

Supplementary information to “Role of Polar Phonons in the Photo Excited State of Metal Halide Perovskites”

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Unit cell structures

The exciton binding energies presented in the paper have been calculated using ‘semi-cubic’ unit cells. These structures have been obtained by allowing all atoms to relax (keeping the experimental lattice shape and volume fixed) using damped relaxation algorithms with a $4 \times 4 \times 4$ k-point grid. The bromine and chlorine structures were constructed from the resulting high-symmetry iodine unit cells.

For these structures, in the first step all degrees of freedom were relaxed (including cell shape and volume) at a high energy cut off of 600 eV. Hereafter, a simulated annealing was performed, linearly cooling the structure from 800K to 500K in 50000 steps. Approximately every ~ 1000 steps a snapshot was taken from the trajectory. For these structures the cell shape as well as the internal coordinates were relaxed and the lowest global energy structure was determined.

To confirm that the lowest energy structures for the primitive unit cells were correctly determined, a second molecular dynamics run was started from the first lowest energy structure. The same annealing procedure was used with the volume and cell shapes fixed to those of the yet best structures. More than 15 structures were picked from the MD and fully relaxed (including volume and cell shape). In only two cases, an even lower energy structure than in the first cycle was found, however, these two structures were only 15 meV lower in energy than in the first cycle. We are therefore confident that we have determined the lowest energy structures for the primitive unit cells reliably. Furthermore, all structures were carefully checked for instabilities in the vibrational frequencies and no instabilities were found, whereas virtually all initial structures constructed from experimental data alone exhibited such instabilities, even after careful relaxation. The resulting structures have been attached to this document.

Model dielectric function

A local model dielectric function (ϵ_m) [1] has been used in the BSE calculations to converge the exciton binding energies on dense k-point grids.

$$\epsilon^{-1}(\mathbf{k} + \mathbf{G}) = 1 - (1 - \epsilon_m^{-1}) e^{-\frac{(2\pi|\mathbf{k}+\mathbf{G}|)^2}{4\lambda^2}}$$

A local function makes the screened Coulomb kernel diagonal ($\mathbf{G} = \mathbf{G}'$) in the screened Coulomb potential and allows us to calculate the high resolution plots of Fig. 1 (right) in the paper. The parameter ϵ_m comes from DFPT calculations on a shifted $8 \times 8 \times 8$ k-point grid and the screening length parameter (λ) was fitted to match the diagonal ($\mathbf{G} = \mathbf{G}'$) part of dielectric function from the GW_0 calculations on the shifted $6 \times 6 \times 6$ k-point grid, see Table 1. This approximation is also used in Ref. [2], however in that work a different functional was used. This approximation works very well, in particular in the low energy part as is illustrated in Fig. 1. The imaginary part of the dielectric function calculated with the ‘normal’ GW-BSE matches with the one calculated with the model BSE (mBSE) method. Both calculations were performed using a $4 \times 4 \times 4$ k-point grid with the same KS orbital basis and GW_0 quasiparticle energies.

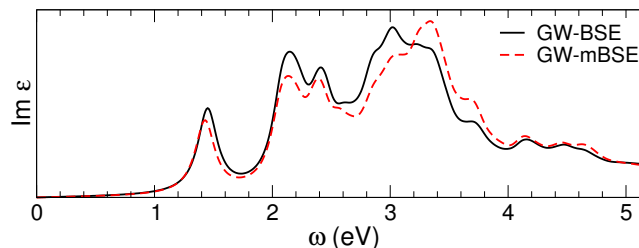


Figure 1: Imaginary part of $\epsilon(\omega)$ calculated with the GW-BSE and GW-(model)BSE method. (MAPbI₃)

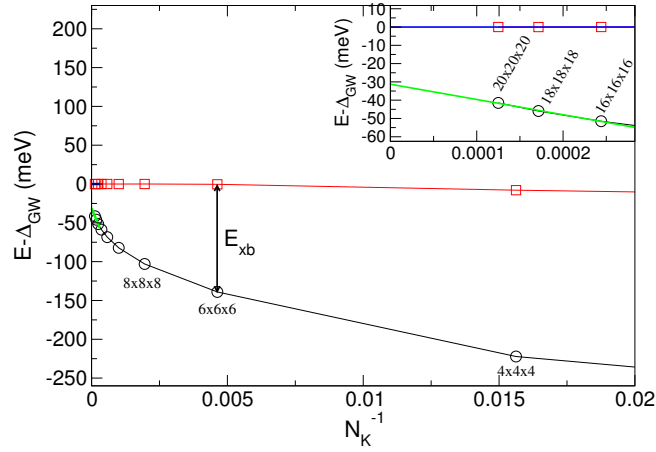


Figure 2: Eigenvalue of the first exciton with e-h interactions (circles) and in the independent particle picture (squares). The exciton binding energy is the difference between these two levels. The inset shows a zoom-in for the levels calculated at dense k-meshes. The green and blue lines are linear fits to the last three data points. (Example: FASnI₃)

Table 1: Parameters of the model dielectric function. Fitted screening length parameter (λ) and the "ion clamped" static dielectric constant (ϵ_∞) calculated using DFPT on a shifted $8 \times 8 \times 8$ k-point grid.

