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# A NOVEL SOLAR CONCENTRATOR SYSTEM FOR COMBINED HEAT AND POWER APPLICATION IN RESIDENTIAL SECTOR

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## ABSTRACT

The research on photovoltaic conversion is continuously overtaking technological challenges and modern PV cells can nowadays be efficiently combined with solar concentrators. In this paper a new photovoltaic solar concentrator model based on non-imaging optics and embedding high efficiency multi-junctions cells is presented. The concentrator has been optimized to maximize the electricity production but it is thought to work in cogeneration to allow also for thermal energy by recovering the residual heat, since an active cooling system for the cells is necessary. The maximization is performed by applying deformations to standard spherical mirrors in order to manage solar aberrations and reshape the solar spot. The induced deformations solve issues related to the disuniformity of the spot focused at the receiver consisting of a dense array of cells thus boosting the conversion efficiency. The efficiency enhancing is obtained thanks to the high matching between the collected solar irradiance and the receiver electrical features. An analytical study, considering residential utilities has been performed in order to understand the energetic and economic performance of the system. In particular, a simulation has been carried out by the use of an in-house-developed calculation code considering a whole year of operation in order to estimate the electrical and thermal energy which can be produced by the solar concentrator and self-consumed by the utilities. Further, the maximum capital cost of the system has been estimated in order to achieve a return of the investment in ten or twelve years.

**Keywords:** Renewable Energy; Solar Concentration; Non Imaging Optics; Combined Heat and Power; Feasibility Study

## NOMENCLATURE

### Abbreviation

AB	Auxiliary Boiler
CC	Compression Chiller
CPV	Concentrating Photovoltaic
CHP	Combined Heat and Power
ES	Electrical Storage
ICE	Internal Combustion Engine
MGT	Micro Gas Turbine
MJ	Multi-Junction
MRC	Micro Rankine Cycle
SC	SOLARIS Concentrator
SE	Stirling Engine
SO	Secondary Optic

### Symbols

C	Capital Cost [€]
DNI	Direct Normal Irradiance [kW/m <sup>2</sup> ]
E	Energy [kWh]
F	Cash Flow [€]
FFS	Fossil Fuel Saving [kWh]
<i>i</i>	Discount Rate [-]
M	Mass [Sm <sup>3</sup> ]
n	Year
NPV	Net Present Value [€]
$\eta$	Efficiency [-]
$\zeta$	Specific Cost [€/kWh or €/Sm <sup>3</sup> ]

73	
74	<i>Subscripts and Superscripts</i>
75	EL Electrical
76	g Natural Gas (fuel)
77	R Reference
78	TH Thermal
79	u Utility

## 80 1. INTRODUCTION

81 The renewable electricity production increased rapidly during the last decades, but the yearly installed capacity of  
82 Concentrating Photovoltaic (CPV) systems [1] had a significant increasing only during the last few years [2]. The crucial driver  
83 of this trend is the development of multi-junction (MJ) solar cells with efficiency higher and higher. Despite MJ cells are mainly  
84 addressed to powering satellites, cost effectiveness for terrestrial use has been demonstrated when they are employed  
85 together with solar concentration [3] especially in very insulated environments or off-grid communities. Currently, a record  
86 efficiency above 45% has been obtained for terrestrial type cells [4]. Among the concentrating systems commercially available  
87 embedding MJ cells, the dense array systems consist in a large reflective element (called dish) focusing the light over an module  
88 of cells arranged one beside the other and electrically connected (mainly in series) to form a single PV receiver. As in the more  
89 diffused single cell point focus systems represented by the Fresnel lens based devices [5-7], the whole mechanical structure  
90 has to accurately track the sun during its daily motion and to make the light rays exactly converging onto the focal plane. To  
91 reproduce defined concentration level and spot shape, a mosaic of low cost flat mirrors mounted on a unique frame is often  
92 employed. Mirrored dishes with diameters ranging from few to tens of meters have been developed and commercialized  
93 during the last ten years working at typical concentration of 500 suns [8-10] even if recent studies shown a good prospective  
94 of increasing the concentration factor towards 1000 suns and beyond [11]. Advantages of the reflective optics are the lack of  
95 chromatic aberration, which gives an higher optical efficiency if compared to systems embedding lenses, a lower cell operating  
96 temperature caused by the necessary active cooling and the possibility to cogenerate both heat and current given by the  
97 cooling system itself. Another advantage, when compared to other CPV technologies, is in the possibility to remove the receiver  
98 in case of cleaning, testing or in case of maintenance and, as solar cell technology improves, to upgrade the whole PV system  
99 by replacing the receiver with an higher efficiency device at very low cost.

100 As the conversion efficiency is the main driver of the CPV technology economic sustainability, an important issue in projecting  
101 dense array systems is represented by the irradiance distribution over the array, a problem widely discussed in bibliography  
102 for single cell systems [12] but less investigated for dense arrays [13, 14]. A non-uniform irradiance pattern could severely  
103 worsen the receiver electrical performance thereby reducing the efficiency. The current produced by the worst illuminated cell  
104 limits the series output current. The cell can be also subject to an overheating due to the dissipation of extra current from  
105 other cells and can eventually break out. The irradiance pattern should rather be as uniform as possible and, at the same time,  
106 the spot shape should resemble the typical rectangular/square shape of the array to prevent spillage losses. Flux uniformity  
107 and spot reshaping are theoretically possible by redesigning the optics of a concentrator using non-imaging optics [15], by  
108 approximating standard imaging mirrors with an array of flat elements, as commonly done in the dishes [16], and/or by adding  
109 secondary optics (SOs) to tailor the flux delivered by the dish [17, 18]. At present, no commercial systems seems to embed SOs  
110 coupled with dense arrays.

111 A CPV dense array concentrator model based on a new optical concept has been briefly described in this work [19]. The design  
112 method used has been conceived to reduce the current mismatch problem by acting on the optical part. The simulation results  
113 shows both high irradiance uniformity and high concentration at the focal plane so that the nominal conversion efficiency of  
114 the receiver almost equals the performance of the embedded cells. The proposed system has been evaluated with a series of  
115 simulations in order to understand its potential as renewable micro-CHP generator with reference to residential utilities. The  
116 electrical and thermal energy production and the maximum sustainable capital cost of the system have been calculated and  
117 will be discussed in the next sections of this paper.

## 118 2. THE SOLARIS CONCENTRATOR MODELING

119 The SOLARIS concentrator [19] has been conceived as a single stage multi-dish reflective optics made by mirrors: seven mirrors  
120 substitute the traditional segmented dish, focusing the light at the same point so that the final illumination pattern impinging  
121 on the receiver results from the sum of the single incoherent illumination produced. Each mirror is a free-form optics, a type  
122 of optics often used for solving the prescribed irradiance problem in lenses of limited dimensions often used as SOs. The design  
123 guideline is to introduce controlled deformations into originally spherical mirrors in order to degrade the solar image thus  
124 obtaining a square spot with prescribed and highly uniform irradiance distribution. Since an accurate imaging formation is not  
125 necessary for a concentrator to work, the radiation bundle redistribution aims at maximizing the conversion efficiency by  
126 matching the spot with receiver features.

127 The system optical/electrical modelling has been carried out with an end-to-end code written on purpose in Interactive Data  
128 Language IDL<sup>®</sup> based on analytical models for both the optics and the receiver including two main subgroups of routines for  
129 individually simulating each part. A third group of procedures calculates the tolerances for the optical/mechanical parameters.  
130 As for the optics, all mirrors have been simulated and designed implementing in the code a well-known analytical model of  
131 aberrations based on the Zernike polynomials [20]. Considering a single spherical mirror, a preliminary optical analysis showed  
132 that very few deformations associated by coefficients to the Zernike modes, can boost the irradiance uniformity starting from  
133 the intrinsically circular solar image (Figure 1). For a single spherical mirror focusing on axis we identified three polynomials:  
134 the 4th, the 11th and the 14th, corresponding precise deformations to be applied to a mirror working defocused as shown in  
135 Table 1. Then, we extended the method to a multi-mirror system, including off-axis mirrors distributed on an hexagonal frame  
136 and other polynomials. Ray tracing techniques have been implemented to simulate and optimize simultaneously all the  
137 reflective surfaces. Each step of the optical modeling and the results have been further checked with the optical design  
138 software Zemax<sup>®</sup> as reference.

