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# **A COPULA-BASED APPROACH TO INVESTIGATE VERTICAL SHOCK PRICE TRANSMISSION IN THE ITALIAN HOG MARKET**

**Capitanio F., Adinolfi F., Goodwin B. K. and Riveccio G.**

## **Abstract**

It is a stylized fact that the Italian farmers do not benefit of casual structure along value chain. Conversely, retailers could advantage of any positive shock price changes occurred in the wholesale supply chain. We investigate the presence of shock price vertical contagion in the Italian hog market, describing the dependence structure along the supply chain and assessing the degree of extreme value dependence. The approach followed is non linear and copula-based, applied on weekly data of hog price changes referred to Italian farm, wholesale and retail branch chain, over the period 1994-2015. In particular, the objective of the analysis consists in to obtain a measure of the relationship between extreme events of returns, estimating the tail dependence coefficients of copula functions involved in the analysis. The empirical findings highlight the asymmetry of price transmission along the hog Italian supply chain, more relevant for wholesale–retail pair.

*Key words: Copula, tail dependence, GARCH model.*

## **Introduction**

Agro-food price asymmetry contagion, under extreme market conditions, is an important yardstick for measuring market inefficiencies. On one hand, this is of relevance from micro-perspective as large and unexpected price movements strongly affect agricultural households' welfare. On the other hand, market distortions are often cited as a ground for government intervention. In this sense, the problem of market volatility is also high on the agenda from macro-perspective.

In well-functioning markets, price shocks are equally transmitted at all market levels, from retailers to producers passing along the wholesale level. The efficiency of a food supply chain is, therefore, crucial to maintain a sustainable distribution of value added and of benefits among the stakeholders (Emmanouilides and Fousekis, 2014).

Several researches have been carried out in order to consider the possible price asymmetry dependence structure, conditioned to direction or magnitude of changes, such as Boyd and Brorsen (1988), which tested, in both cases, for asymmetry in price adjustments in the pork marketing channel, verifying that wholesaler price changes are affected, symmetrically, by price changes occurred at farmer level, and Goodwin and Harper (2000), that revealed important asymmetries in

the U.S. pork sector with a threshold co-integration model, and Ben-Kaabia and Gil (2007) that analyzed a three-regime Threshold Autoregressive Model to verify price asymmetry transmission in Spanish lamb sector. Other models are based on non-stationary feature of time series data, by means of co-integration techniques, see e.g. the regime-switching model of Serra and Goodwin (2003) or the asymmetric long run price linkage of Gervais (2011) and price transmission elasticity of Abbassi et al. (2012).

Anyway, all these models do not take into account, simultaneously, some aspects, such as to model separately the marginal and joint dependence structure of variables in a non-linear and flexible way, to measure the interdependence in presence of extreme market events, in terms of tail dependence measures, and to consider the conditional volatility of time series.

More recently works study the asymmetry in the world of copulas. The copula tool is quite popular in finance and risk management area since the late 1990s (see, for instance, Cherubini et al., 2004, Patton, 2006), but only recently are applied in agro-food economics.

Copulas offer an alternative and flexible way to analyze price co-movements, particularly during extreme market events. A copula function allows to specify, separately, the joint dependence structure from the marginal behavior of time series, enabling a conditional dependence evaluation between extreme events by means of tail dependence coefficients, as measure of the relationship in the tails of the joint distribution. In addition, in order to consider the conditional volatility of each time series, a copula-GARCH approach can be used, allowing to describe time-varying variance of univariate returns.

The latest agro-food economics literature is rich enough of empirical contributes aimed to explore market integration in the copula context. Reboredo (2012) examined co-movement between international food and oil prices; Serra and Gill (2012) analyzed the relationship among biodiesel, diesel and crude oil prices in Spain; Emmanouilides and Fousekis (2014) investigated vertical price dependence in the U.S. beef supply chain, verifying the presence of asymmetry influences in the market, especially for the pair wholesale–retail which is only of positive type; finally, Panagiotou and Stavrakoudis (2015), studying the price dependence structure between different pork cuts in the U.S. industry at retail level, did not find evidence of asymmetry in the price co-movements. In this perspective, analyzing the U.S. hog/pork market, Qiu and Goodwin (2013) explored asymmetric vertical transmission of price changes along the supply chain under extreme market conditions, by means of tail dependence measures based on a copula-GARCH model, applied also in a time-varying framework. Their results show the evidence of symmetric shock price change transmission along farm – wholesale and wholesale – retail pairwise; conversely, the farm– retail return pair is characterized by an asymmetric relationship in the tail of the joint distribution, higher for the upper

than for the lower case. This last feature means that positive extreme returns in one marketing channel, e.g. for the farmer, are connected to positive extreme returns in the other one, for the retailer, and vice versa.

