



Ingredients for 21 cm Intensity Mapping

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Abstract

Current and upcoming radio telescopes will map the spatial distribution of cosmic neutral hydrogen (HI) through its 21 cm emission. In order to extract the maximum information from these surveys, accurate theoretical predictions are needed. We study the abundance and clustering properties of HI at redshifts $z \leq 5$ using TNG100, a large state-of-the-art magnetohydrodynamic simulation of a $75 h^{-1}$ Mpc box size, which is part of the IllustrisTNG Project. We show that most of the HI lies within dark matter halos, and we provide fits for the halo HI mass function, i.e., the mean HI mass hosted by a halo of mass M at redshift z . We find that only halos with circular velocities larger than $\approx 30 \text{ km s}^{-1}$ contain HI. While the density profiles of HI exhibit a large halo-to-halo scatter, the mean profiles are universal across mass and redshift. The HI in low-mass halos is mostly located in the central galaxy, while in massive halos the HI is concentrated in the satellites. Our simulation reproduces the bias value of damped Ly α systems from observations. We show that the HI and matter density probability distribution functions differ significantly. Our results point out that for small halos, the HI bulk velocity goes in the same direction and has the same magnitude as the halo peculiar velocity, while in large halos, differences show up. We find that halo HI velocity dispersion follows a power law with halo mass. We find a complicated HI bias, with HI already becoming nonlinear at $k = 0.3 h \text{ Mpc}^{-1}$ at $z \gtrsim 3$. The clustering of HI can, however, be accurately reproduced by perturbative methods. We find a new secondary bias by showing that the clustering of halos depends not only on mass but also on HI content. We compute the amplitude of the HI shot noise and find that it is small at all redshifts, verifying the robustness of BAO measurements with 21 cm intensity mapping. We study the clustering of HI in redshift space and show that linear theory can explain the ratio between the monopoles in redshift and real space down to 0.3, 0.5, and $1 h \text{ Mpc}^{-1}$ at redshifts 3, 4, and 5, respectively. We find that the amplitude of the Fingers-of-God effect is larger for HI than for matter, since HI is found only in halos above a certain mass. We point out that 21 cm maps can be created from N -body simulations rather than full hydrodynamic simulations. Modeling the one-halo term is crucial for achieving percent accuracy with respect to a full hydrodynamic treatment. Although our results are not converged against resolution, they are, however, very useful as we work at the resolution where the model parameters have been calibrated to reproduce galaxy properties.

Key words: large-scale structure of universe – methods: numerical – radio lines: general

1. Introduction

The Λ CDM model describes how the initial quantum perturbations in the primordial universe grow and give rise to the cosmic web: large accumulations of matter in the form of dark matter halos accrete material through filaments and sheets that surround enormous diffuse regions in space. This model has been successful in explaining a very diverse set of cosmological observables, including, among others, the anisotropies in the cosmic microwave background (CMB), the spatial distribution of galaxies, the statistical properties of the Ly α forest, the abundance of galaxy clusters, and correlations in the shapes of galaxies induced by gravitational lensing.

The Λ CDM model has free parameters that describe physical quantities such as the geometry of the universe, the amount of cold dark matter (CDM) and baryons, the sum of the neutrino masses, the expansion rate of the universe, the nature of dark energy, and the initial conditions of the universe. The current quest in cosmology is to determine the values of these parameters as precisely as possible, by exploiting the fact that they influence the spatial distribution of matter. Thus, by examining the statistical properties of matter tracers such as galaxies and cosmic neutral hydrogen, the spatial distribution of matter can be inferred and the value of the cosmological parameters can be constrained.

The amount of information that can be extracted from cosmological surveys depends on several factors, such as the

volume being covered or the range in scales where theoretical predictions are reliable. For example, in the case of the CMB, theoretical predictions are extremely precise, because the radiation we observe was produced when the fluctuations were in the linear regime. Tracing the large-scale structure of the universe at low redshifts, through spectroscopic galaxy surveys, represents a complementary approach to extracting cosmological information, where much larger volumes can be surveyed but theoretical predictions are more uncertain. For galaxy surveys, the volume that can be probed also limits the method, because at high redshifts, galaxies are fainter and their spectroscopic detection is challenging.

A different way to trace the matter field is through 21 cm intensity mapping (Bharadwaj & Sethi 2001; Bharadwaj et al. 2001; Battye et al. 2004; McQuinn et al. 2006; Chang et al. 2008; Loeb & Wyithe 2008; Bull et al. 2015; Santos et al. 2015; Villaescusa-Navarro et al. 2015). The method consists of carrying out a low angular resolution survey where the total 21 cm flux from unresolved sources is measured on large areas of the sky at different frequencies. The emission arises from the hyperfine splitting of the ground state of neutral hydrogen into two levels because of the spin–spin interaction between the electron and proton. An electron located in the upper energy level can decay into the lower energy state by emitting a photon with a rest wavelength of 21 cm. This method has several advantages over traditional approaches. First, given that the observable is the 21 cm line, the method is spectroscopic in nature. Second, very large cosmological volumes can be surveyed in a fast and efficient manner. Third, the amplitude of the signal depends only on the abundance and clustering of neutral hydrogen, and so cosmic HI can be traced from $z = 0$ to $z \simeq 50$.¹⁴

Current, upcoming, and future surveys such as the Giant Meterwave Radio Telescope (GMRT),¹⁵ the Ooty Radio Telescope (ORT),¹⁶ the Canadian Hydrogen Intensity Mapping Experiment (CHIME),¹⁷ the Five-hundred-meter Aperture Spherical Telescope (FAST),¹⁸ Tianlai,¹⁹ BINGO (Baryon acoustic oscillations In Neutral Gas Observations),²⁰ ASKAP (The Australian Square Kilometer Array Pathfinder),²¹ MeerKAT (The South African Square Kilometer Array Pathfinder),²² HIRAX (The Hydrogen Intensity and Real-time Analysis eXperiment),²³ and the SKA (The Square Kilometer Array)²⁴ will sample the large-scale structure of the universe in the post-reionization era by detecting 21 cm emission from cosmic neutral hydrogen (Choudhuri et al. 2016; Carucci et al. 2017b; Marthi et al. 2017; Sarkar et al. 2018a, 2018b, 2016b).

In order to extract information from those surveys, the observational data has to be compared with theoretical predictions. To linear order, the amplitude and shape of the

21 cm power spectrum is given by

$$P_{21\text{ cm}}(k, \mu) = \bar{T}_b^2 [(b_{\text{HI}} + f\mu^2)^2 P_m(k) + P_{\text{SN}}], \quad (1)$$

where \bar{T}_b is the mean brightness temperature, b_{HI} is the HI bias, f is the linear growth rate, $\mu = k_z/k$, $P_m(k)$ is the linear matter power spectrum, and P_{SN} is the HI shot noise. Here, k_z is the projection of k along the line of sight, which we take to be the z -axis.

At redshifts $z \in [0, 5]$, we have relatively good knowledge of the abundance of cosmic neutral hydrogen, and therefore, of \bar{T}_b . On the other hand, little is known about the value of the HI bias and HI shot noise in that redshift interval. It is important to determine their values since the signal-to-noise ratio and range of scales where information can be extracted critically depend on them. One of the purposes of our work is to measure these quantities at different redshifts. Moreover, it is important to determine the regime where linear theory is accurate. In this work, we investigate in detail at which redshifts and scales the clustering of HI in real space (i.e., the HI bias) and in redshift space (Kaiser factor) becomes nonlinear.

In order to optimize what can be learned from the surveys mentioned above, theoretical predictions in the mildly and fully nonlinear regimes are needed. The halo model provides a reasonably accurate framework for predicting the abundance and clustering of HI from linear to fully nonlinear scales. To apply this method, several ingredients are needed for a given cosmological model: (1) the linear matter power spectrum, $P_{\text{lin}}(k, z)$, (2) the halo mass function, $n(M, z)$, (3) the halo bias, $b(M, z)$, (4) the average HI mass that a halo of mass M hosts at redshift z , $M_{\text{HI}}(M, z)$, which we refer to as the halo HI mass function,²⁵ and (5) the mean density profile of neutral hydrogen within halos of mass M at redshift z , $\rho_{\text{HI}}(r|M, z)$. In addition, the halo model is formulated under the assumption that all HI are confined to dark matter halos. With the above ingredients in hand, one can write the fully nonlinear HI power spectrum as the sum of one-halo and two-halo terms:

$$P_{\text{HI}}(k, z) = P_{\text{HI,1h}}(k) + P_{\text{HI,2h}}(k), \quad (2)$$

$$P_{\text{HI,1h}}(k, z) = \frac{1}{(\rho_c^0 \Omega_{\text{HI}}(z))^2} \int_0^\infty dM n(M, z) M_{\text{HI}}^2 \times (M, z) |u_{\text{HI}}(k|M, z)|^2, \quad (3)$$

$$P_{\text{HI,2h}}(k, z) = \frac{P_{\text{lin}}(k, z)}{(\rho_c^0 \Omega_{\text{HI}}(z))^2} \times \left[\int_0^\infty dM n(M, z) b(M, z) M_{\text{HI}}(M, z) |u_{\text{HI}}(k|M, z)|^2 \right], \quad (4)$$

where ρ_c^0 is the critical density of the universe today and $\Omega_{\text{HI}}(z) = \bar{\rho}_{\text{HI}}(z)/\rho_c^0$, with $\bar{\rho}_{\text{HI}}(z)$ being the mean HI density at redshift z . $u(k|M, z)$ is the Fourier transform of the normalized HI density profile: $u(x|M, z) = \rho_{\text{HI}}(x|M, z)/M_{\text{HI}}(M, z)$.

Some of the goals of our work are to quantify (1) the amount of HI outside of halos, (2) the form of the halo HI mass function, and (3) the density profiles of HI within halos.

While the halo model is a powerful analytic framework, it does not model accurately a number of things, e.g., the transition between the one-halo and two-halo terms (Massara et al. 2014).

²⁵ Note that the term ‘‘HI mass function’’ is commonly used to model the abundance of galaxies with different HI masses. Thus, in order to distinguish the two concepts, we use ‘‘halo HI mass function’’ to refer to the function that returns the average HI mass inside a halo of mass M at redshift z .

¹⁴ At higher redshifts, the atmosphere becomes opaque at the relevant wavelengths.

¹⁵ <http://gmrt.ncra.tifr.res.in/>

¹⁶ <http://rac.ncra.tifr.res.in/>

¹⁷ <http://chime.phas.ubc.ca/>

¹⁸ <http://fast.bao.ac.cn/en/>

¹⁹ <http://tianlai.bao.ac.cn>

²⁰ <http://www.jb.man.ac.uk/research/BINGO/>

²¹ <http://www.atnf.csiro.au/projects/askap/index.html>

²² <http://www.ska.ac.za/meerkat/>

²³ <https://www.acru.ukzn.ac.za/~hirax/>

²⁴ <https://www.skatelescope.org/>

Thus, its accuracy can be severely limited by that. A more precise modeling can be achieved by painting HI on top of dark matter halos according to the HI halo model ingredients (Villaescusa-Navarro et al. 2014), i.e., more like HI halo occupation distribution (HOD) modeling.

Since 21 cm intensity mapping observations are carried out in redshift space, modeling the abundance and spatial distribution of HI in halos is not enough. A complete description also requires knowing the distribution of HI velocities. In this work, we investigate the HI bulk velocities, the velocity dispersion of HI inside halos, and the amplitude of the Fingers of God in the power spectrum.

The standard halo model does not account for the various complexities expected in the real universe, e.g., whether the HI density profiles depend not only on mass but also on the galaxy population (blue/red) of the halo, whether the clustering of halos depends not only on mass but also on environment, and so forth. These questions can, however, be addressed with hydrodynamic simulations, and in this paper we investigate them in detail.

We also study some quantities that can help us to improve our knowledge of the spatial distribution of HI: the probability distribution function of HI, the relation between the overdensities of matter and HI, the contribution of central and satellite galaxies to the total HI mass content in halos, the HI column density distribution function, and the cross-section of damped Ly α systems (DLAs).

We carry out our analysis using the IllustrisTNG Project, state-of-the-art hydrodynamic simulations that follow the evolution of billions of resolution elements representing CDM, gas, black holes, and stars in the largest volumes ever explored at such mass and spatial resolution. Given the realism of our hydrodynamic simulations, we always aim to connect our results to the underlying physical processes. We note that previous works have studied the HI content of simulated galaxies in detail (Duffy et al. 2012; Davé et al. 2013; Bird et al. 2014; Lagos et al. 2014; Bahé et al. 2016; Faucher-Giguère et al. 2016; Crain et al. 2017; Marinacci et al. 2018; Xie et al. 2017; Zoldan et al. 2017).

We also show that once the most important ingredients for modeling the abundance and clustering properties of HI have been calibrated using full hydrodynamic simulations, less costly dark-matter-only simulations or approximate methods such as COLA (Tassev et al. 2013), PEAK-PATCH, or PINOCCHIO (Monaco et al. 2002; Munari et al. 2017) can be used to generate accurate 21 cm maps. Those maps can then be used to study other properties of HI in the fully nonlinear regime, such as the 21 cm bispectrum or the properties of HI voids. In this work, we investigate the accuracy achieved by creating 21 cm maps from N -body simulations with respect to full hydrodynamic simulations.

This paper is organized as follows. In Section 2, we describe the characteristics of the IllustrisTNG simulations and the method we use to estimate the mass of neutral hydrogen associated with each gas cell. We consider different properties of the abundance of HI in Sections 3–12:

1. In Section 3, we compare the overall HI abundance in our simulations to observations.
2. In Section 4, we quantify the fraction of HI within halos and galaxies.
3. In Section 5, we study the halo HI mass function.

4. In Section 6, we investigate the density profiles of HI inside halos.
5. In Section 7, we quantify the fraction of the HI mass in halos in the central and satellite galaxies.
6. In Section 8, we examine the probability distribution function (pdf) of the HI density and compare it with the total matter density pdf.
7. In Section 9, we compute the HI column density distribution function for the absorbers with high column density and quantify the cross-section and bias of DLAs.
8. In Section 10, we consider the bulk velocities of HI inside halos.
9. In Section 11, we investigate the velocity dispersion of HI inside halos and compare it against that of matter.
10. In Section 12, we quantify the relation between the overdensity of matter and HI.

We investigate HI clustering in Sections 13–16:

1. In Section 13, we present the amplitude and shape of the HI bias and investigate how well perturbation theory can reproduce HI clustering in real space.
2. In Section 14, we show that the clustering of dark matter halos in general depends on their HI masses for fixed halo mass.
3. In Section 15, we quantify the amplitude of the HI shot noise.
4. In Section 16, we study the clustering of HI in redshift space.

In Section 17, we estimate the accuracy that can be achieved by simulating HI through a combination of N -body simulations with the results derived in the previous sections rather than through full hydrodynamic simulations. Finally, we provide the main conclusions of our work in Section 18. During the course of the discussion, we provide fitting formulae that can be used to reproduce our results.

We emphasize that our results are not converged against resolution (see Appendix A). This should, however, not be seen as a limitation of our claims, as we present results for TNG100, i.e., at the resolution to which the model parameters have been tuned to reproduce a set of galaxy properties.

2. Methods

2.1. The IllustrisTNG Simulations

The simulations used in this work are part of the IllustrisTNG Project (Marinacci et al. 2018; Naiman et al. 2018; Pillepich et al. 2018a; Springel et al. 2018; Nelson et al. 2018). We employ two cosmological boxes that have been evolved to $z = 0$, TNG100 (which is the same volume as the Illustris simulation; Genel et al. 2014; Vogelsberger et al. 2014a, 2014b) and TNG300, with $75 h^{-1}$ Mpc and $205 h^{-1}$ Mpc comoving on a side, respectively. In particular, we use their high-resolution realizations that evolve baryonic resolution elements with mean masses of $1.4 \times 10^6 M_{\odot}$ and $1.1 \times 10^7 M_{\odot}$, respectively.

These simulations have been run with the AREPO code (Springel 2010), which calculates gravity using a tree-PM method, magnetohydrodynamics with a Godunov method on a moving Voronoi mesh, and a range of astrophysical processes described by subgrid models. These processes include primordial and metal-line cooling assuming a time-dependent uniform UV background radiation, star and supermassive black hole formation, stellar population evolution that enriches

surrounding gas with heavy elements or metals, galactic winds, and several modes of black hole feedback. Importantly, where uncertainty and freedom exist for the implementation of these models, they are parameterized and tuned to obtain a reasonable match to a small set of observational results. These include the galaxy stellar mass function and the baryon content of group-scale dark matter halos, both at $z = 0$. The numerical methods and subgrid physics models build upon Vogelsberger et al. (2013) and are specified in full in Weinberger et al. (2017, 2018) and Pillepich et al. (2018b). Accounts of the match between the simulations and observations in a number of diverse aspects, such as galaxy and halo sizes, colors, metallicities, magnetic fields, and clustering, are presented in the references above as well as in Genel et al. (2018), Vogelsberger et al. (2018), and Torrey et al. (2017).

In this paper, we work mainly with halos identified by the Friends-of-Friends (FoF) algorithm with a linking length of $b = 0.2$ (Davis et al. 1985). We take the halo center as the position of the most bound particle in the halo. For each FoF halo, we also use the halo’s “virial” radius, defined using $M = 4\pi/3\Delta_c\rho_cR^3$, where ρ_c is the critical density of the universe at the halo’s redshift z and $\Delta_c = 18\pi^2 + 82x - 39x^2$, with $x = \Omega_m(1+z)^3/(\Omega_m(1+z)^3 + \Omega_\Lambda) - 1$ (Bryan & Norman 1998). We refer to these objects as “FoF-SO” halos, for “spherical overdensity,” since a single SO (spherical overdensity) halo is identified for each FoF halo.²⁶ Unless stated explicitly, we refer to FoF halos when talking generally about dark matter halos. The SUBFIND algorithm (Springel et al. 2001) has been run to identify self-bound substructures in each FoF halo, and those objects are referred to as “galaxies” in what follows. This class of objects includes both the satellites and the central SUBFIND subhalos of each FoF halo.

2.2. Modeling the Hydrogen Phases

We now describe the method we use to quantify the fraction of hydrogen that is in each phase (neutral, ionized, or molecular) for each Voronoi cell in the simulation.

For non-star-forming gas, we use the division between neutral and ionized mass fractions that is calculated in the IllustrisTNG runs on the fly and is included in the simulation outputs. This breakdown assumes primordial chemistry in photoionization equilibrium with the cosmic background radiation (Faucher-Giguère et al. 2009), including a density-dependent attenuation thereof to account for self-shielding following Rahmati et al. (2013a).

For star-forming gas, we post-process the outputs of the simulations to account for the multiphase interstellar medium, including the presence of molecular hydrogen, H_2 . The values stored in the simulation output are based on the mass-weighted temperature between the cold and hot phases according to the Springel & Hernquist (2003) model and are thus expected to underestimate the neutral hydrogen fraction. Instead, we set the temperature of star-forming cells to $T = 10^4$ K and recalculate the equilibrium neutral hydrogen fraction, also including the self-shielding correction.

The above procedure gives the fraction of hydrogen that is neutral: $M_{\text{NH}}/M_{\text{H}}$, with $M_{\text{NH}} = M_{\text{HI}} + M_{\text{H}_2}$. We then compute the H_2 fraction, $f_{\text{H}_2} = M_{\text{H}_2}/M_{\text{NH}}$, employing the Krumholz, McKee, & Tumlinson (KMT) model (Krumholz et al. 2008, 2009;

McKee & Krumholz 2010; see also Sternberg et al. 2014), which we briefly review here.

The molecular hydrogen fraction, f_{H_2} , which we assume to be non-zero only for star-forming gas, is estimated through

$$f_{\text{H}_2} = \begin{cases} 1 - \frac{0.75s}{1 + 0.25s} & \text{if } s < 2, \\ 0 & \text{if } s \geq 2 \end{cases}, \quad (5)$$

where s is given by

$$s = \frac{\log(1 + 0.6\chi + 0.01\chi^2)}{0.6\tau_c}, \quad (6)$$

and

$$\chi = 0.756(1 + 3.1Z^{0.365}), \quad (7)$$

$$\tau_c = \Sigma\sigma_d/\mu_{\text{H}}. \quad (8)$$

In the above equations, Z represents the gas metallicity in units of solar metallicity (Allende Prieto et al. 2001); σ_d is the cross-section of dust, which we estimate from $\sigma_d = Z \times 10^{-21} \text{ cm}^2$; μ_{H} is the mean mass per hydrogen nucleus, $\mu_{\text{H}} = 2.3 \times 10^{-24} \text{ g}$; and Σ is the surface density of the gas, which we compute as $\Sigma = \rho R$, where ρ is the gas density and $R = (3V/4\pi)^{1/3}$ with V being the volume of the Voronoi cell.

It is possible that our treatment may underestimate the H_2 fractions since (1) the molecular hydrogen fractions go to zero at low densities in the KMT model, (2) we assign molecular hydrogen only to star-forming cells, and (3) it is pessimistic to estimate the surface density from the cell radii. However, we believe that a more precise treatment of H_2 will not affect our results, as its overall abundance is small and therefore not much HI will be transformed into H_2 . In order to test this more explicitly, we have considered two extreme cases in which (1) no H_2 is modeled, and (2) all hydrogen in star-forming cells is in molecular form. We have computed the value $\Omega_{\text{HI}}(z)$ (see Section 3) and did not find significant changes for the first case. On the other hand, at $z \in [1-3]$, the prescription where we put all hydrogen in star-forming cells in molecular form can change results by a factor of $\simeq 2-3$. We note that Diemer et al. (2018) have recently investigated the impact of different H_2 models on the HI mass function, finding that the results are rather insensitive to the method used to simulate molecular hydrogen at $z = 0$, although larger differences show up at higher redshifts. We thus believe that our conclusions are robust against our H_2 treatment at low redshift. Quantifying the uncertainty in our results arising from the H_2 model at higher redshift is beyond the scope of this paper.

We note that in our approach we have considered ionization only from the UV background. In other words, we are ignoring the contribution of ionizing photons from, e.g., local sources (Miralda-Escudé 2005; Schaye 2006; Rahmati et al. 2013b) or X-ray heating from the intracluster medium (Kannan et al. 2016).

Figure 1 shows the $z = 1$ spatial distribution of HI and gas in slices of $5 h^{-1} \text{ Mpc}$ depth throughout the entire TNG100 simulation box as well as in zoomed-in regions thereof. We see that the Ly α forest dominates the abundance of HI in terms of volume, but the HI inside galaxies dominates in terms of mass.

²⁶ Notice that a pure SO algorithm may identify several SO halos inside a single FoF halo (see Appendix D).

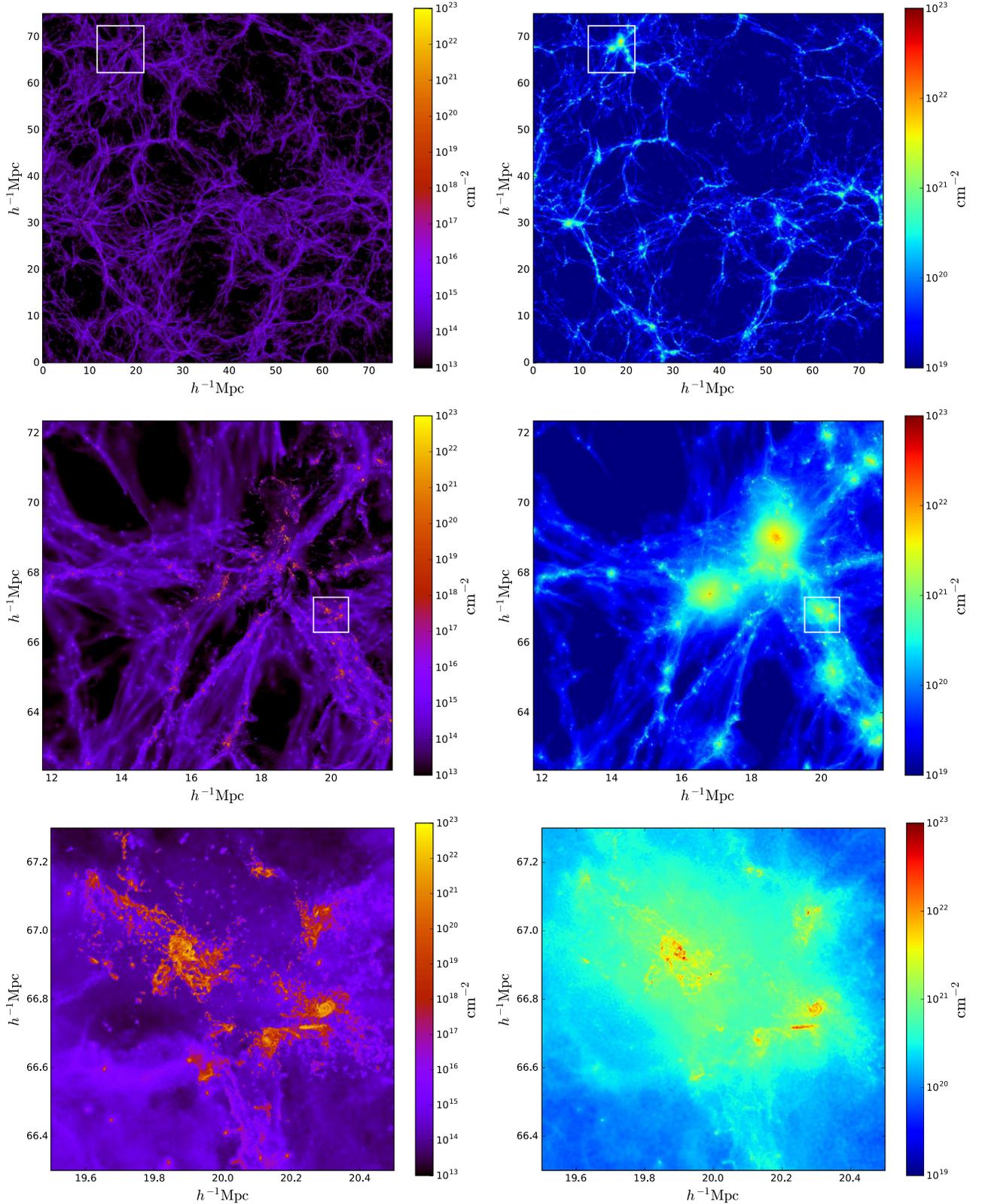


Figure 1. Spatial distribution of neutral hydrogen (left) and gas (right) in slices of $5 h^{-1} \text{Mpc}$ depth at redshift $z = 1$. The upper panels show the distribution in the entire simulation volume of TNG100, while the middle and bottom panels display a zoom-in into the regions marked with a white square in the upper and middle panels, respectively. Although the HI in the Ly α forest occupies most of the volume, the HI in galaxies represents the majority of its total mass.

3. Overall HI Abundance: $\Omega_{\text{HI}}(z)$

Here, we study the overall abundance of neutral hydrogen in the IllustrisTNG simulations. In Figure 2, we show the value of

$\Omega_{\text{HI}}(z)$ from TNG300 (solid black) and TNG100 (dashed black). In this plot, we also indicate measurements from different observations (Rao et al. 2006; Zwaan & Prochaska 2006; Lah et al. 2007; Martin et al. 2010; Songaila & Cowie 2010;

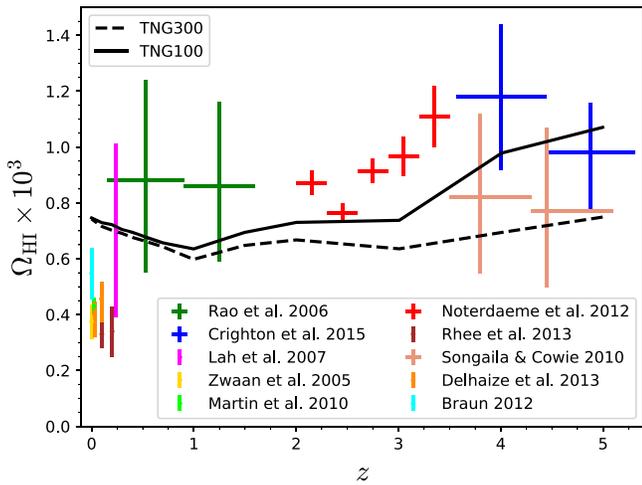


Figure 2. $\Omega_{\text{HI}}(z) = \rho_{\text{HI}}(z)/\rho_c^0$ from observations (colored points) and from the simulations (black lines) as a function of redshift. Our highest resolution simulation, TNG100, reproduces well the abundance of cosmic H I in the post-reionization era, although it slightly overpredicts/underpredicts the H I abundance at $z=0/z \in [2-3.5]$. A simulation with even higher mass resolution would likely yield an increased H I abundance.

Braun 2012; Noterdaeme et al. 2012; Delhaize et al. 2013; Rhee et al. 2013; Crighton et al. 2015).

The agreement between the results from our simulations and observations is good, although the simulations tend to overpredict the amount of H I at redshifts $z < 0.5$ and underpredict the H I abundance at $2 < z < 3.5$. Compared to earlier studies with hydrodynamic simulations (e.g., Davé et al. 2013; Bird et al. 2014) and semi-analytic models (Lagos et al. 2014), however, our results agree better with observations at $z > 1$ and are comparable to the agreement found by Rahmati et al. (2015).

We have investigated whether different H_2 models can improve the agreement between our results and observations at low redshift, finding that they play a very minor role and therefore our conclusions are robust against it. We however believe that the inclusion of the ionization from sources (not incorporated here due to its highly demanding computational needs) can alleviate that tension. Whether this disagreement between observations and simulations is due to the subgrid physics of our simulations or to our approximate modeling of H I is beyond the scope of this work.