139 The receiver has been analytically designed and numerically simulated using a datasheet of commercially available MJ cells  
140 3C40 produced by AZUR SPACE [21] with 39% nominal efficiency at 500 suns at ambient temperature. The electrical scheme  
141 employs series/parallels standard electrical connections. Since the cells include busbars, part of the concentrated light will  
142 necessary impinge on the these inactive areas: the nominal efficiency considering the cell embedded in a dense array is thus  
143 reduced to around 33%. This new value has to be also accounted as the maximum efficiency theoretically obtainable by an  
144 array made with this specific cells.

145 The concentrator has been dimensioned as a power system suitable for the market of medium residential contexts or small  
146 farms, then for a production of around 10 kW<sub>EL</sub>. The diameter of the single mirror has been set 2.6 m, for a system total size of  
147 about 7.8 m and a resulting total optical area slightly bigger than 35 m<sup>2</sup>. Supposing a standard test direct irradiance of 1 kW/m<sup>2</sup>  
148 (1 sun), the collected power will be around 35 kW: with an ideal receiver working at the efficiency of the considered cells, such  
149 a system would deliver more than 10 kWe. The detector distance has been set to 4.8 m in order to have a detector distance to  
150 total diameter ratio (parameter similar to the focal ratio in imaging systems) of 0.6. In general, small focal ratios are preferred  
151 by concentrator designs despite of the higher aberrations introduced in order to achieve high concentration and mechanical  
152 structure compactness.

### 153 3. EFFICIENCY OPTIMIZATION AND PERFORMANCE ANALYSIS

154 The concentrator has been optimized for an average concentration of 500 suns where the cell efficiency curve has a maximum.  
155 Figure 2 depicts the mechanical model of the system and a zoom of the focal zone, where the receiver electrical scheme has  
156 been superimposed to the irradiance pattern simulated after the optimization. The narrow rectangles in figure are strings of  
157 cells series connected. Groups of strings are then parallel connected(not shown in figure) to ensure small parallel mismatches  
158 and to obtain high voltage and small current in output. This condition is always imposed to avoid excessive current dissipation.  
159 The electric model used has ideally no dependence from temperature and spectral variation. Since we deal exclusively with  
160 reflective elements no chromatic aberration is introduced, so the last assumption is realistic. The temperature can also be  
161 considered reasonably constant as efficient cooling systems have been already investigated, as shown in literature [22, 23].

162 The performance curves of the system are presented from Figure 3 to Figure 6. In particular, Figure 3 shows both the power  
163 collected by the concentrator (input power) and the light effectively impinging on the array (collected power). It should be  
164 observed that, at this stage, no model for the bypass diode has been implemented. The mirrors shapes optimized to maximize  
165 the efficiency of this receiver gives a uniform irradiance pattern over the 80% of the total power focused (red zone in Figure  
166 2).

167 The net produced electrical and thermal powers are presented in Figure 4. It can be observed from the figure that the trend of  
168 the curves is linear with the variation of the direct normal irradiance, varying from zero to about 10.4 kW<sub>EL</sub> and 22.8 kW<sub>TH</sub>  
169 respectively for what regards the electrical and thermal power output of the SOLARIS concentrator.

170 Due to the high matching between light and cells, the receiver shows an effective electrical conversion efficiency (see Figure 5  
171 a), defined as the ratio between the electrical produced power and the total input power, equal to 29.4% with a value of direct  
172 normal irradiance equal to 1.0 kW/m<sup>2</sup>. The relative efficiency calculated as the ratio between the electrical produced power  
173 and the only impinging power on the receiver (collected power), rises up to 31.2% always with reference to 1 kW/m<sup>2</sup> of direct  
174 normal irradiance. This value has to be compared with the 33% nominal performance obtainable for the receiver made with  
175 the cells considered (and shows that almost all the cells in the receiver are working approximately at their theoretical  
176 maximum. As can be easily understood, the electrical efficiency of the system depends on the value of direct normal irradiance:  
177 for instance, in case of a value of DNI equal to 0.1 kW/m<sup>2</sup>, the electrical efficiency reduces to 27.4%. This evidence clearly  
178 highlights that the electrical efficiency trend is quite constant with the change in irradiance. Further, the thermal efficiency of  
179 the system (Figure 5) shows a variation from 66.8% (in case of DNI equal to 0.1 kW/m<sup>2</sup>) to 64.8% (with reference to DNI equal  
180 to 1.0 kW/m<sup>2</sup>). The reduction of the thermal efficiency with the increase of the direct normal irradiance can be explained  
181 considering the increase of electrical efficiency. This evidence allows to affirm that also this parameter does not show heavy  
182 changes with the irradiance variation.

183 The total amount of fossil fuel saving (FFS) due to use of SOLARIS concentrator as function of the direct normal irradiance can  
184 be estimated by considering the following relationship:

$$186 \quad FFS = \frac{E_{EL}}{\eta_{EL,R}} + \frac{E_{TH}}{\eta_{TH,R}} \quad (1)$$

187 where  $E_{EL}$  and  $E_{TH}$  are respectively the net electrical and thermal produced energy (with reference to one hour of  
188 operation) of the system, while  $\eta_{EL,R}$  and  $\eta_{TH,R}$  are the electrical and thermal efficiency chosen as reference to compare the  
189 SOLARIS concentrator, in CHP application, with the separate generation of electricity and heat. In this study, a reference value  
190 for the electrical and thermal efficiency respectively 47.6% and 80.0% have been selected [24].

191 Further the avoided emissions of CO<sub>2</sub> can be estimated, by assuming that 2.75 kg of CO<sub>2</sub> are produced per 1 kg of burned CH<sub>4</sub>.  
192 The results of FFS and CO<sub>2</sub> avoided emissions are respectively presented in Figure 6 and in Figure 7. From these figures it can  
193 be observed that, by assuming the nominal performance DNI equal to 1.0 kW/m<sup>2</sup>, the achieved saving in fossil fuel and the  
194 corresponding CO<sub>2</sub> prevented emissions are respectively equal to about 50 kWh and 10 kg.

195 Finally, the nominal performance of the SOLARIS concentrator have been compared to the design electrical and thermal  
196 efficiency of a large number of existing and consolidated technologies usually adopted in CHP application with a produced  
197 electrical power equal or lower than 100 kW, such as internal combustion engines (ICE), micro gas turbines (MGT), Stirling  
198 engines (SE) and micro Rankine cycle (MRC) [25]. The result of the comparison is presented in Figure 8: it can be observed that  
199 the electrical and thermal efficiency of the SOLARIS concentrator can be compared with the internal combustion engines  
200 actually on the market.  
201

#### 202 4. CALCULATION MODEL AND ASSUMPTIONS

203 In order to estimate the performance of the system in Figure 2, under both the energetic and economic point of view, a  
204 parametric analysis has been developed by varying the number of residential utilities served by the solar concentrator. More  
205 in details, the SOLARIS concentrator has been included into a grid, connected to the national electric distribution network, with  
206 the aim of producing electrical, thermal and cooling energy for a group of residential utilities. In Figure 9 a schematic of the  
207 simulated grid is shown, including the SOLARIS concentrator in CHP application, an auxiliary boiler and a compressor chiller.  
208 Further, as it can be seen from the figure, an (i) electrical storage system and a (ii) thermal storage tank have been included in  
209 the calculation in order to minimize the exchange of electrical energy with the grid and the consumption of the fuel for the  
210 boiler. In particular for what regards the storage efficiency of electrical energy an average value of 60% was taken into account.  
211 An in-house-developed calculation code has been developed in Excel VBA environment with the aim of estimating the energetic  
212 and the economic performance of the grid in Figure 9. The developed code is a mixed numerical-empirical tool, based on a  
213 lumped model approach. Each system component is considered as a black box, with a reduced number of key parameters,  
214 simulated with characteristic performance curves. These curves are obtained, when available, from experiments, or from  
215 physical modeling equations. The main input of the model are: (i) the user demand time profiles, (ii) the operating boundary  
216 conditions (ambient conditions, geographical position, etc.), (iii) the regulation strategy and the (iv) components parameters.  
217 The main output of the model are the energy fluxes, the efficiencies of each components and the economic performance of  
218 the SOLARIS concentrator.