Then, in order to measure the asymmetry of shock price transmission along the Italian hog supply chain, starting from the idea of Qiu and Goodwin (2013) and defining the joint co-movement of farm, wholesale and retail price changes, a copula-based approach has been applied, which enables to estimate the dependence structure in presence of extreme values assumed by returns.

Moreover, since 2008 the European Commission has stressed that the experience of the 2007/2008 price peaks has shown that magnitude and asymmetry recorded in the price adjustment process represent serious concerns about the functioning of the European agro-food supply (EC, 2008). The same report underlines how the empirical evidence in this regard is, however, contrasting, highlighting even very different conclusions depending on the markets and the countries investigated. Same conclusions for the specific sector of the hog supply chain, for which the Commission found, however, some significant trends, such as the slowness with which in many countries price changes move from upstream to downstream, symptomatic of the fact that only a limited part of the changes in consumer prices is generated by changes recorded in the primary phase of the supply chain, and the presence of imperfections in the competitive structure of the supply chains.

In Italy the question is of particular importance for the value generated by the supply chain. One of the most advocated options is to promote, within the framework of the discipline of inter-professional organization, long-term contracts shared by an important part of the operators in the supply chain and based on indexation mechanisms connected, at least in part, to feed prices, which represents about 40% of the average costs borne by Italian pig producers.

In this context, the aim of this work is threefold. First of all, to the best of our knowledge, we contribute to the literature as the primary attempt in agro-food Italian market in the copula tool framework, then, we describe the relationship among extreme values along Italian hog supply chain also in terms of trivariate copula tail dependence measures, both in the upper and lower case and, finally, we define the policy implications of the analysis results.

The paper is structured as follows: theoretical backgrounds are given in section 1, focusing, in particular, on statistical properties of copula functions, of tail dependence coefficients and of non-parametric tail dependence measures. The section 2 provides empirical results of the analysis of joint tail co-movements along the Italian hog supply chain. Some concluding remarks are reported in section 3.

## 1. Theoretical Framework

### 1.1 Copula function properties

A copula function is an  $n$ -variate distribution function defined on the unit cube  $[0, 1]^n$ , with uniformly distributed margins, with the following properties:

- the range of copula  $C(u_1, \dots, u_n)$  is the unit interval  $[0, 1]$ ;
- $C(u_1, \dots, u_n) = 0$  if any  $u_i = 0$  for  $i = 1, \dots, n$ ;
- $C(1, \dots, 1, u_i, 1, \dots, 1) = u_i$  for all  $u_i \in [0, 1]$ ;

The copula-based pillar is the Sklar's theorem (Sklar, 1959), which justifies the role of copula as dependence function, shows that, for continuous multivariate distributions, the univariate margins can be separated from the dependence structure which is completely captured by a copula function.

**Theorem 1** Let  $H(\cdot)$  be a joint distribution function of continuous random variables  $x_i$  (for  $i = 1, \dots, n$ ) with marginal distribution functions  $F_i(\cdot)$ , then, there exists a copula function  $C$ , such that:

$$H(x_1, \dots, x_n) = C(F_1(x_1), \dots, F_n(x_n))$$

where  $F_i(\cdot) = P(X_i \leq x_i) = u_i$  (for  $i = 1, \dots, n$ ) and every  $u_i = (u_1, \dots, u_n)^T$  is uniform in  $[0, 1]^n$ .

If  $F_i(\cdot)$  is continuous, then the copula  $C$  is unique; otherwise,  $C$  is uniquely determined on  $[F_1(x_1), \dots, F_n(x_n)]$ . Conversely, if  $C$  is a copula and  $F_i(\cdot)$  is a distribution function, then the function  $H$  defined above is a joint distribution function with margin  $F_i(\cdot)$ .