The overall H I mass in the simulations depends on resolution, such that the simulation with higher resolution, TNG100, contains between $\approx 2.5\%$ and $\approx 40\%$ more H I in the redshift interval $z = 0-5$ than TNG300. This is mainly a consequence of the fact that TNG300 cannot resolve the smallest halos where H I resides but we believe that this is also due to our H I/ H_2 postprocessing (see Appendix A for resolution tests). This can be seen in Figure 4, where we show the H I mass within halos versus the total halo mass. In TNG300, halos with masses only above $2 \times 10^9 h^{-1} M_\odot$ can be resolved, assuming a minimum of 50 CDM particles in a halo. From Figure 4, we see that the amount of H I in halos below that mass is not negligible at high redshift, thus we would expect that Ω_{HI} will be lower at high redshift in TNG300 in comparison with TNG100, as we find. We note that at low redshift, the results of TNG100 and TNG300 are very similar. Since our results for the H I abundance in halos are not converged (see Appendix A), this agreement is just a

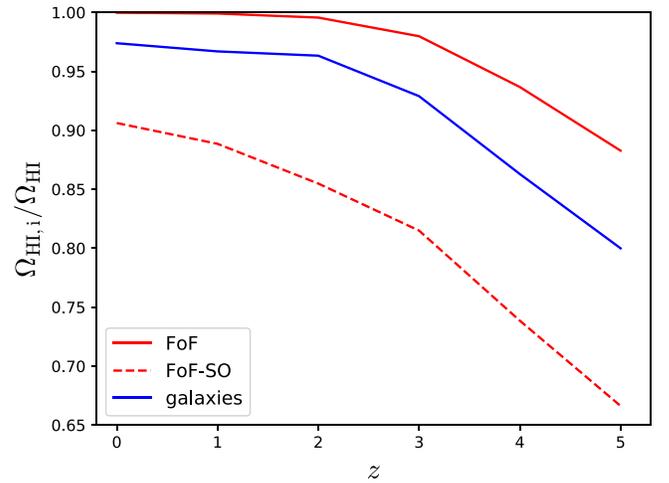


Figure 3. The fraction of total H I mass that is inside FoF halos (solid red lines), FoF-SO halos (dashed red lines), and galaxies (blue lines) as a function of redshift. At low redshift, nearly all H I is located within FoF halos and galaxies, while at high redshift, the amount of H I outside FoF halos/galaxies can be 10%/20%. There is a significant amount of H I in the outskirts of FoF halos: the fraction of H I inside FoF-SO halos ranges from 90% at $z = 0$ to 67% at $z = 5$.

coincidence. It is not clear to us whether a higher resolution simulation will output a larger or smaller value of Ω_{HI} at $z \simeq 0$.

In this paper, we examine the most important properties of cosmic neutral hydrogen over a wide range of redshifts. Not being able to resolve the H I that is contained within the smallest halos impacts our results in several ways. For example, the values of the H I bias, H I shot noise, the H I halo mass function, or the amplitude of the H I Fingers-of-God effect will be affected by this. For this reason, from now on we focus our analysis on the TNG100 simulation.

4. H I Fraction in Halos and Galaxies

The fraction of the total H I mass that resides within halos is an important ingredient for theoretical frameworks that aim to model the abundance and clustering properties of cosmic neutral hydrogen, such as the halo model (Cooray & Sheth 2002; Barnes & Haehnelt 2014; Villaescusa-Navarro et al. 2014; Padmanabhan & Refregier 2017; Padmanabhan et al. 2016, 2017). In particular, these methods make the assumption that all H I are confined within halos, whose properties, such as spatial distribution or abundance, are well-described by analytic models and/or numerical simulations.

In contrast to the gas in halos, the properties of the gas in the intergalactic medium (IGM) are more difficult to model analytically (see, however, Iršič & McQuinn 2018). The standard approach has been to characterize the gas in the IGM using numerical simulations. If a significant amount of H I is found outside halos, any standard H I halo model will need to be complemented with either simulations or further analytic ingredients. Below, we determine the amount of H I that is outside of halos to quantify the limitations of standard H I halo models.

We have computed the H I mass inside each FoF, FoF-SO, and galaxy in the simulation at several redshifts. In Figure 3, we show, for each of these object types, the fraction of the total H I mass in the simulation that resides inside all objects combined.

We find that at redshifts $z \leq 2$, more than 99% of all H I is contained within FoF halos. While a significant fraction of the baryons lie outside these regions, the IGM is highly ionized at these times. At these redshifts, the fraction of H I within galaxies is larger than 95%. We note that SUBFIND may not identify any subhalo/galaxy within an FoF halo. This could happen for several reasons, like low density or virialization not having been reached. Thus, we conclude that at these redshifts, $\simeq 5\%$ of the cosmic neutral hydrogen is outside galaxies²⁷ but inside halos.

The fraction of H I within FoF halos and galaxies decreases monotonically with redshift. At redshift $z = 5$, the H I inside FoF halos only accounts for 88% of the total H I, while the mass within galaxies is 80%. These results are in qualitative agreement with Villaescusa-Navarro et al. (2014), who studied the H I outside halos using a different set of hydrodynamic simulations. Moreover, we find that our results are not significantly affected by mass resolution, since the same analysis carried out for the TNG300 simulation gives similar results.

We consider our finding that the fraction of H I outside halos increases with redshift to be reasonable. At high redshift, the gas in the IGM is denser and the amplitude of the UV background is lower, and so it is easier for that gas to host higher fractions of neutral hydrogen (see Appendix B for further details).

The fraction of H I outside FoF-SO halos is not negligible, varying from 10% at $z = 0$ to 33% at $z = 5$. On average, the ratio of H I mass in FoF-SO halos to that in FoF halos is similar to the ratio between their total masses. Thus, FoF's host more H I than FoF-SO halos simply because they are larger and more massive. This also tells us that the regions beyond the virial radius of typical halos are neither H I-poor nor H I-rich, while when this is examined specifically in massive halos we find these regions to be H I rich (see Appendix D for further details).

We thus conclude that while the standard assumption that all H I lies within halos is reasonable at $z \leq 2$, at high redshift it begins to break down since a small fraction is located outside halos ($\sim 10\%$ at $z = 5$). The numbers derived here can be used to quantify the limitations of H I halo models that target the distribution of H I at high redshift.

5. Halo H I Mass Function

In the previous section, we have shown that most of the H I is inside halos, justifying the use of H I halo models to characterize the spatial distribution of H I. As discussed in the introduction, besides the linear matter power spectrum, halo mass function, and halo bias, we need to know the halo H I mass function (i.e. the average H I mass hosted by a halo of mass M at redshift z) and the spatial distribution of H I inside halos. Below, we investigate the former: $M_{\text{H I}}(M, z)$.

We emphasize the paramount importance of this function by noting that knowing it is sufficient for predicting the amplitude and shape of the 21 cm power spectrum to linear order (see Equation (1)):

$$P_{21 \text{ cm}}(k, \mu, z) = \bar{T}_b(z)^2 [(b_{\text{H I}}(z) + f(z)\mu^2)^2 P_m(k, z) + P_{\text{SN}}(z)],$$

²⁷ We emphasize that the term ‘‘galaxy’’ should be considered in our framework, not in the traditional observational definition. For instance, gas far away from the center of a halo but gravitationally bound to it will still be considered as belonging to that galaxy.

where $\bar{T}_b(z)$, $b_{\text{H I}}(z)$, and $P_{\text{SN}}(z)$ can all be derived from $M_{\text{H I}}(M, z)$ as

$$\bar{T}_b(z) = 189h \left(\frac{H_0(1+z)^2}{H(z)} \right) \Omega_{\text{H I}}(z) \text{ mK}, \quad (9)$$

$$\Omega_{\text{H I}}(z) = \frac{1}{\rho_c^0} \int_0^\infty n(M, z) M_{\text{H I}}(M, z) dM, \quad (10)$$

$$b_{\text{H I}}(z) = \frac{1}{\rho_c^0 \Omega_{\text{H I}}(z)} \int_0^\infty n(M, z) b(M, z) M_{\text{H I}}(M, z) dM, \quad (11)$$

$$P_{\text{SN}}(z) = \frac{1}{(\rho_c^0 \Omega_{\text{H I}}(z))^2} \int_0^\infty n(M, z) M_{\text{H I}}^2(M, z) dM, \quad (12)$$

where $n(M, z)$ and $b(M, z)$ are the halo mass function and halo bias, respectively. Knowledge of this function can be used to understand the impact of different phenomena on the amplitude and shape of the 21 cm power spectrum such as neutrino masses (Villaescusa-Navarro et al. 2015), warm dark matter (Carucci et al. 2015), or modified gravity (Carucci et al. 2017a).

For each dark matter halo in the simulation, we have computed its enclosed H I mass. In Figure 4, we show the H I mass versus halo mass for each single FoF halo in the simulation at redshifts 0, 1, 2, 3, 4, and 5. The color indicates the number of halos in each bin. We show this map rather than the $M_{\text{H I}}(M, z)$ function since the former contains more information, such as the scatter in $M_{\text{H I}}(M, z)$. The vertical lines represent a halo mass comprising 50 CDM particles. Its purpose is just to provide the reader with a halo mass for barely resolved halos. We, however, emphasize that 50 CDM particles will not be enough to have internal halo properties, such as concentration, converged.

The halo H I mass function increases monotonically with halo mass. Two trends can be identified: (1) in the high-mass end, $M_{\text{H I}}(M, z)$ can be approximated by a power law, and (2) in the low-mass end, it has a sharp cutoff. A good fit to our results is given by

$$M_{\text{H I}}(M, z) = M_0 \left(\frac{M}{M_{\text{min}}} \right)^\alpha \exp(- (M_{\text{min}}/M)^{0.35}). \quad (13)$$

The free parameters are M_{min} , which sets the cutoff mass in $M_{\text{H I}}(M, z)$; α , which controls the slope of the function at the high-mass end; and M_0 , which determines the overall normalization and represents $\simeq 40\%$ of the H I mass of a halo of mass M_{min} . We have fitted our results to this function and give the best fitting values for both FoF and FoF-SO halos in Table 1. The green lines in Figure 4 indicate the best fits at each redshift.

At redshifts $z \geq 3$, for FoF halos, α is $\simeq 0.75$, while it decreases at lower redshifts: $\alpha = 0.60$ at $z = 2$, $\alpha = 0.53$ at $z = 1$, and $\alpha = 0.24$ at $z = 0$. We interpret this as a result of several physical processes, such as AGN feedback and ram-pressure and tidal stripping, being more efficient at removing gas from galaxies at lower redshift than at higher redshifts.

The value of M_{min} decreases monotonically with redshift, from $\simeq 2 \times 10^{12} h^{-1} M_\odot$ at $z = 0$ to $2 \times 10^{10} h^{-1} M_\odot$ at $z = 5$. This indicates that as the redshift increases, lower mass halos host H I. In Appendix C, we discuss the physical origin of the cutoff in the halo H I mass function and the relative importance of supernova feedback and gas stripping, and the UV background for this.

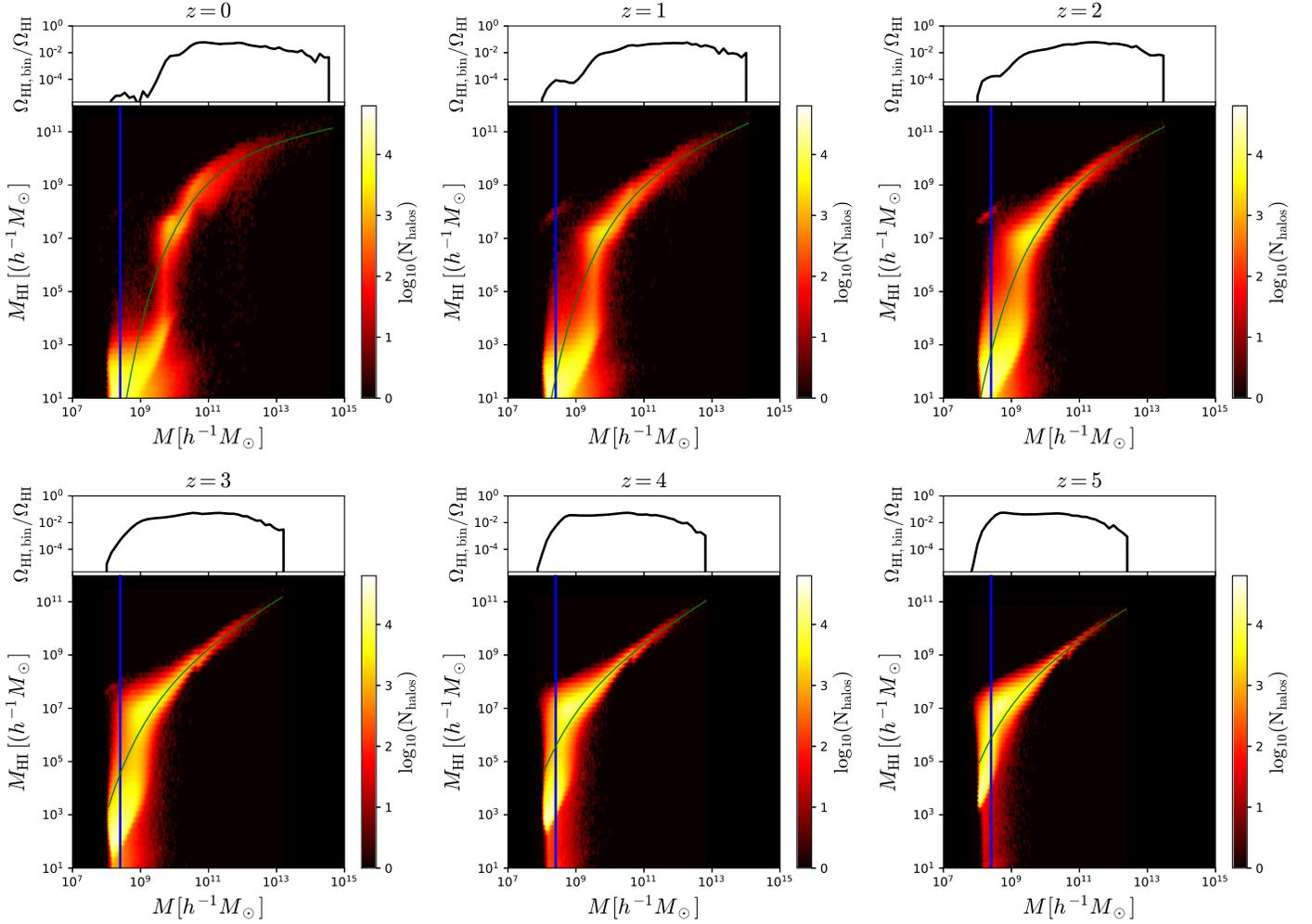


Figure 4. Halo HI mass function. For each FoF halo of the simulation TNG100, we compute the total HI mass it hosts. The plots show the HI mass vs. halo mass, color coded by the number of halos in each bin. The blue vertical lines show the mass corresponding to a halo that hosts 50 dark matter particles, which we adopt as a rough mass resolution threshold for dark matter halos. We take narrow bins in halo mass and compute the total HI mass in each of them. The top part of each panel shows the ratio between the total HI mass in the bin and the total HI mass in all halos. Our results can be well reproduced by the fitting formula $M_{\text{HI}}(M, z) = M_0 x^\alpha e^{-1/x^{0.35}}$, with $x = M/M_{\text{min}}$. The best fits are shown with green lines at each redshift. We emphasize that our results are not converged against resolution (see Appendix A). This should, however, not be seen as a limitation of our claims, as we present results for TNG100, i.e., at the resolution to which the model parameters have been tuned to reproduce a set of galaxy properties. For instance, our results for the halo HI mass function at $z = 0$ are in excellent agreement with observations (Obuljen et al. 2018b).

Similar conclusions can be reached when computing $M_{\text{HI}}(M, z)$ using FoF-SO halos (see Table 1). The derived values of α , M_0 , and M_{min} are roughly compatible, within the errors, between FoF and FoF-SO halos. There are, however, systematic differences between the best-fit values from FoF and FoF-SO, which is because the total amount of HI in a given halo is sensitive to its definition, as we will see below.

For FoF-SO halos, we can relate halo masses to circular velocities through $V_{\text{circ}} = \sqrt{GM/R}$, where G is the gravitational constant and M and R are the halo mass and radius. Expressing M_{min} in terms of circular velocities, we obtain $V_{\text{circ}}(M_{\text{min}}) \simeq 180 \pm 20 \text{ km s}^{-1}$ for $z \in [0, 2]$ and $V_{\text{circ}}(M_{\text{min}}) \simeq 120 \pm 20 \text{ km s}^{-1}$ for $z \in [3, 5]$. This suggests that the minimum halo mass that can host HI depends primarily on the depth of its gravitational potential and that at lower redshifts, the potential has to be deeper since astrophysical processes such as AGN feedback, tidal stripping, and so forth are more effective at removing gas from small halos.

Since our parameterization of the halo HI mass function does not have a “hard” cutoff, the value of M_{min} only represents

a mass scale at which the halo HI mass function changes its trend. In other words, halos with masses around M_{min} host a significant amount of HI. It is also very interesting to quantify the cutoff in the halo HI mass function more rigidly, i.e., so that halos below a certain mass contain a negligible amount of HI.

We have calculated the halo mass at which 98% of all HI in halos is above that mass and only 2% is in smaller halos. We term this halo mass as a “hard cutoff mass,” M_{hard} ,

$$\frac{\int_0^{M_{\text{hard}}} n(M, z) M_{\text{HI}}(M, z) dM}{\int_0^\infty n(M, z) M_{\text{HI}}(M, z) dM} = 0.02, \quad (14)$$

and we show the corresponding values in Table 1. For FoF-SO halos, we obtain 1.3×10^{10} , 6.1×10^9 , 2.5×10^9 , 7.6×10^8 , 2.3×10^8 , and $1.7 \times 10^8 h^{-1} M_\odot$ at redshifts 0, 1, 2, 3, 4, and 5, respectively. These can be transformed to circular velocities, giving 34, 35, 31, 24, 19, and 18 km s^{-1} at redshifts 0, 1, 2, 3, 4, and 5, correspondingly. The values we infer do not change

Table 1.
We Fit Our Results for the $M_{\text{HI}}(M, z)$ Function to the Form $M_0 x^\alpha \exp(-1/x^{0.35})$, where $x = M/M_{\text{min}}$

| z | FoF | | | | FoF-SO | | | |
|-----|-----------------|--------------------------------|--|---|-----------------|--------------------------------|--|---|
| | α | M_0 [$h^{-1} M_\odot$] | M_{min} [$h^{-1} M_\odot$] | M_{hard} [$h^{-1} M_\odot$] | α | M_0 [$h^{-1} M_\odot$] | M_{min} [$h^{-1} M_\odot$] | M_{hard} [$h^{-1} M_\odot$] |
| 0 | 0.24 ± 0.05 | $(4.3 \pm 1.1) \times 10^{10}$ | $(2.0 \pm 0.6) \times 10^{12}$ | 1.5×10^{10} | 0.16 ± 0.05 | $(4.1 \pm 1.0) \times 10^{10}$ | $(2.4 \pm 0.7) \times 10^{12}$ | 1.3×10^{10} |
| 1 | 0.53 ± 0.06 | $(1.5 \pm 0.7) \times 10^{10}$ | $(6.0 \pm 2.9) \times 10^{11}$ | 6.9×10^9 | 0.43 ± 0.06 | $(1.8 \pm 0.8) \times 10^{10}$ | $(8.6 \pm 4.2) \times 10^{11}$ | 6.1×10^9 |
| 2 | 0.60 ± 0.05 | $(1.3 \pm 0.6) \times 10^{10}$ | $(3.6 \pm 1.6) \times 10^{11}$ | 3.1×10^9 | 0.51 ± 0.05 | $(1.5 \pm 0.7) \times 10^{10}$ | $(4.6 \pm 2.1) \times 10^{11}$ | 2.5×10^9 |
| 3 | 0.76 ± 0.05 | $(2.9 \pm 2.0) \times 10^9$ | $(6.7 \pm 4.0) \times 10^{10}$ | 9.9×10^8 | 0.69 ± 0.06 | $(3.7 \pm 2.6) \times 10^9$ | $(9.6 \pm 6.0) \times 10^{10}$ | 7.6×10^8 |
| 4 | 0.79 ± 0.04 | $(1.4 \pm 1.0) \times 10^9$ | $(2.1 \pm 1.3) \times 10^{10}$ | 3.9×10^8 | 0.61 ± 0.06 | $(4.5 \pm 2.7) \times 10^9$ | $(7.6 \pm 4.4) \times 10^{10}$ | 2.3×10^8 |
| 5 | 0.74 ± 0.04 | $(1.9 \pm 1.2) \times 10^9$ | $(2.0 \pm 1.2) \times 10^{10}$ | 2.7×10^8 | 0.59 ± 0.07 | $(4.1 \pm 2.8) \times 10^9$ | $(5.4 \pm 3.6) \times 10^{10}$ | 1.7×10^8 |

Note. This table shows the best-fit value of the free parameters, for FoF and FoF-SO halos, at different redshifts. The column M_{hard} indicates the value of our hard cutoff mass, which is defined so that halos with masses $M \geq M_{\text{hard}}$ host 98% of all H I in halos. For FoF-SO halos, we can express M_{hard} in terms of circular velocities, giving 34, 35, 31, 24, 19, and 18 km s⁻¹ at redshifts 0, 1, 2, 3, 4, and 5, respectively.

much if we use a threshold equal to 99%. We thus conclude that at redshifts $z \leq 2$, only halos with circular velocities above about 30 km s⁻¹ host H I, while at redshifts $z \geq 3$, the H I is only in halos with circular velocities above ~ 20 km s⁻¹.

A more conventional parameterization of the halo H I mass function

$$M_{\text{HI}}(M, z) = M_0 \left(\frac{M}{M_{\text{min}}} \right)^\alpha \exp(-M_{\text{min}}/M) \quad (15)$$

also reproduces our results. The fit in Equation (13) is, however, preferred for our results since at high redshift, $M_{\text{HI}}(M, z)$ falls more slowly for very low halo masses than the standard profile. In order to facilitate the comparison with works using the above parameterization (e.g., Bagla et al. 2010; Castorina & Villaescusa-Navarro 2017; Obuljen et al. 2018a; Padmanabhan et al. 2017; Villaescusa-Navarro et al. 2017; Pénin et al. 2018), we also provide the best-fit values for the more conventional fit in Appendix E.

6. H I Density Profile

Another important ingredient in describing the spatial distribution of cosmic neutral hydrogen using H I halo models is the density profile of H I inside halos (see Equations (2)–(4)). In this section, we investigate the spatial distribution of H I inside simulated dark matter halos.

Since FoF halos can have very irregular shapes, we have computed the H I profiles inside FoF-SO halos. For each FoF-SO halo, we have computed the H I mass within narrow spherical shells up to the virial radius, and from them the H I profile. Figure 5 shows the individual H I profiles for halos in a narrow mass bin at different redshifts with gray lines. The large halo-to-halo scatter is surprising and highlights the fact that individual H I profiles, as opposed to dark matter ones, are far from universal.

The scatter is particularly large toward the centers of massive halos, as discussed below, as well as for halos with masses around or below the cutoff we observe in Figure 4. This is expected, as the halo H I mass function also exhibits large scatter in that range. As we will see later in Section 14, the clustering of halos in that mass range depends significantly on their H I mass. Thus, it is likely that the H I content of these halos is influenced by their environment, so small halos around more massive ones may have lost or gained a significant fraction of their H I mass due to related effects.

The scatter generally tends to be lower at higher redshifts and, in particular, is small in halos with masses above $10^{10} h^{-1} M_\odot$ at redshift $z = 5$. This is related to the lower scatter we find at high redshift in the halo H I mass function, $M_{\text{HI}}(M, z)$ (see Figure 4). We speculate that this originates from a reduced role that AGN feedback and environmental gas stripping play at earlier times.

The blue lines in Figure 5 show the mean and the standard deviation of the H I profiles from all halos that lie in each mass bin and redshift, while the red lines display the median. Clearly, in some cases they differ substantially. This behavior can be partially attributed to the H I profiles arising from two distinct populations: i.e., H I-rich blue galaxies versus H I-poor red ones (Nelson et al. 2018). This can clearly be seen in the panel in Figure 5 corresponding to halos in the mass range $M \in [1-2] \times 10^{12} h^{-1} M_\odot$ at $z = 0$. In this range, some halos have a core in their H I profiles while others do not. The reason is that the central galaxy of some halos is experiencing AGN feedback (those with holes in the profile) and are therefore becoming red, while the galaxies in the other halos are not yet being affected by AGN feedback, remaining blue (Nelson et al. 2018).

We find that the H I density profiles of small halos ($M \lesssim 10^{12} h^{-1} M_\odot$) increase toward their halo center. We note, however, that the amplitude of the H I profile tends to saturate, i.e., the slope of the profiles declines significantly toward the halo center. For example, at $z = 0$ and $z = 1$ and for halos with masses larger than $10^{11} h^{-1} M_\odot$, the mean H I profiles change slope around $\sim 20 h^{-1}$ kpc. This is expected since neutral hydrogen at high densities will turn into molecular hydrogen and stars on short timescales. For higher halo masses ($M \simeq 10^{13} h^{-1} M_\odot$), the H I density profile exhibits a hole in the center. This is caused by AGN feedback in the central galaxy of those halos. We note that higher densities in the center of halos can give rise to the formation of molecular hydrogen, which can produce a similar effect (Marinacci et al. 2018). Holes, which extend even further than in groups, are also found in the H I profiles of galaxy clusters, which we, however, do not show here since there are only a few of them and only at low redshift.

We illustrate these features of the H I profiles in Figure 6, where we show the spatial distribution of H I in and around four individual halos with masses 10^{11} , 10^{12} , 10^{13} , and $10^{14} h^{-1} M_\odot$ at redshifts 0 or 1. We have selected these halos by requiring that their H I density profiles are close to the mean. It can be seen that H I is localized in the inner regions of small

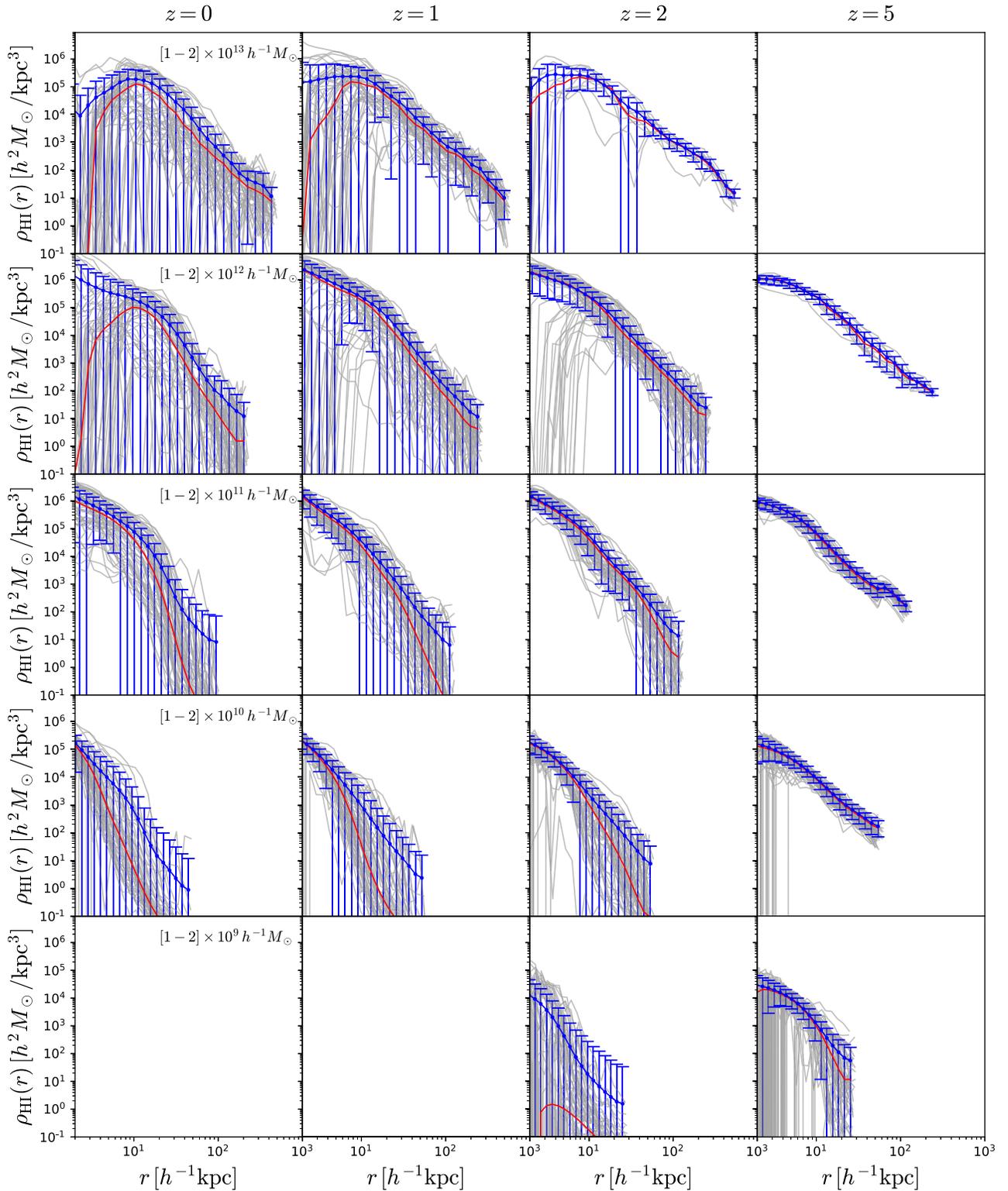


Figure 5. Density profiles of H I for halos of different masses in different rows (see labels in the left column) at redshifts $z = 0$ (left), $z = 1$ (middle left), $z = 2$ (middle right), and $z = 5$ (right). In each panel, we display up to 50 individual profiles (gray lines), the mean profile and the standard deviation (blue lines), and the median profile (red lines). Empty panels correspond to situations with either no halos (top right) or with halos far below the cutoff mass M_{min} . In contrast to dark matter, H I density profiles are not universal, and they exhibit, in most of the cases, a very large scatter. The H I–H₂ transition saturates the amplitude of the profiles in the core, while processes such as AGN feedback create H I holes in the core of the most massive halos. The mean and the median can be quite different, indicating that the distribution is asymmetric. In some cases, that asymmetry is due to the presence of two different populations such as blue and red galaxies. We emphasize that our results are not converged against resolution (see Appendix A). This should, however, not be seen as a limitation of our claims, as we present results for TNG100, i.e., at the resolution to which the model parameters have been tuned to reproduce a set of galaxy properties.