219 For each domestic utilities, the following assumptions have been taken into account: (i) yearly required electrical, thermal and  
220 cold energy equal respectively to 3200 kWh, 20000 kWh and 3500 kWh (corresponding to about 1000 kWh of electrical energy)  
221 [26]. More in details, the electrical, thermal and cooling load of each household has been estimated for an entire year with  
222 reference to 8760 hours. The adopted electrical load curve is the result of the overlap of the various appliances which, in  
223 average, can be found in an Italian house; lighting, computer sites, cold and hot appliances, cleaning appliances, and audiovisual  
224 sites, were considered; also the stand-by mode was taken into account for the estimation of the electrical load curve. The  
225 thermal load curve, instead, is the sum of space heating and hot water demand; it was assumed that hot water demand is  
226 almost constant during the entire year being not influenced by the ambient air temperature or by the season, while the space  
227 heating demands is strictly dependent on the external temperature. More details on the household load profile can be found  
228 in [27].

229 The solar radiation has been estimated according to a latitude equal to 44.51 deg and longitude to 11.35 deg (corresponding  
230 to Bologna location) [28]. This calculation has been carried out by means of a routine, which is able to estimate (considering  
231 an entire year of operation – 8760 hours) the position of the sun, the direct and diffused radiation components incident on a  
232 horizontal surface, the direct, diffused and reflected radiation components incident on the SOLARIS concentrator. More details  
233 about the adopted physical-mathematical model can be found in an Authors' previous work [29].

234 Finally, the performance of the solar concentrator have been calculated on the basis of the curves in Figure 3, in Figure 4, and  
235 in Figure 5, while the batteries behavior is performed considering non-dimensional curves related to main parameters (i.e.  
236 maximum power in charging mode or in discharging mode, battery voltage, etc.) as function of the state of charge (SOC). Once  
237 the battery storable energy is defined, the main parameters can be estimated by means of curves obtained by interpolating  
238 the main characteristics of a wide range of batteries available on the market [30].

239 **5. ENERGETIC PERFORMANCE EVALUATION**

240 With reference to the scheme in Figure 9, the SOLARIS concentrator produced and the self-consumed electrical energy amounts  
241 are presented in Figure 10, as function of the number of considered utilities. In this figure, also the electrical energy purchased  
242 from the network is drawn. Further, the ratio of the self-consumed electrical energy to (i) the total amount of energy produced  
243 by the SOLARIS concentrator and to (ii) the electrical energy required by the considered utilities is drawn in Figure 11. In the  
244 same figure, the ratio between the electrical energy purchased from the network and the total amount of energy required by  
245 the utilities is also presented.

246 From Figure 4, it can be seen that being constant the SOLARIS concentrator produced electrical energy, the amount of self-  
247 consumed energy increases with the number of served utilities. The self-consumed energy is the sum of the fraction of SOLARIS  
248 concentrator produced energy which is directly sent to the utilities and of the energy initially stored into the batteries and then  
249 used to cover the energy demand. Also the total amount of energy purchased from the national distribution network, as  
250 expected, increases with the number of utilities: it should be noted that in case of one or two utilities this value is equal to  
251 zero, while increases up to about 2000 kWh/year and to slightly less than 10000 kWh/year respectively in case of three and  
252 five utilities (see Figure 10). With reference to Figure 11, the previous considerations allows to highlight that the SOLARIS  
253 concentrator can completely satisfy the electrical needs in case of one or two utilities and covers about the 84% of the  
254 electricity demand if three utilities are connected. The remaining fraction of the electricity demand (16%) is then covered by  
255 purchasing energy from the national distribution network. The ratio between self-consumed energy and demand decreases to  
256 the 53% in case of five considered utilities.

257 On the other side, considering the ratio between the self-consumed electrical energy and the total amount of electrical energy  
258 produced by the SOLARIS concentrator, it can be noted that this value is equal to 29% and to 53% in case of one and two  
259 utilities. The 73% of produced electrical energy is instead self-consumed if three utilities are taken into account. This  
260 percentage, for a number of utilities greater than three, slightly increases reaching a value of 75% and 77% respectively in case  
261 of four and five utilities. Always referring to the scheme in Figure 9, it can be observed that the remaining amount of the  
262 produced energy is stored into batteries without being used for the utilities or it is lost due to their storage efficiency. On this  
263 regard, the graph in Figure 12 shows the total amount of electricity sent to the batteries by dividing it between (i) the fraction  
264 used for the utilities demand, (ii) the losses and (iii) the stored energy which is not used. It can be observed from the figure  
265 that this last fraction becomes equal to zero if three utilities or more are taken into account. Further, as expected, the total  
266 energy sent to the batteries decreases with the increase of the utilities units.

267 For what concerns the utilities heat demand for space heating and hot water production, in Figure 13 the SOLARIS concentrator  
268 produced and the self-consumed thermal energy is presented as function of the number of considered utilities. Also the  
269 auxiliary boiler production is presented in this figure. Further, as already presented for the electrical energy, the ratio of the  
270 self-consumed thermal energy to (i) the total production of SOLARIS concentrator and to (ii) the utilities demand is drawn in  
271 Figure 14. In this case it can be observed that, unless the case with only one utility, the SOLARIS concentrator thermal  
272 production is not able to cover the heat demand of every utilities. Also in this case (see Figure 9), the self-consumed energy is  
273 equal to the sum of the term directly sent from the SOLARIS concentrator to the utilities and of the energy initially stored and  
274 then used in a later time. It can be noted, that in this case the losses of the thermal storage are negligible respect to the  
275 electrical storage losses: this explains why the produced energy and the self-consumed terms (Figure 13) appear almost  
276 coincident for a number of utilities equal or greater than two. In other words (Figure 14) the 100% of the SOLARIS concentrator  
277 thermal production can be recovered to partially cover the heat demand of two or more utilities. For instance, with three  
278 utilities, the SOLARIS concentrator allows to satisfy the 56% of the total demand, while the auxiliary boiler covers the remaining  
279 44%. The boiler contribution rises up to the 66% of the heat demand in case of five utilities.

280 The above considerations make it possible to identify as three the number of utilities that will optimize the energy flows in  
281 order to maximize the self-consumed thermal and electrical energy, on one side, and to minimize both the purchasing from  
282 the national distribution network and the use of the boiler, on the other side. In fact, it can be considered that with two utilities  
283 a fraction of the electrical energy stored into the batteries is not used to satisfy the demand (see Figure 12), while with four  
284 utilities the boiler should cover slightly less than the 60% of the heat demand (see Figure 14).

285 **6. ECONOMIC ANALYSIS**

286 The economic analysis was conducted in order to identify the maximum capital cost that can be paid off in ten or in twenty  
287 years. More in details, for each of the analyzed cases was estimated the annual savings achievable by the non-purchase of  
288 electricity and gas to the boiler.

289 By considering the following relationship:

290  
291 
$$NPV = -C + \sum_{n=1}^{n_{max}} \frac{F_n}{(1+i)^n} \tag{2}$$

292 being:  
293

294  $NPV$ : net present value;  
 295  $C$ : capital cost;  
 296  $F_n$ : annual cash flow;  
 297  $n_{max}$ : maximum year of operation (equal to 10 or to 20)  
 298  $i$ : discount rate.

300 The maximum capital cost can be calculated by equating to zero the above expression; it follows:

$$302 \quad C_{max} = \sum_{n=1}^{n_{max}} \frac{F_n}{(1+i)^n} \quad (3)$$

304 where the cash flow can be expressed as:

$$306 \quad F_n = (E_{EL,u} - E_{EL}) \cdot \zeta_{EL} + (M_{g,u} - M_g) \cdot \zeta_g \quad (4)$$

308 being:

310  $E_{EL,u}$ : the total electrical energy required by the utilities [kWh];  
 311  $E_{EL}$ : the total electrical energy produced by the SOLARIS concentrator system and self-consumed by the utilities [kWh];  
 312  $M_{g,u}$ : the total amount of natural gas used in the boiler to produce the yearly thermal energy demand of the utilities [Sm<sup>3</sup>];  
 313  $M_g$ : the amount of natural gas burned into the boiler when the SOLARIS concentrator is used [Sm<sup>3</sup>];  
 314  $\zeta_{EL}$ : the cost of electrical energy [€/kWh];  
 315  $\zeta_g$ : the cost of natural gas [€/Sm<sup>3</sup>].

317 For this analysis, the cost of electrical energy and natural gas were chosen respectively 250 €/MWh and 0.45 €/Sm<sup>3</sup>. Further,  
 318 the discount rate was assumed to be 8%. The results of the economic analysis are presented in Figure 15.