### 1.2 Tail dependence for copulas

Tail dependence is a measure of concordance between less probable values of variables. This concordance tends to concentrate on the lower and upper tails of the joint distribution.

In a bivariate context, let  $F_i$  be the marginal distribution function of a random variable  $X_i$  ( $i=1,2$ ) and let  $u$  be a threshold value; then the lower tail dependence coefficient,  $\lambda_L$ , is defined as

$$\lambda_L = \lim_{u \rightarrow 0^+} P \left\{ X_2 \leq F_2^{-1}(u) \mid X_1 \leq F_1^{-1}(u) \right\}$$

and, hence

$$P\{X_2 \leq F_2^{-1}(u) | X_1 \leq F_1^{-1}(u)\} = \frac{P\{X_1 \leq F_1^{-1}(u), X_2 \leq F_2^{-1}(u)\}}{P\{X_1 \leq F_1^{-1}(u)\}} = \frac{C(u, u)}{u}.$$

Then, an alternative definition, in terms of copula function, is

$$\lambda_L = \lim_{u \rightarrow 0^+} \left\{ \frac{C(u, u)}{u} \right\}.$$

In a similar way, the upper tail dependence is given by,

$$\lambda_U = \lim_{u \rightarrow 1^-} P\{X_2 > F_2^{-1}(u) | X_1 > F_1^{-1}(u)\}$$

For  $\lambda_U \in (0, 1]$ ,  $X_1$  and  $X_2$  are asymptotically dependent on the upper tail; if  $\lambda_U$  is null,  $X_1$  and  $X_2$  are asymptotically independent.

Hence,

$$P\{X > F_2^{-1}(u) | X_1 > F_1^{-1}(u)\} = \frac{1 - P\{X_1 \leq F_1^{-1}(u)\} - P\{X_2 \leq F_2^{-1}(u)\} + P\{X_1 \leq F_1^{-1}(u), X_2 \leq F_2^{-1}(u)\}}{1 - P\{X_1 \leq F_1^{-1}(u)\}}.$$

Then, it is possible to recur to an alternative and equivalent definition, for continuous random variables, from which it is clear that the concept of tail dependence is indeed a copula property (Joe, 1997)

$$\lambda_U = \lim_{u \rightarrow 1^-} \frac{\hat{C}(1-u, 1-u)}{1-u} = \lim_{u \rightarrow 1^-} \left\{ \frac{1 - 2u + C(u, u)}{1-u} \right\}.$$

Where  $\hat{C}$  is the survival copula function defined as

$$\begin{aligned} \hat{C}(1-u_1, 1-u_2) &= 1 - P\{X_1 \leq F_1^{-1}(u_1)\} - P\{X_2 \leq F_2^{-1}(u_2)\} + P\{X_1 \leq F_1^{-1}(u_1), X_2 \leq F_2^{-1}(u_2)\} \\ &= 1 - P(U_1 \leq u_1) - P(U_2 \leq u_2) + P(U_1 \leq u_1, U_2 \leq u_2) \end{aligned}$$

It is simple to show that  $\hat{C}$  is strictly related to the copula function through the following relationship

$$\hat{C}(1-u_1, 1-u_2) = 1 - u_1 - u_2 + C(u_1, u_2)$$

A multivariate generalization of the tail dependence coefficients (De Luca and Riveccio, 2009) consists in to consider  $h$  variables and the conditional probability associated to the remaining  $n - h$  variables, given, respectively, by

$$\begin{aligned}\lambda_L^{1\dots h|h+1\dots n} &= \lim_{u \rightarrow 0^+} P(F_1(X_1) \leq u, \dots, F_h(X_h) \leq u \mid F_{h+1}(X_{h+1}) \leq u, \dots, F_n(X_n) \leq u) \\ &= \lim_{u \rightarrow 0^+} \left\{ \frac{C_n(u, \dots, u)}{C_{n-h}(u, \dots, u)} \right\}.\end{aligned}$$

Indeed, the upper (lower) tail dependence coefficient can be interpreted as the probability of very high (low) returns for  $h$  assets provided that very high (low) returns have occurred for the remaining  $n-h$  assets.

$$\begin{aligned}\lambda_U^{1\dots h|h+1\dots n} &= \lim_{u \rightarrow 1^-} P(F_1(X_1) > u, \dots, F_h(X_h) > u \mid F_{h+1}(X_{h+1}) > u, \dots, F_n(X_n) > u) \\ &= \lim_{u \rightarrow 1^-} \left\{ \frac{\hat{C}_n(1-u, \dots, 1-u)}{\hat{C}_{n-h}(1-u, \dots, 1-u)} \right\}.\end{aligned}$$

### 1.3 Non parametric tail dependence measures

In order to select an adequate copula function able to capture accurately the dependence structure showed by co-movements of extreme return pair-wise, can be useful to estimate the empirical tail dependence by mean of non-parametric method.