X_3	λ	ϵ_∞
MASnI ₃	1.05	9.18
FASnI ₃	1.05	8.06
FAPbI ₃	1.05	7.10
MAPbI ₃	1.05	6.83
MASnBr ₃	1.13	5.89
FAPbBr ₃	1.13	5.25
MAPbBr ₃	1.13	5.15
FASnBr ₃	1.13	5.32
FAPbCl ₃	1.17	4.27
MAPbCl ₃	1.17	4.22
FASnCl ₃	1.17	4.07
MASnCl ₃	1.17	4.05

K-point convergence

The calculated exciton binding energies have been carefully converged with respect to the k-point grid density. Coarse meshes result in exciton binding energies up to an order too large. The exciton binding energies presented in the paper are the result of a linear extrapolation to an infinite k-point grid[2] as is illustrated in Figure 2.

References

- [1] Bechstedt, F., Sole, R. D., Cappellini, G. & Reining, L. An efficient method for calculating quasiparticle energies in semiconductors. *Sol. State Comm.* **84**, 765 – 770 (1992).
- [2] Fuchs, F., Rödl, C., Schleife, A. & Bechstedt, F. Efficient $\mathcal{O}(N^2)$ approach to solve the bethe-salpeter equation for excitonic bound states. *Phys. Rev. B* **78**, 085103 (2008).

All unit cell structures have been added and formatted as Crystallographic Information File (CIF) files. The CIF formatted files can, for instance, be viewed with the freely available atomic structure visualization package VESTA (<http://jp-minerals.org/vesta/>).

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%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% IODINES %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

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  _atom_site_type_symbol
Pb1      1.0    0.4861    0.4861    0.4875    Biso  1.000000  Pb
I1       1.0    0.5120    0.9835    0.4332    Biso  1.000000  I
I2       1.0    0.9835    0.5120    0.4332    Biso  1.000000  I
I3       1.0    0.4532    0.4532    0.9702    Biso  1.000000  I
C1       1.0    0.9915    0.9915    0.9155    Biso  1.000000  C
N1       1.0    0.0237    0.0237    0.1454    Biso  1.000000  N
H1       1.0    0.9256    0.9256    0.2345    Biso  1.000000  H
H2       1.0    0.1796    0.9924    0.1930    Biso  1.000000  H
H3       1.0    0.9924    0.1796    0.1930    Biso  1.000000  H
H4       1.0    0.0986    0.0986    0.8292    Biso  1.000000  H
H5       1.0    0.0279    0.8258    0.8756    Biso  1.000000  H
H6       1.0    0.8258    0.0279    0.8756    Biso  1.000000  H

```

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%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
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_atom_site_B_iso_or_equiv
_atom_site_type_symbol
Pb1      1.0      0.4738      0.4781      0.4738      Biso  1.000000 Pb
I1       1.0      0.5200      0.9790      0.5200      Biso  1.000000 I
I2       1.0      0.4615      0.4943      0.9772      Biso  1.000000 I
I3       1.0      0.9772      0.4943      0.4615      Biso  1.000000 I
N1       1.0      0.0504      0.0274      0.7929      Biso  1.000000 N
N2       1.0      0.7929      0.0274      0.0504      Biso  1.000000 N
H1       1.0      0.0303      0.8062      0.0303      Biso  1.000000 H
H2       1.0      0.7173      0.1604      0.9959      Biso  1.000000 H
H3       1.0      0.7307      0.9601      0.1837      Biso  1.000000 H
H4       1.0      0.9959      0.1604      0.7173      Biso  1.000000 H
H5       1.0      0.1837      0.9601      0.7307      Biso  1.000000 H
C1       1.0      0.9606      0.9485      0.9606      Biso  1.000000 C