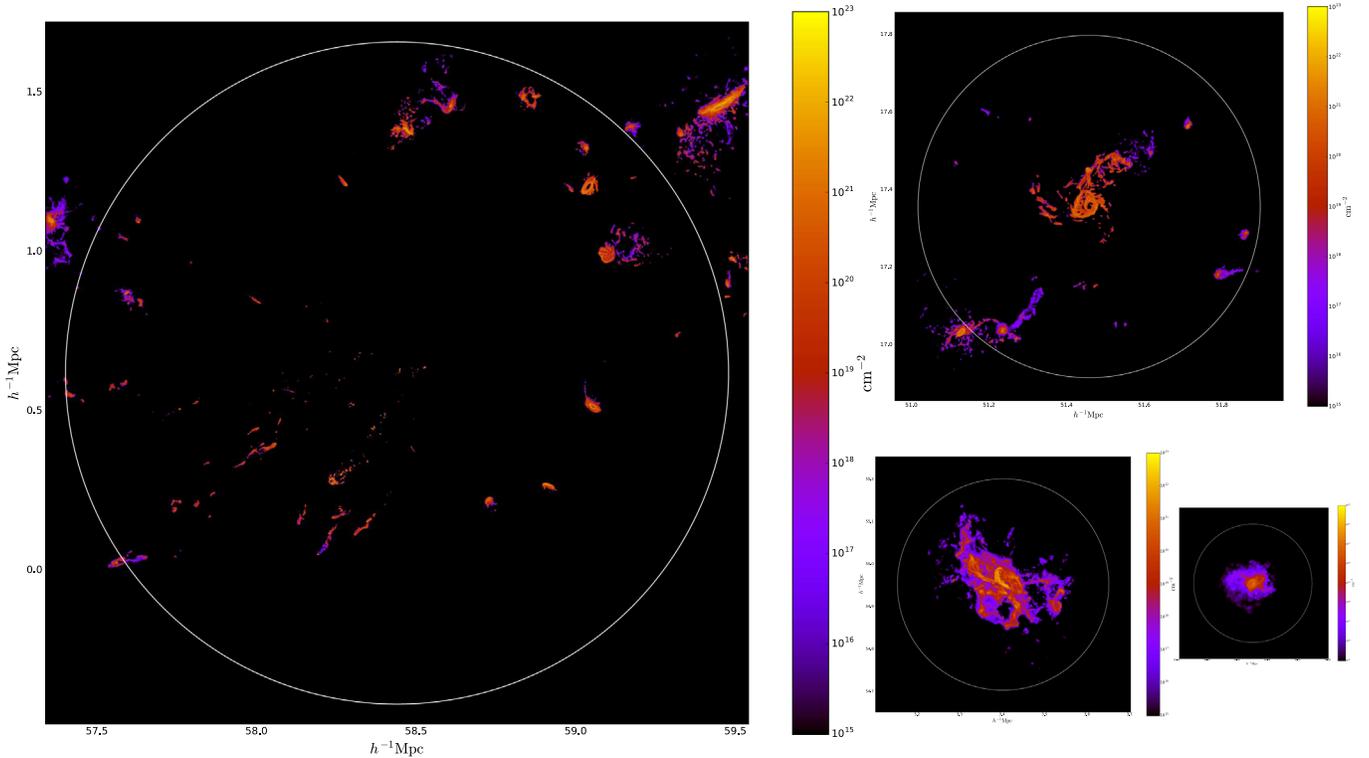


Figure 6. To better understand the features in the H I profiles of Figure 5, we have chosen halos with H I profiles close to the mean. The images show the H I column density for halos of mass $\sim 10^{14} h^{-1} M_{\odot}$ at $z = 0$ (left), $\sim 10^{13} h^{-1} M_{\odot}$ at $z = 0$ (top right), $\sim 10^{12} h^{-1} M_{\odot}$ at $z = 1$ (bottom middle), and $\sim 10^{11} h^{-1} M_{\odot}$ at $z = 0$ (bottom right). The center of galaxy clusters is typically occupied by H I-poor ellipticals, whereas H I-rich spirals reside in the centers of lower mass halos. Processes such as tidal and ram-pressure stripping efficiently remove gas from galaxies near the centers of galaxy clusters. In small halos ($\lesssim 10^{12} h^{-1} M_{\odot}$), gas can cool and accumulate in the center while in groups, AGN feedback produces holes in the core of the H I profile (see top-right panel). The “cuspsiness” of the H I profiles increases with decreasing halo mass, but saturates due to the formation of H_2 .

halos, while for groups, the central galaxy exhibits a hole produced by AGN feedback. For galaxy clusters, the central regions have little H I. This happens because the central galaxy is an H I-poor elliptical, and ram-pressure and tidal stripping are very efficient in removing the gas content of galaxies passing near the center. The analysis in this section suggests that analytical approaches to the distribution of DLAs employing a universal H I profile, e.g., (Padmanabhan et al. 2017) will not be able to reproduce observations.

In order to quantitatively investigate what the effective average H I density profile is across different halo masses and redshift, we use the mean measured H I density profile and test two models of H I density that both include an exponential cutoff on small scales.

First we consider a simple power law with an exponential cutoff on small scales—Model 1:

$$\rho_{\text{HI}}(r) = \frac{\rho_0}{r^{\alpha_*}} \exp(-r_0/r), \quad (16)$$

where ρ_0 is the overall normalization, α_* is the slope parameter, and r_0 is the inner radius at which the density drops and the profile changes its slope.

Second, we consider an altered Navarro–Frenk–White (NFW) profile (Maller & Bullock 2004; Barnes & Haehnelt 2014), found to be a good fit to the multiphase gas distribution at high redshifts in hydrodynamical simulations, with an exponential cutoff on

small scales—Model 2:

$$\rho_{\text{HI}}(r) = \frac{\rho_0 r_s^3}{(r + 3/4 r_s)(r + r_s)^2} \exp(-r_0/r), \quad (17)$$

where ρ_0 is the overall normalization and r_s is the scale radius of the H I cloud. In both cases, the overall normalization, ρ_0 , is fixed such that the volume integral of the model density profile integrated up to the virial radius of a given halo matches the mean total H I mass obtained from the density profile found in simulations (blue lines in Figure 5). We are then left with two free parameters for each model: $\{\alpha_*, r_0\}$ and $\{r_s, r_0\}$. We fit these models to the measured mean H I density profiles, limiting our analysis only to the scales above $r \geq 2h^{-1}$ kpc. For the uncertainties in the density profiles, we use the scatter among different galaxies (blue error bars in Figure 5) and assume that these uncertainties are uncorrelated between different scales.

The best-fit values along with the 68% confidence intervals are presented in Table 2, while in Figure 31 in Appendix F we show the best-fit results for Model 1. Based on the resulting best-fit χ^2 , we find that both Model 1 and 2 are good fits for all the considered redshifts and halo masses, except for the most massive halo bin $M_h = 10^{14} [h^{-1} M_{\odot}]$ at $z = 0$. We find the difference in the best-fit χ^2 between the two models to be negligible. This is to be expected since the models are rather similar and have the same slope on large scales. In the case of Model 1, we find the H I density profile slope to be consistent

Table 2
Best-fit Values of the Parameters Determining the H I Density Profiles

| Model 1—Power Law + Exponential Cutoff: α_* , $\log_{10} r_0$ [h^{-1} Mpc] | | | | | | | | | | | | |
|--|-------------------------------|-------------------------|----------------------------------|-------------------------|----------------------------------|-------------------------|----------------------------------|-------------------------|----------------------------------|-------------------------|----------------------------------|-------------------------|
| z | $M_h = 10^9 [h^{-1} M_\odot]$ | | $M_h = 10^{10} [h^{-1} M_\odot]$ | | $M_h = 10^{11} [h^{-1} M_\odot]$ | | $M_h = 10^{12} [h^{-1} M_\odot]$ | | $M_h = 10^{13} [h^{-1} M_\odot]$ | | $M_h = 10^{14} [h^{-1} M_\odot]$ | |
| 0 | ... | ... | $3.04^{+0.04}_{-0.03}$ | $-3.59^{+0.85}_{-0.92}$ | $3.03^{+0.03}_{-0.02}$ | $-2.8^{+0.5}_{-1.2}$ | $3.02^{+0.03}_{-0.03}$ | $-2.32^{+0.33}_{-1.15}$ | $3.00^{+0.04}_{-0.04}$ | $-1.71^{+0.09}_{-0.12}$ | $2.92^{+0.03}_{-0.03}$ | $-1.91^{+0.11}_{-0.14}$ |
| 1 | $3.3^{+1.3}_{-0.7}$ | $-2.5^{+1.1}_{-1.6}$ | $3.05^{+0.02}_{-0.02}$ | $-3.72^{+0.77}_{-0.84}$ | $3.02^{+0.02}_{-0.02}$ | $-3.3^{+0.7}_{-1.1}$ | $3.00^{+0.03}_{-0.02}$ | $-2.32^{+0.16}_{-0.28}$ | $2.99^{+0.03}_{-0.03}$ | $-1.77^{+0.09}_{-0.11}$ | ... | ... |
| 2 | $3.07^{+0.10}_{-0.08}$ | $-3.2^{+0.9}_{-1.2}$ | $3.03^{+0.01}_{-0.02}$ | $-3.64^{+0.78}_{-0.89}$ | $3.01^{+0.01}_{-0.01}$ | $-2.75^{+0.26}_{-0.68}$ | $3.00^{+0.02}_{-0.02}$ | $-2.18^{+0.09}_{-0.12}$ | $2.98^{+0.02}_{-0.01}$ | $-1.74^{+0.04}_{-0.05}$ | ... | ... |
| 3 | $3.05^{+0.02}_{-0.02}$ | $-3.63^{+0.85}_{-0.93}$ | $3.02^{+0.02}_{-0.02}$ | $-3.1^{+0.5}_{-1.1}$ | $3.00^{+0.01}_{-0.01}$ | $-2.52^{+0.13}_{-0.20}$ | $3.00^{+0.02}_{-0.02}$ | $-2.09^{+0.06}_{-0.07}$ | ... | ... | ... | ... |
| 4 | $3.04^{+0.02}_{-0.02}$ | $-3.3^{+0.7}_{-1.0}$ | $3.00^{+0.01}_{-0.01}$ | $-2.46^{+0.15}_{-0.24}$ | $3.00^{+0.01}_{-0.01}$ | $-2.32^{+0.07}_{-0.08}$ | $2.99^{+0.01}_{-0.01}$ | $-2.04^{+0.03}_{-0.04}$ | ... | ... | ... | ... |
| 5 | $3.03^{+0.02}_{-0.02}$ | $-2.9^{+0.5}_{-1.2}$ | $3.00^{+0.01}_{-0.01}$ | $-2.28^{+0.09}_{-0.12}$ | $3.00^{+0.01}_{-0.01}$ | $-2.18^{+0.04}_{-0.05}$ | $3.00^{+0.01}_{-0.01}$ | $-2.02^{+0.03}_{-0.03}$ | ... | ... | ... | ... |
| Model 2—Altered NFW + Exponential Cutoff: $\log_{10} r_s$ [h^{-1} Mpc], $\log_{10} r_0$ [h^{-1} Mpc] | | | | | | | | | | | | |
| 0 | ... | ... | $-4.0^{+0.7}_{-0.7}$ | $-3.8^{+0.8}_{-0.8}$ | $-3.7^{+0.6}_{-0.9}$ | $-3.4^{+0.7}_{-1.0}$ | $-3.2^{+0.7}_{-1.1}$ | $-3.1^{+0.8}_{-1.3}$ | $-3.0^{+1.0}_{-1.3}$ | $-1.8^{+0.1}_{-1.0}$ | $-2.3^{+0.5}_{-1.7}$ | $-2.6^{+0.7}_{-1.6}$ |
| 1 | $-2.8^{+1.8}_{-1.5}$ | $-3.3^{+1.2}_{-1.1}$ | $-4.0^{+0.5}_{-0.6}$ | $-3.7^{+0.6}_{-0.8}$ | $-3.9^{+0.6}_{-0.7}$ | $-3.6^{+0.7}_{-0.9}$ | $-3.0^{+0.4}_{-1.2}$ | $-2.9^{+0.6}_{-1.4}$ | $-2.2^{+0.3}_{-1.6}$ | $-2.4^{+0.6}_{-1.7}$ | ... | ... |
| 2 | $-3.7^{+0.9}_{-0.8}$ | $-3.7^{+0.9}_{-0.9}$ | $-3.8^{+0.5}_{-0.7}$ | $-3.5^{+0.5}_{-0.9}$ | $-3.6^{+0.5}_{-0.9}$ | $-3.3^{+0.6}_{-1.1}$ | $-2.8^{+0.3}_{-1.3}$ | $-2.6^{+0.4}_{-1.5}$ | $-1.8^{+0.1}_{-0.2}$ | $-3.0^{+0.8}_{-1.3}$ | ... | ... |
| 3 | $-3.8^{+0.6}_{-0.8}$ | $-3.5^{+0.6}_{-0.9}$ | $-3.6^{+0.5}_{-0.8}$ | $-3.3^{+0.5}_{-1.1}$ | $-3.3^{+0.4}_{-1.0}$ | $-3.0^{+0.5}_{-1.3}$ | $-2.8^{+0.4}_{-1.3}$ | $-2.4^{+0.3}_{-1.4}$ | ... | ... | ... | ... |
| 4 | $-3.6^{+0.5}_{-0.9}$ | $-3.2^{+0.5}_{-1.1}$ | $-3.2^{+0.4}_{-1.1}$ | $-3.0^{+0.4}_{-1.3}$ | $-2.9^{+0.3}_{-1.3}$ | $-2.7^{+0.4}_{-1.4}$ | $-2.6^{+0.3}_{-1.4}$ | $-2.4^{+0.3}_{-1.2}$ | ... | ... | ... | ... |
| 5 | $-3.4^{+0.5}_{-1.0}$ | $-3.1^{+0.5}_{-1.1}$ | $-2.7^{+0.2}_{-1.1}$ | $-3.1^{+0.7}_{-1.3}$ | $-2.5^{+0.1}_{-1.1}$ | $-3.3^{+1.0}_{-1.2}$ | $-2.2^{+0.1}_{-0.4}$ | $-3.1^{+0.8}_{-1.2}$ | ... | ... | ... | ... |

Note. We show the resulting parameters for the two different models considered (see text): an altered NFW profile with an exponential cutoff on small scales (top) and a simple power law with an exponential cutoff on small scales (bottom), as a function of the halo mass (columns) and redshift (rows).

with a value of $\alpha_* = 3$ for all halo masses and redshifts. The inner radius r_0 depends on the halo mass and is larger for larger halo masses at a fixed redshift, while at a fixed halo mass, it increases with increasing redshift. For example, for halos with $M_h \leq 10^{11} h^{-1} \text{Mpc}$ and $z \leq 2$, r_0 is below the minimum scale considered, and the uncertainties are rather large. In the case of Model 2, we find a similar behavior. The inferred values of r_0 are consistent between the two models, with Model 2 having larger uncertainties due to the degeneracy between parameters r_0 and r_s .

We note that other observational and simulation studies have found that the HI surface density profile of galaxies can be reproduced by an exponential profile (Obreschkow et al. 2009; Wang et al. 2014). Based on these studies, other spherically averaged density models have been used in the literature, e.g., an exponential profile (Padmanabhan et al. 2017). We find that using an exponential profile for the spherically averaged profile does not reproduce our mean data very well.

7. HI in Centrals and Satellites Galaxies

It is interesting to quantify what fraction of HI mass inside halos comes from their central and satellite galaxies. This will help us to better understand the HI density profiles (see Section 6) and improves our intuition for the amplitude of the HI Fingers-of-God effect (see Section 16).

For each FoF halo, we have computed its total HI mass, the HI mass within its central galaxy, and the HI mass inside its satellites. We emphasize that our definition of central galaxy departs significantly from that used in observations, as we consider the central galaxy to be the most massive subhalo. In general, this subhalo hosts the particle at the minimum of the gravitational potential and is therefore the classical central galaxy, but it also has a significant spatial extent and particles far away from the halo center can be associated with this subhalo, unless they are bound to a satellite.

We take narrow bins in halo mass and compute the average HI mass for each of the above quantities. The outcome is shown in Figure 7. The black lines in the upper panels show the halo HI mass function, while the red and blue ones display the average HI mass inside the central and satellite galaxies as a function of halo mass. The bottom panels show the fraction of HI mass within halos that comes from the central and the satellite galaxies.

Aside from very low-mass halos ($M \lesssim 10^9 h^{-1} M_\odot$), the fraction of HI in the central galaxy decreases with halo mass, while the fraction of HI in satellites increases, independent of redshift. For small halos, nearly all of the HI are located in the central galaxy, as expected. For halos of masses $\sim 5 \times 10^{12} h^{-1} M_\odot$, the fraction of HI in the central galaxy and in satellites is roughly the same, almost independent of redshift. For more massive halos, the total HI mass is dominated by the HI in satellite galaxies.

At high redshift, the contribution of satellites to the total HI mass in small ($M \in [10^{10}-10^{11}] h^{-1} M_\odot$) halos is non-negligible: $\simeq 20\%$. At $z = 0$ and for galaxy clusters $M \gtrsim 10^{14} h^{-1} M_\odot$, the contribution of the central galaxy to the total HI mass is negligible, as expected.

The HI mass in very low-mass halos ($M \lesssim 10^9 h^{-1} M_\odot$) is small, in particular at low redshift. For some of these halos, the sum of the HI mass in the central and satellite subhalos is much less than the total HI mass. In such cases, some of the HI mass was determined by SUBFIND to be unbound. In a fraction of

these halos, no bound structure was identified by SUBFIND altogether, rendering the combined HI masses of the central and satellites, which by definition do not exist, to be zero, even if the FoF group contains some HI.

8. HI Probability Distribution Function

We now study other quantities that, although not ingredients for HI halo models, will help us better understand the spatial distribution of neutral hydrogen. One of those quantities is the density pdf, which we investigate in detail in this section and compare to that of matter.

We compute the density fields of neutral hydrogen and total matter in the whole simulation volume using cloud-in-cell (CIC) interpolation on a grid with 2048^3 cells in real space, namely $\approx 36.6 h^{-1} \text{kpc}$ across each grid cell. We then smooth those fields with top-hat filters of radii 1 and $5 h^{-1} \text{Mpc}$. We have chosen those values for the smoothing scale, R , as a compromise between large and small scales. On one hand, the volumes of our simulations do not allow us to explore values much larger than $\approx 5 h^{-1} \text{Mpc}$, while on the other hand we take $1 h^{-1} \text{Mpc}$ as a representative estimate of the nonlinear regime. In Figure 8, we show the pdf's, computed as the number of cells in a given interval in overdensity, over the total number of cells, divided by the width of the overdensity interval.

While the density pdf of the matter field is highly non-Gaussian at low redshift, for either of the two smoothing scales we consider here, at high redshift it becomes more nearly Gaussian, as expected. At redshifts $z \geq 4$ and for $R = 5 h^{-1} \text{Mpc}$, the matter pdf can be well approximated by a log-normal distribution

$$\text{pdf}(\delta) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left[-\frac{(\log(1+\delta) + \sigma^2/2)^2}{2\sigma^2}\right], \quad (18)$$

where we consider σ to be a free parameter. We find $\sigma = 0.21$ at $z = 5$ and $\sigma = 0.28$ at $z = 4$. At lower redshifts and for smaller values of the smoothing scale, the log-normal function does not provide a good fit to our results, as expected (see e.g., Uhlemann et al. 2016).

The HI density pdf exhibits a different behavior compared to the matter pdf. First, the abundance of large HI overdensities remains roughly constant with redshift, independent of the smoothing scale considered. Second, for a smoothing scale of $1 h^{-1} \text{Mpc}$, the HI pdf hardly changes with redshift.

For redshifts $z \geq 3$, a log-normal distribution characterizes our results relatively well: for $R = 1 h^{-1} \text{Mpc}$, $\sigma \simeq 1.9$, while for $R = 5 h^{-1} \text{Mpc}$, $\sigma \simeq 1$ at $z = 3$, $\sigma \simeq 0.9$ at $z = 4$, and $\sigma \simeq 0.8$ at $z = 5$. At lower redshifts, a log-normal distribution does not provide a good match to the simulations.

To understand the physical origin of the differences between the pdf's of HI and matter density, it is useful to relate the width of the pdf to the amplitude of the HI power spectrum. This is possible since the amplitude of the HI power spectrum represents a measurement of the variance of the field at a given scale. Low values of the HI power spectrum indicate that HI is distributed homogeneously, while higher values mean that spatial variations in HI density can be large.

One of the reasons that the HI density pdf is roughly similar across redshifts—while this is less true of the matter density pdf—is that the amplitude of the HI power spectrum depends more weakly on redshift than does the matter power spectrum

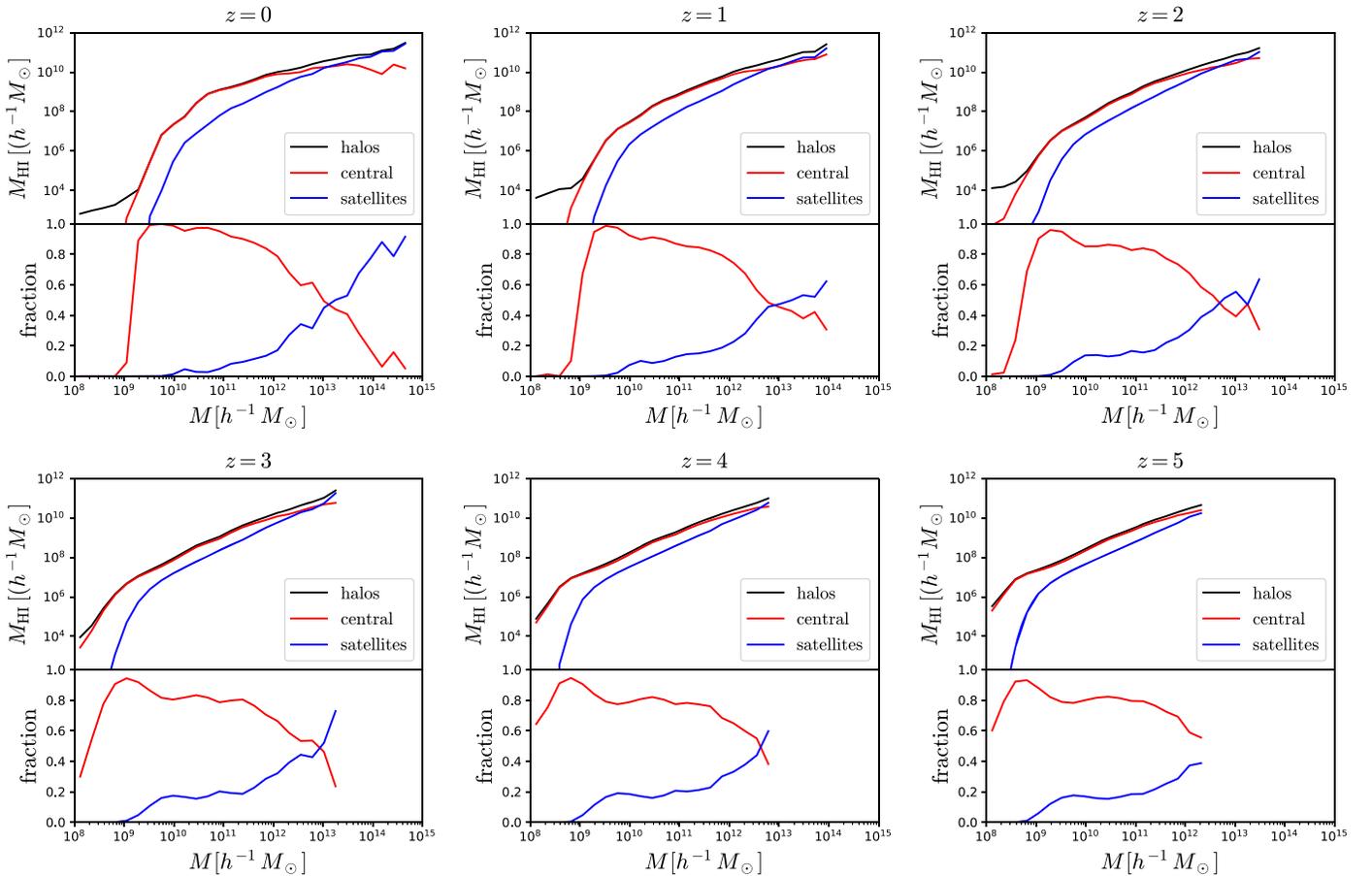


Figure 7. The black lines show the average H I mass inside halos as a function of mass, i.e., the halo H I mass function, at redshifts 0 (top left), 1 (top middle), 2 (top right), 3 (bottom left), 4 (bottom middle), and 5 (bottom right). The red and blue lines represent the average H I mass within central and satellite galaxies as a function of halo mass. The bottom panels display the fraction of H I mass inside halos that is embedded in centrals and satellites. The H I mass of halos below $\approx 5 \times 10^{12} h^{-1} M_{\odot}$ is dominated by H I in the central galaxy, while the H I in satellites dominates the H I content of more massive halos. For small halos, the H I mass in central and satellite galaxies is less than the total H I mass in halos. This happens because the H I in those halos is small in mass and “diffuse.”

(see Section 13). Thus, the variance of the H I pdf is necessarily smaller than that of the matter pdf. Since the amplitude of the H I power spectrum is larger than that of the matter power spectrum at high redshifts, the variance of the H I pdf is larger than that of the matter pdf at those redshifts, as we find. Finally, in the central region of a void, the matter density will be low, but the H I density will be even lower.²⁸ Thus, we find that there will be more cells with low H I overdensity than with low matter overdensity.

It can be seen for both H I and matter that the distributions are broader for a smoothing scale of $1 h^{-1} \text{Mpc}$ than for $5 h^{-1} \text{Mpc}$. This is expected since when smoothing over larger scales, any field will become more homogeneous and therefore the width of its pdf will become smaller. This can also be quantified through the amplitude of the power spectrum, using the same reasoning as above.

9. H I Column Density Distribution Function and DLA Cross-sections

Another quantity commonly employed to study the abundance of neutral hydrogen in the post-reionization era is the H I

column density distribution function (H I CDDF), defined as

$$f_{\text{H I}}(N_{\text{H I}}) = \frac{d^2 n(N_{\text{H I}})}{dN_{\text{H I}} dX}, \quad (19)$$

where n is the number of lines of sight with column densities between $N_{\text{H I}}$ and $N_{\text{H I}} + dN_{\text{H I}}$, and $dX = H_0(1+z)^2/H(z)dz$ is the absorption distance. This quantity can be inferred directly from observations of the Ly α forest.

Here, we investigate the H I CDDF, focusing on absorbers with high column densities: DLAs, $N_{\text{H I}} \geq 10^{20.3} \text{cm}^{-2}$. We also examine the DLA cross-sections, which are required both observationally (Font-Ribera et al. 2012; Alonso et al. 2018; Pérez-Ràfols et al. 2018) and theoretically (Castorina & Villaescusa-Navarro 2017).

In Figure 9, we show an example of the spatial distribution of gas and H I around a massive halo at redshift $z = 3$. As in this case, DLAs correspond to gas in galaxies, gas recently stripped from galaxies, and gas in streams.

The H I CDDF at redshifts 0, 1, 2, 3, 4, and 5 is computed using the following procedure (we refer the reader to Appendix B of Villaescusa-Navarro et al. 2014 for further details). We approximate each Voronoi cell by a uniform sphere with radius equal to $R = (3V/4\pi)^{1/3}$, where V is the volume of the cell, and determine the H I column density of a line through it from $N_{\text{H I}} = \rho_{\text{H I}} d$, where $\rho_{\text{H I}} = M_{\text{H I, cell}}/V$ and d is the length of the

²⁸ In order to have a significant amount of H I, self-shielding is required. Thus, in low-density regions, H I will be highly ionized.

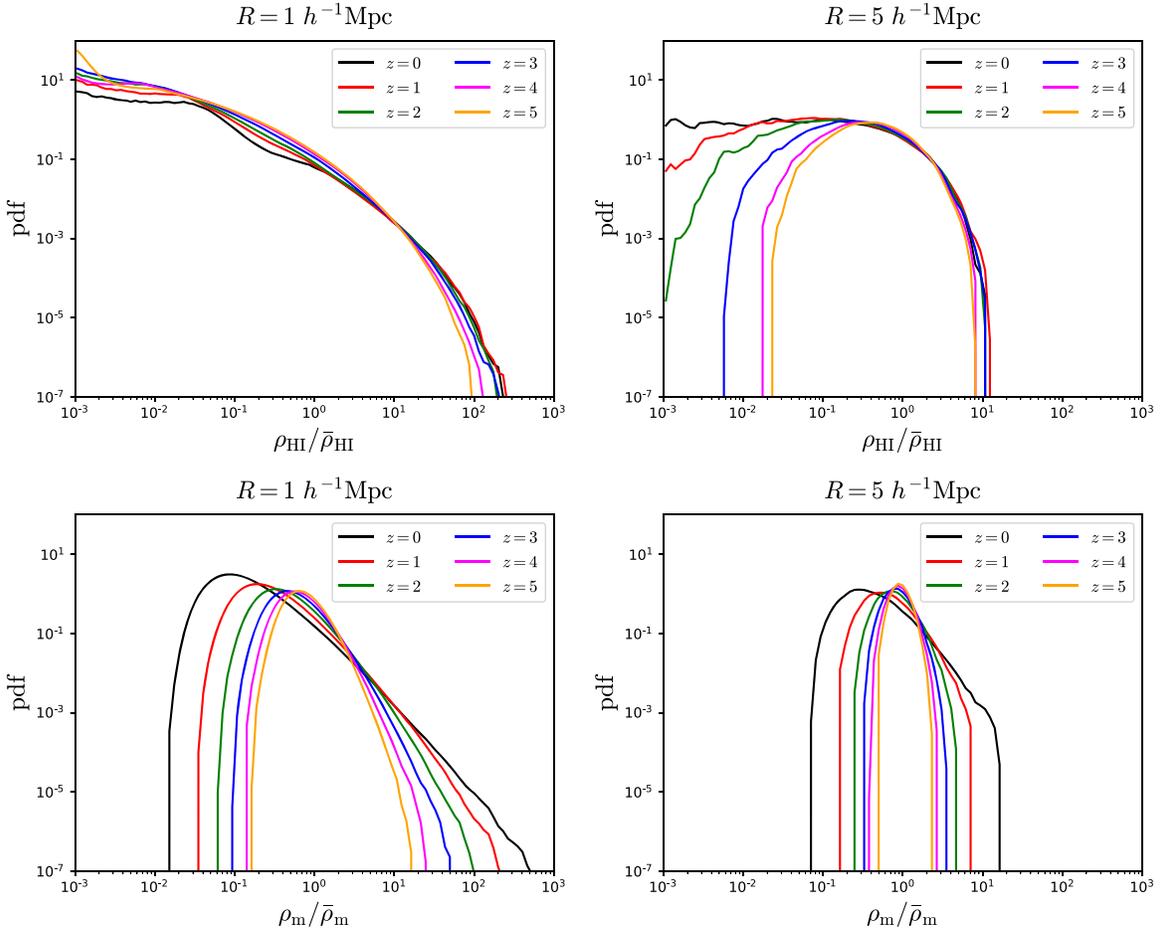


Figure 8. The density fields of H I (top) and matter (bottom) smoothed with a top-hat filter of 1 (left) and 5 (right) h^{-1} Mpc. This figure shows the pdf of those fields at several redshifts (see legend). Deviations from Gaussianity are larger in the H I field than in the matter field at all redshifts. For small smoothing scales, the H I density pdf barely changes with redshift. At high redshifts, both the H I and the matter fields are well described by a log-normal distribution.

segment intersecting the sphere. The simulation volume is projected along the z -axis and a grid with $20,000 \times 20,000$ points is overlaid. Each point is considered to be a line of sight, and the column density along it is estimated as the sum of the column densities of all Voronoi cells contributing to it. Since our box size is relatively small, the probability of encountering more than a single absorber with a large column density along the line of sight is negligible. Thus, if the column density of a given line of sight is larger than $\sim 10^{19} \text{ cm}^{-2}$, it can be attributed to a single absorber. We repeated the tests carried out in Villaescusa-Navarro et al. (2014) to verify that (1) the grid is fine enough to achieve convergence in the CDDF, and (2) the results do not change if the CDDF is computed by slicing the box into slabs of different widths.