319 The results show that a capital cost equal to about 31'000 € (10 years) or slightly lower than 46'000 € (20 years) can be achieved.  
 320 From the figure it can be observed that the increase in the maximum capital cost becomes negligible with a number of utilities  
 321 greater than three. In fact, with reference to 3 utilities, the maximum sustainable capital cost of the system is equal to about  
 322 30'000 € in case of 10 years of return of the investment or 44'000 if 20 years are taken into account. This last evidence confirms  
 323 that three utilities are the optimum choice under both the energetic and the economic point of view.

324 Further, it should be taken into account that in many country, such as Italy, the production of electrical energy from renewable  
 325 source is strongly incentivized. This additional economic advantage can obviously increase, depending on its amount, the values  
 326 presented in Figure 15.

327 This last analysis clearly indicates that the development of renewable generators and consequently of storage systems could  
 328 have a market in household sector only if the costs of these technologies will show a sensible decrease in the next upcoming  
 329 years.

## 330 7. CONCLUDING REMARKS

331 In this study, a new concept of photovoltaic solar concentrator based on non-conventional mirrors coupled with high efficiency  
 332 triple-junctions cells has been analyzed and discussed. An analytical study considering residential utilities has been performed  
 333 in order to assess the energetic and economic performance of the system. Results suggest that the proposed system can  
 334 optimize the electrical and thermal fluxes in case of 3 residential utilities minimizing the exchange of electrical energy with the  
 335 grid and allowing the total recovery of the produced thermal energy. The economic analysis which has been developed  
 336 indicates that the maximum sustainable capital cost of the system ranges between 30'000 € and 44'000 € depending on the  
 337 years which are considered for the return of the investment.

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## FIGURE CAPTIONS

**Figure 1.** Effects introduced in the solar image by the indicated polynomials

**Figure 2.** Mechanical shaded model of the SOLARIS concentrators and zoom of the focal zone showing the irradiance pattern and the receiver scheme

**Figure 3.** Power collected by the concentrator (input power) and the light effectively impinging on the array (collected power) of the SOLARIS concentrator as function of DNI at the collector aperture

**Figure 4.** Produced electrical and thermal power of the SOLARIS concentrator as function of DNI at the collector aperture

**Figure 5.** Net thermal (a) and electrical (b) efficiency of the SOLARIS concentrator as function of DNI at the collector aperture

**Figure 6.** Fossil fuel saving of the SOLARIS concentrator as function of DNI at the collector aperture

**Figure 7.** CO<sub>2</sub> avoided emissions of the SOLARIS concentrator as function of DNI at the collector aperture

**Figure 8.** Thermal efficiency vs electric efficiency for micro CHP technologies compared to SOLARIS concentrator

**Figure 9.** Schematic of the simulated grid including the SOLARIS concentrator

**Figure 10.** SOLARIS concentrator produced electrical energy, self-consumed for the utilities and purchased from the network

**Figure 11.** Electrical energy balance

**Figure 12.** Energy balance of batteries

**Figure 13.** SOLARIS concentrator produced thermal energy, self-consumed for the utilities and produced from the boiler

**Figure 14.** Thermal energy balance

**Figure 15.** SOLARIS concentrator maximum sustainable capital cost as function of the number of served utilities

423 **TABLE CAPTIONS**

424 **Table 1.** 2D and 3D representations of the main polynomials involved in the modelling

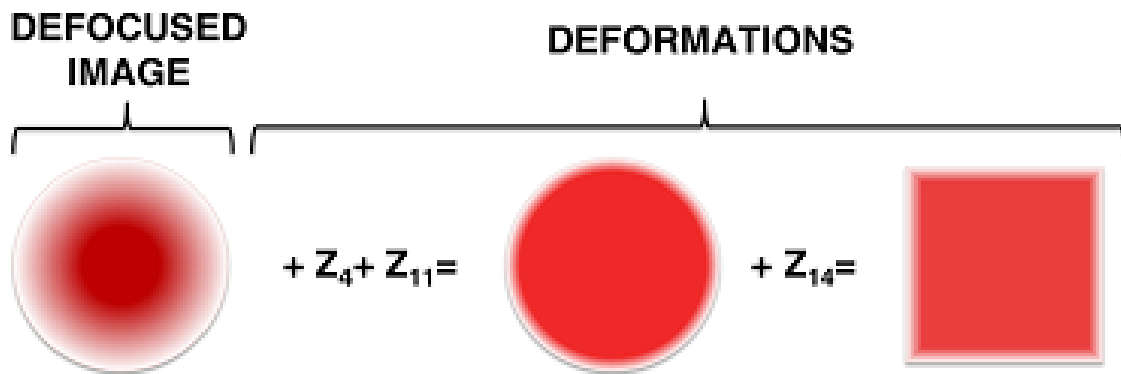
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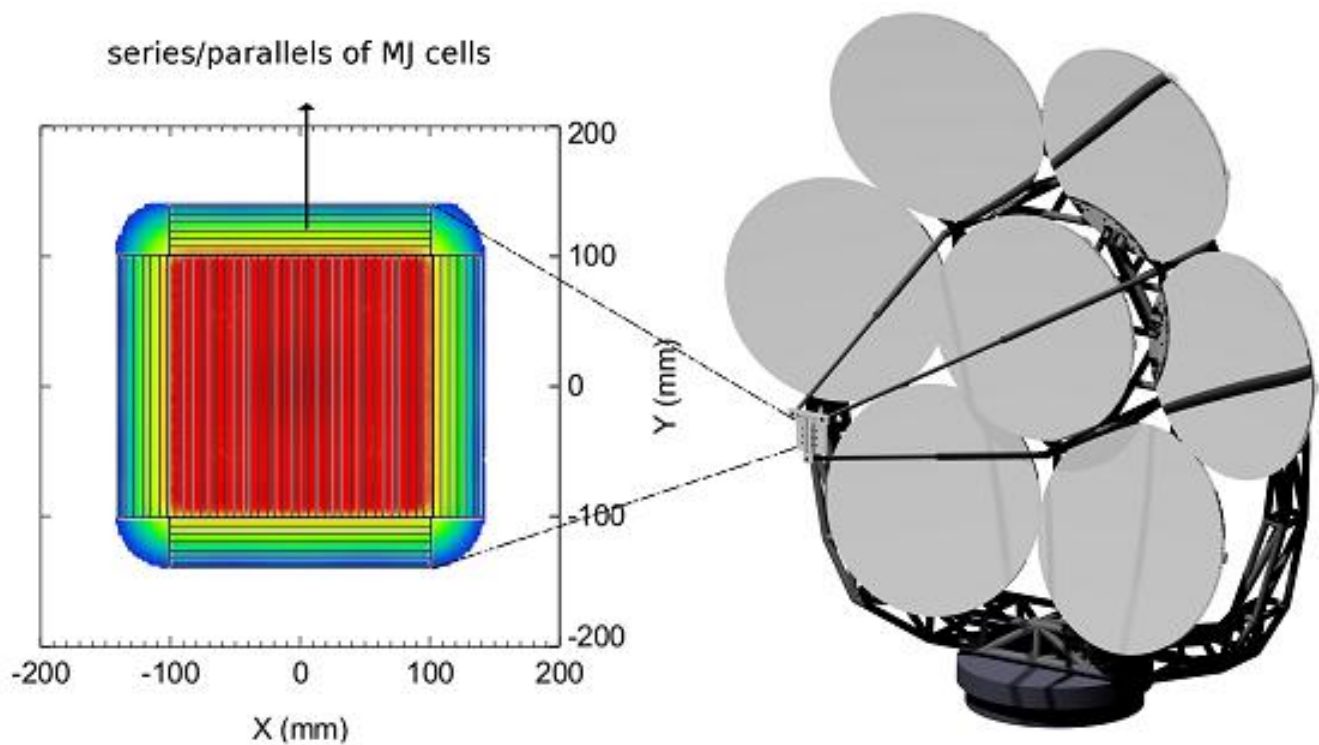
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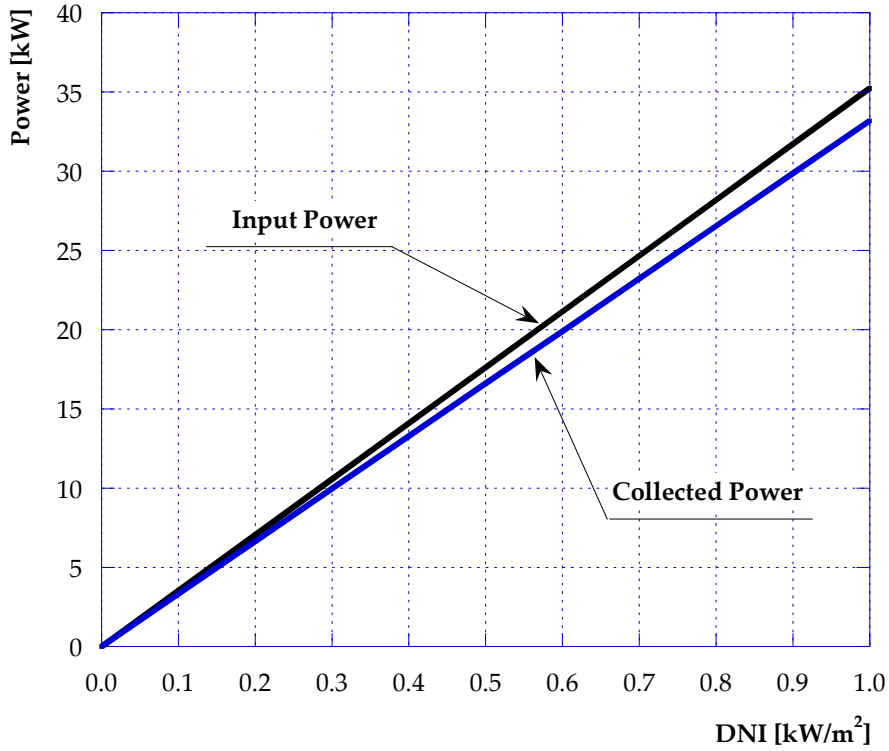