```

%%%

_pd_phase_name 'FASnI3'
_cell_length_a 6.3292
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_cell_length_c 6.3290
_cell_angle_alpha 90
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_cell_angle_gamma 90.0582
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_atom_site_type_symbol
Sn1 1.0 0.3658 0.3658 0.5000 Biso 1.000000 Sn
I1 1.0 0.3458 0.8880 0.5000 Biso 1.000000 I
I2 1.0 0.8880 0.3458 0.5000 Biso 1.000000 I
I3 1.0 0.4175 0.4175 0.0000 Biso 1.000000 I
N1 1.0 0.8438 0.8438 0.1829 Biso 1.000000 N
N2 1.0 0.8438 0.8438 0.8171 Biso 1.000000 N
H1 1.0 0.7296 0.7296 0.1966 Biso 1.000000 H
H2 1.0 0.7296 0.7296 0.8034 Biso 1.000000 H
H3 1.0 0.9081 0.9081 0.3163 Biso 1.000000 H
H4 1.0 0.9081 0.9081 0.6837 Biso 1.000000 H
H5 1.0 0.0347 0.0347 0.0000 Biso 1.000000 H
C1 1.0 0.9119 0.9119 0.0000 Biso 1.000000 C

%%%

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_cell_angle_gamma 90
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_atom_site_B_iso_or_equiv
_atom_site_type_symbol
Sn1 1.0 0.0121 1.0000 0.9084 Biso 1.000000 Sn
I1 1.0 0.5166 1.0000 0.8552 Biso 1.000000 I
I2 1.0 0.9760 1.5000 0.8634 Biso 1.000000 I
I3 1.0 0.0583 1.0000 0.3812 Biso 1.000000 I
C1 1.0 0.5313 0.5000 0.3335 Biso 1.000000 C
N1 1.0 0.4546 1.5000 0.5583 Biso 1.000000 N
H1 1.0 0.7078 0.5000 0.3332 Biso 1.000000 H
H2 1.0 0.4708 0.3552 0.2526 Biso 1.000000 H
H3 1.0 0.4708 0.6448 0.2526 Biso 1.000000 H
H4 1.0 0.2876 1.5000 0.5711 Biso 1.000000 H
H5 1.0 0.5072 1.3644 0.6422 Biso 1.000000 H
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%*****
%*****BROMINES*****
%*****

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  _atom_site_type_symbol
Pb1      1.0      0.3917      0.4790      0.4814      Biso  1.000000  Pb
Br1      1.0      0.3400      0.9781      0.5293      Biso  1.000000  Br
Br2      1.0      0.8885      0.4863      0.4462      Biso  1.000000  Br
Br3      1.0      0.4203      0.4717      0.9842      Biso  1.000000  Br
N1       1.0      0.8268      0.8355      0.8780      Biso  1.000000  N
N2       1.0     -0.0000      0.1176      0.0324      Biso  1.000000  N
H1       1.0      0.9416      0.8247      0.7416      Biso  1.000000  H
H2       1.0      0.9944      0.2311      0.1562      Biso  1.000000  H
H3       1.0      0.7004      0.7260      0.8940      Biso  1.000000  H
H4       1.0      0.1294      0.1187      0.9089      Biso  1.000000  H
H5       1.0      0.7090      0.9833      0.1721      Biso  1.000000  H
C1       1.0      0.8405      0.9790      0.0327      Biso  1.000000  C

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_atom_site_fract_z
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Br1 1.0 0.4842 0.8866 0.5457 Biso 1.000000 Br
Br2 1.0 0.9094 0.3337 0.5134 Biso 1.000000 Br
Br3 1.0 0.4656 0.3372 0.0114 Biso 1.000000 Br
N1 1.0 0.8300 0.7241 0.0364 Biso 1.000000 N
N2 1.0 0.0654 0.9959 0.9873 Biso 1.000000 N
H1 1.0 0.7319 0.7707 0.8896 Biso 1.000000 H
H2 1.0 0.9884 0.0664 0.8363 Biso 1.000000 H
H3 1.0 0.7915 0.5924 0.1363 Biso 1.000000 H
H4 1.0 0.2004 0.0677 0.0470 Biso 1.000000 H
H5 1.0 0.0913 0.7676 0.2609 Biso 1.000000 H
C1 1.0 0.9986 0.8271 0.1001 Biso 1.000000 C