We show the results in Figure 10. We find excellent agreement with the observations, which are shown as black points with error bars, at redshifts [1.8–3.5] (Péroux et al. 2005), [2.0–3.5] (Noterdaeme et al. 2012), [3.5–5.4] (Crighton et al. 2015), and [1.5–5.0] (Zafar et al. 2013). The differences between the observed and simulated CDDFs, e.g., the amplitude of the H I CDDF around 10^{20} – 10^{21} cm^{-2} , are related to the mismatch between Ω_{HI} from observations and TNG100 (see Figure 2), since

$$\Omega_{\text{HI}}(z) = \frac{m_{\text{H}} H_0}{c \rho_c^0} \int_0^\infty f_{\text{HI}}(N_{\text{HI}}, z) N_{\text{HI}} dN_{\text{HI}}, \quad (20)$$

where m_{H} is the mass of the hydrogen atom and c is the speed of light. In agreement with previous works, we find that the H I CDDF exhibits a weak dependence on redshift (see, e.g., Rahmati et al. 2013a). This self-similarity can be associated with the weak redshift dependence that we observe in the high-overdensity tail of the H I density pdf for small smoothing scales (see Figure 8).

Next, we examine the cross-section of DLAs. For each dark matter halo of the simulation, the area covered by DLAs with different column densities is computed. Then, all halos within mass bins are selected, and the mean and standard deviation of their DLA cross-sections are determined. As shown in Figure 11, we find that, for fixed column density, the DLA cross-section increases with halo mass, while the cross-section decreases with column density for halos of fixed mass.

The cross-section of the DLAs is well fitted by the following function

$$\sigma(M|N_{\text{HI}}, z) = A \left(\frac{M}{h^{-1} M_\odot} \right)^\alpha (1 - e^{-(M/M_0)^\beta}). \quad (21)$$

Here, A is a parameter that controls the overall normalization of function, while α sets the slope of the cross-section for large halo masses, and M_0 determines the characteristic halo mass where the DLA cross-section exponentially decreases at a rate controlled by β .

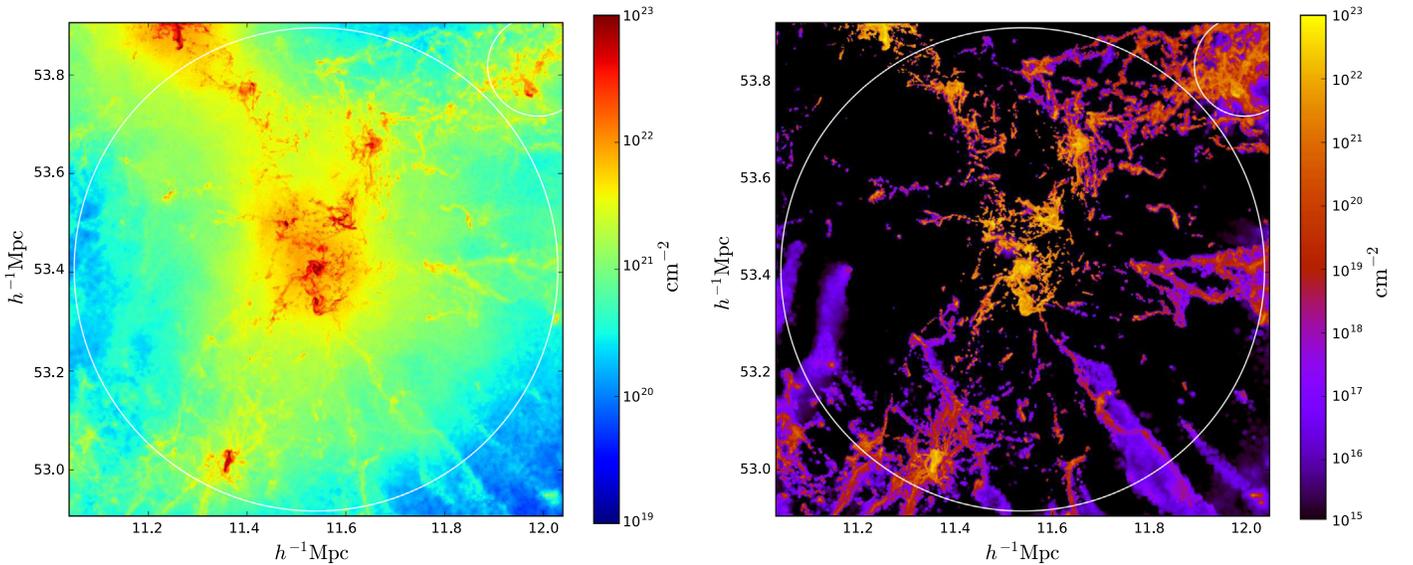


Figure 9. Column density of gas (left panel) and H I (right panel) around a massive halo of mass $1.5 \times 10^{13} h^{-1} M_{\odot}$ at $z = 3$. The white circles show the position and radius of dark matter halos.

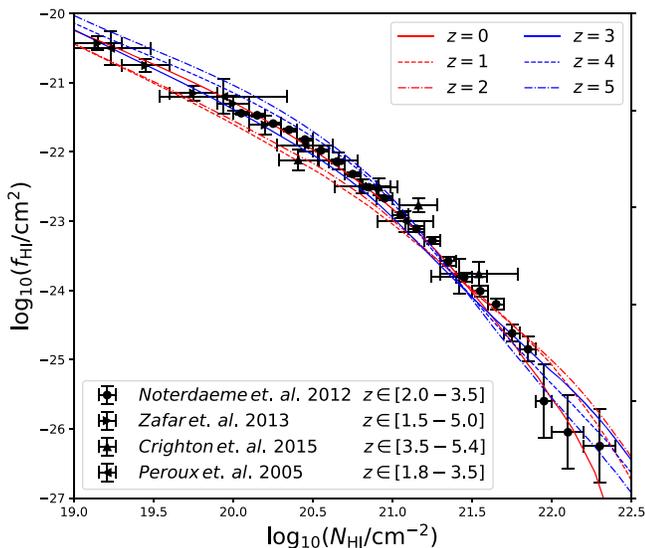


Figure 10. H I column density distribution function as a function of the H I column density from the TNG100 simulation at redshifts 0 (solid red), 1 (dashed red), 2 (dotted-dashed red), 3 (solid blue), 4 (dashed blue), and 5 (dotted-dashed blue). Data from observations are shown as black points with error bars.

We fit our results at redshifts $z \in [2, 4]$ using the above form and find $\alpha = 0.82$ in the large majority of the cases, while β is well approximated by $\beta = 0.85 \cdot \log_{10}(N_{\text{HI}}/\text{cm}^{-2}) - 16.35$. There is also a strong correlation between A and M_0 , given by $A \cdot M_0 = 0.0141 h^{-2} \text{ kpc } M_{\odot}$. The only dependence on redshift enters through M_0 , the value of which is given in Table 3. We find that M_0 decreases with redshift, in agreement with the halo H I mass function, which implies that less massive halos can host H I at higher redshifts.

The fits to the simulation results, shown as dashed lines in Figure 11, are a good approximation for column densities below 10^{22} cm^{-2} , but apparently less so at higher column densities; e.g., the fit for column densities above $10^{22.5} \text{ cm}^{-2}$ and low halo masses is several orders of magnitude below the mean. This is mainly an illusion of the fact that some error bars

are larger than the value. The reduced χ^2 obtained from the fits in all cases is below 0.35. The preferred value for α is slightly larger at higher redshifts, but the redshift dependence is so weak that for simplicity we did not use it in our fitting. The largest discrepancy between the fit and our results occurs at $z = 2$ for the DLAs with column densities larger than 10^{22} cm^{-2} . In Castorina & Villaescusa-Navarro (2017), it was suggested that a very good fit to the column density distribution and the DLA bias can be obtained assuming the differential cross-section, $d\sigma/dN_{\text{HI}}$, is roughly independent of column density. This implies that the linear bias of different absorbers will be very similar, and the measurements in the BOSS survey of Pérez-Ràfols et al. (2018) confirm this simple picture, although with large error bars. As discussed above, our fit to Equation (21) indicates that the slope α to a very good approximation is not a function of column density, and the N_{HI} dependence of β can be moved to the normalization constant A using their tight correlation. If we then look at the expression for the linear bias of a given absorber,

$$b_{N_{\text{HI}}}(z) = \frac{\int_0^{\infty} b(M, z) n(M, z) \sigma(M|N_{\text{HI}}, z) dM}{\int_0^{\infty} n(M, z) \sigma(M|N_{\text{HI}}, z) dM}, \quad (22)$$

we note that A cancels between the numerator and the denominator, and the only column density dependence is left in β , and it is rather small. The analytical calculation in Castorina & Villaescusa-Navarro (2017) therefore agrees with the measurements in IllustrisTNG, and future observations will tell us whether or not our current understanding of the cross-section is correct.

We have used the above expression to estimate the bias of the DLAs. We take the DLAs cross-section (for absorbers with $N_{\text{HI}} > 10^{20} \text{ cm}^{-2}$) and halo mass function from our simulations and use the formula in Sheth et al. (2001) to compute the halo bias. We obtain values of the DLA bias equal to 1.7 at $z = 2$ and 2 and $z = 3$. Considering that the DLA bias follows a linear relation between $z = 2$ and $z = 3$, we obtain $b_{\text{DLA}}(z = 2.3) = 1.8$, in agreement with the latest observations by Pérez-Ràfols et al. (2018): $b_{\text{DLAs}} = 1.99 \pm 0.11$. We have

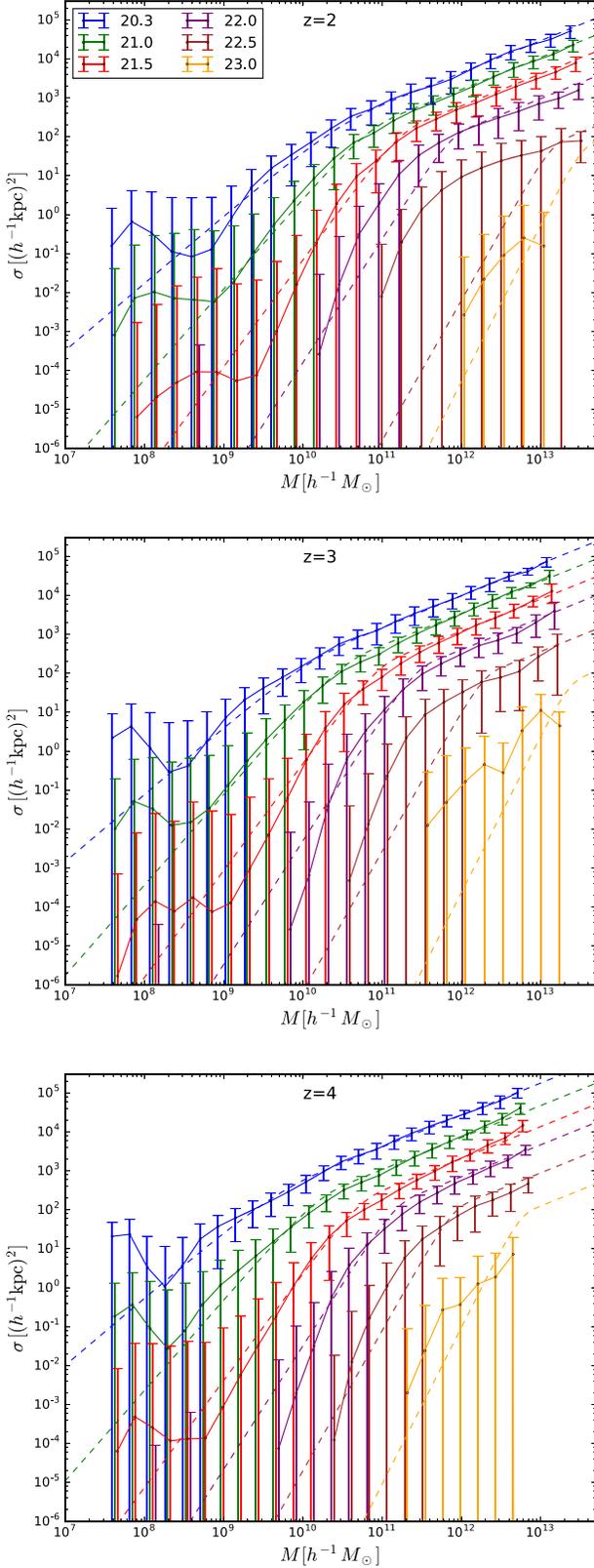


Figure 11. The cross-section of DLAs (dark matter halo area covered by DLAs) with column densities above $10^{20.3}$ (blue), 10^{21} (green), $10^{21.5}$, 10^{22} (purple), $10^{22.5}$ (brown), and 10^{23} (orange) cm^{-2} at redshifts $z = 2$ (top), $z = 3$ (middle), and $z = 4$ (bottom). The points with error bars are measurements from the TNG100 simulation while the dashed lines represent our fit using Equation (21).

Table 3

Fits to the DLA Cross-section from Simulations Using Equation (21)

| | $z = 2$ | $z = 3$ | $z = 4$ |
|------|---------|---------|---------|
| 20.0 | 10.23 | 9.89 | 9.41 |
| 20.3 | 10.34 | 10.00 | 9.56 |
| 21.0 | 10.77 | 10.45 | 10.14 |
| 21.5 | 11.20 | 10.91 | 10.68 |
| 22.0 | 11.83 | 11.39 | 11.14 |
| 22.5 | 13.11 | 12.26 | 11.87 |
| 23.0 | 13.49 | 13.34 | 12.72 |

Note. This table shows the value of $\log_{10} M_0$ at different redshifts and DLA column densities. The value of the other parameters in Equation (21) are given by $\alpha = 0.82$, $\beta = 0.85 \cdot \log_{10}(N_{\text{HI}}/\text{cm}^{-2}) - 16.35$ and $A \cdot M_0 = 0.0141 h^{-2} \text{kpc} M_{\odot}$.

repeated the above calculations using our fit for the DLA cross-section, taking the halo mass function from Sheth & Tormen (2002) or Crocce et al. (2010), and find that our results barely change.

We believe that the above calculation should be considered as a lower bound. In other words, the halo bias may be underestimated when calculated using Sheth et al. (2001). The reason is that we obtain a value of the HI bias (see Section 13), computed without any assumption, of 2 at $z = 2$ and 2.56 at $z = 3$, i.e., $b_{\text{HI}}(z = 2.3) = 2.17$. Following the theoretical arguments in Castorina & Villaescusa-Navarro (2017), it is reasonable to expect that $b_{\text{HI}} \simeq b_{\text{DLAs}}$. We thus conclude that both estimations of the DLA bias are in agreement with observations.

10. HI Bulk Velocity

In Section 4, we showed that nearly all of the HI at redshifts $z \leq 5$ reside within halos. Thus, the elements needed to describe the abundance and spatial distribution of HI in real space through HI halo models are the halo HI mass function and the HI density profiles. To model the distribution of HI in redshift space, an additional ingredient is required: the velocity distribution of HI inside halos. This quantity can be used in both HI halo models and HI HOD models. The accuracy that can be achieved with the former may not be high, due to the limitations of the formalism itself. On the other hand, HI HOD, i.e., painting HI on top of dark matter halos from either N -body or fast numerical simulations like COLA (Tassev et al. 2013), can produce highly accurate results. Hence, we examine the velocity distribution of HI inside halos, beginning with the HI bulk velocity in this section and continuing with the HI velocity dispersion in the next section, and, in both cases, comparing with the results for all matter.

For each dark matter halo in the simulation, we have computed the HI bulk velocity as

$$V_{\text{HI}} = \frac{\sum_i M_{\text{HI},i} V_{\text{HI},i}}{\sum_i M_{\text{HI},i}}, \quad (23)$$

where the sum runs over all gas cells belonging to the halo, and $M_{\text{HI},i}$ and $V_{\text{HI},i}$ are the HI mass and peculiar velocity of cell i , respectively. The peculiar velocity of halos, V_h , is computed in a similar manner, but summing over all resolution elements in

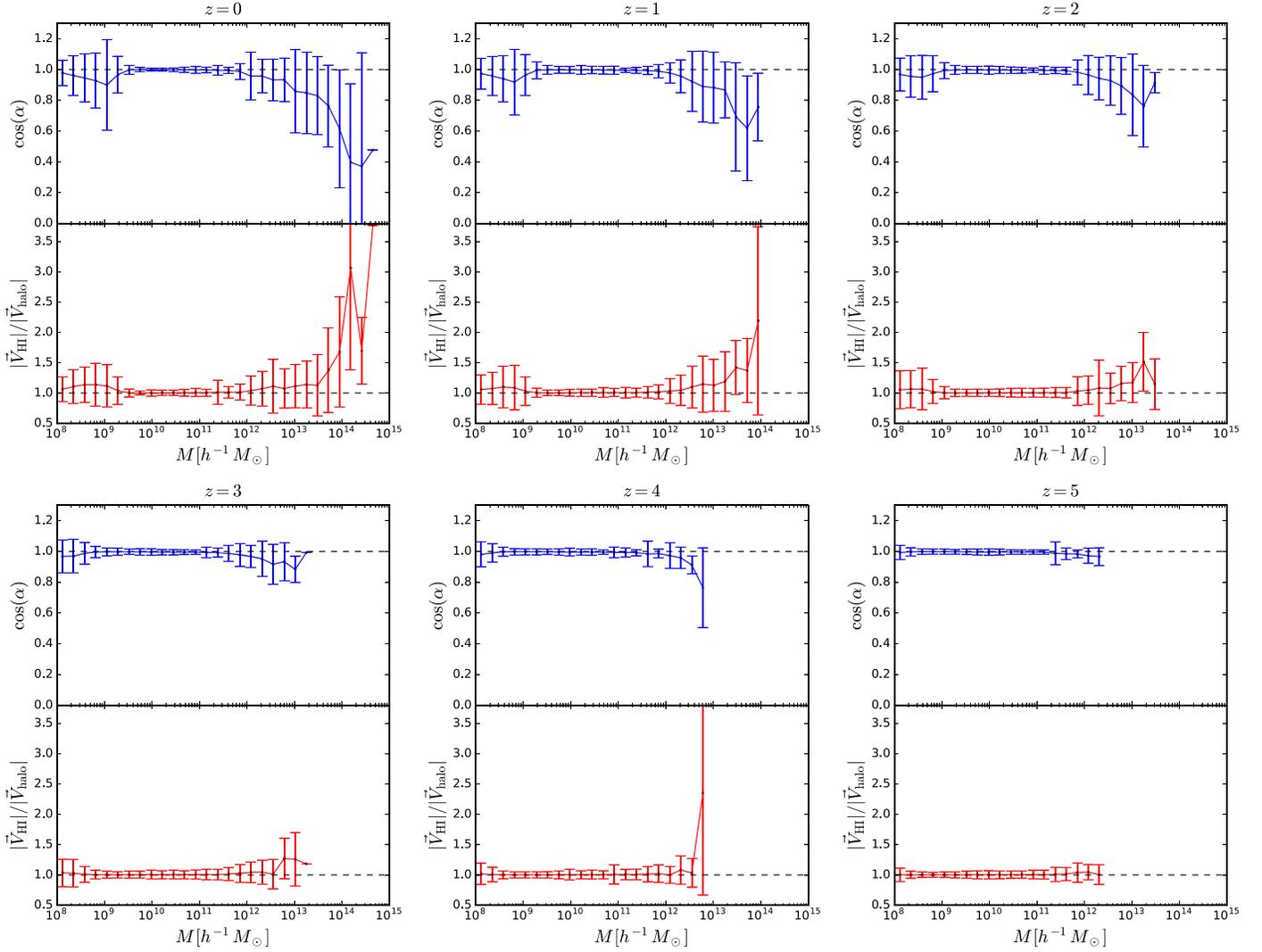


Figure 12. The upper panels show the average angle between the H I and halo peculiar velocity vectors, $\cos(\alpha) = \mathbf{V}_{\text{HI}} \cdot \mathbf{V}_h / (|\mathbf{V}_{\text{HI}}| |\mathbf{V}_h|)$, as a function of halo mass. The bottom panels display the average ratio between the moduli of the H I and halo peculiar velocity vectors as a function of halo mass. Only halos with total H I mass above $10^5 h^{-1} M_\odot$ are included. We show results at redshift 0 (top left), 1 (top middle), 2 (top right), 3 (bottom left), 4 (bottom middle), and 5 (bottom right). While the H I bulk velocity traces the halo peculiar velocity for small halos in both modulus and direction, there are departures for larger halos. This happens because most of the H I in small halos is in the central galaxy while in larger halos, the contribution from satellites becomes more important.

the halo (gas, CDM, stars, and black holes) and weighting their velocities by their corresponding masses.

Here, we examine (1) whether the peculiar velocity of the H I points in the same direction as the halo peculiar velocity, and (2) whether the modulus of the H I peculiar velocity is the same as that of the halo peculiar velocity. The first point is addressed by computing the angle between the peculiar velocities of H I and the halo from

$$\cos(\alpha) = \frac{\mathbf{V}_{\text{HI}} \cdot \mathbf{V}_h}{|\mathbf{V}_{\text{HI}}| |\mathbf{V}_h|} \quad (24)$$

for each halo in the simulation. We do not consider halos with total H I masses below $10^5 h^{-1} M_\odot$, since we expect the H I peculiar velocities of those halos to be uncorrelated with the halo peculiar velocity. For example, the H I in such halos mass can be from a single cell that is partially self-shielded and not bound to the halo. Moreover, in the limit where the H I mass is close to zero, the H I velocity dispersion is not well defined. Thus, in order to avoid such circumstances, we adopt the above

threshold, which corresponds to the mass of $\simeq 1/5$ of a completely self-shielded gas cell. However, we find that this threshold does not have a significant impact on our results. Choosing a different value hardly changes our results, with the only consequence being that the scatter of very small halos is affected. We then take narrow bins in halo mass and compute the mean value of $\cos(\alpha)$ and its standard deviation. The results are shown in the upper panels of Figure 12.

For small halos, $M \lesssim 10^{12} h^{-1} M_\odot$, $\cos(\alpha) \simeq 1$, indicating that the H I and halo peculiar velocities are aligned. This is expected because the H I is mainly located in the inner regions in low-mass halos, which usually traces well the peculiar velocity of the halo. For smaller halos, the value of $\cos(\alpha)$ deviates from 1, with increased scatter. This happens for halo masses below the cutoff scale, $\sim M_{\text{min}}$. In at least some cases, this is likely due to halos acquiring H I through an unusual mechanism, e.g., by passing through an H I-rich filament, so that the H I bulk velocity will not be correlated with the halo peculiar velocity. On the other hand, we find significant misalignments between the H I and halo peculiar velocities for

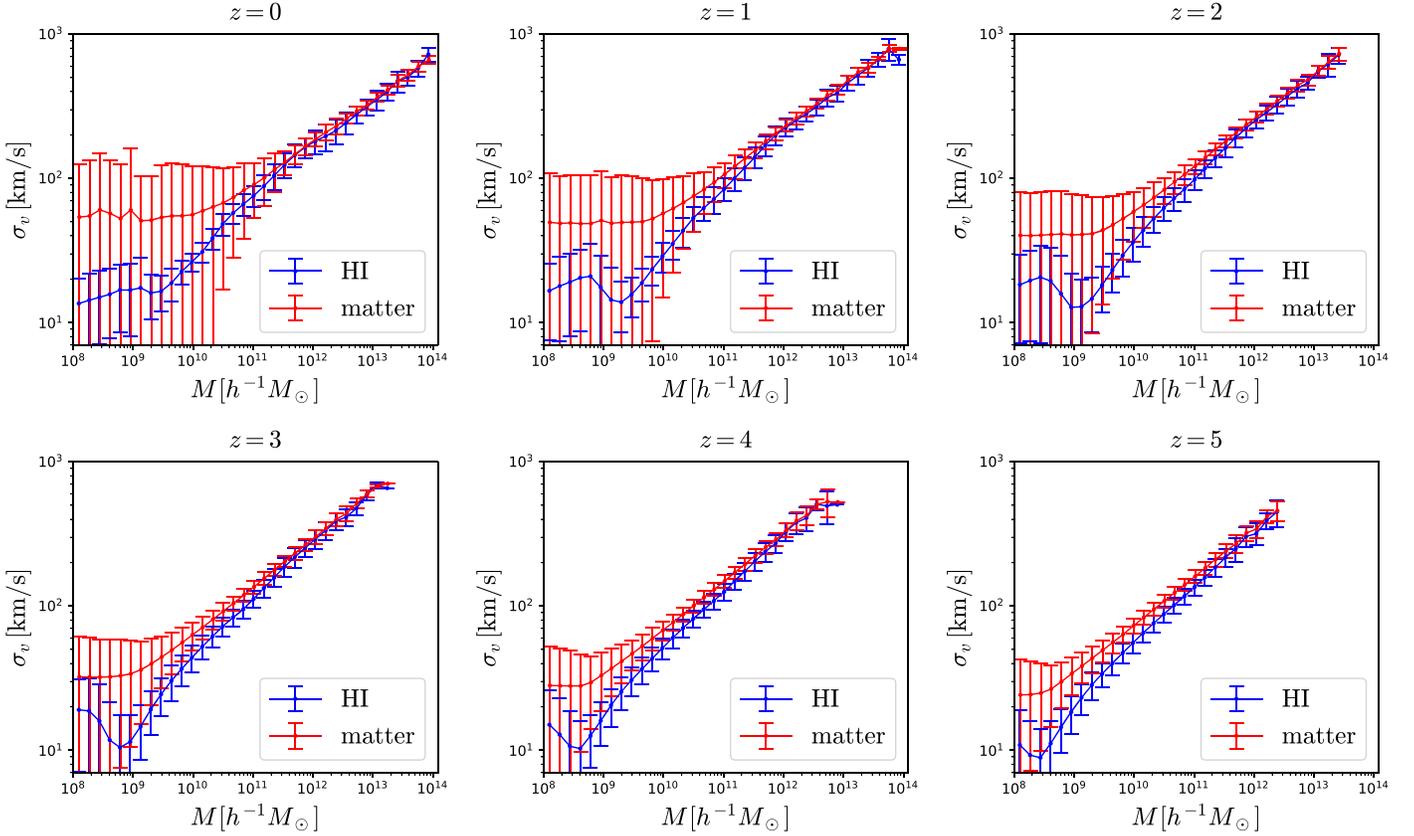


Figure 13. The mean and standard deviation of the 3D velocity dispersion of HI (blue lines) and CDM (red lines) as a function of halo mass at redshifts 0 (top left), 1 (top middle), 2 (top right), 3 (bottom left), 4 (bottom middle), and 5 (bottom right). Our results are well represented by a simple power law, $\sigma = \sigma_{10}(M/10^{10} h^{-1} M_{\odot})^{\alpha}$, with the best-fit parameter given in Table 4. At low redshift, the velocity dispersion of HI is very similar to that of CDM, while at high redshift, the CDM exhibits values larger than HI.

the most massive halos at any redshift. This is because the HI content of these halos is largely contributed by satellites, whose peculiar motions do not necessarily trace those of the halo. We return to this point below.

Further, in the bottom panels of Figure 12, we show the average and standard deviation of the ratio between the moduli of the HI and halo peculiar velocities, $|V_{\text{HI}}|/|V_h|$. This quantity is again calculated in narrow bins in halo mass, for all halos with HI mass larger than $10^5 h^{-1} M_{\odot}$.

For small halos, the moduli of the HI and halo peculiar velocities are essentially the same. For halos with masses below $\sim M_{\text{min}}$, the modulus ratio can be larger than 1, and its scatter increases. This is for the same reason as above: the HI content of some of those halos may not be bound to the halos and are instead part of a filament. For massive halos, the modulus of the HI peculiar velocity can be much larger than that of the halo peculiar velocity. As earlier, this is because the HI peculiar velocity is dominated by the HI in satellites, whose peculiar velocities do not perfectly trace the halo peculiar velocity.

To corroborate the assertion that the peculiar velocities of satellites do not trace the halo peculiar velocity in either modulus or direction, we have performed the following test. We compute the peculiar velocities of halo satellites and compared their mean, weighted by the total mass of each satellite, against the peculiar velocity of their host halo. The velocities of the satellites do not have the same modulus or direction as those of the host halo, showing similar trends to those for HI, with differences increasing with halo mass.

Thus, for small halos, where most of the HI is in the central galaxy, the HI bulk velocity traces the halo peculiar velocity well, in both modulus and direction. On the other hand, the contribution of satellites to the total HI mass in halos increases with mass, and since the bulk velocities of satellites do not trace the halo peculiar velocity, the HI bulk velocities will diverge, in modulus and direction, from the halo peculiar velocity, with differences increasing with halo mass.

11. HI Velocity Dispersion

For each halo in the simulation, we have computed the 3D velocity dispersion of its HI from

$$\sigma_{\text{HI}}^2 = \frac{\sum_i M_{\text{HI},i} |V_{\text{HI},i} - V_{\text{HI}}|^2}{\sum_i M_{\text{HI},i}}, \quad (25)$$

where the sums run over all gas cells belonging to the halo. $M_{\text{HI},i}$ and $V_{\text{HI},i}$ are the HI mass and velocity of gas cell i , and V_{HI} is the HI bulk velocity, computed as in Equation (24).

We then take narrow bins in halo mass and compute the mean and standard deviation of the HI velocity dispersion. Figure 13 shows the results, as well as a comparison with matter, whose properties are calculated analogously, but considering all mass elements within halos, i.e., gas, CDM, stars, and black holes.

As expected, the velocity dispersion of both HI and CDM increases with halo mass, independent of redshift. The results

Table 4

The Mean 3D Velocity Dispersion of Both Matter and H I Inside Halos Can be Represented by the Relation $\sigma = \sigma_{10}(M/10^{10} h^{-1} M_{\odot})^{\alpha}$

| z | Matter | | H I | |
|---|-------------------------------------|-------------|-------------------------------------|-------------|
| | σ_{10} [km s ⁻¹] | α | σ_{10} [km s ⁻¹] | α |
| 0 | 49 ± 5 | 0.28 ± 0.01 | 31 ± 1 | 0.35 ± 0.01 |
| 1 | 56 ± 4 | 0.30 ± 0.01 | 34 ± 1 | 0.37 ± 0.01 |
| 2 | 59 ± 3 | 0.32 ± 0.01 | 39 ± 2 | 0.38 ± 0.01 |
| 3 | 64 ± 3 | 0.33 ± 0.01 | 44 ± 2 | 0.39 ± 0.01 |
| 4 | 70 ± 2 | 0.33 ± 0.01 | 51 ± 2 | 0.39 ± 0.01 |
| 5 | 75 ± 2 | 0.33 ± 0.01 | 54 ± 2 | 0.40 ± 0.01 |

Note. The table gives the best fits for σ_{10} and α for matter and H I at different redshifts.

can be represented by a simple power law,

$$\sigma_v(M) = \sigma_{10} \left(\frac{M}{10^{10} h^{-1} M_{\odot}} \right)^{\alpha}, \quad (26)$$

where σ_{10} and α are free parameters with best-fit values provided in Table 4.