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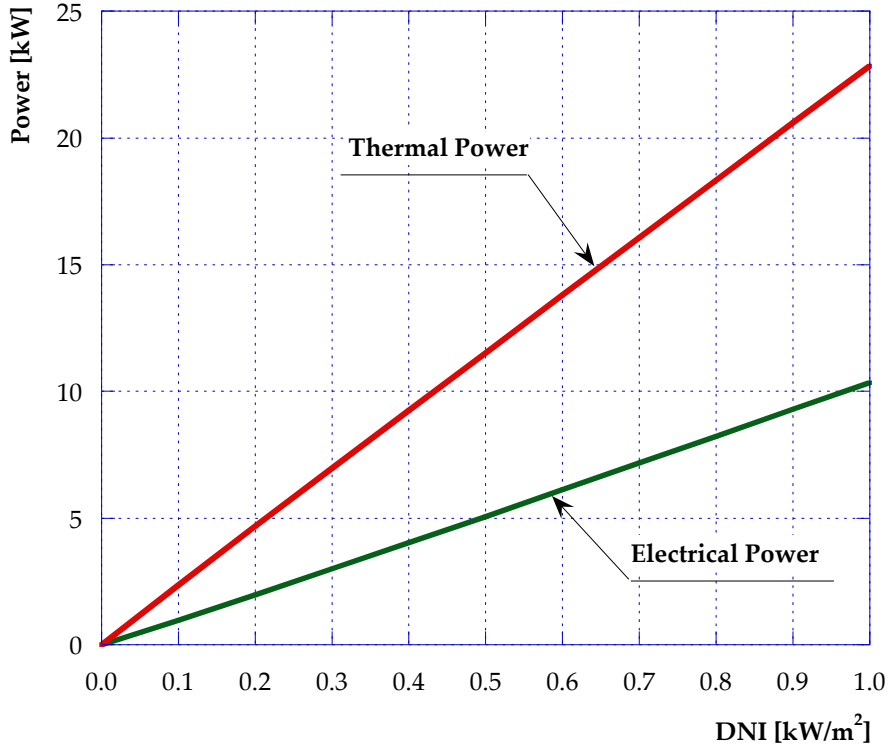
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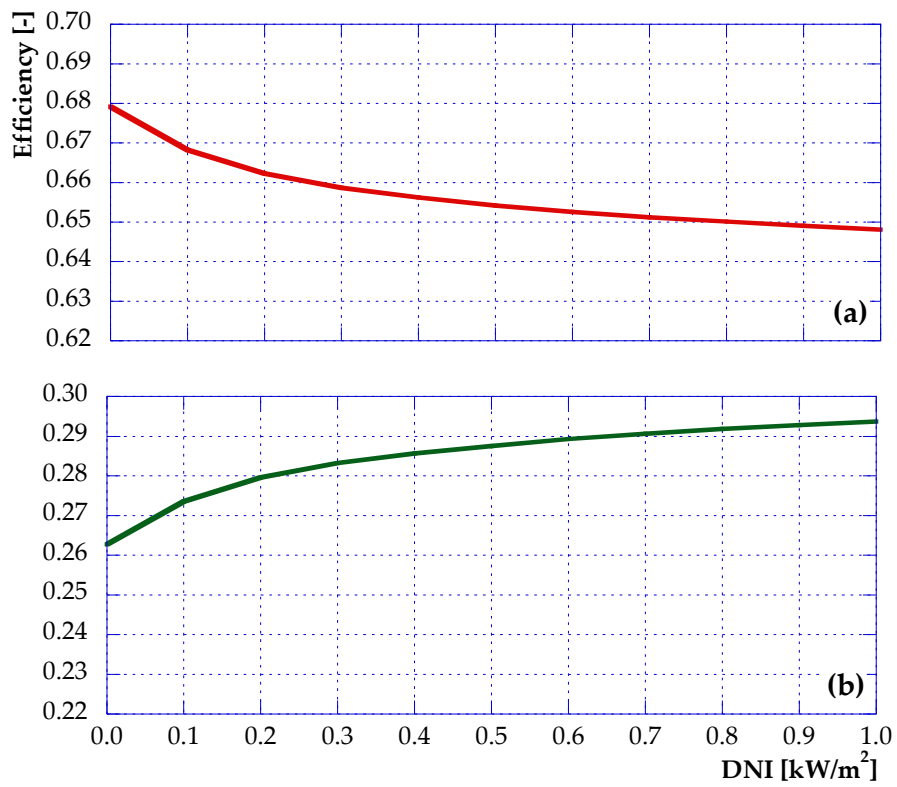
**Figure 3.** Power collected by the concentrator (input power) and the light effectively impinging on the array (collected power) of the SOLARIS concentrator as function of DNI at the collector aperture



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**Figure 4.** Produced electrical and thermal power of the SOLARIS concentrator as function of DNI at the collector aperture

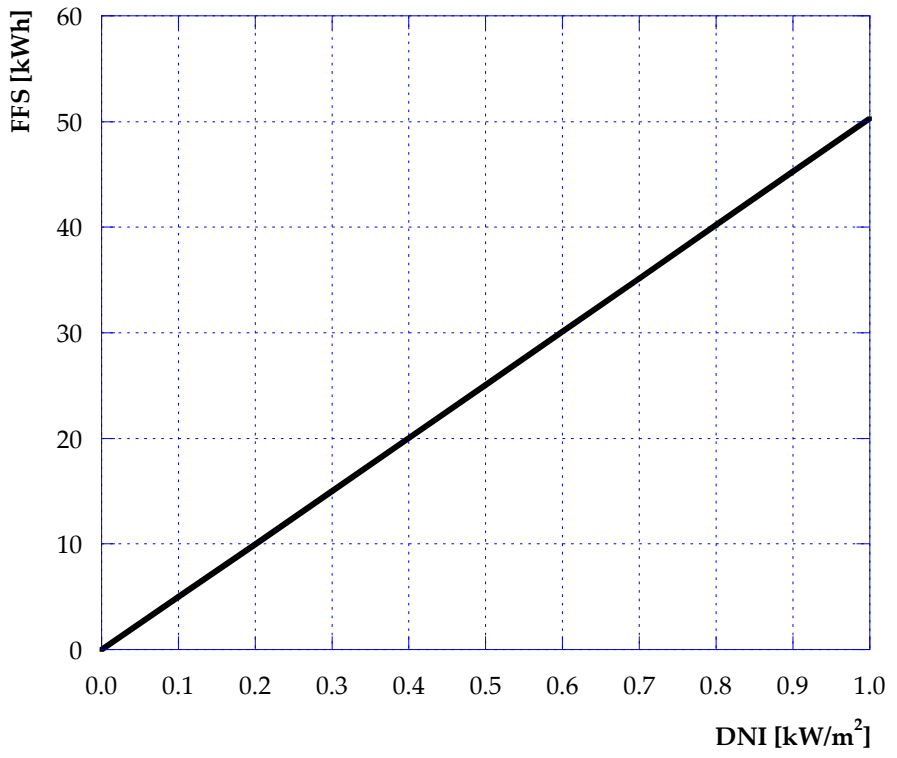
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Figure 5. Net thermal (a) and electrical (b) efficiency of the SOLARIS concentrator as function of DNI at the collector aperture



