Q^k} \Psi'(\cdot) \gamma F^k(\hat{q}^{gk}) f^k(q) dq - \hat{\lambda} p F^k(\hat{q}^{gk}) + \mu^k \left[\gamma^k F^k(\hat{q}^{gk}) - y + v'(1 - c_p^{gk}) - \beta v'(c_p^{gk}) \right] = 0. \quad (\text{A.16})$$

while the FOCs with respect to the transfers $T_{h\ell}^k$, $k = A, B$, and $T_{hh}^A = T_{hh}^B = T_{hh}$ are:

$$-E_{h\ell}^k[\Psi'] F^k(\hat{q}^{gk}) + \mu^k + \hat{\lambda} F^k(\hat{q}^{gk}) = 0 \quad (\text{A.17})$$

$$\begin{aligned} -E_{hh}^A[\Psi'] [1 - F^A(\hat{q}^{gA})] - \mu^A + \hat{\lambda} [1 - F^A(\hat{q}^{gA})] \\ -E_{hh}^B[\Psi'] [1 - F^B(\hat{q}^{gB})] - \mu^B + \hat{\lambda} [1 - F^B(\hat{q}^{gB})] = 0 \end{aligned} \quad (\text{A.18})$$

Combining (A.17) for $k = A, B$ with (A.18) yields

$$\hat{\lambda} = \sum_{k=A}^B \left\{ E_{h\ell}^k[\Psi'] F^k(\hat{q}^g) + E_{hh}^k[\Psi'] [1 - F^k(\hat{q}^{gk})] \right\} = E[\Psi'] \quad (\text{A.19})$$

Substituting for $\hat{\lambda}$ and μ^k from (A.19) and (A.17) into (A.16) then yields

$$\begin{aligned} E_{h\ell}^k[\Psi'] F^k(\hat{q}^{gk}) [y - v'(1 - c_p^{gk}) + \beta v'(c_p^{gk})] + \gamma^k F^k(\hat{q}^{gk}) E_{hh}^A[\Psi'] (1 - F^k(\hat{q}^{gk})) - E[\Psi'] y F^k(\hat{q}^{gk}) \\ + \left[E_{h\ell}^k[\Psi'] F^k(\hat{q}^{gk}) - E[\Psi'] F(\hat{q}^{gk}) \right] \left[\gamma^k F(\hat{q}^{gk}) - y + v'(1 - c_p^{gk}) - \beta v'(c_p^{gk}) \right] = 0. \end{aligned}$$

Simplifying and rearranging then successively yields

$$\begin{aligned} & \gamma^k F(\hat{q}^{gk}) E_{hh}^k[\Psi'](1 - F^k(\hat{q}^{gk})) + \gamma^k F^k(\hat{q}^{gk}) E_{hl}^k[\Psi'] F^k(\hat{q}^{gk}) - E[\Psi'] y F^k(\hat{q}^{gk}) \\ & + [-E[\Psi'] F^k(\hat{q}^{gk})] \left[\gamma^k F(\hat{q}^{gk}) - y + v' \left(1 - c_p^{gk} \right) - \beta v' \left(c_p^{gk} \right) \right] = 0, \end{aligned}$$

$$\begin{aligned} & \gamma^k F^k(\hat{q}^{gk}) E^k[\Psi'] - E[\Psi'] y F^k(\hat{q}^{gk}) \\ & + [-E[\Psi'] F^k(\hat{q}^{gk})] \left[\gamma^k F^k(\hat{q}^{gk}) - y + v' \left(1 - c_p^{gk} \right) - \beta v' \left(c_p^{gk} \right) \right] = 0, \end{aligned}$$

$$\begin{aligned} & \gamma^k E^k[\Psi'] - E[\Psi'] y \\ & + [-E[\Psi']] \left[\gamma^k F^k(\hat{q}^{gk}) - y + v' \left(1 - c_p^{gk} \right) - \beta v' \left(c_p^{gk} \right) \right] = 0, \end{aligned}$$