The mean H I velocity dispersions are always equal to or smaller than the matter velocity dispersions. For large halo masses, both exhibit the same amplitude, but for low-mass halos, the H I velocity dispersion is less than that of matter. The typical halo masses where the velocity dispersions diverge is around $10^{12} h^{-1} M_{\odot}$, with higher redshifts exhibiting departures at larger masses. This behavior is embedded in the slope of the $\sigma_{\text{HI}}(M)$ relation, the value of which, α , is larger than that of $\sigma_{\text{m}}(M)$ at all redshifts, and more so at higher redshifts.

For very small halos, and particularly at low redshift, the velocity dispersion of H I is much smaller than that of matter. This is a consequence of several factors. First, $\sigma_{\text{m}}(M)$ is artificially high, as the relation flattens out toward low masses. By comparing to a version of Figure 13 (not shown) generated from a lower resolution analog of the same cosmological volume (TNG100-2; see Nelson et al. 2018), we conclude that this is due to finite numerical resolution, driven by particles in the outskirts of the halos, which does not apply to the H I, which is centrally concentrated. In addition, we have examined a few individual low-mass halos and found that in some cases, the H I arises from just a few cells, or even just a single one. In those cases, the H I bulk velocity will be set by these few cells and the H I velocity dispersion will be artificially suppressed due to sampling, again from a finite resolution. As we move to more massive halos, the contribution of H I from satellites increases, and those satellites trace the underlying matter distribution more closely.

The scatter in the H I velocity dispersion for very low-mass halos is typically much smaller than the scatter in the matter velocity dispersion. One reason for this is that the H I velocity dispersion has been computed only for halos with total H I masses above $10^5 h^{-1} M_{\odot}$. Without such a threshold, the scatter in the H I velocity dispersion would be much larger. That is because if the H I mass in a halo is very low, it will often not be bound to the halo, e.g., the halo is crossing a filament that hosts a small amount of H I. In that case, H I velocity dispersions can be large. For example, several highly ionized unbound gas cells can produce a large, unphysical, velocity dispersion.

12. H I Stochasticity

The relation between H I and matter is given, to linear order, by $\delta_{\text{HI}} = b_{\text{HI}} \delta_{\text{m}} + \epsilon$, where ϵ is the stochasticity. Below, we examine whether or not this relation reproduces our results in real space and the amplitude of the stochasticity.

As for the density pdf's (see Section 8), we compute the density fields of H I and matter on a grid with 2048^3 cells employing the CIC mass-assignment scheme. We then compute the overdensity of each field and smoothed them with a top-hat filter of radius 1 or $5 h^{-1}$ Mpc. Next, we randomly select a subset of cells and make a scatter plot between the overdensities of H I and matter for each chosen cell. The results are shown in Figures 14 ($R = 1 h^{-1}$ Mpc) and 15 ($R = 5 h^{-1}$ Mpc).

For $R = 1 h^{-1}$ Mpc, two trends can be distinguished. The Ly α forest shows up as cells with matter overdensities below the mean and very low H I overdensities because the gas there is mostly ionized. For large matter overdensities, the H I within halos is self-shielded. The density $\rho_{\text{m}}/\bar{\rho}_{\text{m}} \simeq 0.4$ marks a transition from one regime to the other, indicating that H I self-shielding does not take place in lower matter overdensities. In all cases, the H I overdensity increases with matter overdensity.

At higher redshifts, the range occupied by matter and H I overdensities is smaller. As the universe becomes more homogeneous, fluctuations are smaller. This behavior can also be seen in the pdf's of Figure 8. The scatter in the overdensity relations also decreases toward higher redshift.

The dashed black lines show the predictions from linear theory, $\delta_{\text{HI}} = b_{\text{HI}} \delta_{\text{m}}$, where b_{HI} is the linear H I bias measured from the simulation (see Section 13 and Table 5). As expected, linear theory is not accurate in this regime because the bias is not linear on the smoothing scale considered. An exception is for $z = 1$, where linear H I bias reproduces the results reasonably well. This is because the H I bias is relatively flat at that redshift (see Figure 16).

As we move to a larger smoothing radius, the morphology of the results changes, as can be seen in Figure 15, where $R = 5 h^{-1}$ Mpc. Now, the H I and matter overdensities extend over a smaller range, because the smoothing is over a larger scale, making the field more homogeneous. In addition, the Ly α forest is no longer visible because in the neighborhood of the highly ionized H I in filaments, i.e., the Ly α forest, there will always be some halo within $5 h^{-1}$ Mpc that contains self-shielded H I gas.

As above, we find that H I overdensities increase with matter overdensities at all redshifts. However, at high redshift, the slope of the relation becomes more pronounced. This behavior can be partly explained by linear H I bias, shown as dashed black lines. As with $R = 1 h^{-1}$ Mpc, linear bias can explain the results relatively well at $z = 1$. At other redshifts, linear bias is more accurate than for smaller smoothing scales, as expected, but the agreement is not good for both large and small matter overdensities. Again, the scatter reduces with redshift.

13. H I Bias

We now examine different aspects of H I clustering in detail. In this section, we focus on the amplitude and shape of the H I bias.

The relation between the clustering of H I and that of dark matter involves the H I bias through $P_{\text{HI}}(k) = b_{\text{HI}}^2(k) P_{\text{m}}(k)$. The matter power spectrum, the quantity that contains

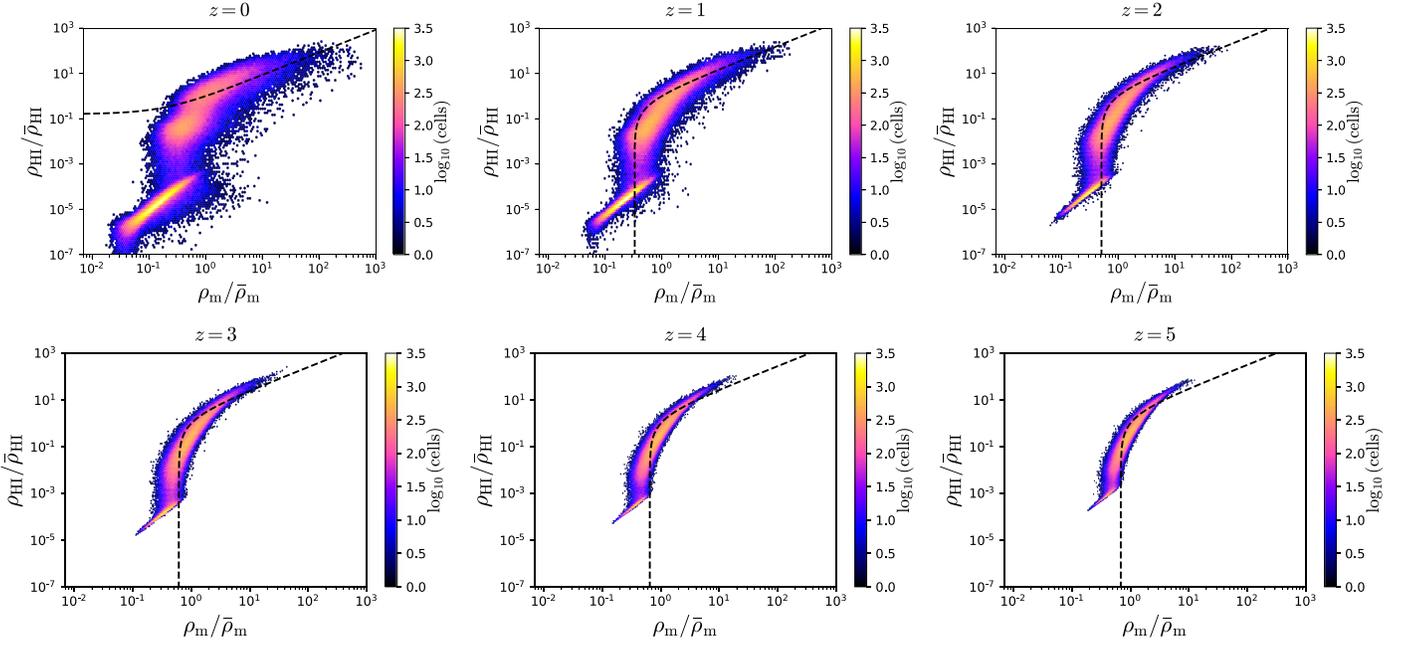


Figure 14. Relations between the H I and matter density fields smoothed with a top-hat filter of radius $R = 1 h^{-1}$ Mpc, shown as scatter plots between the respective overdensities at redshifts $z = 0$ (top left), $z = 1$ (top middle), $z = 2$ (top right), $z = 3$ (bottom left), $z = 4$ (bottom middle), and $z = 5$ (bottom right). The colors indicate the number of cells in each hexabin. The presence of the Ly α forest can be seen at low matter and H I overdensities, while the H I inside halos dominates the behavior of the relation for $\rho_{\text{HI}}/\bar{\rho}_{\text{HI}} \gtrsim 0.1$. The H I–matter relation is tighter at high redshift than at low redshift. The dashed black lines show the expectation from linear theory, $\delta_{\text{HI}} = b_{\text{HI}}\delta_{\text{m}}$, where b_{HI} is the large-scale H I bias, taken from Table 5.

information on the values of the cosmological parameters, can thus be inferred only if bias is understood (see Pénin et al. 2018 for a detailed discussion on the H I scale-dependence bias). On linear scales, the H I bias is constant, but on small scales, we expect to see scale dependence. It is important to determine the scales on which the H I bias is dependent and whether or not analytic models can reproduce that behavior.

We have computed the H I and matter auto-power spectrum and the H I–matter cross-power spectrum of the simulation at redshifts 0, 1, 2, 3, 4, and 5. The H I bias is then obtained using two different definitions: $b_{\text{HI}}(k) = \sqrt{P_{\text{HI}}(k)/P_{\text{m}}(k)}$ and $b_{\text{HI}}(k) = P_{\text{HI-m}}(k)/P_{\text{m}}(k)$. While the latter is “preferred,” as it does not suffer from stochasticity, the former is closer to observations. The results are shown in Figure 16.

The amplitude of the H I bias on large scales increases with redshift, from $\simeq 0.85$ at $z = 0$ to $\simeq 3.20$ at $z = 5$. On the largest scales that can be probed with TNG100, the amplitude of the H I bias is independent of the method used to estimate it. We assume that the values on large scales are equal to the linear H I bias, but note that there could be small corrections to those because of box size. The linear H I bias at different redshifts is given in Table 5. These values can be reproduced from the halo H I mass function as

$$b_{\text{HI}}(z) = \frac{\int_0^\infty n(M, z)b(M, z)M_{\text{HI}}(M, z)dM}{\int_0^\infty n(M, z)M_{\text{HI}}(M, z)dM}, \quad (27)$$

and therefore, the amplitude of the H I bias is sensitive to the astrophysical parameters α and M_{min} (see Section 5). Note, however, that the agreement between the above expression and the simulation results is not perfect because, among other things, our models for the halo mass function and halo bias do not include corrections for baryonic effects.

At $z = 0$, the H I bias exhibits a scale dependence even on the largest scales we can probe, due to the fact that the matter power spectrum at the scales probed by TNG100 is not in the linear regime at such low redshift. The dip in the H I bias at $k \simeq 1 h \text{Mpc}^{-1}$, which has also been found in observations (Anderson et al. 2018), is interesting. At $z = 1$, the bias remains almost constant down to rather small scales, $k \simeq 1 h \text{Mpc}^{-1}$. These trends agree with the findings of Springel et al. (2018), who studied galaxy bias for different galaxy populations at different redshifts. At high redshifts, $z \geq 2$, the H I bias already exhibits a dependence on scale at $k = 0.3 h \text{Mpc}^{-1}$, even though these scales are close to linear at those redshifts. Our results are also in qualitative agreement with those of Sarkar et al. (2016a), who studied the H I bias by painting H I on top of dark matter halos. The scale dependence of the bias is not necessarily a bad thing, as long as we can use perturbative methods to predict the shape of the H I power spectrum. For this purpose, we have compared the measurements of the H I power spectrum in TNG100 to analytical calculations using Lagrangian Perturbation Theory (LPT). The first-order LPT solution is the well-known Zel’dovich approximation (ZA) (Zel’dovich 1970; White 2014), for which we can simply write

$$P_{\text{HI}} = b_{\text{HI}}^2 P_{\text{ZA}}(k) + N, \quad (28)$$

and then fit for the two free parameters in the above equation. The constant piece takes care of the shot noise and any other term that is scale independent and uncorrelated with the H I field and therefore can be treated as noise in a cosmological analysis (Seljak & Vlah 2015). Given the small volume of TNG100, a perturbative analysis makes sense only at high redshifts, where linear and mildly nonlinear modes are

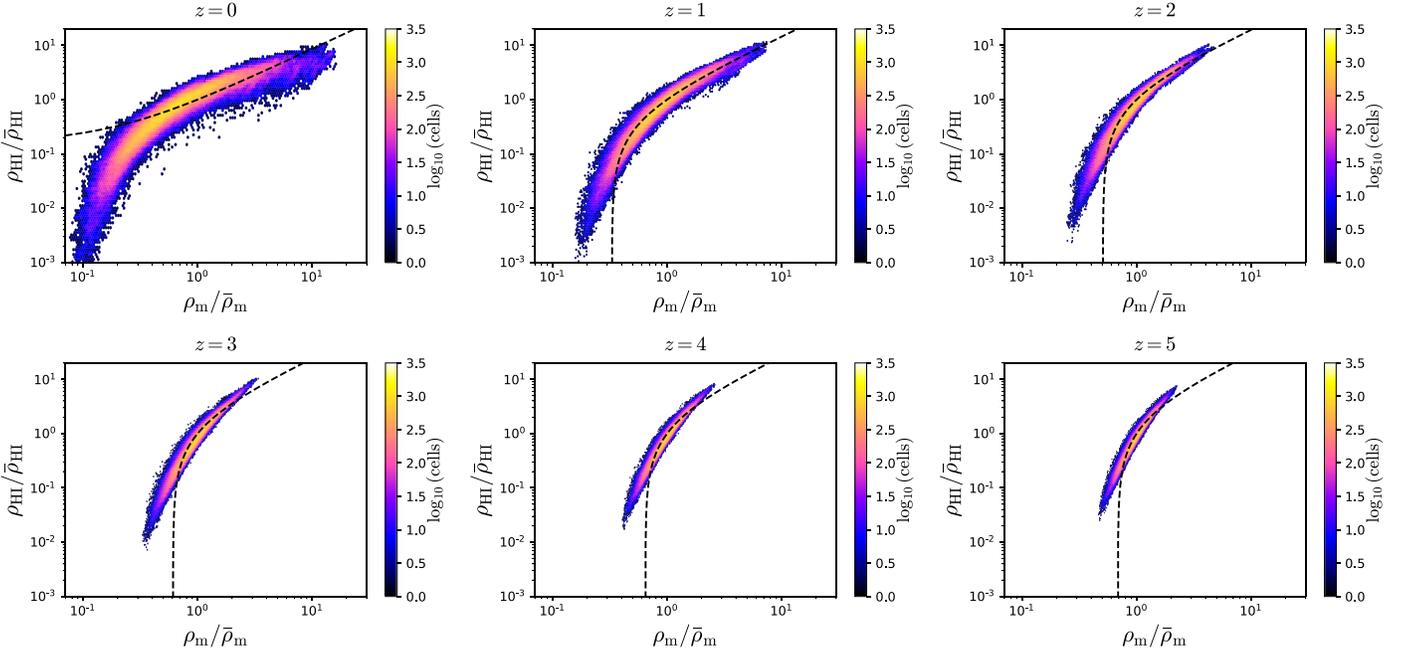


Figure 15. Same as Figure 14, but for a smoothing scale of $5 h^{-1}$ Mpc.

Table 5

Values of the HI Bias and HI Shot Noise from the Simulation at Different Redshifts

| z | 0 | 1 | 2 | 3 | 4 | 5 |
|---|------|------|------|------|------|------|
| b_{HI} | 0.84 | 1.49 | 2.03 | 2.56 | 2.82 | 3.18 |
| $P_{\text{HI}}^{\text{SN}}$ [$(h^{-1} \text{ Mpc})^3$] | 104 | 124 | 65 | 39 | 14 | 7 |

contained in the box, thus we restrict the comparison of Equation (28) with the measurements in the simulation to $z \geq 2$. The upper panel in Figure 17 shows the measurements of the HI power spectrum at different redshifts, using the same color scheme as in the previous figures. The points with error bars have been shifted horizontally to avoid overlap and facilitate the visual comparison with the theoretical models. The dashed lines display the fit to Equation (28) including all the modes up to $k_{\text{max}} = 1 h \text{ Mpc}^{-1}$. The fit is quite accurate, despite its simple functional form, and it confirms the HI distribution as an ideal tracer for cosmological studies. The continuous lines show the next to leading order, i.e., one-loop, calculation in LPT (Vlah et al. 2016; Modi et al. 2017), which includes an improved treatment of nonlinearities in the matter fields as well as several nonlinear bias parameters. Up to the scale we include in the fit, there is no difference between the two approaches, with the one-loop calculation also working on smaller scales not included in the analysis. The fact that the ZA works so well in describing the simulation measurements could vastly simplify the cosmological analysis and interpretation of 21 cm surveys observing at high redshift. For instance, interferometric surveys with a large instantaneous field of view like CHIME will be forced to include all of the complications arising from the curved sky, which are very easily handled in the ZA (Castorina & White 2018a, 2018b).

14. Secondary HI Bias

It is well known that the clustering of halos depends primarily on mass. However, mass is not the only variable that determines halo clustering; there is also a dependence on halo age (Sheth & Tormen 2004; Gao et al. 2005), concentration (Wechsler et al. 2006), subhalo abundance (Wechsler et al. 2006; Gao & White 2007), halo shape (Faltenbacher & White 2010), spin (Gao & White 2007), and environment (Xu & Zheng 2018; Han et al. 2018; Salcedo et al. 2018). Here, we identify a new secondary bias, originating from the HI content of halos.

Differently from the previous quantities, which are properties of the dark matter halos, the HI content is more related to the properties of the galaxies inside a halo, e.g., whether galaxies are red or blue. Thus, a study of this kind can only be carried out using hydrodynamic simulations.

To study this issue, we apply the following procedure. First, all halos whose total mass is within a relatively narrow mass bin are selected. The HI mass inside each of those halos, and the median value are determined. Next, the halos are split into two categories: HI rich and HI-poor, depending on whether the HI content of a particular halo is above or below the median, respectively. Finally, we compute the power spectrum of 1) all halos, 2) HI-rich halos, and 3) HI-poor halos.

The results are shown in Figure 18 at redshifts 0, 1, 2, 3, and 4 and for three different mass bins, $M \in [10^8 - 10^9] h^{-1} M_{\odot}$, $M \in [10^9 - 10^{10}] h^{-1} M_{\odot}$, and $M \in [10^{10} - 10^{11}] h^{-1} M_{\odot}$. The black lines indicate the power spectrum of all halos, while the blue and red lines represent the power spectra of the HI-rich and HI-poor halos, respectively.

Going toward smaller scales, the amplitudes of the different power spectra first flatten and then rise back up. This happens (1) because we approach the shot-noise limit and (2) due to aliasing. The shot-noise level of the HI-rich/-poor halos is different from that of all halos, as the latter contain, by definition, twice as many halos than the former. Thus, on small

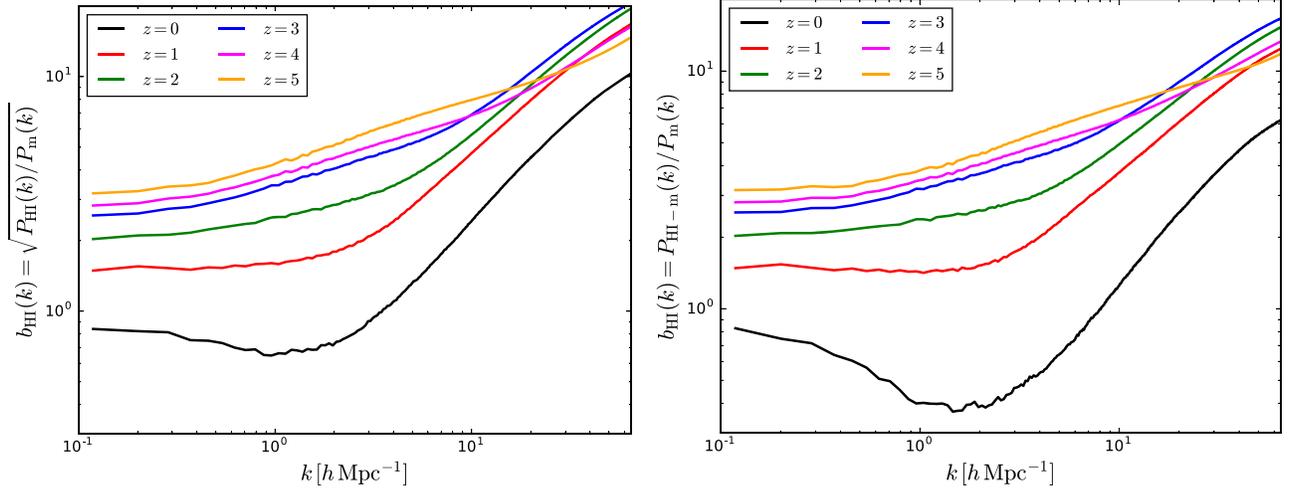


Figure 16. H I bias at redshifts 0 (black), 1 (red), 2 (green), 3 (blue), 4 (purple), and 5 (orange) computed as the square root of the ratio between the H I and matter power spectra (left), and as the ratio between the H I–matter cross-power spectrum and the matter power spectrum. The value of the H I bias increases with redshift. At high redshift, the H I bias becomes nonlinear on scales $k \gtrsim 0.3 h \text{ Mpc}^{-1}$. We emphasize that our results are not converged against resolution (see Appendix A). This should, however, not be seen as a limitation of our claims, as we present results for TNG100, i.e., at the resolution to which the model parameters have been tuned to reproduce a set of galaxy properties. For instance, our results for the H I bias at $z = 0$ are in excellent agreement with observations (Obuljen et al. 2018b).

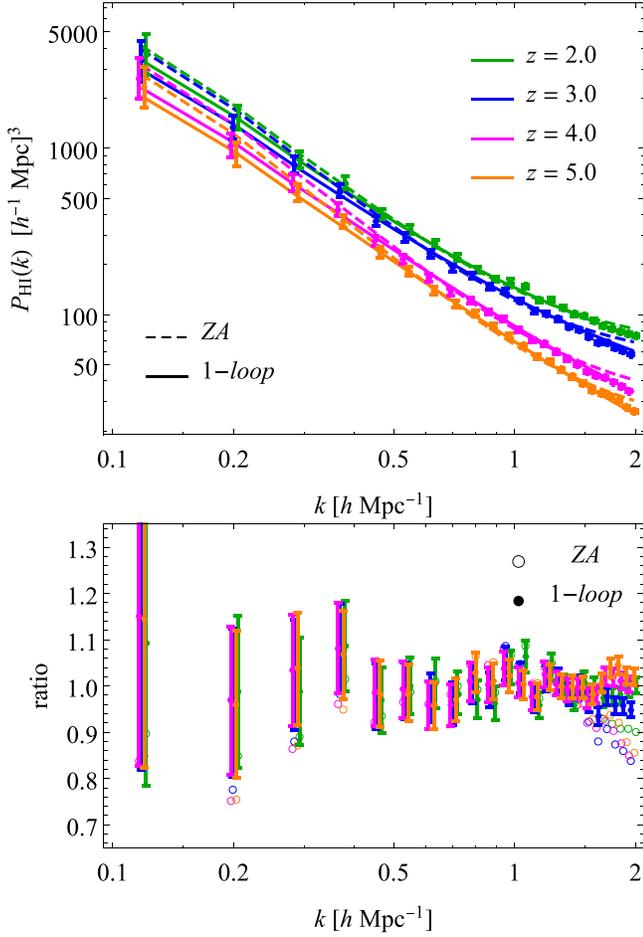


Figure 17. Top panel: H I power spectrum as a function of redshift measured in TNG100 (points with error bars). For visualization purposes only, the data at different redshift have been shifted horizontally to avoid overlap. The dashed lines show the analytical calculation assuming the ZA, whereas the continuous lines correspond to the one-loop calculation. Both models have been fitted to $k = 1 h \text{ Mpc}^{-1}$. See text for details. Bottom panel: ratio of the measured power to the analytical models. Filled points show the one-loop result, while the empty ones show the comparison to the ZA.

scales, the amplitude of the H I-rich and H I-poor halos is expected to be the same but higher by a factor of 2 than that of all halos, as is indeed seen.

For all redshifts and mass intervals considered, the clustering of H I-rich galaxies is different from that of H I-poor ones, showing that halo clustering depends not only on mass but on H I content as well. The difference in the clustering of H I-poor and H I-rich halos decreases, in general, with halo mass. At $z = 0$, the amplitude of the power spectrum of the H I-rich and H I-poor halos can be almost one order of magnitude different for halos in the $[10^9-10^{10}] h^{-1} M_{\odot}$ mass bin. The largest differences are seen for halos with masses around or below M_{min} at that particular redshift, namely, around the mass scale where the H I content starts being exponentially suppressed (see Section 5).

At $z = 0$, and for the mass bin intervals considered here, the H I-poor halos are more strongly clustered than the H I rich halos. On the other hand, at high redshift, the situation is the opposite, and H I-rich halos are more strongly clustered than H I-poor halos. At $z = 1$, we find that depending on the halo mass considered, H I-rich halos can be more or less clustered than H I-poor halos. We note that Guo et al. (2017) found that the clustering of H I galaxies from the ALFALFA survey at $z \sim 0$ shows a bias systematically lower than mass-selected halos, in agreement with our results for H I-rich halos.

Although the halo mass bins are fairly narrow, is not unreasonable to suspect that the most massive halos will have larger H I masses, and therefore, this could introduce some natural splitting that arises just from halo mass and not from H I secondary bias. In order to test this, we split the halos according to their median total halo mass and repeated the above analysis. We find that the clustering of the two samples is almost indistinguishable, ruling out the possibility that halo mass is affecting our results.

At low redshift, small halos near big ones are more likely to be stripped of their gas content. Thus, H I-poor halos should be more strongly clustered than H I-rich halos, as we find. This possibility has been recently suggested to explain the secondary bias that arises from several halo properties in Salcedo et al. (2018) and Han et al. (2018).

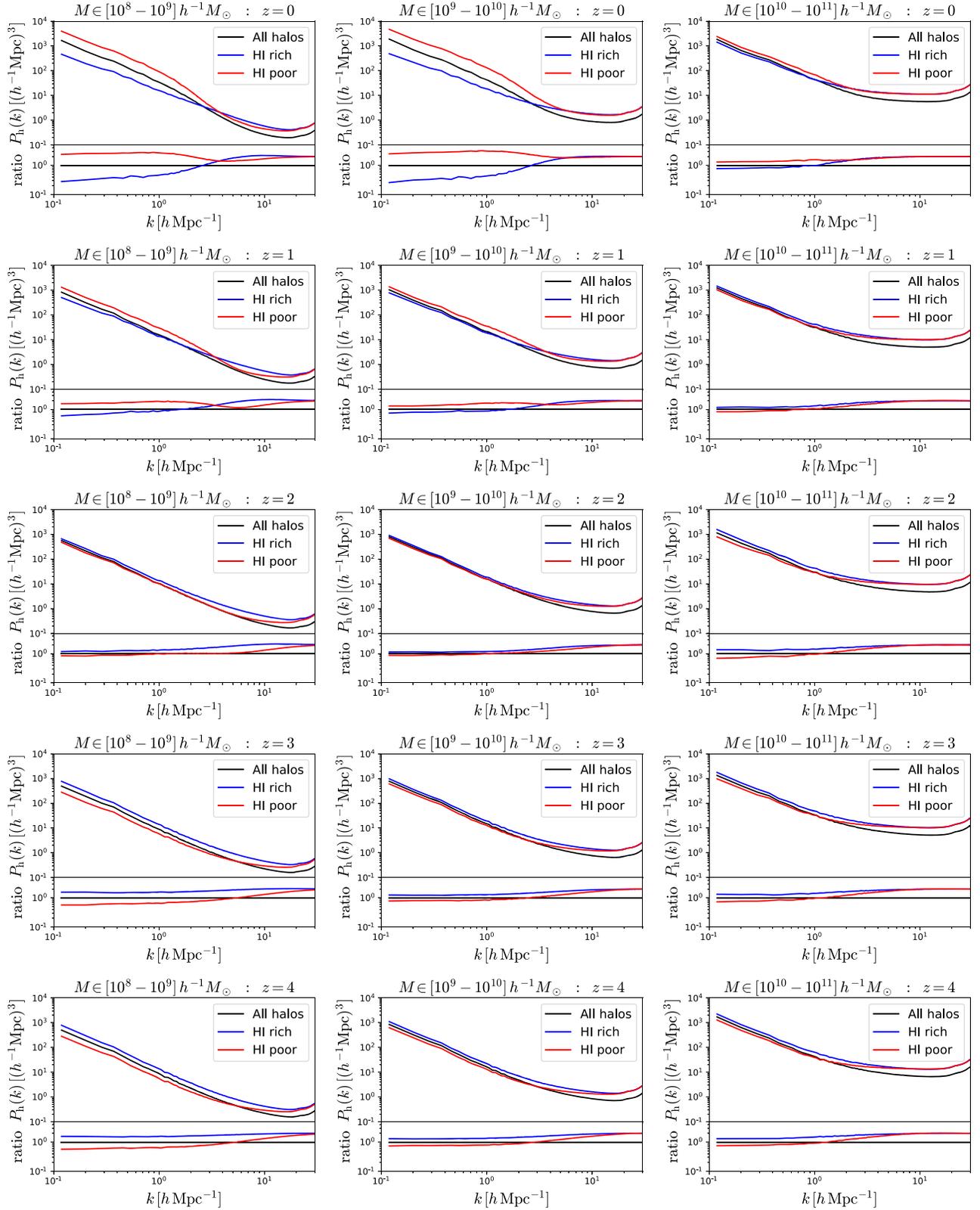


Figure 18. We select dark matter halos in narrow mass bins and compute their power spectra, shown with solid black lines. We then compute the H I mass inside each halo and find the median value of all halos in that mass bin. Next, we split the halos into two sets, those with H I mass above (H I rich) or below (H I poor) the median. Finally, we compute the power spectrum of the halos in each set and show the results with blue (H I rich) and red (H I poor) lines. The results are shown at redshifts 0, 1, 2, 3, and 4 from top to bottom and for halos in the 10^8 – 10^9 (left column), 10^9 – 10^{10} (middle column), and 10^{10} – 10^{11} $h^{-1} M_{\odot}$ mass bin intervals. The upper part of each panel displays the different halo power spectra while the bottom part shows the same results normalized by the power spectrum of all halos. The clustering of halos depends not only on mass but also on H I content. The magnitude of this effect is generally larger for smaller halos. At low redshift, H I-poor halos are more clustered than H I-rich halos, but at high redshift, the trend reverses.