The non-parametric bivariate coefficient of lower tail dependence,  $\lambda_L^{NP}$ , can be obtained as (De Luca and Riveccio, 2009)

$$\lambda_L^{NP}(k) = P(X_2 \leq x_2^* \mid X_1 \leq x_1^*),$$

or conversely, where  $x_i^*$  is assumed to be  $\mu_i - k\sigma_i$ . This statistic depends on  $k$ .

The concept of bivariate upper tail dependence is defined in a similar way as

$$\lambda_U^{NP}(k) = P(X_2 > x_2^* \mid X_1 > x_1^*),$$

where  $x_i^*$  is assumed to be  $\mu_i + k\sigma_i$ .

## 2. Empirical analysis

### 2.1 Data and modeling procedure

We have analysed the price co-movements in the hog Italian market, verifying the dependence structure of hog weekly data prices, from January 1994 to December 2014, concerning the farm, wholesale and retail distribution channels.

The analysis of prices reveals that a crisis in the hog market begun in the 1998 continued throughout the 1999, in all three chains. Besides, a more recent shock in the farm market occurred in the 2008, as shown in the figure 1, as result of high levels of raw material costs employed in the breeding and of energy resources.

In all three series is not present any trend, as showed by the results of Augmented Dickey-Fuller (ADF) test (Dickey and Fuller, 1979) applied to farm, wholesale and retail price time series.

Moreover, we intend to study the supply chain co-movements of weekly returns. Therefore, in the first, we have obtained log-returns, calculating the natural logarithm of ratios between the price at time  $t$  and the same price at time  $t-1$ , for each branch chain. Then, an *ARMA-GARCH* model has been applied to taking into account the presence of a conditional serial dependence of returns, both in mean and in variance framework. After estimating marginal behaviour of each time series of returns, we investigated the presence of a conditional cross-section dependence (as suggested in Qui and Goodwin, 2013), applying a cross-equation model to the standardized residual pair-wise obtained from the estimated *ARMA-GARCH* structure. Afterwards, we transform the standardized residuals of cross-equation model into uniform margins, input argument of copula functions. Concluding, a copula function has been employed to join the uniform margins into a multivariate distribution. This method, called *Inference For Margins (IFM)* method, allows to specify separately, in a simple (instead of the full maximum likelihood, more computationally complex) and flexible way (also in non linear and asymmetric framework), the dependence structure of returns, by means of the maximum likelihood estimation method for the parameters involved at each step of the procedure.

Finally, in order to measure the conditional dependence between extreme events occurred along the pork supply chain, tail dependence coefficients are estimated.

We derived, besides, a trivariate copula function in order to estimate the upper and lower tail dependence coefficients among the three branch chains. Starting from the standardize skew-t residuals of an *ARMA-GARCH* model before and, then, on the residuals of the conditional cross-equation model (VAR) with skew-t innovations, we applied the uniform transformation to obtain the trivariate copula margins. Then, a copula model is selected from the main families, such as



Elliptical and Archimedean. In this case, the method could consist in a non-linear VAR (Vector AutoRegressive) model (see, e.g. Bianchi et al., 2010) with three variables, applying a copula function on VAR skew-elliptical distributed residuals. Tail dependence coefficients for the multivariate t-copula are obtained according to Joe (2014).

## 2.2 Results

The analysis of branch chain returns highlights a more high volatility of wholesale returns (see table 1), while the farm and retail returns are quite stable over the time, reporting very low fluctuations in the considered period. In addition, calculating the non parametric tail dependence measures at same time lag  $t$  (table 2), we note a significant upper tail dependence between farm and retail returns and a symmetric non-zero tail dependence between farm and wholesale price changes. This implies that, in the same week, positive extreme values of farm prices changes are linked to positive extreme values of retail returns, and vice versa; but negative shocks of a variable does not affect the other one. For the pair farm-wholesale, we observe a significant joint tail co-movement, both in the upper and lower case.