$$\begin{aligned} & \gamma^k E^k[\Psi'] \\ & + [-E[\Psi']] \left[\gamma^k F^k(\hat{q}^{gk}) + v' \left(1 - c_p^{gk} \right) - \beta v' \left(c_p^{gk} \right) \right] = 0, \end{aligned}$$

$$\begin{aligned} & \gamma^k E^k[\Psi'] - \gamma^k E[\Psi'] \\ & + [-E[\Psi']] \left[\gamma^k F^k(\hat{q}^{gk}) - \gamma^k + v' \left(1 - c_p^{gk} \right) - \beta v' \left(c_p^{gk} \right) \right] = 0, \end{aligned}$$

and finally

$$v' \left(1 - c_p^{gk} \right) - \beta v' \left(c_p^{gk} \right) = (1 - F^k(\hat{q}^{gk})) \gamma^k + \gamma^k \frac{E^k[\Psi'] - E[\Psi']}{E[\Psi']},$$

which is (38).

A.10 General specification of the norm

In our earlier paper, we considered a social norm based on the behavior of the median mother in the female population and we added an appendix dealing with a general specification of the norm, which includes *average* and *median* as special cases. We have used the *average* norm in this paper because with that specification a (Pigouvian) linear subsidy is sufficient to achieve the first best when only efficiency matters. This implies that we have a clear benchmark against which we can assess the impact of redistributive considerations. In our earlier paper where only efficiency matters we show that with a norm based on the *median*, the optimal linear subsidy is already below the Pigouvian level. So using the *median* norm in our current analysis would imply that redistributive concerns exacerbate distortions already existing when only efficiency matters. This would make the expressions less transparent, while the main point, namely that in the linear case redistribution reduces the subsidy, continues to go through. As a matter of fact the result holds for any norm specification where the norm cost is given by

$$\gamma(\max\{0; c^T - c_f\});$$

where the “target level” c^T is given by:

$$c^T = K(F(\hat{q}))c_f, \quad (\text{A.20})$$

so that it depends both on the share of traditional mothers and on the amount of their informal child care.³⁴ When $K(F) = F$ we obtain the *average* norm and the norm cost is $\gamma F(\hat{q})c_f$. When instead $K(F) = 0$ for $F \leq 1/2$ and $K(F) = 1$ for $F > 1/2$ we obtain the *median* norm and the norm cost, for $F \geq 1/2$, is γc_f .

We have established in Section 7 that a nonlinear policy brings us back to the Pigouvian rule for the child-care subsidy. We show below that this result does not depend on the specification of the norm. In particular, it continues to hold for the median norm.

To see that, consider again the FOC of the government program with respect to formal child care for traditional couples, c_p^g , derived in (27) which holds for a given \hat{q} . Replacing the average by the median is the same as redefining γ such that

$$\gamma^M = \frac{\gamma}{F(\hat{q})},$$

where the superscript M refers to the *median* and where the denominator reflects the property that, with $\bar{c} = c^M F(\hat{q})$,

$$\frac{\partial c^M}{\partial c_f} = \frac{\partial \bar{c}}{\partial c_f} \frac{1}{F(\hat{q})},$$

where $c_p^g = 1 - c_f$.

Substituting γ by γ^M in equation (29) we obtain

$$s^g = \frac{[1 - F(\hat{q}^g)]}{F(\hat{q})} \gamma,$$

which is the Pigouvian rule for a median norm; see equation (23) in Barigozzi *et al.* (2018). Any intermediate case with the target level given by (A.20) can be dealt with in a similar way and also yields the Pigouvian rule. As explained in Section 7, this is in line with intuitions: with the nonlinear subsidy a distortion in child care does not relax the incentive constraint and there is no reason to deviate from the Pigouvian rule.

³⁴ As long as $K'(F) < \frac{K(F)}{F}$, that is as long as K is concave.