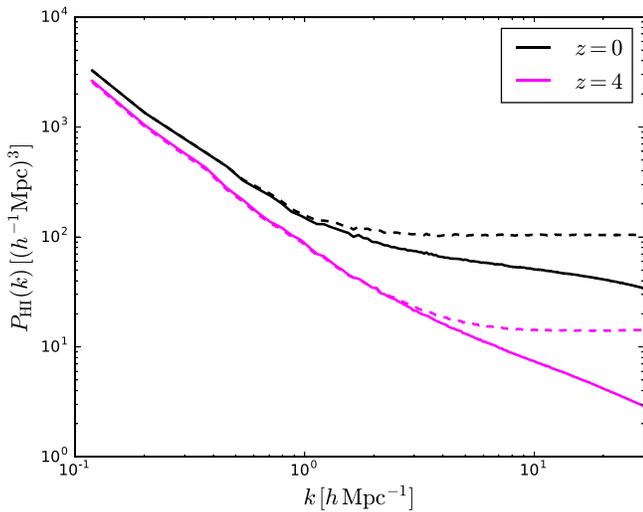


Figure 19. HI shot noise. This figure shows the standard HI power spectrum (solid lines) and the power spectrum when the HI inside halos is placed in the halo center (dashed lines) at redshifts $z = 0$ (black) and $z = 4$ (purple). For the former, we can see both the one- and two-halo terms, while for the latter, the one-halo term is just the HI shot noise.

On the other hand, at high redshift, gas stripping by nearby halo neighbors should be less effective, as the largest halos are not yet very massive and there has been less physical time for these processes to operate. We speculate that at high redshift, regions around massive halos are richer in HI than other regions. For example, in regions with higher density, we would expect the filaments to be slightly more dense and therefore will host more HI. Halos connected by those filaments may thus become HI rich. This naive picture can be seen in Figure 27, where at high redshift, the filaments in the denser regions host more HI than in less dense regions.

15. HI Shot Noise

An important consideration in any cosmological survey is shot noise, as its amplitude determines the maximum scale where cosmological information can be extracted from (see Equation (1)). However, it can also be used to learn about the galaxy population hosting the HI (Wolz et al. 2017, 2018). The purpose of this section is to quantify the amplitude of the HI shot noise from our simulations.

We now illustrate why computing the HI shot noise is slightly more complicated than determining the shot noise for other tracers, such as halos, where the value of the shot noise is simply given by the amplitude of the power spectrum on small scales.

The solid lines of Figure 19 show the HI power spectrum at redshifts 0 and 4. It can be seen that those power spectra receive contributions from both the one- and two-halo terms, i.e., the power spectrum on very small scales does not become constant, in contrast with the halo power spectrum. This happens simply because there is structure in HI inside halos and galaxies (see Figure 6).

In order to isolate the contribution of the HI shot noise, i.e., to avoid the one-halo term contribution, we do the following. We compute the total amount of HI inside every halo in the simulation and place that HI mass in the halo center. We then compute the HI power spectrum of that configuration. Since in that case there is no HI structure inside halos, there is no one-halo term, and the amplitude of the HI power spectrum

on small scales is just the HI shot noise. The dashed lines in Figure 19 display the results.

It can be seen that on large scales, the amplitude of the HI power spectrum of the two configurations is essentially identical. The small differences at $z = 4$ arise from the HI that is outside of halos (see Figure 3), whose contribution is not accounted for with our procedure. That contribution should, however, have a negligible impact on the amplitude of the HI shot noise. On small scales, the lack of the one-halo term when we artificially place the HI at the halo center makes it possible to isolate the value of the HI shot noise. We determine the value of the HI shot noise by averaging the amplitude of the HI power spectrum on scales $k \in [20-30] h \text{ Mpc}^{-1}$ and show the results in Table 5.

The HI shot noise can also be computed using the halo model framework (assuming all HI are in halos) as (Castorina & Villaescusa-Navarro 2017)

$$\begin{aligned}
 P_{\text{HI}}^{\text{SN}}(z) &= \lim_{k \rightarrow 0} P_{1\text{h,HI}}(k, z) = \frac{1}{[\rho_c^0 \Omega_{\text{HI}}(z)]^2} \\
 &\times \int_0^\infty n(M, z) M_{\text{HI}}^2(M, z) dM \\
 &= \frac{\int_0^\infty n(M, z) M_{\text{HI}}^2(M, z) dM}{\left[\int_0^\infty n(M, z) M_{\text{HI}}(M, z) dM \right]^2}. \quad (29)
 \end{aligned}$$

If we use the Sheth & Tormen (ST) formula (Sheth & Tormen 2002) for the halo mass function in this expression²⁹ and our fitting formula for $M_{\text{HI}}(M, z)$ (see Table 1), we obtain values for the HI shot noise in agreement with those measured directly in the simulation.

In order to validate our results, we have estimated the HI shot noise by measuring the stochasticity between the HI and the matter fields (Seljak et al. 2009)

$$P_{\text{HI}}(k) - \frac{P_{\text{HI-m}}^2(k)}{P_m(k)}, \quad (30)$$

which at low enough k should correspond to the uncorrelated part of the HI power spectrum, i.e., P_{SN} . However, the shot-noise amplitudes we obtain in this case are much larger than those found using our fiducial procedure. By repeating this approach for halos, we also find that we cannot recover the standard $1/\bar{n}$ result. Our findings are in agreement with those of other studies, see Hand et al. (2017) and reference therein, and point toward some lack of understanding of the noise properties in low-mass halos even in gravity-only simulations. For better comparison with previous work, which always considered Poissonian shot noise, we assume P_{SN} is given by the fiducial halo model procedure, and defer a study of this unexpected disagreement to future work.

We find that the HI shot noise is low at all redshifts. This is in broad agreement with the analytical work of Castorina & Villaescusa-Navarro (2017), whose results at high redshift had, however, a large theoretical error. Our shot-noise values are slightly lower than those in that paper, mostly because the values of M_{min} at high z that we find here are lower than those considered in Castorina & Villaescusa-Navarro (2017).

²⁹ We find that the halo mass function in IllustrisTNG is well reproduced by the ST form.

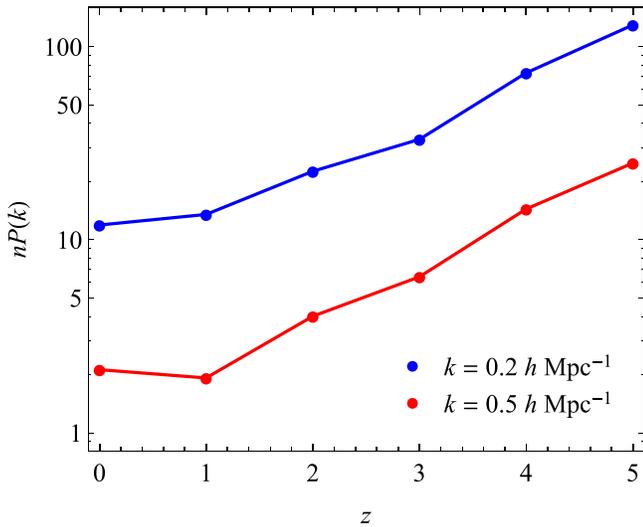


Figure 20. An important quantity for BAO studies is $nP_{0.2}$, defined as the ratio between the amplitudes of the cosmological signal and the shot-noise level at $k = 0.2 h \text{ Mpc}^{-1}$. In this plot, we show this quantity in blue as a function of redshift using TNG100 measurements. We find that it is large at all redshifts, indicating that shot noise is not important for BAO studies with 21 cm intensity mapping. In order to extract information from small scales, it is also crucial to have a large nP at high k . The red line shows that this is indeed the case at $k = 0.5 h \text{ Mpc}^{-1}$ for all redshifts considered in our work.

The low values of shot noise we find have important implications. First, 21 cm intensity mapping experiments that aim at measuring the BAO peak (Obuljen et al. 2018a) position such as CHIME, OOTY, BINGO, HIRAX, or SKA will barely be affected by shot noise. We illustrate this in Figure 20, where we plot, in blue,

$$nP_{0.2}(z) = \frac{P_{\text{HI}}(k = 0.2 h \text{ Mpc}^{-1}, z)}{P_{\text{SN}}(z)} \quad (31)$$

as a function of redshift. We obtain values of $nP_{0.2}$ above $\simeq 15$ at all redshifts, showing that shot-noise contamination on BAO scales is minimal. This is a great advantage over traditional methods such as galaxy surveys.

Second, the shot-noise levels are very low at high redshift. This means that shot noise does not erase the cosmological information on small scales. The red line shows the value of nP at $k = 0.5 h \text{ Mpc}^{-1}$, which is still much larger than one and implies that these modes can be in principle measured in the cosmic variance limit. With accurate theory predictions such as the one described in the previous section, this information can be retrieved and used to reduce errors in the values of the cosmological parameters.

16. Redshift-space Distortions

Twenty-one centimeter intensity mapping observations probe the spatial distribution of cosmic neutral hydrogen in redshift space, not in real space. Thus, it is of utmost importance to understand the impact of peculiar velocities on the clustering of HI. In this section, we study the clustering of neutral hydrogen in redshift space.

Here, we make use of the plane-parallel approximation to displace the positions of particles and Voronoi cells from real

(\mathbf{x}) to redshift space (\mathbf{s}) through

$$\mathbf{s} = \mathbf{x} + \frac{1+z}{H(z)} \mathbf{v}_{\parallel}(\mathbf{r}), \quad (32)$$

where $\mathbf{v}_{\parallel}(\mathbf{r})$ is the peculiar velocity of the particle/cell along the line of sight. We use the three Cartesian axes as different lines of sight. Our results represent the mean over the three axes.

We have computed the clustering of HI in redshift space and show the results in Figure 21. Although we have computed the HI monopoles, quadrupoles, and hexadecapoles, the latter two are too noisy so we restrict our analysis to the monopoles.

We show with red/blue lines the monopoles in real/redshift space in this figure. The two main physical processes governing the effect of peculiar velocities can clearly be seen. On large scales, the clustering of HI in redshift space is enhanced due to the Kaiser effect (Kaiser 1987). On small scales, the peculiar velocities of HI inside halos give rise to the Fingers of God, suppressing the amplitude of the HI power spectrum.

The bottom part of each panel of Figure 21 shows the ratio between the monopoles in redshift and real space as a solid black line. The black dashed line displays the prediction of linear theory for that ratio, i.e.,

$$\frac{P_0^s(k)}{P_0^r(k)} = 1 + \frac{2}{3}\beta + \frac{1}{5}\beta^2, \quad (33)$$

where $\beta = f/b_{\text{HI}}$, with $f \simeq \Omega_m^{0.545}(z)$ being the linear growth rate. We have estimated β using the values of the linear HI bias from Table 5.

As expected, linear theory is not able to describe our results at low redshift. This is because the scales we probe in TNG100 are too small for linear theory to hold. On the other hand, we find that the Kaiser factor can reasonably well explain the monopole ratio down to $k \simeq 0.3, 0.5,$ and $1.0 h \text{ Mpc}^{-1}$ at redshifts 3, 4, and 5, respectively.

Given the results in Section 13, our findings are not surprising, and we plan to compare the measurements in TNG100 to redshift-space LPT analytical predictions in upcoming work.

As an alternate way to visualize the consequences of redshift-space distortions, we show the two-dimensional power spectrum of cosmic HI in the top two rows of Figure 22, at redshifts from 0 to 5. The Kaiser effect manifests itself as a squeezing of isopower contours along the perpendicular direction on large scales. It is apparent down to relatively small scales at high redshift, as expected.

On small scales, the Fingers of God arise as isopower contours propagating farther in the perpendicular than the radial direction. At low redshift and on small scales, we find that isopower contours exhibit a very weak dependence on the perpendicular direction, i.e., $P_{\text{HI}}^s(k_{\parallel}, k_{\perp}) \simeq P_{\text{HI}}^s(k_{\parallel})$.

We show the results for the 2D matter power spectrum in the bottom rows of Figure 22. It can be seen that (1) the Kaiser effect is visible down to smaller scales than in the HI field at high redshift and (2) the magnitude of the Fingers of God is lower in the matter field than in the HI field.

The halo model can be used to understand why the magnitude of the Fingers of God is higher in HI than in matter. Each dark matter halo will show up in redshift space not as a sphere but as an ellipsoid, due to internal peculiar velocities. The eccentricity of those ellipsoids will depend primarily on halo mass: the velocity dispersion in large halos

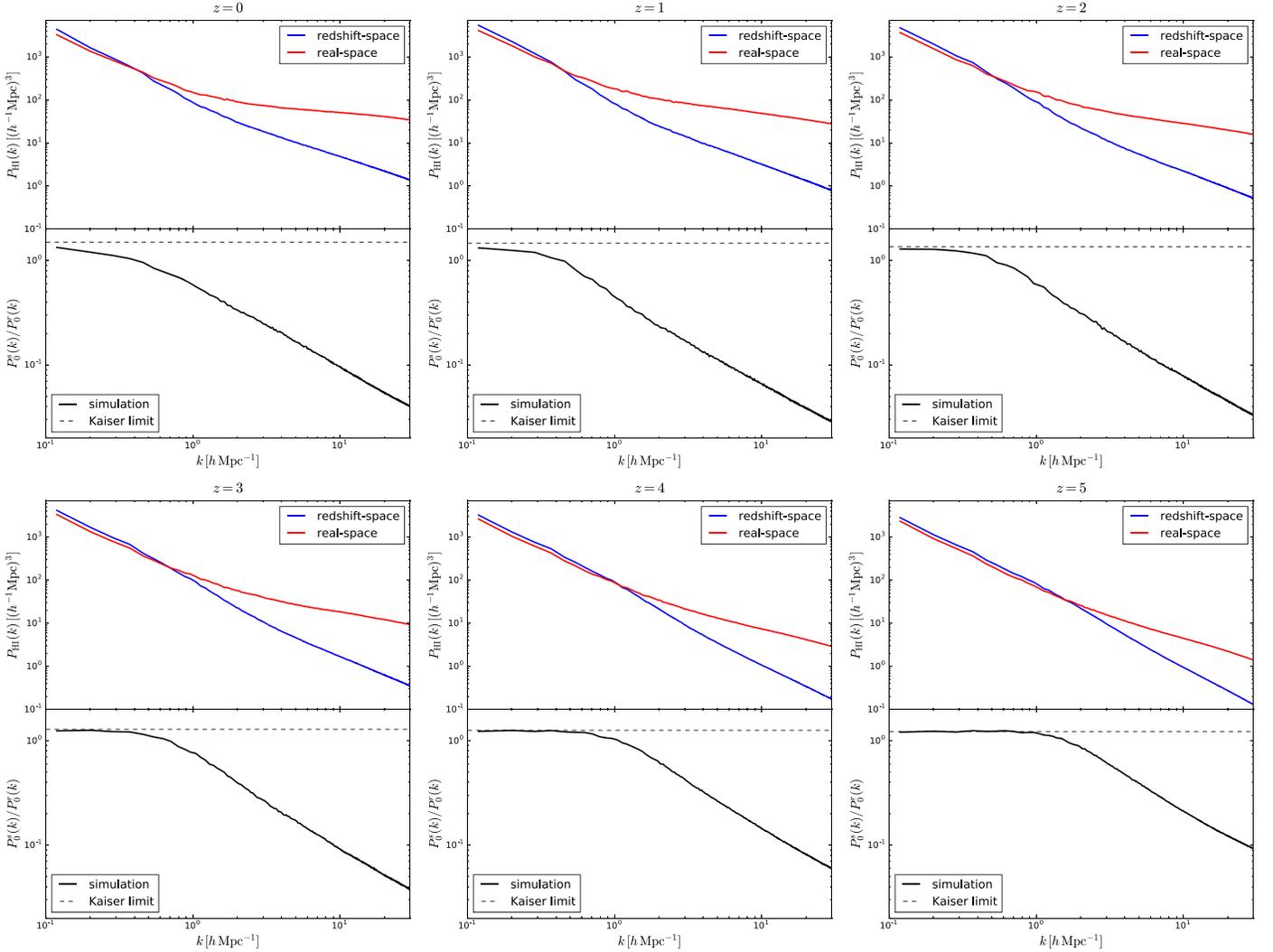


Figure 21. Impact of redshift-space distortions on the H I power spectrum at redshifts 0 (top left), 1 (top middle), 2 (top right), 3 (bottom left), 4 (bottom middle), and 5 (bottom right). The upper part of each panel shows the H I power spectrum (monopole) in real space (red) and redshift space (blue). The bottom part displays the ratio between the monopoles in redshift and real space (solid black) and the prediction of linear theory (dashed black). Redshift-space distortions enhance/suppress power on large/small scales. Linear theory can explain the H I clustering in redshift space down to very small scales at high redshift, while it cannot explain it at low redshift on the scales we probe in the simulations.

will be higher than that in small halos, so their eccentricity will be larger. The amplitude of the matter power spectrum on small scales will be dominated by small halos, whose velocity dispersions are not large.

On the other hand, we know for HI that since there is a cutoff in the halo HI mass function, halos below a certain mass will not contribute to the HI power spectrum. Thus, it is expected that the amplitude of the Fingers of God will be larger in the HI field than in the matter field because (1) the velocity dispersions of HI and matter/CDM are similar (see Section 11), and (2) in the HI field, we do not have the contribution of small halos that dominates the amplitude of the power on small scales.

In order to corroborate this hypothesis, we have taken all halos with masses above $10^{10} h^{-1} M_{\odot}$, and we have computed the power spectrum of the matter inside them. In that case, we observe very similar results to those from the HI, i.e., the amplitude of the Fingers of God of that particle distribution is much larger than the one for all matter.

The impact of redshift-space distortions on the HI power spectrum has recently been studied in Sarkar & Bharadwaj (2018)

using N -body simulations. Following their work, we have tried to model the 2D HI power spectrum using the following phenomenological expression

$$P_{\text{HI}}^s(k, \mu) = (1 + \beta\mu^2)^2 P_{\text{HI}}^r(k) \frac{1}{\left(1 + \frac{1}{2}k^2\mu^2\sigma_p^2\right)^2}, \quad (34)$$

where $\beta = f/b_{\text{HI}}$, $P_{\text{HI}}^r(k)$ is the fully nonlinear HI power spectrum, and σ_p is a phenomenological parameter that accounts for the Fingers-of-God effect. The reason for using this expression is that even if the HI bias is nonlinear, we will recover the Kaiser factor when computing the monopole ratio (see Figure 21) at high redshift, where the amplitude of the Fingers of God is small.

By fitting the above expression to our 2D HI power spectrum down to $k = 1 h \text{ Mpc}^{-1}$ and assuming Gaussian errors, we find that this approach works reasonably well, $\chi^2/\text{d.o.f} \simeq [1.5\text{--}2.2]$, with $\sigma_p = 1.73, 2.09, 1.37, 0.93, 0.34$, and 0 at redshifts 0, 1, 2, 3, 4, and 5, respectively. However, by

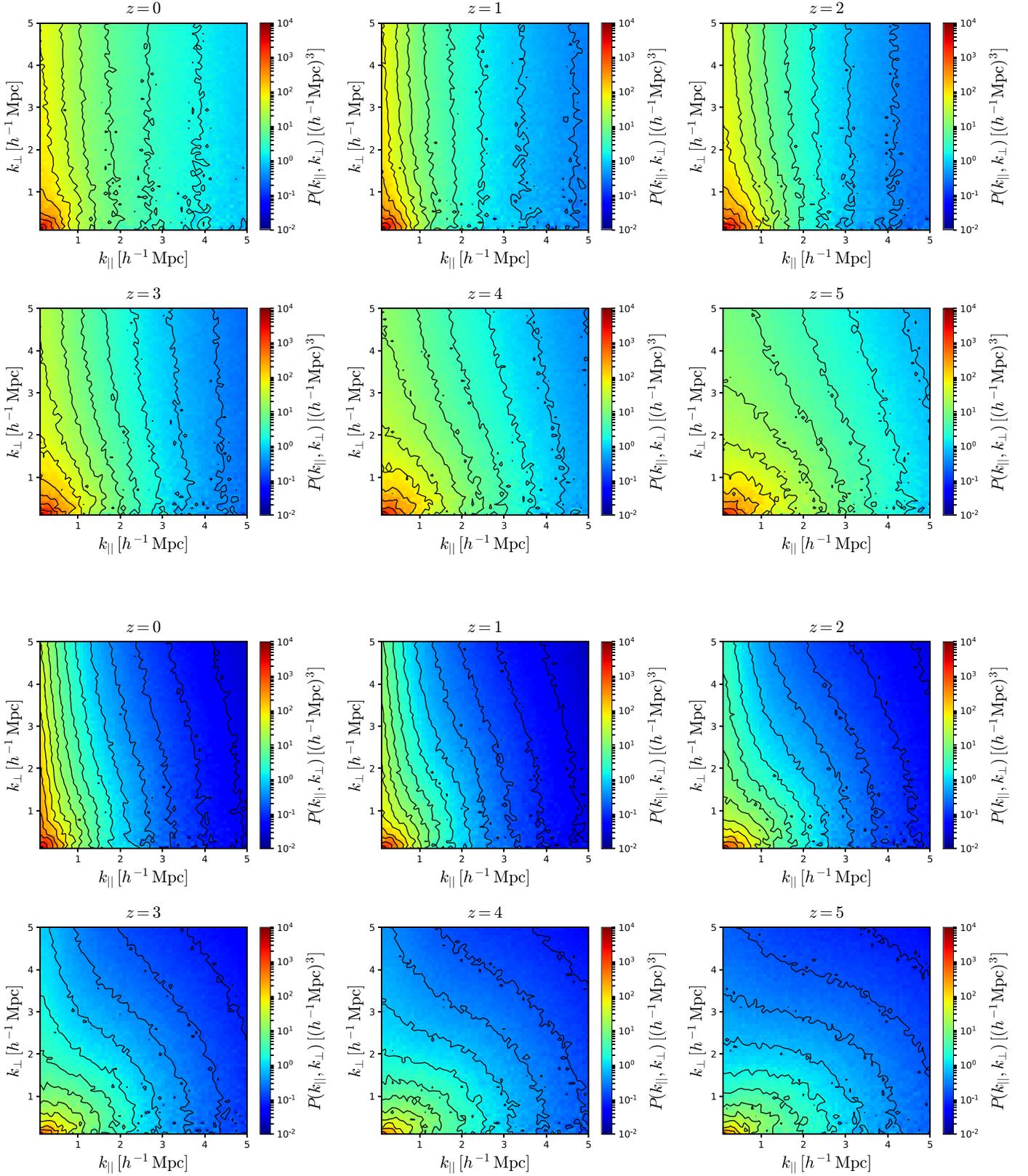


Figure 22. Top two rows: 2D power spectrum of HI at redshifts 0 (upper left), 1 (upper middle), 2 (upper right), 3 (bottom left), 4 (bottom middle), and 5 (bottom right). Even though the small volume of our simulation makes the 2D power spectrum noisy on large scales, the Kaiser effect can be seen, particularly at high redshifts, as isopower contours being squeezed in the k_{\perp} direction. On small scales, the 2D power spectrum is dominated by the Fingers of God, whose amplitude is larger than that in the matter field and is more important at low redshift. Bottom two rows: same as above but for matter instead of HI.

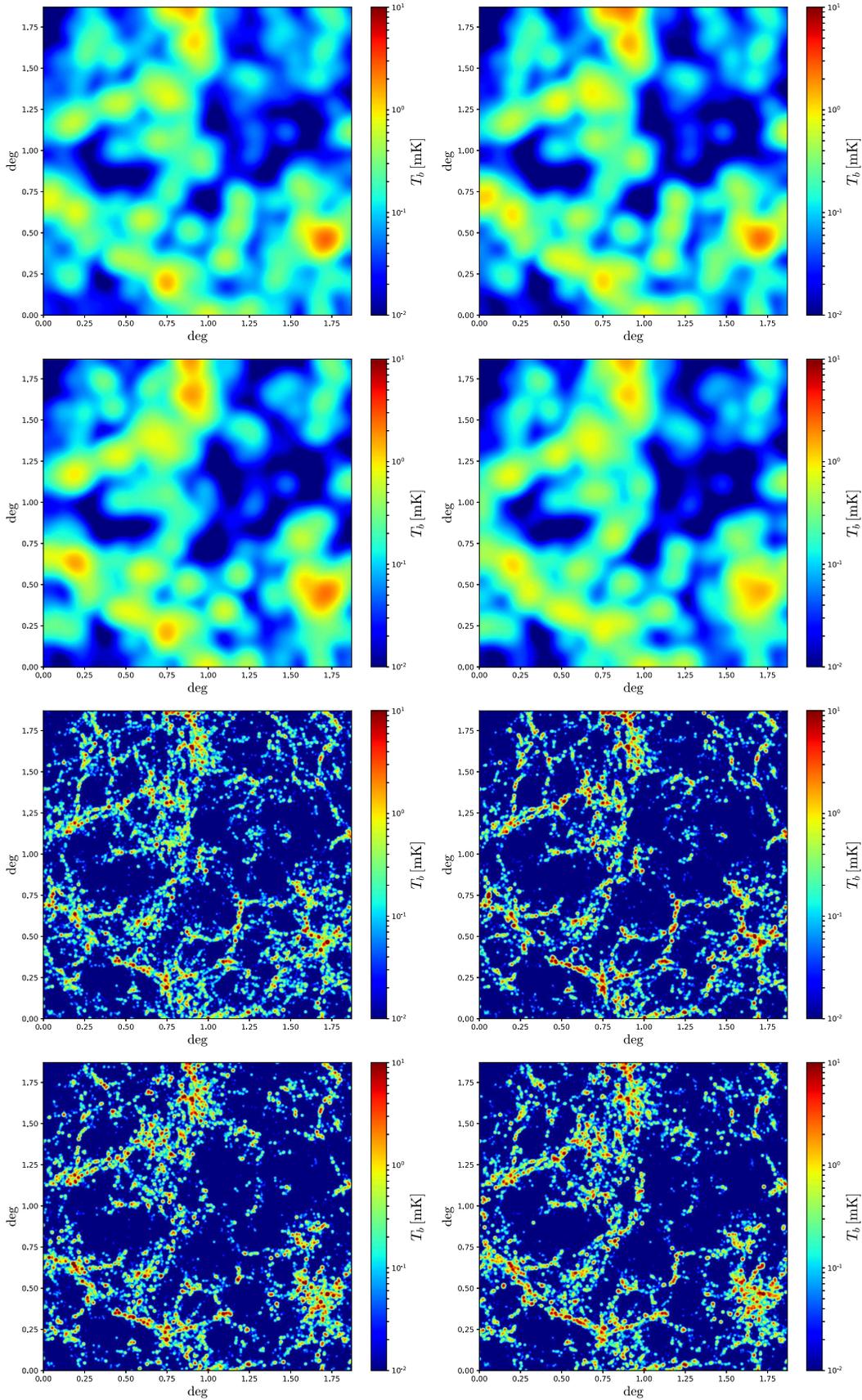


Figure 23. 21 cm maps at 710 MHz with 1 MHz bandwidth over an area of $\sim 4 \text{ deg}^2$. The upper and bottom pairs of panels show maps with angular resolutions of $3'$ and $0.3'$, respectively. Within each pair, the top one was made in real space and the bottom in redshift space. The maps on the right column have been generated from the computationally expensive IllustrisTNG simulations, while the maps on the left were generated by painting H I on top of dark matter halos from computationally cheap N -body simulations using the ingredients studied in this paper.

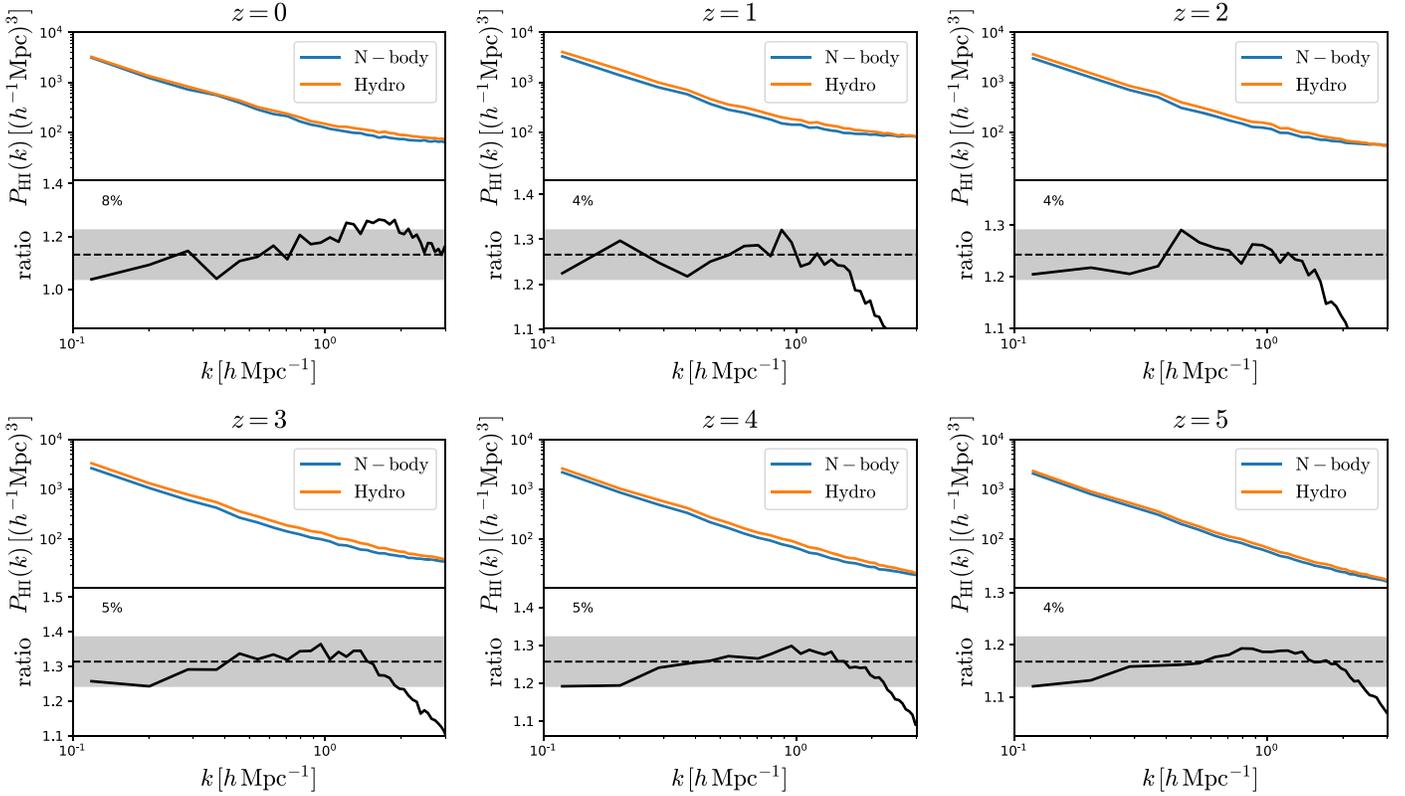


Figure 24. A comparison of the spatial distribution of HI from IllustrisTNG vs. the one obtained by placing HI in the centers of halos in an N -body simulation at redshift 0 (upper left), 1 (upper middle), 2 (upper right), 3 (bottom left), 4 (bottom middle), and 5 (bottom right). The HI mass assigned to each halo in the N -body run is taken from our tabulated $M_{\text{HI}}(M, z)$ in Table 1. We compute the HI power spectrum in real space for both configurations: N -body (blue) and hydro (green). The black line in the bottom part of each panel shows the ratio between the power spectra. Although the overall normalization can be different (see the text for more details), it is more important to reproduce the shape. The black shaded region shows the variation in shape from the largest scales to $k = 1 \text{ h Mpc}^{-1}$ and quoted with a number in the bottom part of each panel. This simple procedure allows us to generate mock 21 cm maps whose underlying power spectrum is accurate at $\approx 5\%$ down to $k = 1 \text{ h Mpc}^{-1}$.

computing the monopole from the above expression

$$P_{\text{HI}}^0(k) = \frac{1}{2} \int_{-1}^1 P_{\text{HI}}^s(k, \mu) d\mu \quad (35)$$

and comparing with our measurements, we do not find good agreement.