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Figure 6. Fossil fuel saving of the SOLARIS concentrator as function of DNI at the collector aperture

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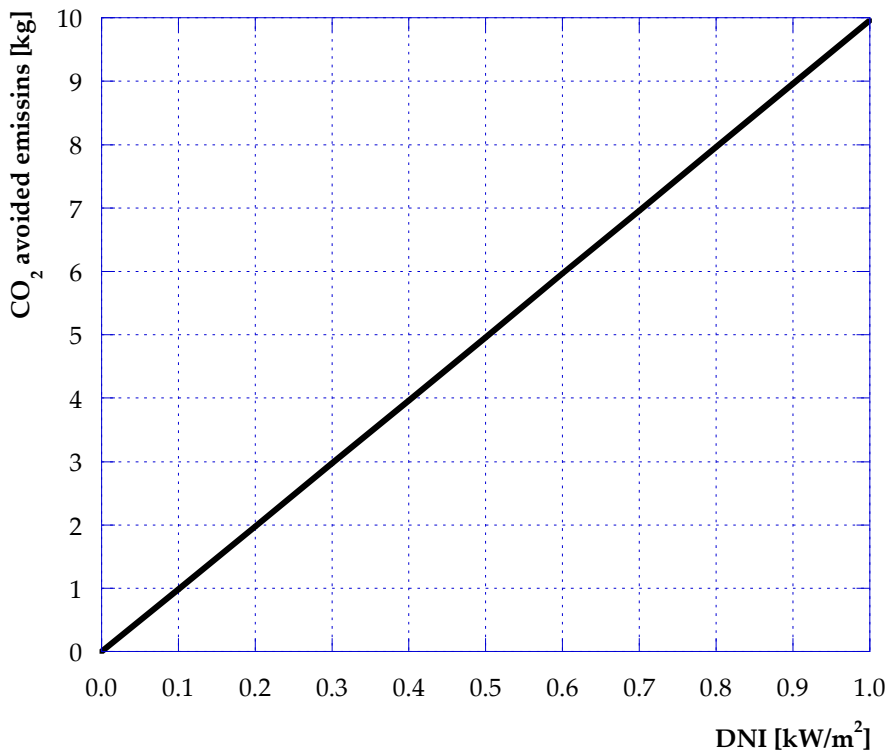


Figure 7. CO<sub>2</sub> avoided emissions of the SOLARIS concentrator as function of DNI at the collector aperture

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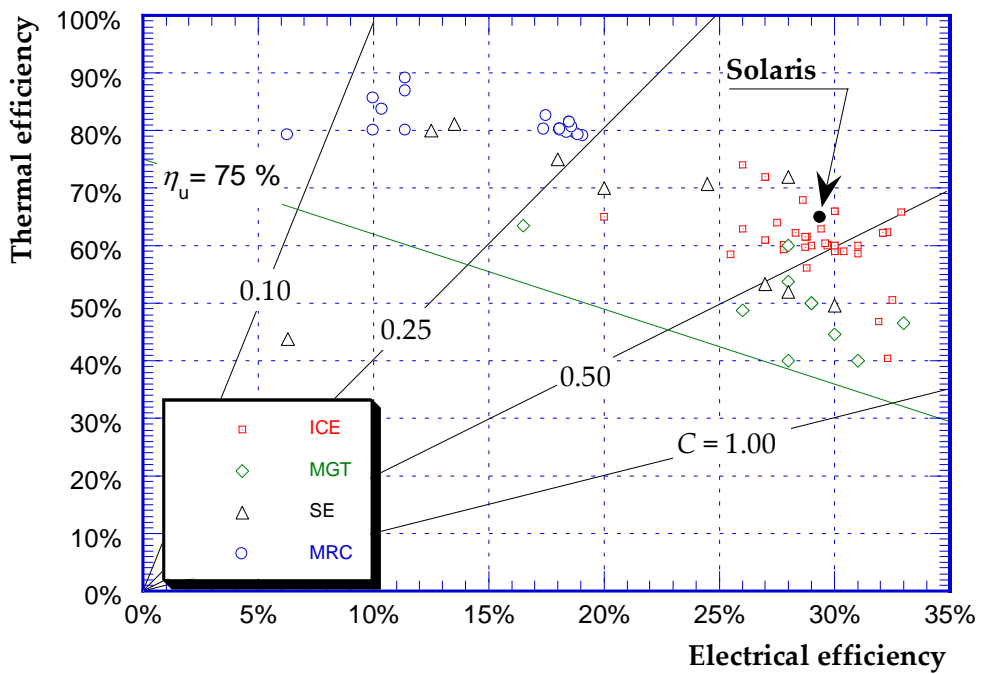
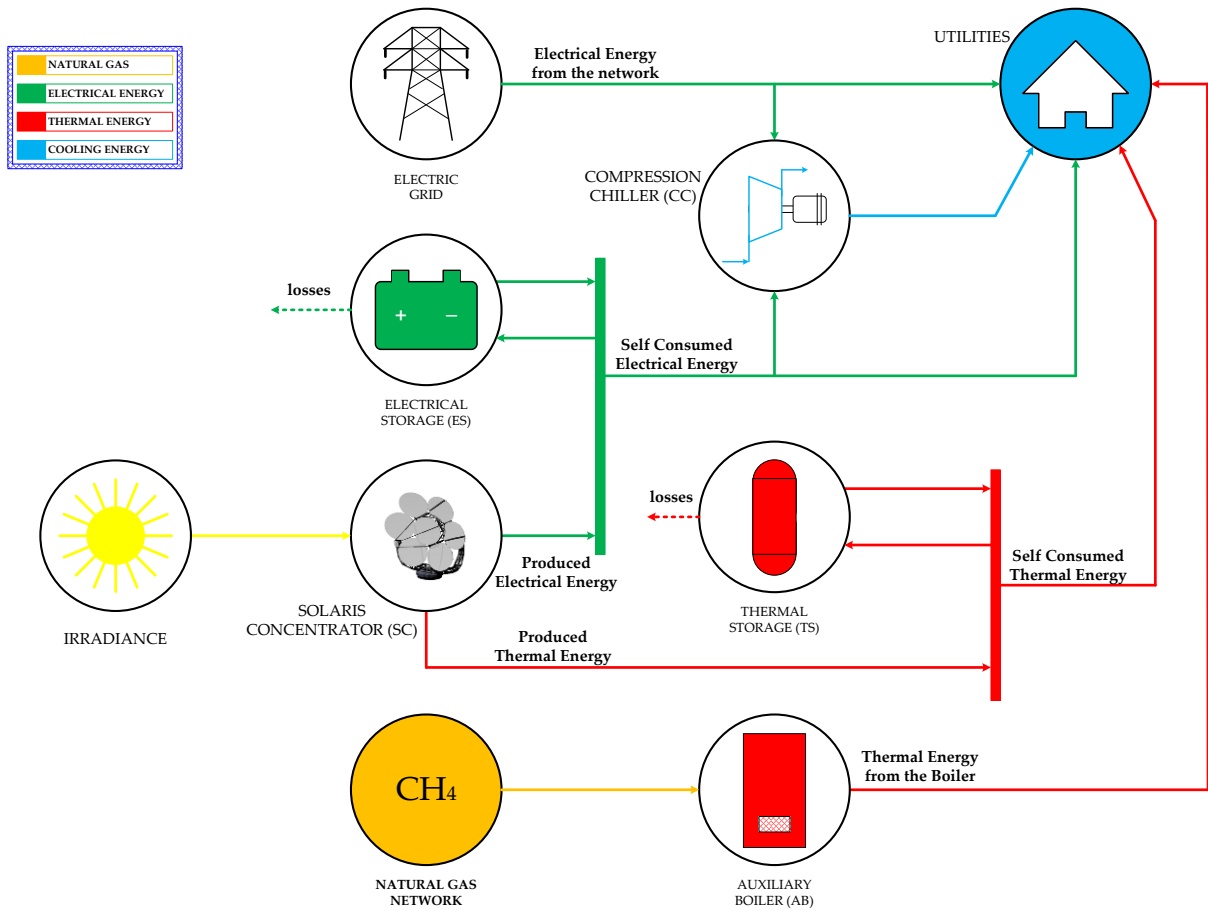


