

Gravity Compensation of a 6-UPS Parallel Kinematics Machine Tool Through Elastically Balanced Constant-Force Generators

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Gravity compensation is a viable strategy to improve the performance of manipulators, particularly in terms of power consumption. This work studies the static balancing of a prototypal 5-axis parallel kinematics machine tool with UPS-legs. Exact gravity compensation is achieved by turning the legs into constant-force generators, through tension springs. A numerical multibody model is implemented and simulated within a commercial software environment (MSC Adams™) to assess the effectiveness of the proposed balancing strategy.

Keywords: static balancing, gravity compensation, elastic compensation, constant-force generator, Parallel Kinematics Machine, 5-axis machine tool.

1. INTRODUCTION

A mechanism is said to be statically balanced (or gravity compensated) if its total potential energy is invariant for any admissible pose. In such an instance, no motor actions are required to sustain the weight of its moving parts. Gravity compensation through passive (i.e. not actuated) devices is a common practice for heavy-duty serial manipulators [1-4], since it brings essential benefits, namely lower motor loads, enhanced energy efficiency, reduced vibrational levels [5], quality precision in manufacturing [6, 7], improved safety and productivity [8]. It is proven convenient for closed-loop mechanisms as well, provided that gravity loads are comparable with inertial actions [9-11]. Hence, static balancing is suitable for applications featuring parallel robots with a heavy moving platform, long working periods in rest position and operations at low/moderate dynamics, e.g. robotically assisted surgery and machining tasks [12,13]. In particular, the implementation of a gravity compensation strategy is expected to significantly enhance the operation of parallel kinematics machine tools (PKMs), which typically meet all the mentioned specifications [13-16].

Numerous approaches have been developed for the gravity compensation of both serial and parallel robots [17-26]. The study deals with static balancing of parallel robots, achieved by making the legs operate as constant-force generators (CFGs), a concept developed in [9, 22, 27]. By following this strategy, a set of leg-exerted constant forces that realizes the neutral equilibrium of the moving platform is firstly determined. Then, each leg is made to generate the required force by installing balancing components whose parameters are determined

by imposing a condition of constant potential energy.

In particular, this work presents the gravity compensation of a 5-axis machine tool with six UPS-legs (i.e. featuring a universal-prismatic-spherical joint sequence, underline denoting the actuated one). A solution for turning UPS-legs into CFGs through pure elastic compensation has been recently proposed [28]. This new method is expected to provide better working performance with respect to known solutions requiring sliding counterweights [9], which are difficult to be implemented in practice and may worsen the robot dynamic operation. Indeed, balancing counterweights considerably increase the robot mass, hence possibly inducing higher motor loads [24, 29]. Moreover they may trigger vibration phenomena [30-33], thus being potentially detrimental for PKMs in terms of machining tolerances and cutting tool life [34, 35].

A feasible solution for achieving exact gravity compensation (i.e. without residual unbalanced loads) is analytically derived. Its effectiveness is assessed through numerical simulations in a multibody environment.

The paper is organized as follows. Section 2 describes the studied PKM. Section 3 presents the balancing procedure and the simulation results. Section 4 draws some conclusions.

2. DESCRIPTION OF THE PARALLEL KINEMATICS MACHINE TOOL

The machine tool architecture considered in this work characterizes a prototypal 5-axis PKM, namely the Mikromat 6X [36]. Schematics of the PKM are represented in Figure 1. A fixed coordinate system, $\Sigma = XYZ$, is defined as shown in Figure 1. Its origin, O , coincides with the center of mass (COM) of the moving platform, G_p (lying along the spindle rotational axis), at the PKM reference position. The Z-axis is vertical and directed like the gravity vector, \mathbf{g} . A coordinate system attached to the platform, $\Sigma' = X'Y'Z'$, centered in O' and coincident with Σ at the PKM reference position is also set.