We have also repeated the above exercise for the models considered in Sarkar & Bharadwaj (2018), concluding that none of those represent a good description of our results. We leave a more detailed analysis of this issue to future work.

17. 21 cm Maps

The HI properties studied in this paper can be used to generate mock 21 cm maps. In this section, we study (1) whether less computationally expensive simulations can be used to create 21 cm maps and (2) the importance of accounting for the one-halo term when making mocks.

The right column of Figure 23 shows 21 cm maps created from the spatial distribution of HI in the TNG100 simulation. From top to bottom, these maps show the 21 cm map in real space with $3'$ angular resolution (top), 21 cm map in redshift space with $3'$ angular resolution (top middle), 21 cm map in real space with $0.3'$ angular resolution (bottom middle), and 21 cm map in redshift space with $0.3'$ angular resolution (bottom). All of those maps are centered at a frequency of 710 MHz ($z = 1$) and have a bandwidth of 1 MHz ($\approx 5 \text{ h}^{-1} \text{ Mpc}$).

The procedure used to create these maps is as follows. First, the HI density field is computed by assigning HI masses of gas cells (either in real or redshift space) to a grid of 2048^3 cells using the nearest-grid-point (NGP) mass-assignment scheme. Then, we select a slice of the HI density field grid whose width is taken to reproduce the desired frequency bandwidth. Next, that slice is projected onto a two-dimensional grid, and HI densities are transformed to brightness temperatures through

$$T_b(\mathbf{x}) = 189 \text{ h} \left(\frac{H_0(1.0 + z)^2}{H(z)} \right) \frac{\rho_{\text{HI}}(\mathbf{x})}{\rho_c} \text{ mK}. \quad (36)$$

Finally, we convolve that grid with a Gaussian filter of radius $R = \theta \chi$, where θ is the desired angular resolution and χ is the comoving distance to redshift z (or frequency ν).

The 21 cm maps on the left column of Figure 23 have been created from an N -body simulation that shares the same initial conditions as TNG100, i.e., TNG100-1-DM, but whose computational cost is over an order of magnitude lower. In that simulation, we have placed an HI mass given by $M_{\text{HI}}(M, z)$ from Table 1 on the center of each dark matter halo. Then, we have followed the procedure outlined above to create the 21 cm maps. To make 21 cm maps in redshift space, we displace the HI mass that we put in the center of each halo according to the peculiar velocity of that halo.

It can be seen that the qualitative agreement between the maps from the full hydrodynamic simulation and the cheaper N -body one is very good. In Figure 24, we quantify this visual

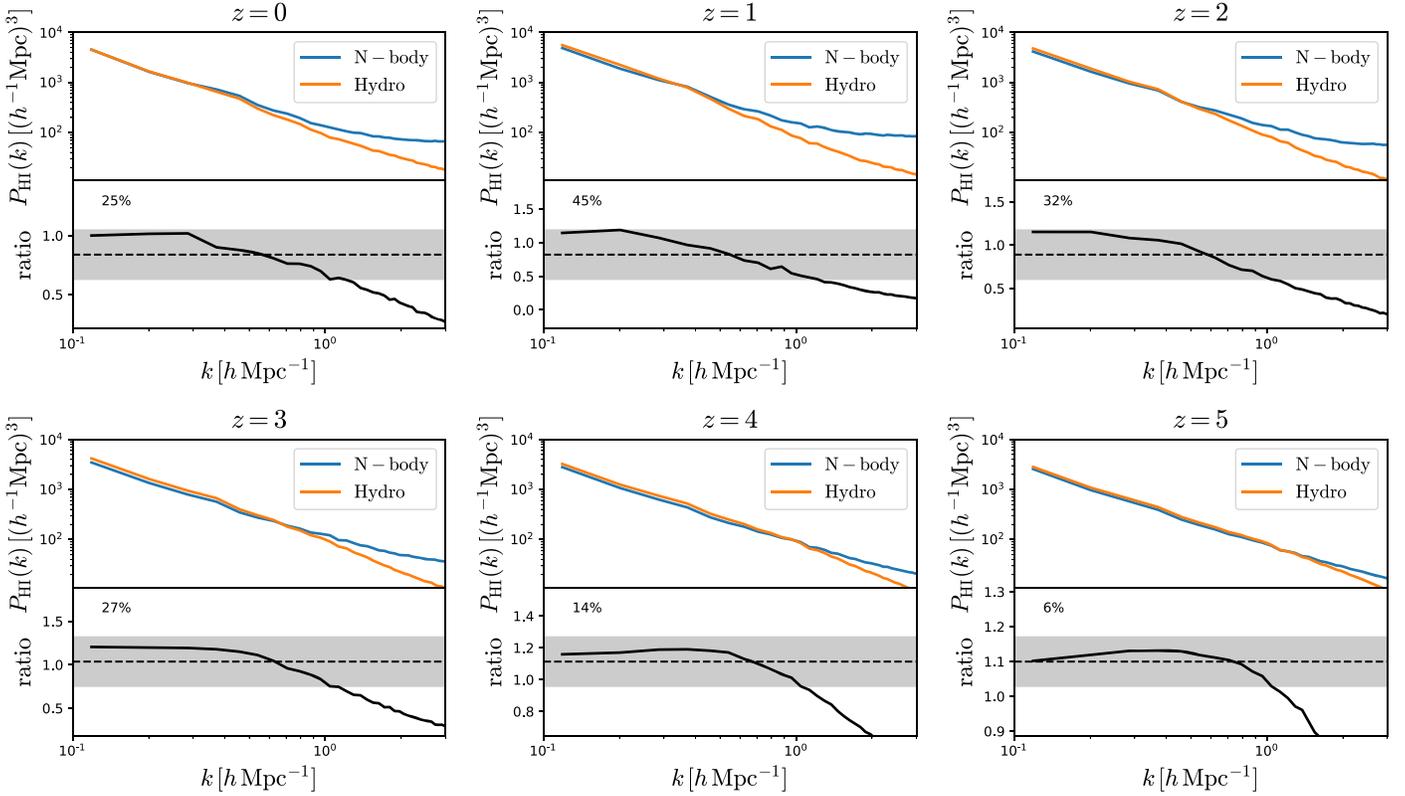


Figure 25. Same as Figure 24, but for H I monopole in redshift space. It can be seen that the distributions of H I in the two configurations differ more significantly than in real space. The origin of this large discrepancy, which is more prominent at low redshift, is the lack of the Fingers of God in the modeling of H I with the N -body simulations, since we place all H I in the halo center. More realistic 21 cm maps need to account for the H I velocity dispersion inside halos.

Table 6

We Find that an Expression Like $M_0 x^\alpha \exp(-1/x^{0.35})$, where $x = M/M_{\min}$, Reproduces Our Results Well for the Halo H I Mass Function, $M_{\text{H I}}(M, z)$

| z | FoF | | | FoF-SO | | |
|-----|-----------------|-------------------------------|------------------------------------|-----------------|-------------------------------|------------------------------------|
| | α | M_0 [$h^{-1} M_\odot$] | M_{\min} [$h^{-1} M_\odot$] | α | M_0 [$h^{-1} M_\odot$] | M_{\min} [$h^{-1} M_\odot$] |
| 0 | 0.49 ± 0.03 | $(2.1 \pm 0.7) \times 10^9$ | $(5.2 \pm 1.3) \times 10^{10}$ | 0.42 ± 0.03 | $(2.4 \pm 0.8) \times 10^9$ | $(5.6 \pm 1.4) \times 10^{10}$ |
| 1 | 0.76 ± 0.03 | $(4.6 \pm 2.1) \times 10^8$ | $(2.6 \pm 1.0) \times 10^{10}$ | 0.67 ± 0.04 | $(6.5 \pm 3.5) \times 10^8$ | $(3.3 \pm 1.5) \times 10^{10}$ |
| 2 | 0.80 ± 0.03 | $(4.9 \pm 2.1) \times 10^8$ | $(2.1 \pm 0.7) \times 10^{10}$ | 0.72 ± 0.03 | $(5.9 \pm 2.7) \times 10^8$ | $(2.4 \pm 0.9) \times 10^{10}$ |
| 3 | 0.95 ± 0.03 | $(9.2 \pm 4.7) \times 10^7$ | $(4.8 \pm 1.9) \times 10^9$ | 0.90 ± 0.03 | $(1.0 \pm 0.6) \times 10^8$ | $(5.5 \pm 2.3) \times 10^9$ |
| 4 | 0.94 ± 0.02 | $(6.4 \pm 3.7) \times 10^7$ | $(2.1 \pm 1.0) \times 10^9$ | 0.82 ± 0.03 | $(1.6 \pm 0.8) \times 10^8$ | $(4.5 \pm 1.9) \times 10^9$ |
| 5 | 0.90 ± 0.02 | $(9.5 \pm 5.8) \times 10^7$ | $(1.9 \pm 1.0) \times 10^9$ | 0.84 ± 0.04 | $(1.1 \pm 0.9) \times 10^8$ | $(2.6 \pm 1.7) \times 10^9$ |

Note. In the past, expressions like $M_0 x^\alpha \exp(-1/x)$ have been widely used to model that quantity. In this work, we find that the latter reproduces well the high-mass end of $M_{\text{H I}}(M, z)$ but it underestimates the low-mass end. However, that expression still provides a good χ^2 when fitting our results. In order to help in comparisons with previous works, we provide here the best-fit values for α , M_0 , and M_{\min} when fitting our halo H I mass function with $M_0 x^\alpha \exp(-1/x)$. The left/right part shows the results for the FoF and FoF-SO halos.

agreement by computing the H I power spectrum of the hydrodynamic and N -body simulations in real space at different redshifts.

We find that the amplitude of the two H I power spectra can be significantly different, between 10% and 40%. We attribute these differences to the inaccuracies of our $M_{\text{H I}}(M, z)$ function (e.g., we do not require our fit to reproduce $\Omega_{\text{H I}}(z)$, to the effects of baryons on the halo mass function and halo clustering, which are ignored in this exercise, and to the omission of the one-halo term at very high k . For the latter, we emphasize that in this section we do not consider the spatial distribution of H I inside halos, which we leave to future work.

However, once the difference in amplitude is taken into account, we find that shapes differ by only $\simeq 5\%$ from the largest scales down to $k = 1 \text{ h Mpc}^{-1}$ at all redshifts. This is rather remarkable considering that the one-halo term was not accounted for. This exercise demonstrates that populating dark matter halos from a computationally cheap N -body simulation with H I can yield results that are reasonable, at least in shape, at a few percent level in the fully nonlinear regime at all relevant redshifts.

In Figure 25, we show the comparison between the H I power spectra from IllustrisTNG and the N -body simulation in redshift space at several redshifts. As for the comparison in real

space, the amplitude of the two power spectra can be quite different for the same reasons outlined above. However, even when the normalization offset is taken into account, there are larger shape differences than in real space. For instance, at $z = 1$, the discrepancies up to $k = 1 h \text{ Mpc}^{-1}$ can be as large as 45%. That difference declines with redshift, so that at $z = 5$ it is only 6%, very similar to the differences we find in real space.

The larger differences in redshift space can be attributed to the Fingers of God. Here, we did not attempt to model the one-halo term and, therefore, the H I Fingers of God are not present in our mock maps, while they are in those created from IllustrisTNG. As we saw in Section 16, the H I Fingers of God can propagate to relatively large scales and affect the amplitude and shape of the H I power spectrum. At higher redshift, the magnitude of the Fingers of God is lower, so the agreement between IllustrisTNG and the N -body mocks is expected to improve, as we observe. Finally, the agreement between the different maps also depends on bandwidth. For larger bandwidths, the Fingers-of-God effects will have a smaller impact. We could also argue that beam smoothing in IM surveys will further reduce the effect of the Fingers of God in the final measured power spectrum.

We emphasize that our results are not converged against resolution (see Appendix A). This should, however, not be seen as a limitation of our claims, as we present results for TNG100, i.e., at the resolution to which the model parameters have been tuned to reproduce a set of galaxy properties. Besides, the purpose of this section is not to claim an absolute calibration of 21 cm maps via N -body simulations, but instead that given the spatial distribution of H I (at a given resolution in our case), most of the information can be condensed into a set of simple parameters and reproduced through N -body simulations.

We conclude that 21 cm intensity maps can be created via less computationally expensive simulations, like N -body, or via fast simulations, e.g., COLA (Tassev et al. 2013) or Pinocchio (Monaco et al. 2002), instead of expensive hydrodynamic simulations. It is, however, very important to account for the one-halo term, i.e., the Fingers of God, as expected when modeling the distribution of H I in redshift space.

18. Summary and Conclusions

A goal of current and upcoming radio telescopes is to map the spatial distribution of matter by detecting 21 cm emission from cosmic neutral hydrogen. The very large volumes that can be sampled through 21 cm intensity mapping observations will place tight constraints on the values of the cosmological parameters (Bull et al. 2015; Villaescusa-Navarro et al. 2015; Obuljen et al. 2017; Sprenger et al. 2018). In order to extract maximum information from these surveys, accurate theory predictions are needed.

Theory predictions to linear order are well known. For instance, the amplitude and shape of the 21 cm power spectrum are given by

$$P_{21 \text{ cm}}(k, \mu) = \bar{T}_b^2 (b_{\text{HI}} + f\mu^2)^2 P_m(k) + P_{\text{SN}}, \quad (37)$$

where $\bar{T}_b \propto \Omega_{\text{HI}}$ is the mean brightness temperature, b_{HI} is the H I bias, f is the linear growth rate, $\mu = k_z/k$, $P_m(k)$ is the linear matter power spectrum, and P_{SN} is the H I shot noise. While the value of \bar{T}_b is relatively well known from several observations across the redshift range $z \in [0, 5]$, little is known about b_{HI}

and P_{SN} . In this work, we have quantified them and studied the scales where linear theory holds, e.g., when the H I bias becomes nonlinear.

Accurate theory predictions in the mildly or fully nonlinear regimes will allow us to recover the large amount of information embedded in the spatial distribution of H I on small scales. There are several techniques for accomplishing this, such as perturbation theory, H I halo models, or numerical simulations. The purpose of our work has been to study the ingredients that these techniques employ. For example, H I halo models require the halo H I mass function and the H I density profile as inputs.

Our purpose here is not limited to analytic approaches, but also to understand how H I is distributed across the universe and how it evolves with time. We have shown that even with a subset of the ingredients studied in this work, one can model the spatial distribution of H I in the fully nonlinear regime without the use of computationally expensive hydrodynamic simulations, but using H I HOD models.

We have carried out our analysis using IllustrisTNG (Marinacci et al. 2018; Naiman et al. 2018; Pillepich et al. 2018a; Springel et al. 2018; Nelson et al. 2018), a sophisticated series of cosmological hydrodynamical simulations that have been shown to be in broad agreement with many basic observables, and run at an unprecedented combination of large volume and high resolution, therefore providing an excellent testbed for accurately investigating the distribution of H I from the disks of spiral galaxies to cosmological scales.

We outline the main conclusions of our work below:

1. We find that almost all H I in the universe are inside halos: from more than 99% at $z = 0$ to around 88% at $z = 5$. The fraction of H I outside halos increases with redshift because the gas in the IGM is denser and the amplitude of the UV background decreases with redshift (at $z > 2$). This justifies the use of halo models to model the distribution of H I in the universe, but quantifies their limitations at high redshifts. The fraction of H I inside galaxies is slightly lower than that in halos. At $z = 0$, $\simeq 97\%$ of all H I are inside galaxies, while at $z = 5$ this number decreases to $\simeq 80\%$.
2. We find that the halo H I mass function, i.e., the average H I mass hosted by a halo of mass M at redshift z , is well reproduced by a function like

$$M_{\text{HI}}(M, z) = M_0 \left(\frac{M}{M_{\text{min}}} \right)^\alpha \exp(-M_{\text{min}}/M)^{0.35},$$

where M_0 , M_{min} , and α are free parameters. The best-fit values are given in Table 1 for both FoF and FoF-SO halos. The value of α increases with redshift, likely indicating that at low redshift, processes such as ram-pressure and tidal stripping, and AGN feedback make galaxies in clusters H I poor. We find that M_{min} decreases with redshift. On the other hand, only halos with circular velocities above around 30 km s^{-1} host a significant H I mass fraction. Although the fit is slightly worse, our halo H I mass function can also be well reproduced by the function

$$M_{\text{HI}}(M, z) = M_0 \left(\frac{M}{M_{\text{min}}} \right)^\alpha \exp(-M_{\text{min}}/M),$$

the best-fit values of which are given in Table 6 to facilitate comparison with previous works.

3. We find that the HI density profiles inside halos exhibit a large halo-to-halo variation. HI profiles are sensitive to the physical processes that occur in and around halos, such as AGN feedback and tidal stripping. The HI profile of small halos ($M \lesssim 10^{12} h^{-1} M_\odot$) is not cuspy, but its amplitude saturates. This is expected as HI at high densities will turn into molecular hydrogen and then stars over short time periods. More massive halos exhibit holes in their centers. For galaxy groups, this is mostly due to AGN feedback, while in galaxy clusters the holes are large and generated by a combination of AGN feedback, and ram-pressure and tidal stripping. We find that the average HI density profiles are universal and can be reproduced by an expression like

$$\rho_{\text{HI}}(r) = \frac{\rho_0}{r^{\alpha_*}} \exp(-r_0/r) \quad (38)$$

or

$$\rho_{\text{HI}}(r) = \frac{\rho_0 r_s^3}{(r + 3/4r_s)(r + r_s)^2} \exp(-r_0/r), \quad (39)$$

where ρ_0 , α_* , r_0 , and r_s are free parameters. We fix the value of ρ_0 by requiring that $M_{\text{HI}}(M) = \int_0^{R_v} 4\pi r^2 \rho_{\text{HI}}(r) dr$, where R_v is the halo virial radius. The best-fit values for α_* , r_0 , and r_s can be found in Table 2.

4. We find that the HI mass in small/big halos is mostly located in its central/satellite galaxies. The fraction of the total HI mass in halos that is within the central galaxy decreases with halo mass, while the opposite trend occurs for the satellites. For halos of masses $\sim 5 \times 10^{12} h^{-1} M_\odot$, the HI mass in the central galaxy is similar to that of the satellites, almost independent of redshift. The HI mass fraction in the central galaxy of clusters is negligible at $z = 0$. At high redshift, $z \geq 2$, the fraction of the halo HI mass in satellites is roughly 20% for small halos $M \in [10^{10} - 10^{11}] h^{-1} M_\odot$.
5. We find that the pdf of the HI density field is quite different from that of the matter field. In general, the HI pdf is broader, indicating that the HI is more clustered than matter. The amplitude of the pdf for low overdensities is higher for HI than for matter, indicating that HI voids are emptier than matter voids. At high redshift, the HI and matter density pdf can be well reproduced by a log-normal, while at low redshift, the log-normal is not a good description of our results.
6. We find that the HI column density distribution function is nearly constant across redshifts, in agreement with previous studies and with observations. In the redshift range $z \in [2, 4]$, we find that the DLA cross-section depends on both halo mass and HI column density, and its mean value can be well reproduced by

$$\sigma_{\text{DLAs}}(M|N_{\text{HI}}, z) = AM^\alpha (1 - e^{-(M/M_0)^\beta}), \quad (40)$$

where $\alpha = 0.82$, $\beta = 0.85 \log_{10}(N_{\text{HI}}/\text{cm}^{-2}) - 16.35$, $A \cdot M_0 = 0.0141 h^{-2} \text{kpc} M_\odot$, and the best-fit values of M_0 are given in Table 3. We argued that the small dependence of the above relation on column density implies that the bias of different absorbers will be very similar. We estimate the DLA bias using two methods and find agreement with observations in both.

7. We find that for small halos, $M \lesssim 10^{12} h^{-1} M_\odot$, the bulk velocities of HI inside halos trace very well, in modulus and direction, the peculiar velocity of the halos they reside in. On the other hand, for bigger halos, we observe differences, in modulus and direction, between the HI and halo peculiar velocities. This happens because while for small halos most of the HI are in the central galaxy, for larger halos a significant HI mass is in satellites, whose peculiar velocities do not trace that of the halo.
8. We find that the velocity dispersion of HI inside halos can be well reproduced by a simple power law,

$$\sigma(M) = \sigma_{10} \left(\frac{M}{10^{10} h^{-1} M_\odot} \right)^\alpha, \quad (41)$$

where σ_{10} and α are free parameters whose best-fit values are given in Table 4. While at $z = 0$ the mean velocity dispersions of CDM and HI are similar (for halos above $\simeq 5 \times 10^{10} h^{-1} M_\odot$), at higher redshifts they diverge for small halos, with HI having a lower amplitude than CDM. The mass where they diverge increases with redshift, but is typically around $10^{12} h^{-1} M_\odot$. In general, for fixed mass and redshift, the variance in the velocity dispersion of HI is larger than that of CDM, reflecting the larger variation in HI profiles than CDM profiles inside halos.

9. We find that the values of the HI bias on the largest scales we can probe is equal to 0.84, 1.49, 2.03, 2.56, 2.82, and 3.18 at redshifts 0, 1, 2, 3, 4, and 5, respectively. While the HI bias is relatively flat down to $k \simeq 1 h \text{Mpc}^{-1}$ at $z = 1$, it is already nonlinear at $k \simeq 0.3 h \text{Mpc}^{-1}$ at $z \geq 3$. Our results suggest that the HI bias becomes more nonlinear with redshift. This is expected as the value of the linear bias increases with redshift. We have shown that the perturbative approaches based on LPT are able to reproduce the clustering measurement up to $k = 1 h/\text{Mpc}^{-1}$, therefore making possible, at least in principle, to extract cosmological information from such small scales.
10. We identify a new secondary halo bias. Halos of the same mass are clustered differently depending on their HI mass. At low redshift, HI-poor halos are more clustered than HI-rich halos. However, at high redshift, the situation is reversed, and HI rich halos cluster more strongly than HI-poor halos. We believe that this is mainly driven by environment. At low redshift, small halos may lose their gas due to stripping by a larger neighboring halo, so HI-poor halos will be more clustered than field HI-rich halos. On the other hand, at high redshift, gas stripping is likely less effective, so HI-rich halos will be found around larger halos, and therefore, their clustering will be higher.
11. We quantify the amplitude of the HI shot noise to be 104, 124, 65, 39, 14, and 7 ($h^{-1} \text{Mpc}$)³ at redshifts 0, 1, 2, 3, 4, and 5, respectively. These low levels imply that BAO measurements through 21 cm intensity mapping are hardly affected by shot noise. Furthermore, the very low shot-noise levels at high redshift suggest that a large amount of cosmological information can be extracted from the clustering of HI on small scales.

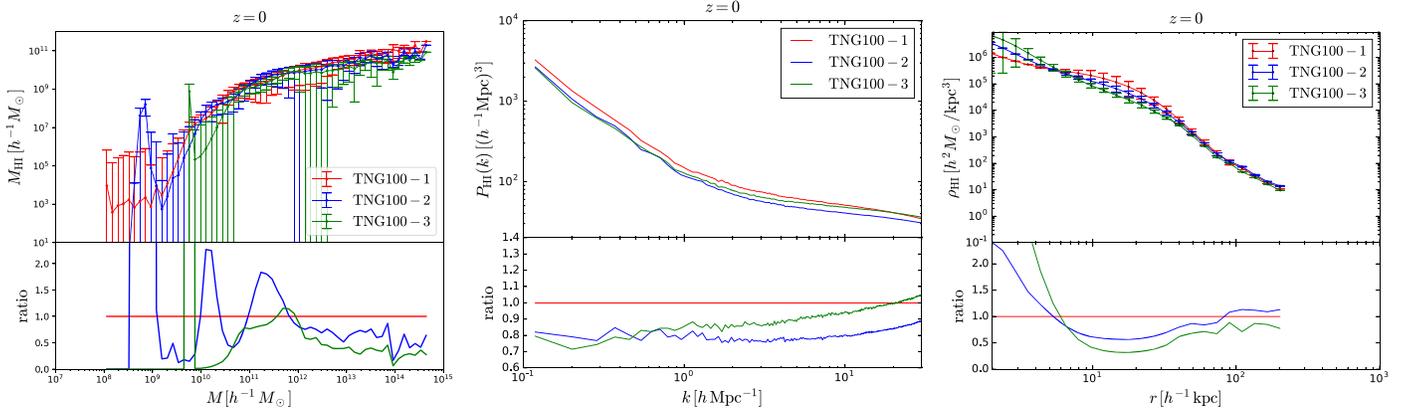


Figure 26. Impact of resolution on the halo HI mass function (left), HI power spectrum (middle), and HI density profile (right) at $z = 0$. The red, blue, and green lines show the results for TNG100-1, TNG100-2 and TNG100-3, respectively. For the halo HI mass function and the HI density profile, we show the mean values and the scatter, while for the HI power spectrum, we only show the mean. The bottom panels show the ratio between the results and the outcome from TNG100-1. It can be seen that none of these quantities are converged against resolution.

12. We find that the relation between ρ_m and ρ_{HI} cannot be explained with linear theory for smoothing scales $\leq 5 h^{-1} \text{Mpc}$ at any redshift. The scatter in that relation decreases with redshift, and much larger HI overdensities can be found for the same matter overdensities.
13. We find that the Kaiser factor alone cannot explain the clustering of HI in redshift space at low redshift, as expected, given the small volume of our simulations. But, at high redshift, the ratio between the monopoles in redshift and real space can be explained with linear theory down to 0.3, 0.5, and $1 h \text{Mpc}^{-1}$ at redshifts 3, 4, and 5, respectively. This is rather surprising, taking into account that the HI bias becomes nonlinear already at $k = 0.3 h \text{Mpc}^{-1}$ at those redshifts.
14. We find that the two-dimensional HI power spectrum in redshift space exhibits large differences with respect to the matter field. Those differences arise mainly because the amplitude of the Fingers of God is higher for HI than for matter. This can be understood by taking into account that HI resides only in relatively massive halos. While the amplitude of the matter power spectrum on small scales is dominated by small halos with low velocity dispersion, only HI halos above $\simeq M_{\text{min}}$, i.e., with larger velocity dispersion, can contribute. We find that standard phenomenological models to describe the clustering in 2D in redshift space are not adequate for reproducing our results.
15. We show that accurate 21 cm maps can be created from N -body simulations, rather than full hydrodynamic simulations, by using the ingredients studied in our work. In real space and without modeling the one-halo term, the agreement in the shape of the 21 cm power spectrum from N -body and IllustrisTNG is around 5% down to $1 h \text{Mpc}^{-1}$ at all redshifts. In redshift space, however, the lack of the one-halo term, i.e., the HI Fingers of God, induces much larger errors in the 21 cm power spectrum from N -body versus hydrodynamic simulations at low redshift, e.g., 45% at $z = 1$. Modeling the one-halo term is thus crucial for creating mock 21 cm maps.

We emphasize that our results are not converged against resolution (see Appendix A). This should, however, not be seen

as a limitation of our claims, as we present results for TNG100, i.e., at the resolution to which the model parameters have been tuned to reproduce a set of galaxy properties.

The HI properties investigated in this work will help to improve our knowledge of the way neutral hydrogen is distributed across the universe. The different quantities we have studied can be used as input to analytic approaches like HI halo models or to create very accurate mock 21 cm maps.

The Python/Cython scripts written to carry out the analysis performed in our work can be found in https://github.com/franciscovillaescusa/Pylians/tree/master/HI_Illustris. Our scripts made use of the PYLIANS Python routines, publicly available at <https://github.com/franciscovillaescusa/Pylians>.

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Appendix A Resolution Tests

In this section, we study whether our results are converged or are at least converging against changes in particle mass and spatial resolution. In Figure 2, we found that the values of $\Omega_{\text{HI}}(z)$ for TNG100 and TNG300 are in agreement to better than 10% below $z = 1$ and to better than 25% below $z \sim 3$, but can disagree more substantially at higher redshifts. We interpreted that result considering the fact that TNG300 cannot resolve halos that host HI as small as those that TNG100 resolves. Besides, we also stated that for well-resolved halos, the total HI mass inside them is resolution-dependent.

We now explicitly show these results by comparing the $M_{\text{HI}}(M, z)$ function from TNG100-1, TNG100-2, and TNG100-3 in the left panel of Figure 26. TNG100-1 corresponds to what we have called TNG100 in this work, while TNG100-2 and TNG100-3 only differs from TNG100-1 in mass resolution: TNG100-1/-2/-3 follow initially $1820^3/910^3/455^3$ CDM particles and $1820^3/910^3/455^3$ gas cells.