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_atom_site_type_symbol
Pb1 1.0 0.4981 0.5137 0.5544 Biso 1.000000 Pb
Br1 1.0 0.4641 0.0140 0.5118 Biso 1.000000 Br
Br2 1.0 0.9984 0.4798 0.5123 Biso 1.000000 Br
Br3 1.0 0.5376 0.5524 0.0459 Biso 1.000000 Br
C1 1.0 0.0294 0.0463 0.9767 Biso 1.000000 C
N1 1.0 0.9579 0.9736 0.1959 Biso 1.000000 N
H1 1.0 0.9022 0.1095 0.2922 Biso 1.000000 H
H2 1.0 0.8271 0.8420 0.1734 Biso 1.000000 H
H3 1.0 0.0945 0.9184 0.2917 Biso 1.000000 H
H4 1.0 0.8830 0.1078 0.8824 Biso 1.000000 H
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Br2 1.0 0.9929 0.4584 0.8549 Biso 1.000000 Br
Br3 1.0 0.9287 0.9521 0.3312 Biso 1.000000 Br
C1 1.0 0.4480 0.4372 0.3874 Biso 1.000000 C
N1 1.0 0.5097 0.5220 0.1705 Biso 1.000000 N
H1 1.0 0.3732 0.5740 0.4875 Biso 1.000000 H
H2 1.0 0.3217 0.2863 0.3513 Biso 1.000000 H
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%%%%%%%%%%
 %%%%%%%%%%-----CHLORINES-----%%%%%%%%%%
 %%%%%%%%%%

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  _atom_site_B_iso_or_equiv
  _atom_site_type_symbol
Pb1      1.0      0.4260      0.4361      0.4908      Biso  1.000000  Pb
Cl1      1.0      0.3950      0.9283      0.4726      Biso  1.000000  Cl
Cl2      1.0      0.9337      0.4670      0.4726      Biso  1.000000  Cl
Cl3      1.0      0.4226      0.4394      0.0052      Biso  1.000000  Cl
N1       1.0      0.0804      0.0493      0.9393      Biso  1.000000  N
N2       1.0      0.8128      0.7816      0.9393      Biso  1.000000  N
H1       1.0      0.1547      0.9974      0.7806      Biso  1.000000  H
H2       1.0      0.8646      0.7073      0.7806      Biso  1.000000  H
H3       1.0      0.1531      0.1789      0.0243      Biso  1.000000  H
H4       1.0      0.6832      0.7089      0.0243      Biso  1.000000  H
H5       1.0      0.8497      0.0124      0.2073      Biso  1.000000  H
C1       1.0      0.9120      0.9500      0.0350      Biso  1.000000  C
  
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_atom_site_type_symbol
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Cl1 1.0 0.4952 0.9087 0.5428 Biso 1.000000 Cl
Cl2 1.0 0.9145 0.3283 0.5424 Biso 1.000000 Cl
Cl3 1.0 0.4375 0.3857 0.1280 Biso 1.000000 Cl
N1 1.0 0.0522 0.0385 0.0058 Biso 1.000000 N
N2 1.0 0.7851 0.7710 0.0064 Biso 1.000000 N
H1 1.0 0.0063 0.1047 0.8480 Biso 1.000000 H
H2 1.0 0.7185 0.8166 0.8486 Biso 1.000000 H
H3 1.0 0.1736 0.1186 0.0925 Biso 1.000000 H
H4 1.0 0.7053 0.6497 0.0935 Biso 1.000000 H
H5 1.0 0.0000 0.8240 0.2738 Biso 1.000000 H
C1 1.0 0.9477 0.8759 0.1018 Biso 1.000000 C

%%%

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_cell_angle_gamma 94.9603
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_symmetry_Int_Tables_number 1

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_atom_site_fract_x
_atom_site_fract_y
_atom_site_fract_z
_atom_site_adp_type
_atom_site_B_iso_or_equiv
_atom_site_type_symbol
Pb1 1.0 0.5413 0.6291 0.5590 Biso 1.000000 Pb
Cl1 1.0 0.5766 0.1283 0.6028 Biso 1.000000 Cl
Cl2 1.0 0.0404 0.6642 0.6041 Biso 1.000000 Cl
Cl3 1.0 0.5055 0.5917 0.0633 Biso 1.000000 Cl
C1 1.0 0.0099 0.1016 0.1473 Biso 1.000000 C
N1 1.0 0.0837 0.1707 0.9172 Biso 1.000000 N
H1 1.0 0.2230 0.3076 0.9396 Biso 1.000000 H
H2 1.0 0.1375 0.0250 0.8188 Biso 1.000000 H
H3 1.0 0.9406 0.2267 0.8162 Biso 1.000000 H
H4 1.0 0.1627 0.0388 0.2476 Biso 1.000000 H
H5 1.0 0.9487 0.2571 0.2441 Biso 1.000000 H
H6 1.0 0.8641 0.9581 0.1181 Biso 1.000000 H