Figure 8. Thermal efficiency vs electric efficiency for micro CHP technologies compared to SOLARIS concentrator

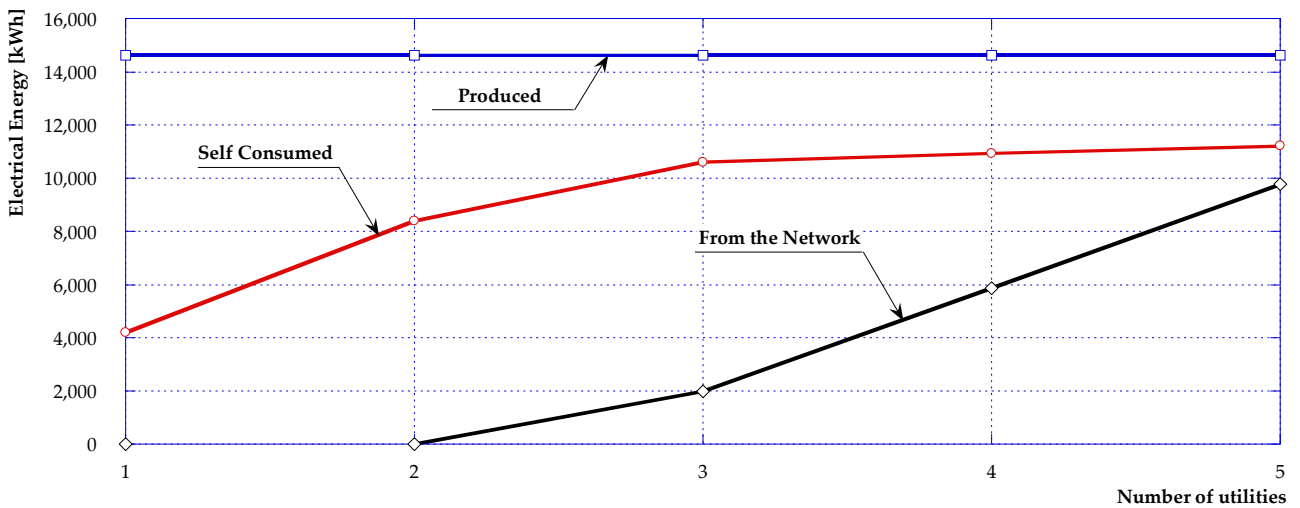
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Figure 9. Schematic of the simulated grid including the SOLARIS concentrator

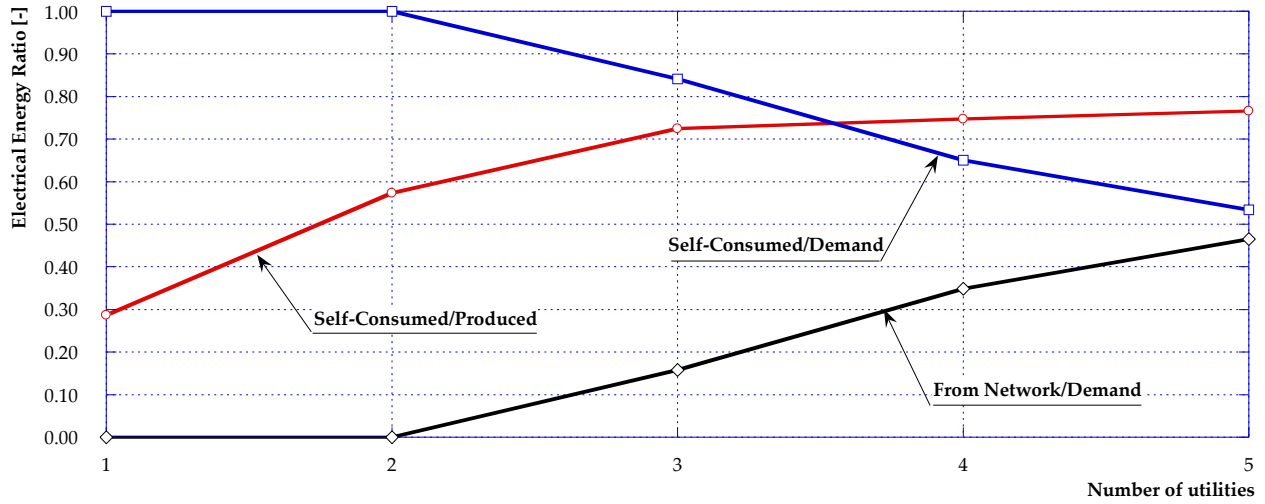


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Figure 10. SOLARIS concentrator produced electrical energy, self-consumed for the utilities and purchased from the network

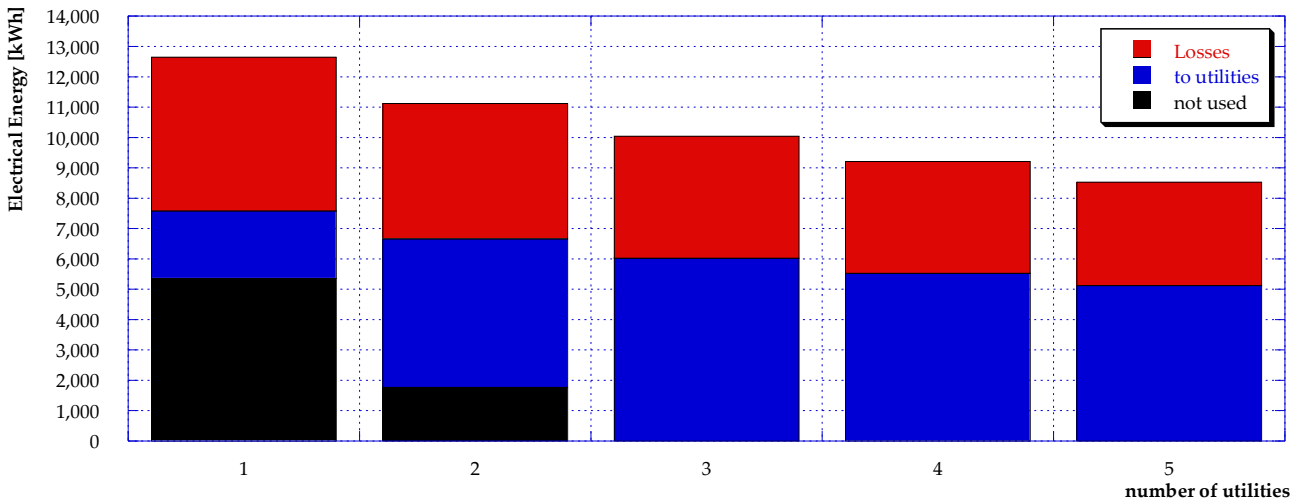


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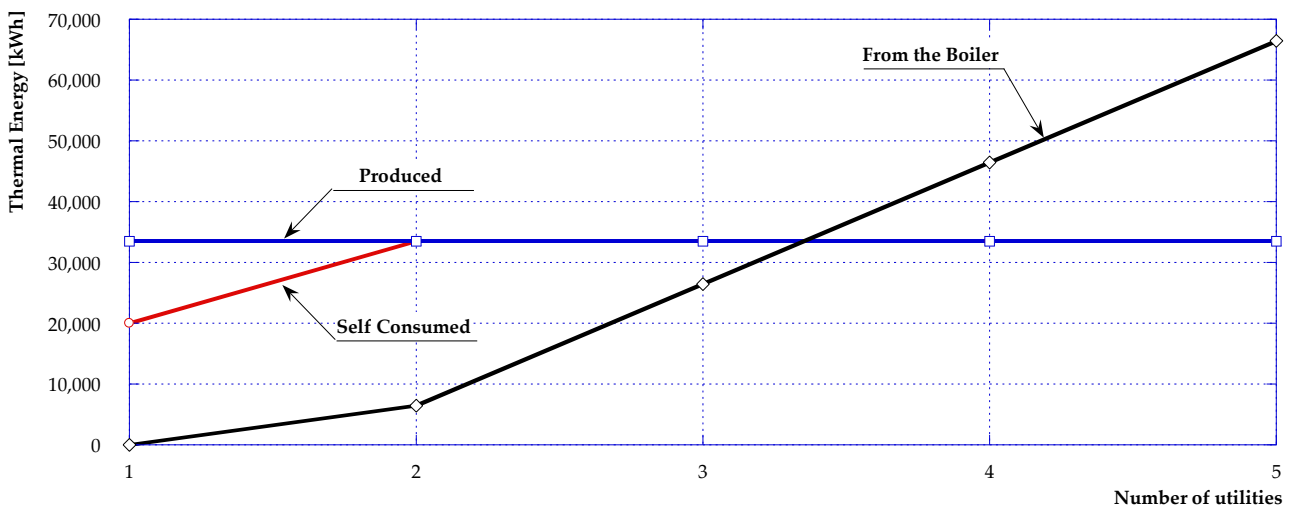
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Figure 11. Electrical energy balance