As can be seen, for halo masses above $\sim 10^{12} h^{-1} M_{\odot}$, our results (dis)agree on average by up to a factor of 1.6–1.7 (1.3–1.4) within a factor of 64 (8) in particle mass resolution. At the low-mass end, the results of the different simulations can (dis)agree by up to factors of 3 or more. This is not surprising: while, e.g., halos of $10^9 h^{-1} M_{\odot}$ are relatively better resolved for TNG100-1, they only host a few hundred resolution elements in TNG100-2, and they are below the mass resolution for TNG100-3. On the other hand, at the high-mass end, we find that the average HI mass still depends on resolution, with larger HI masses at progressively better resolutions. This is interesting and possibly related to the HI/H₂ postprocessing, as in fact the total gas fraction within the virial radius of halos is consistent to better than 10%–20% across the TNG100-1, TNG100-2, and TNG100-3 resolution levels (see Figure A2 of Pillepich et al. 2018a).

A lack of convergence can be seen in the HI power spectrum, the results for which we show in the middle panel of Figure 26. The three different resolution runs are consistent with one another to better than 30% across spatial scales, but within this agreement (or discrepancy, according to the point of view and needs of the reader), the amplitude of the power spectrum at different spatial separations does not necessarily change monotonically at increasingly better resolutions.

The right panel of Figure 26 shows the results for the HI density profile within halos of masses $M \in [1-2] \times 10^{12} h^{-1} M_{\odot}$. Within the studied resolution range, the TNG results (dis)agree within a factor of 1.4–1.6 outside radii of 10 kpc, but can disagree more substantially in the innermost regions of the halos. In fact, at radii near the virial radius, results are almost converged to better than 20%, suggesting that differences among resolutions are not due to small differences in the halo masses or radii.

All previous results are at $z = 0$. We find similar results at higher redshifts for the considered quantities above. We have repeated the above exercise with a simulation with $25 h^{-1} \text{Mpc}$ and 2×1024^3 CDM particles and gas cells, i.e., at a higher mass resolution than TNG100-1, reaching similar conclusions.

We emphasize that our HI mass results, although they are not fully converged at the TNG100 or TNG300 resolution or are not converging against resolution, are still valuable, as they come from a physical model that is consistent (to different levels of agreement) with a large number of observed galaxy properties and statistics.³⁰

Appendix B

Time Evolution of HI in the Intergalactic Medium

In Section 4, we found that while at $z \leq 2$ most of the universe HI mass is inside halos, at higher redshift, an increasing fraction of it is located outside halos. In order to visualize this effect, we show in Figure 27 the spatial distribution of HI in a slice of $5 h^{-1} \text{Mpc}$ width across

$10 \times 10 (h^{-1} \text{Mpc})^2$. We show in that figure the HI column density in comoving units to facilitate the comparison across redshifts. We note that our color palette may produce the incorrect impression that at $z = 5$ there is much more HI than at $z = 0$. We have explicitly checked that the sum of all column densities across all pixels in our figures gives a similar value across redshifts, indicating that Ω_{HI} is very similar in all panels.

It can be seen that at low redshift, most of the HI mass is inside galaxies, while the hydrogen in the filaments is highly ionized. At higher redshifts, on the other hand, the gas in the intergalactic medium becomes denser and the filaments contain a larger amount of HI. The lower amplitude of the UV background at those redshifts facilitates gas self-shielding. Given these effects, it is thus natural that the fraction of HI outside dark matter halos increases with redshift.

Appendix C

Origin of the Cutoff in the Halo HI Mass Function

We saw in Section 5 that the halo HI mass function exhibits a cutoff at low masses. In this appendix, we shed light on the physical origin of that feature.

The lack of HI gas in small halos may be due to (1) a deficit in the abundance of gas in those halos, (2) gas being present but highly ionized, or a mixture of (1) and (2). We quantify the gas content of dark matter halos in TNG100 by computing their gas fraction, i.e., the ratio between the gas mass to the total mass. In the left panel of Figure 28, we show the average gas fraction as a function of halo mass at different redshifts. In this plot, we show results only for halos whose masses are above the mass of 50 CDM particles.

We find that the gas fraction of the smallest halos shown at high redshifts is around ~ 0.12 . As we go to higher halo masses, some stars form, and supernova feedback expels the gas of these halos. In even more massive halos, the gravitational potential is deeper, and hence the mass-loading factors of galactic winds in the TNG model are lower, rendering it more difficult for supernova feedback to eject gas from halos. This explains the dip we observe around $5 \times 10^9 h^{-1} M_{\odot}$ halos at high redshift. In halos with masses above $\sim 3 \times 10^{11} h^{-1} M_{\odot}$, AGN feedback becomes effective at expelling their gas, explaining the peak at around that mass. Finally, as we go to even higher mass halos, a smaller fraction of the gas can be expelled by AGN feedback since the gravitational potential becomes deeper, explaining the dip around $3 \times 10^{12} h^{-1} M_{\odot}$ halos.

It is interesting to note that the gas fraction of small halos decreases quickly with redshift. We will see below that this is caused by the UV background. At low redshift, the gas fraction of small halos is small, so it is reasonable to expect that very little HI is found in those halos. However, as we go to higher redshifts, the gas fraction of halos at the hard cutoff mass M_{hard} (defined such that halos with masses below M_{hard} host only 2% of all HI that are in halos; see Equation (14)) is rather large. We show this with colored stars in that figure. Thus, the cutoff in the halo HI mass function cannot be explained, at high redshift, by the lack of gas in halos. A better explanation is that the gas in these halos is highly ionized.

The average HI mass to gas mass ratio is shown in the right panel of Figure 28. We find that halos at the hard cutoff mass M_{hard} exhibit similarly low HI to gas mass fractions across

³⁰ See <http://www.tng-project.org> for a list of results.

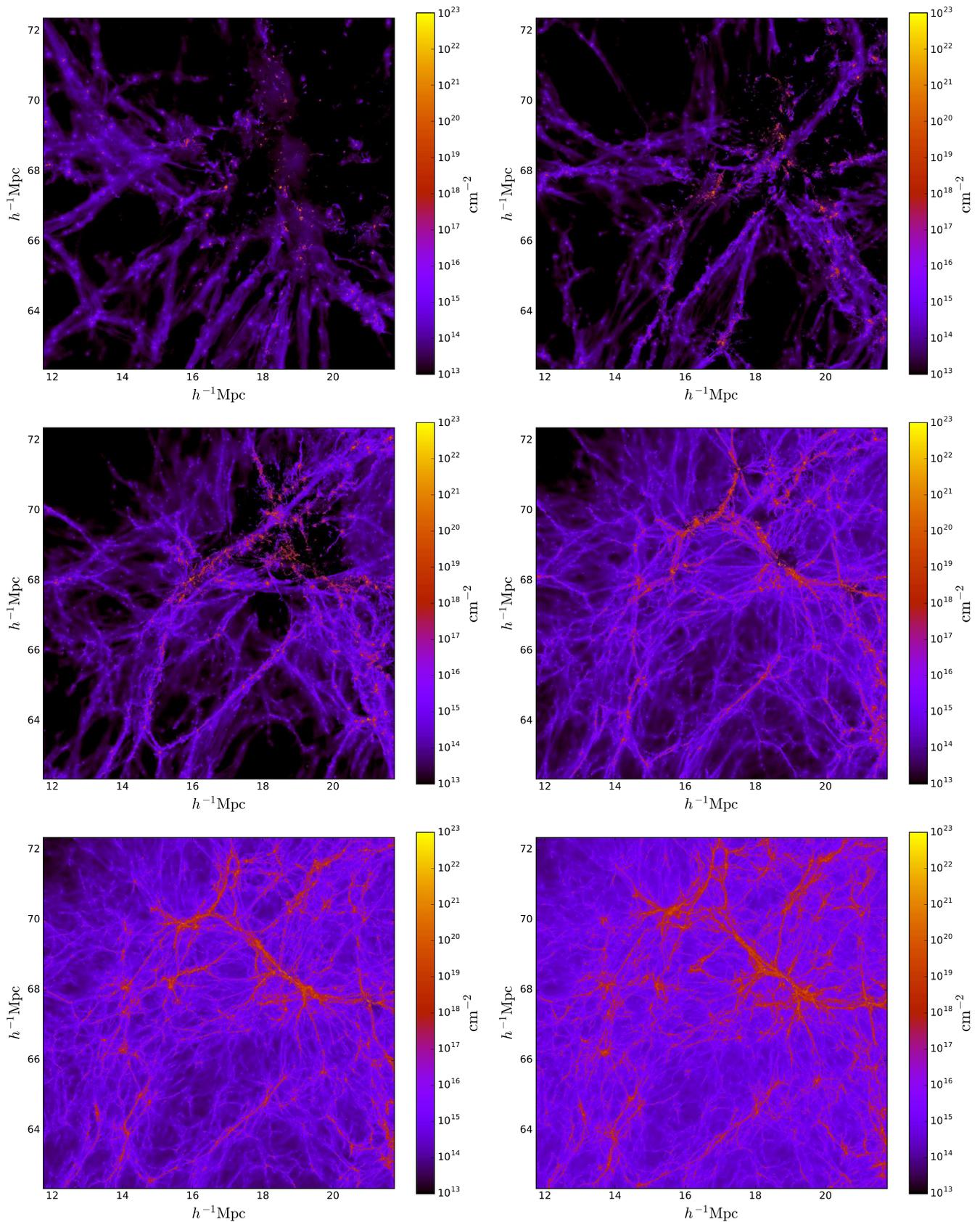


Figure 27. Spatial distribution of H I in a slice of $10 \times 10 \times 5 (h^{-1} \text{Mpc})^3$ at redshifts 0 (top left), 1 (top right), 2 (middle left), 3 (middle right), 4 (bottom left), and 5 (bottom right). The color indicates the H I column density in comoving cm^{-2} units to facilitate the comparison across redshifts. The region shown is the same as that in Figure 1 (top and middle panels). At higher gas densities, the column densities of H I are higher in the intergalactic medium. It can be seen that some filaments host a significant H I mass at high redshift, while at low redshift the H I is mostly locked inside galaxies. This explains why the fraction of H I outside halos increases with redshift.

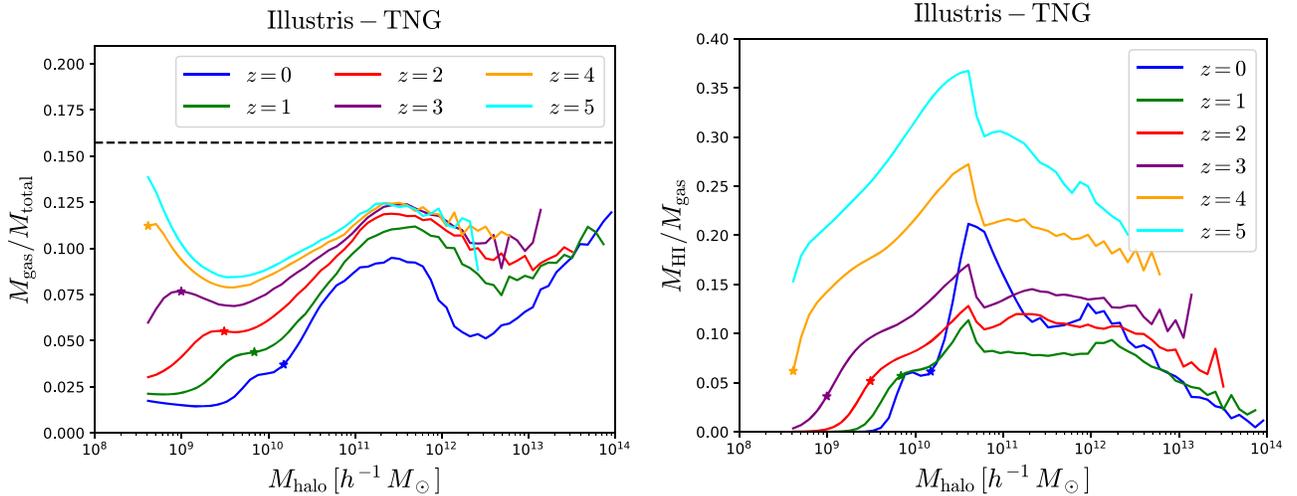


Figure 28. Average gas fraction (left) and average HI mass to gas mass ratio (right) in halos as a function of their mass at redshifts 0 (blue), 1 (green), 2 (red), 3 (purple), 4 (yellow), and 5 (cyan) in IllustrisTNG. We show results only for halos with masses larger than 50 CDM particles. The stars indicate the hard cutoff mass (i.e., halos below that mass contain only 2% of all HI inside halos). The gas content of small halos declines with time. The features we observe in the plot are due to (1) supernova feedback (removes gas of small halos), (2) AGN feedback (removes gas from large halos), and (3) the UV background (reduces the gas content of small halos). The dashed black line shows the cosmological baryon fraction, Ω_b/Ω_m . It can be seen that halos at the hard cutoff mass have a very different gas fraction, while almost all of them have the same HI to gas mass ratio. Thus, the lack of HI gas in small halos is more related to gas being ionized than a lack of gas.

redshifts: $\simeq 5\%$. Thus, while there is a significant amount of gas in these halos at high redshift, HI formation is impeded, likely due to the gas being at high temperature and diffuse. The low HI to gas mass ratio shows up at all redshifts for low-mass halos. However, this is the case particularly at low redshift, where the HI to gas mass fraction of small halos is practically zero, showing how difficult it is to form HI in these halos. We speculate that this is related to the fact that for fixed halo mass, the density of gas and CDM increases with redshift. Thus, for example, while for halos with masses $\simeq 10^9 h^{-1} M_\odot$ the gas fraction increases by only $\simeq 60\%$ from $z = 3$ to $z = 5$, the HI to gas mass ratio changes by more than 400%, showing how denser gas enables the formation of HI.

We thus conclude that the reason why there is almost no HI in small halos is because the gas in these halos is highly ionized, presumably because its low density and high temperature prevent HI formation.

It is interesting to understand why the gas fraction of small halos decreases with redshift. We argue that this effect is due to the UV background. In order to demonstrate our claim, we have run three hydrodynamic simulations with radiative cooling and star formation but without feedback (neither galactic winds nor AGN). In two of them, no heating by the UV background is included, one with 2×256^3 CDM+baryon resolution elements and another with 2×512^3 CDM+baryon resolution elements. In the third one, we have heating by the UV background with 2×512^3 CDM+baryon resolution elements. In all cases, the simulation box is $25 h^{-1}$ Mpc across.

We have computed the average baryon fraction, i.e., the mass in gas and stars over the total mass, in these simulations and show the results in Figure 29. The top panel shows the baryon fraction for these simulations and TNG100 at $z = 0$. We find that in simulations without feedback, the gas content of small halos exhibits a cutoff that occurs at higher masses when the UVB is present.

The bottom panels of Figure 29 show the time evolution of the average baryon fraction as a function of halo mass. It can be seen that in both types of simulations, with and without UV background, the gas fraction of small halos decreases with redshift. We speculate that in the case of no UV background, many small halos lie in the vicinity of massive halos, whose presence can strip the gas from these small halos, and further, that the same mechanism may explain the dependence of halo clustering on HI mass we described in Section 14. Although not shown here, we find that our results at $z > 5$ for the case with no UV background are in agreement with those by Qin et al. (2017). For the case with UV background and no feedback, our results are also in agreement with Qin et al. (2017) for redshifts below the time where the UV background is turned on.

The effect of the UV background on the baryon fraction of small halos is more pronounced, as can be seen in the bottom-right panel of Figure 29. We believe that the reason for this behavior is that the hot intergalactic gas cannot cluster in small halos since their gravitational potential is not deep enough (Okamoto et al. 2008; Bose et al. 2018).

We thus conclude that at low redshift, small halos have a low gas fraction. There are several mechanisms that can remove the gas from such halos, such as tidal stripping by neighbors, the heating of the intergalactic medium by the UV background, and supernova feedback. Our results suggest the most effective one for the lowest masses is the presence of the UV background. The little gas inside those halos is highly ionized, so no HI is found within them.

Appendix D HI Content in FoF versus FoF-SO Halos

We found in Section 4 that the HI mass inside FoF and FoF-SO halos is quite different. Here, we determine the reason for this difference.

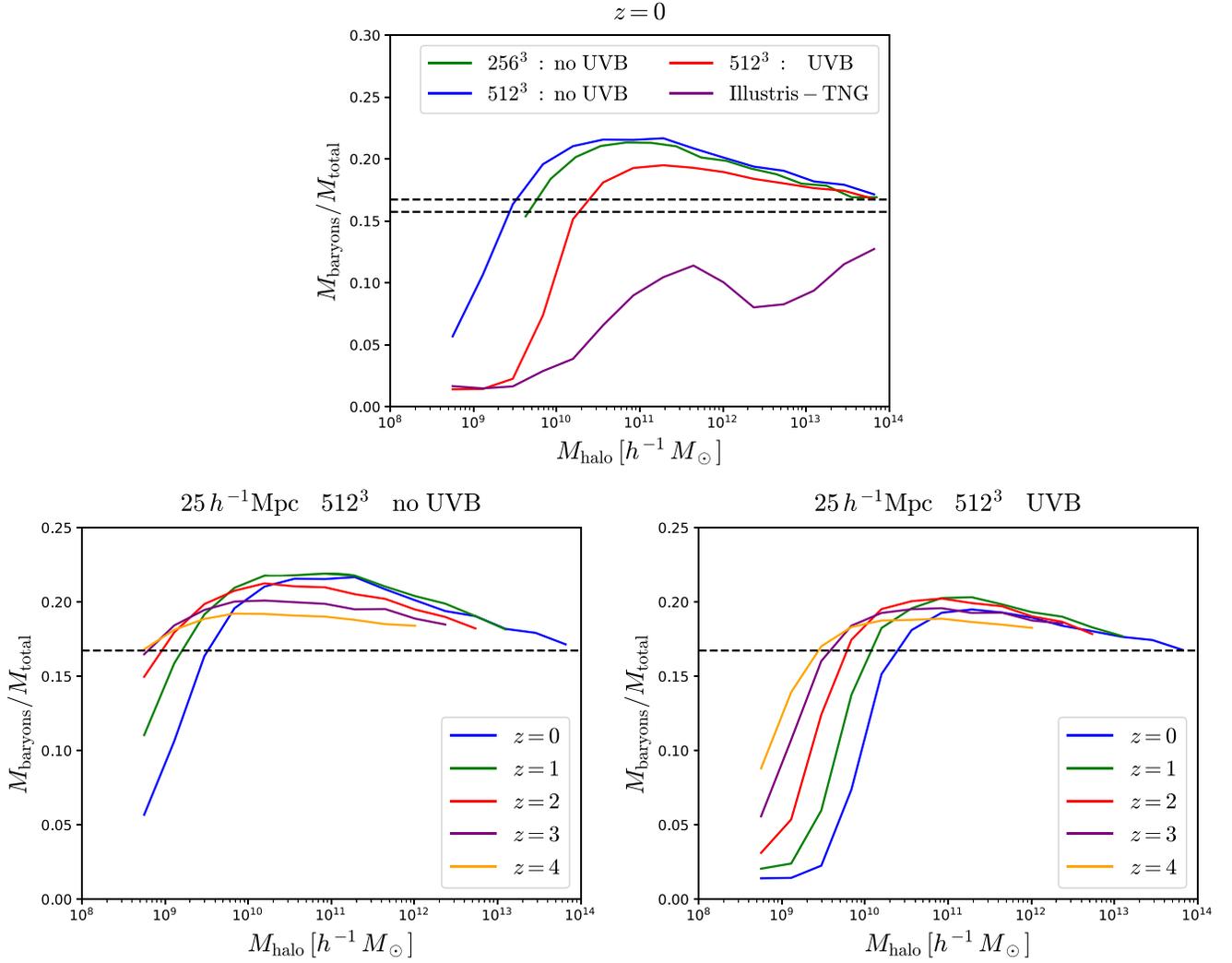


Figure 29. We show the average baryon fraction, i.e., the fraction of the mass in baryons (gas+stars) over the total mass in halos, as a function of halo mass. In the upper panel, we show results at $z = 0$ for three different simulations: (1) a simulation with 2×256^3 resolution elements and no UV background (green), (2) a simulation with 2×512^3 resolution elements and no UV background (blue), and (3) a simulation with 2×512^3 resolution elements and UV background (red). All simulations are in a box of $25 h^{-1}$ Mpc size, and no feedback is incorporated in any of them. The bottom panels display the results for the simulations with 2×512^3 with (right) and without (left) at different redshifts. The dashed black line indicates the cosmic baryon fraction, Ω_b/Ω_m . Since the values of the cosmological parameters are slightly different between IllustrisTNG and the other simulations, we show two horizontal lines in the upper panel. It can be seen that the presence of the UV background removes the baryonic, and therefore also the H I, content of small halos. It is interesting that even if the UV background is not present, very small halos exhibit a deficit in their baryon fraction.

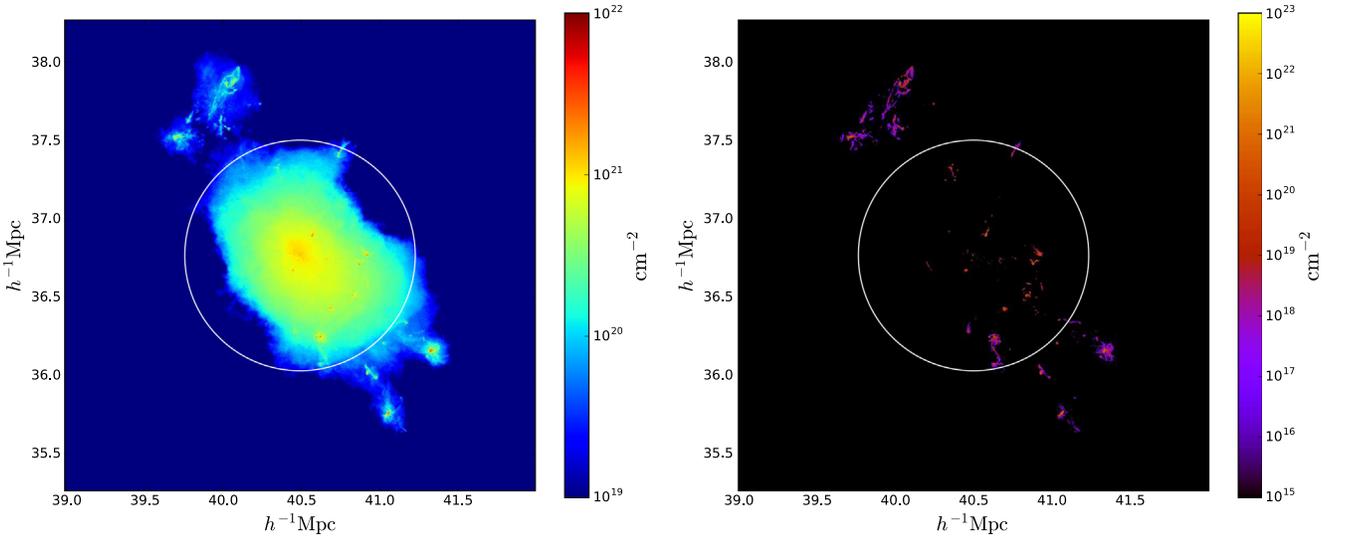


Figure 30. Comparison between the gas and H I content in FoF vs. FoF-SO halos. The images show the column density of gas (left) and H I (right) from the cells belonging to an FoF halo of mass $5 \times 10^{13} h^{-1} M_{\odot}$ at $z = 0$. The white circle shows the position of the halo center and its SO radius. While the gas content in the FoF and SO halos is similar, the FoF halo has almost a factor of 2 more H I than the SO halo.

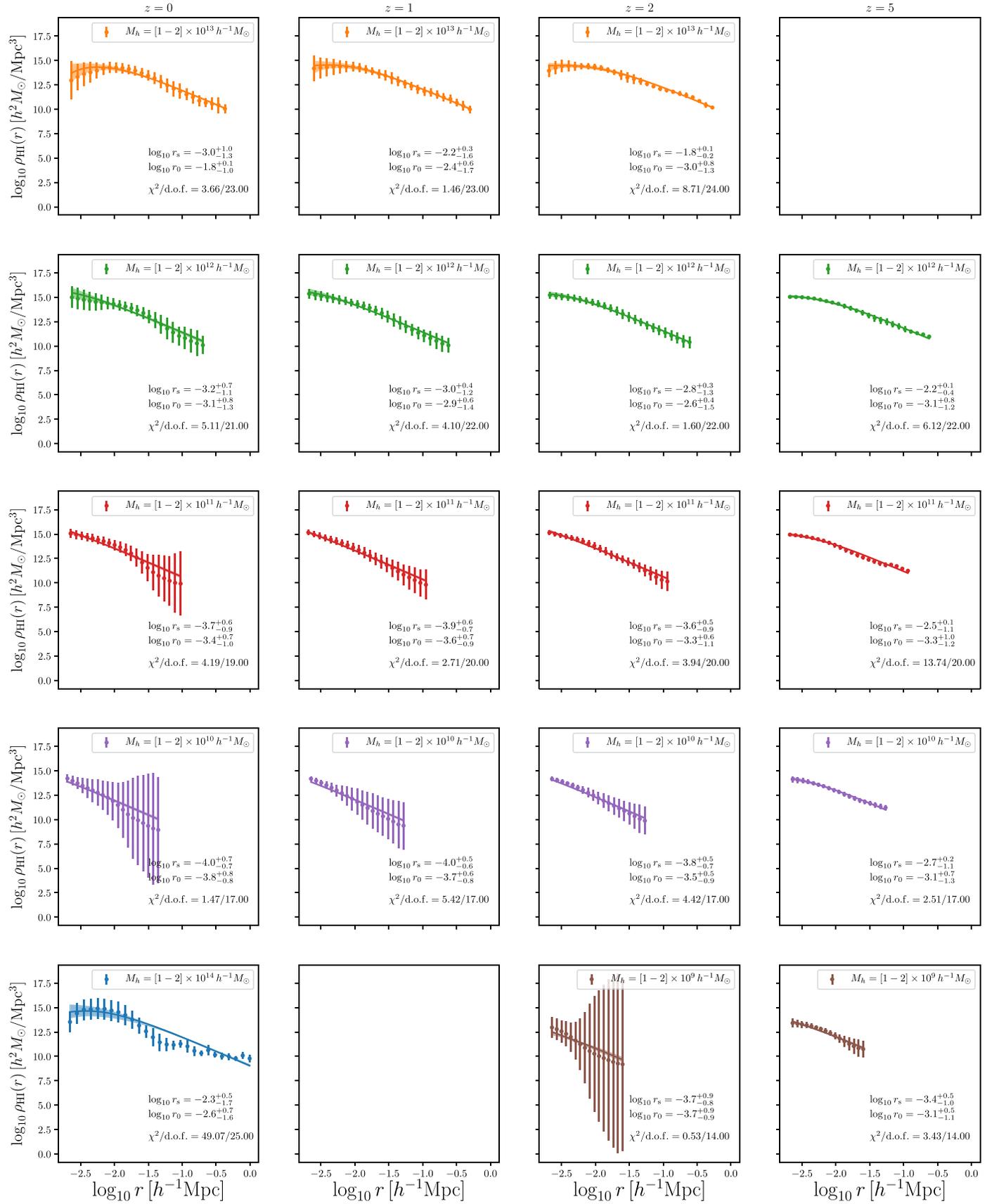


Figure 31. Each panel shows the mean and standard deviation of the H I profiles for halos in the mass range indicated in the upper-left part. We fit the results using the form $\rho_{\text{HI}}(r) = \exp(-r_0/r) \rho_0 r_s^3 / [(r + 3/4 r_s)(r + r_s)^2]$, where ρ_0 , r_s , and r_0 are free parameters. The best fit is shown with a solid line. The dashed region represents the error on the fit. The value of ρ_0 is fixed by requiring that $M_{\text{HI}} = 4\pi \int_0^{R_v} r^2 \rho_{\text{HI}}(r) dr$, where R_v is the halo virial radius. Each panels show the best-fit values of r_0 and r_s , and the value of χ^2 .

We have computed the total mass inside FoF and FoF-SO halos, and we find that the former host $\sim 9\%$ more mass than the latter at $z = 0$. This difference is almost equal to the deficit in HI mass we find between FoF-SO and FoF halos at that redshift (see Figure 3). Similar results hold at higher redshift, where the differences in total mass and HI are slightly larger ($\approx 25\%$ at $z = 5$). This indicates that the deficit in HI mass we find in FoF-SO halos with respect to FoF is simply due to the fact that the latter host a larger total mass, and therefore more HI.

We note, however, that there are some situations where the difference in HI mass can be much larger than the difference in total mass. We illustrate one of these situations in Figure 30. We have selected the gas cells belonging to an FoF halo of mass $M = 5 \times 10^{13} h^{-1} M_{\odot}$ at redshift $z = 0$. The total mass inside the FoF and FoF-SO halos are nearly the same, while the HI masses vary by a factor of 2. In Figure 30, we plot the column density of gas and HI from the gas cells belonging to that halo. In the same plot, we mark the radius of the corresponding FoF-SO halo with a white line. It can be seen that while most of the gas in the FoF halo is inside the virial radius of the SO halo, the situation is quite different for HI. The HI mass outside the SO radius is almost equal to the one inside. The reason is that the FoF algorithm links the external galaxies to the main halo, and these galaxies are rich in HI. We have found that this situation is usual for the most massive halos at each redshift.

Appendix E Halo HI Mass Function

In Section 5, we found that the halo HI mass function, $M_{\text{HI}}(M, z)$, from IllustrisTNG can be well reproduced by a fitting formula like $M_0 x^{\alpha} \exp(-1/x^{0.35})$, where $x = M/M_{\text{min}}$. In the literature, however, an expression of the type $M_0 x^{\alpha} \exp(-1/x)$ has been widely used (e.g., Bagla et al. 2010; Castorina & Villaescusa-Navarro 2017; Obuljen et al. 2017; Padmanabhan et al. 2017; Villaescusa-Navarro et al. 2017; Pénin et al. 2018). We have fit our results to that function, and while the reduced χ^2 is larger than that with our fiducial function, it is still a good fit to the underlying data. We thus provide in Table 6 the best-fit values of the parameters α , M_0 , and M_{min} of the latter expression in order to help in the comparison with previous works. We note that the value of M_{hard} , i.e., the hard cutoff mass (see Section 5), is not affected by using a different parameterization for the halo HI mass function. Thus, the values we quote in Table 1 are valid also here.

Appendix F Fit to HI Profiles

The points with error bars in Figure 31 show the mean HI density profiles within halos of different halo masses at different redshifts (they are the same as the blue lines in Figure 6). The solid lines represent the best fit obtained when we fit those results with a HI density profile as

$$\rho_{\text{HI}}(r) = \frac{\rho_0 r_s^3}{(r + 3/4 r_s)(r + r_s)^2} \exp(-r_0/r). \quad (42)$$

In each panel of the plot, we show the best-fit values of r_s and r_0 , and the value of the reduced χ^2 . The value of ρ_0 is fixed by requiring that $M_{\text{HI}} = 4\pi \int_0^{R_v} r^2 \rho_{\text{HI}}(r) dr$, where R_v is the halo virial radius.

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