Conversely, the non parametric tail dependence measures, if calculated at different time lag, between  $t$  and  $t-1$  (or two consecutive weeks) on each asset pair-wise (table 3), exhibit the absence of tail dependence, in the lower case, between retail/wholesale and farm price changes, as conditioning variable. This could mean an absence of effects of farm extreme negative returns over retail/wholesale price changes at different lags. If farm chain has a lower return in a week, other prices do not change the next week. In the upper case, the impact is the same. Then, positive extreme events occurred in one week for farm, do not impact on the other variables in the following week. The impulse response function, typical of Vector Autoregressive models, could show this asymmetrical behaviour.

On the other side, the non parametric tail dependence coefficients displayed between retail and wholesale is symmetrical in both quadrant of the joint distribution, justifying the application of a symmetrical tail dependence copula, like the Student's-  $t$  copula function. In particular, the non parametric tail dependence values suggest that the extreme returns at farm level do not affect extreme wholesale and retail price changes, if considered at different period of observation, and this future could suggest the use of a null tail dependence copula, like the Frank copula. But the values of non parametric tail dependence coefficients calculated for the same week ( $t$ ) for each return pair lead to apply an upper tail dependence copula, e.g. the Gumbel copula.

For this reason, we have analysed all well-known copula functions, which belong to Elliptical and Archimedean families, characterize by all tail dependence structures.

Table 4 presents the parameter values obtained applying the *ARMA-GARCH* model, with innovations skew- $t$  distributed, to the three univariate returns and by the cross-equation effect model employed on each return pair. The significant lag order is 1 for wholesale/retail with respect to farm price changes (at  $t-1$ , the previous week) and for farm/retail with respect to wholesale returns (at  $t-1$ ); on the contrary, farm/wholesale – retail pair-wise do not show any significant lag order; in this last case, there is not evidence of relationship over the time among retail and the remaining two market chains.

Below, table 5 reports the fitting values of some main copulas involved in the analysis. We have estimated all possible copula pairs, choosing the copula with the best fit to the data, according to the minimum value assumed by Akaike Information Criterion (AIC) and Bayesian Information Criterion (BIC).

The best fit copula model for the first pair of assets, denoted as  $u_1$  and  $u_2$ , respectively farm and wholesale returns, is the Frank copula, that implies a null tail dependence, both for the upper and lower coefficients; this means that extreme values of a variable have no influence on the other ones. Therefore, the upper tail dependence, exhibited between farm and wholesale price changes at the same week, becomes not significant when calculated after using conditional mean and variance model for returns. As a matter of fact, the Gumbel copula exhibits the best fit to the data when the IFM method is applied in absence of a conditional model for the price changes, such as the *ARMA-GARCH* model and the conditional serial dependence equations. In addition, not considering the cross-equation effects, the copulas are identical to the copulas obtained taking into account the cross-section dependence between variables. This means that only the univariate conditional dependence in mean and variance has really influence on dependence structure of returns.

Conversely, the copula that better represents the dependence structure between wholesale and retail price changes is the Student's- $t$  copula, which is characterized by symmetric non-null tail dependence coefficients ( $\lambda_L = \lambda_U = 0.065$ ). This suggests a weak relationship in the tail of joint distribution, such that positive (negative) shock for wholesale (retail) returns are followed by positive (negative) shock for retail (wholesale) returns at the same time.

Also for the last return pair, farm and retail, the tail dependence coefficient is null, because the choice of copula lies on two copulas (AIC value suggests the selection of Joe-Frank copula, while the BIC value indicates the Frank copula, both characterized by null tail dependence coefficients). The symmetric extreme price changes co-movements are annulled by the conditional structure of returns, in the univariate and bivariate framework. This feature leads to conclude that joint co-movements under extreme market conditions are weak or null.

Further, we want to verify the presence of a conditional dependence in the tails of the trivariate joint distribution, in order to assess the degree of this relationship considering the whole dependence structure of the pork supply chain. To this end, we estimate some copulas as reported in table 7, according to the procedure described in section 2.1.