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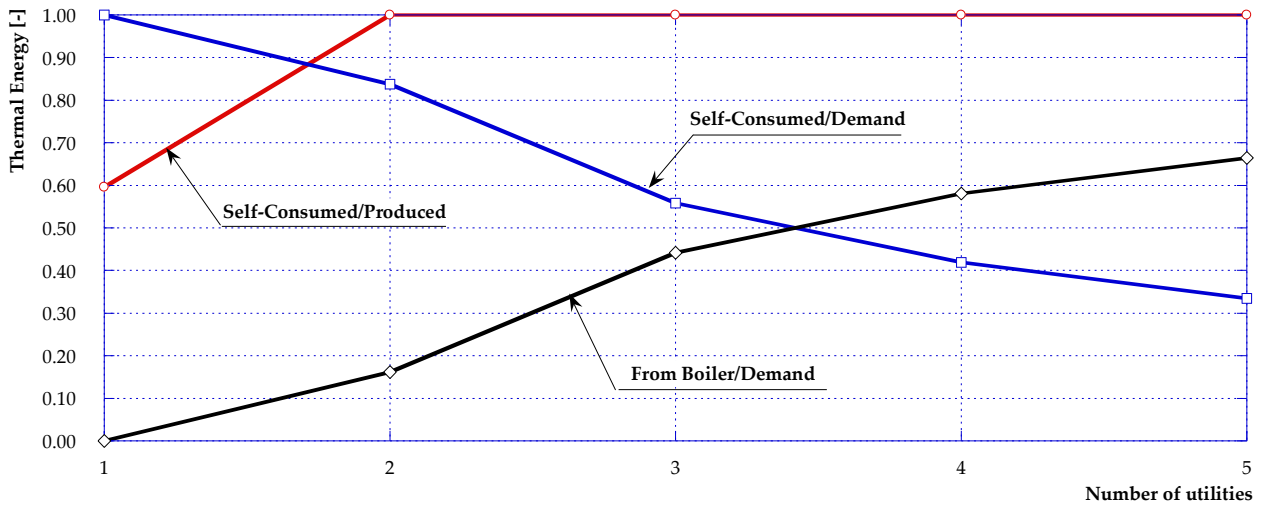
Figure 12. Energy balance of batteries



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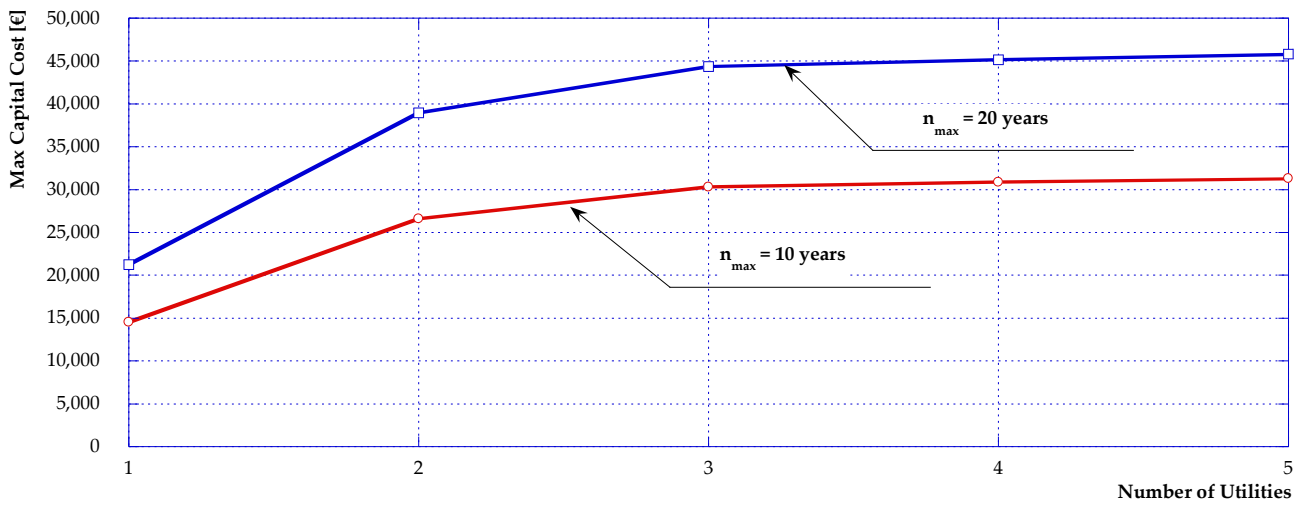
Figure 13. SOLARIS concentrator produced thermal energy, self-consumed for the utilities and produced from the boiler

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Figure 14. Thermal energy balance

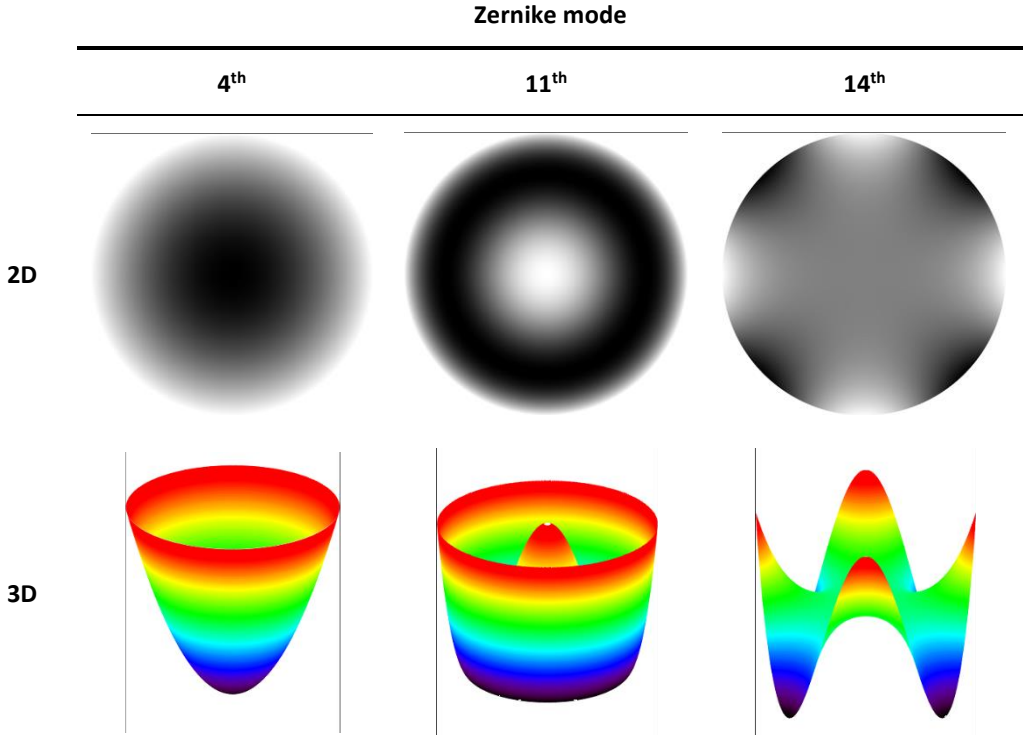


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Figure 15. SOLARIS concentrator maximum sustainable capital cost as function of the number of served utilities

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Table 1. 2D and 3D representations of the main polynomials involved in the modelling



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