The results show the best fit of the  $t$ -Copula with symmetrical, not null, tail dependence. Tail dependence coefficients reported at the end of table 8, measure the relationship between extreme values at the same lag  $t$ . As shown in table 8, the tail dependence coefficients are quite low, underlying the same conclusions pointed out in the bivariate case and by the non parametric tail dependence, higher for wholesale-retail pair and close to zero for those remaining.

This price adjustment asymmetry in favour of retail - wholesale channels reflects the weakness of the producer that fails to adjust prices under positive extreme market conditions. In the same way, in case of extreme negative conditions at farm level, retail/wholesale prices will not reproduce the same remarkable reduction.

### **3. Conclusion**

We estimated the tail co-movements in the joint distribution along hog supply chain in Italy, following the approach proposed in Qiu and Goodwin, 2013.

It turned out that tail price co-movement for farm-wholesale pair is null and it is well described with a Frank copula, characterized by zero tail dependence, such as for the pair farm-retail, whose dependence structure is defined by a Joe Frank copula; conversely, the relationship among wholesale-retail price changes is symmetrical and rather weak, but not null, and it is represented by a Student's- $t$  copula, with identical non zero tail dependence coefficients.

These results underline an asymmetrical shock price vertical contagion, showing a better price adjustments along the wholesale–retail chain.

The value chain in the hog supply chain is effectively integrated and the policy decisions at one point will cause ripple effect on the other linkages. Hence, the policies should take into account the effect of impact on the entire value chain as to enable the hog producers capture the benefits of value addition.

Price Transmission Along Cotton Value Chain (PDF Download Available). Available from: [https://www.researchgate.net/publication/270275574\\_Price\\_Transmission\\_Along\\_Cotton\\_Value\\_Chain](https://www.researchgate.net/publication/270275574_Price_Transmission_Along_Cotton_Value_Chain) [accessed Feb 21 2018].

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**Fig. 1 Weekly Hog Prices: Jan 1994-Dec 2014**

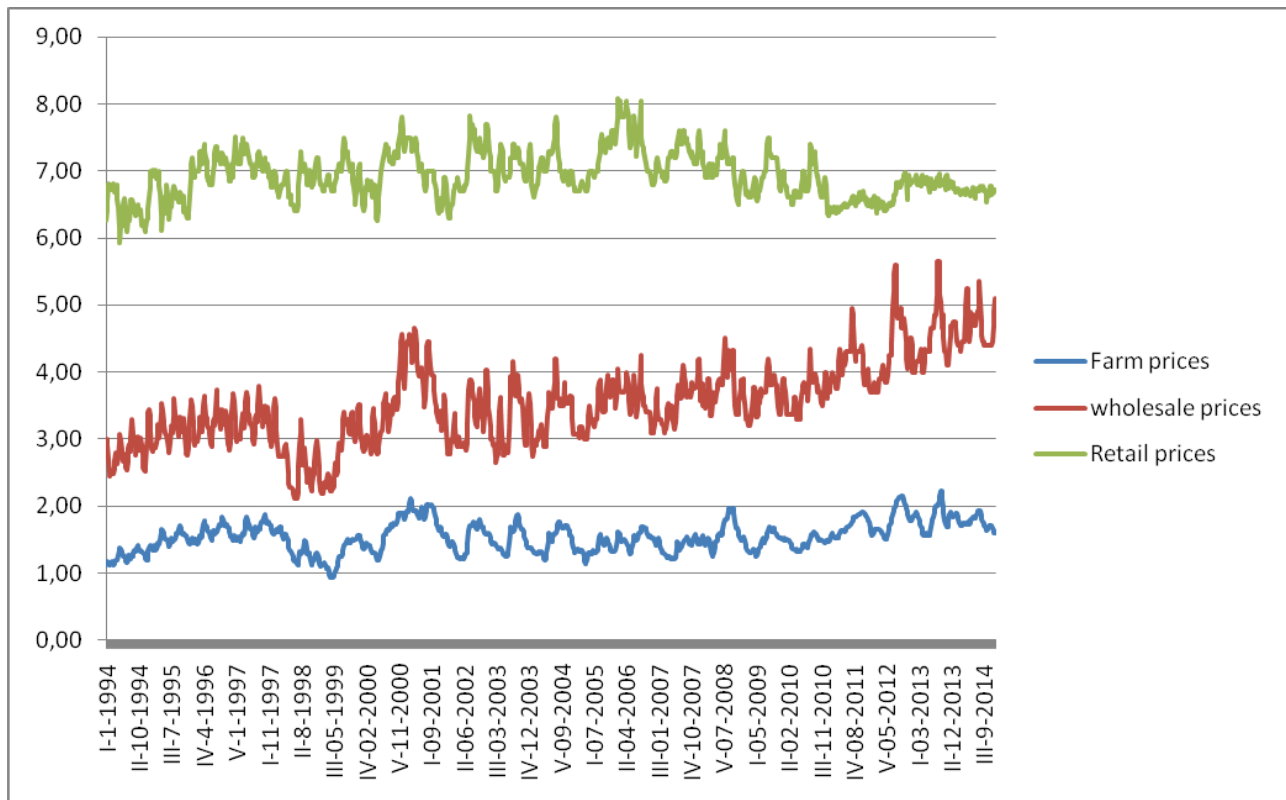


Table 1. Summary statistics of farm, wholesale and retail returns

Descriptive statistics	Return		
	Farm	Wholesale	Retail
Mean	0,0003	0,0005	0,0001
St. deviation	0,0268	0,0440	0,0157
Skewness	0,6222	0,1533	-0,0266
Kurtosis	1,3959	0,7716	1,2074

Table 2. Non parametric tail dependence coefficients at time  $t$  ( $k=2$ )

	Conditioning variable		
	Farm	Wholesale	Retail
<b>Lower tail dep</b>			
Farm	-	0.071	0.000
Wholesale	0.125	-	0.229
Retail	0.000	0.286	-
<b>Upper tail dep</b>			
Farm	-	0.330	0.067
Wholesale	0.230	-	0.133
Retail	0.051	0.148	-

Table 3. Non parametric tail dependence coefficients between time  $t$  and  $t-1(k=2)$ 

Lower tail dep	Conditioning variable		
	Farm	Wholesale	Retail
Farm	-	0.107	0.080
Wholesale	0.000	-	0.029
Retail	0.000	0.180	-
Upper tail dep	Conditioning variable		
	Farm	Wholesale	Retail
Farm	-	0.190	0.130
Wholesale	0.100	-	0.060
Retail	0.100	0.150	-

Table 4. ARMA-GARCH and of Cross-equation effects models

MODEL	Coefficient	Return					
		Farm		Wholesale		Retail	
		Estimate	Std. Error	Estimate	Std. Error	Estimate	Std. Error
ARMA-GARCH Shew-e innovations	$\sigma^2_1$	-0.16070	0.10190	1.00000	0.05545	1.00000	0.07222
	$\sigma^2_2$	-	-	-0.52838	0.05338	-0.27120	0.03089
	$\rho_{\sigma^2_1}$	1.00000	0.00461	-0.58892	0.05892	-0.28870	0.07105
	$\rho_{\sigma^2_2}$	0.38420	0.00136	-0.28551	0.05451	-	-
	$\sigma_{\omega,gr}$	0.00007	0.00003	0.00051	0.00017	0.00003	0.00001
	$\alpha_{\mu,gr1}$	0.14920	0.04084	0.11865	0.04132	0.11750	0.03980
	$\beta_{\mu,gr1}$	0.70120	0.08220	0.59979	0.15100	0.74880	0.08297
	$\omega_{gr}$	1.12500	0.04786	1.04217	0.03861	1.02700	0.03699
	$\omega_{grs}$	8.05300	1.80600	6.54074	1.39425	6.01000	1.15100
Cross-equation effects	Intercept	-	-	0.01745	0.02892	0.00387	0.02980
	$F_{farm,t-1}$	-	-	0.14883	0.02850	0.16767	0.02723
	$\omega_{gr}$	-	-	0.99390	0.03900	0.98896	0.03400
	$\rho_{\sigma^2_{farm},1}$	-	-	0.09277	0.17400	0.08587	0.19200
	$\rho_{\sigma^2_{farm},2}$	-	-	3.05402	1.85900	9.65080	2.28100
	Intercept	-0.00025	0.02897	-	-	0.00007	0.02910
	$W_{wholesale,t-1}$	0.10663	0.02895	-	-	0.25300	0.02720
	$\omega_{gr}$	0.99280	0.02800	-	-	0.96443	0.03200
	$\rho_{\sigma^2_{wholesale},1}$	0.37930	0.13000	-	-	0.09151	0.18500
	$\rho_{\sigma^2_{wholesale},2}$	1.49070	0.62700	-	-	3.23883	1.84000
	Intercept	0.00197	0.03017	0.01911	0.03018	-	-
	$R_{retail,t-1}$	0.04901	0.02951	0.01145	0.02884	-	-
	$\omega_{gr}$	0.99980	0.02800	1.00080	0.03100	-	-
	$\rho_{\sigma^2_{retail},1}$	0.95430	0.19700	0.19750	0.19800	-	-
	$\rho_{\sigma^2_{retail},2}$	1.68730	0.73400	2.38930	1.28700	-	-

**Table 5. LogLikelihood (LogL), AIC and BIC of some main copulas exploited in the analysis**

Bivariate Copula	LogL			AIC			BIC		
	$u_1, u_2$	$u_2, u_3$	$u_1, u_3$	$u_1, u_2$	$u_2, u_3$	$u_1, u_3$	$u_1, u_2$	$u_2, u_3$	$u_1, u_3$
Student's- <i>t</i>	115.30	139.00	35.42	-226.60	-274.00	-66.84	-216.60	-264.00	-56.84
Gaussian	112.15	129.50	34.92	-222.30	-257.00	-67.84	-217.30	-252.00	-62.84
Clayton	75.44	107.90	28.65	-148.88	-213.80	-55.30	-143.88	-208.80	-50.30
Gumbel	102.50	118.80	27.12	-203.00	-235.60	-52.24	-198.00	-230.60	-47.24
Frank	117.60	123.90	35.97	-233.20	-245.80	-69.94	-228.20	-240.80	-64.94
Joe	77.31	85.96	16.68	-152.62	-169.92	-31.36	-147.62	-164.92	-26.36
Joe-Frank	115.64	123.83	37.86	-227.28	-243.66	-71.72	-217.29	-233.66	-61.72

We denote with  $u_1$ =uniform margin for farm returns,  $u_2$ =uniform margin for wholesale returns,  $u_3$ = uniform margin for retail returns

**Table 6. Estimated parameters of the selected bivariate copulas and tail dependence coefficients**

Copula	Parameter	Farm-Wholesale	Wholesale-Retail	Farm-Retail
Frank	$\delta^*$	2.987		
		(0.1968)		
	$\lambda_L = \lambda_U$	0.000		
Student's- <i>t</i>	$\rho$		0.464	
			(0.024)	
	$\nu$		8.124	
			(2.185)	
Joe-Frank	$\lambda_L = \lambda_U$		0.065	
	$\theta^{**}$			2.251
				(0.736)
	$\delta^{**}$			0.665
				(0.188)
Frank	$\lambda_L = \lambda_U$			0.000
	$\delta^*$			1.583
				(0.1868)
	$\lambda_L = \lambda_U$			0.000

The expressions of copulas are given in Joe (1997)

\* $0 \leq \delta \leq \infty$ , \*\*  $\theta \geq 1$ ,  $0 \leq \delta \leq 1$

**Table 7. LogLikelihood (LogL), AIC and BIC of some main trivariate copulas**

Trivariate copula	LogL	AIC	BIC
Student's- <i>t</i>	250,70	-495,40	-480,41
Gaussian	242,50	-481,00	-471,00
Clayton	160,10	-318,20	-313,20
Gumbel	168,10	-334,20	-329,20
Frank	197,10	-392,20	-387,20
Joe	115,80	-229,60	-224,60



**Table 8. Estimated parameters of the selected trivariate Student's-*t* copula and tail dependence coefficients**

Pair	Parameter	Estimate	St. error
Farm-Wholesale	$\rho_{12}$	0.4385	0.0238
Farm-Retail	$\rho_{23}$	0.2396	0.0287
Wholesale-Retail	$\rho_{13}$	0.4634	0.0231
-	$\nu$	16.0153	4.5617
Farm-Wholesale	$\lambda_L=\lambda_U$	0.0196	
Farm-Retail	$\lambda_L=\lambda_U$	0.0049	
Wholesale-Retail	$\lambda_L=\lambda_U$	0.0230	