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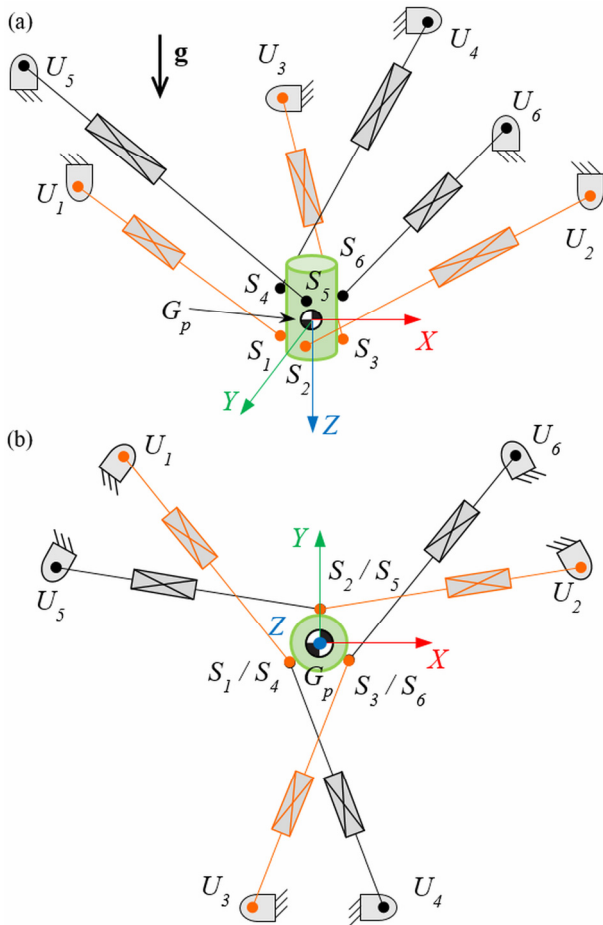


Figure 1. Schematics of the studied PKM: (a) isometric and (b) bottom view.

The PKM features six UPS legs arranged in a 6-6 configuration. Its moving platform includes the electrospindle, the tool holder and the six spherical connections. The centers of the S-joints, referred to as points S_i ($i=1, \dots, 6$), lie on two distinct parallel planes, which are orthogonal to the Z-axis. The centers of the U-joints, referred to as points U_i ($i=1, \dots, 6$), also form two distinct parallel planes orthogonal to Z.

The main dimensions assumed in this work for the studied PKM are reported in Table 1. A cubic workspace with an edge of 630 mm is considered.

Table 1. Main geometry parameters of the PKM.

Point	Coordinates in Σ [mm]		
	X	Y	Z
S_1	-200.00	-115.47	240.00
S_2	0.00	230.94	240.00
S_3	200.00	-115.47	240.00
S_4	-200.00	-115.47	-60.00
S_5	0.00	230.94	-60.00
S_6	200.00	-115.47	-60.00
U_1	-1320.00	1270.17	-890.00
U_2	1760.00	508.07	-890.00
U_3	-440.00	-1778.24	-890.00
U_4	440.00	-1778.24	-1460.00
U_5	-1760.00	508.07	-1460.00
U_6	1320.00	1270.17	-1460.00

3. GRAVITY COMPENSATION OF THE PKM

In [9, 22] the analytical conditions for the static balancing of 6-DOF spatial parallel mechanisms by using CFGs are derived. Firstly, the approach therein developed determines a set of constant (in both magnitude and direction) actions, namely forces \mathbf{I}_n and torques $\boldsymbol{\tau}_n$ ($n=1, \dots, N$) that the N legs must exert on the moving platform of mass m_p in order to realize its neutral equilibrium. If the platform is connected to the legs by means of spherical joints (as in case of UPS-legs), only forces \mathbf{I}_n are exerted by the legs.

Then, the legs are turned into CFGs for generating the required forces, by installing proper balancing components. Hence, the problem becomes finding the neutral equilibrium of each leg subjected to its weight, the external actions provided by the balancing components and a constant force opposite to the one exerted on the platform, $\mathbf{f}_n = -\mathbf{I}_n$. The parameters characterizing the balancing components attached to each leg can be determined by imposing that the total potential energy of the leg keeps invariant.

3.1 Static balancing of the platform

A set of six constant forces \mathbf{I}_i , exerted by the i th leg in S_i ($i=1, \dots, 6$), that achieves the platform neutral equilibrium can be found by imposing the following conditions, as derived in [9]:

$$\mathbf{W}_p + \sum_{i=1}^6 \mathbf{I}_i = 0 \quad (1)$$

$$\sum_{i=1}^6 \mathbf{I}_i \mathbf{p}_i^T = 0 \quad (2)$$

where the platform weight $\mathbf{W}_p = m_p \mathbf{g}$ and the forces \mathbf{I}_i are expressed in Σ , whereas the position vectors $\mathbf{p}_i = S_i - O'$ are expressed in Σ' . Equations (1) and (2) consist in twelve scalar relations in eighteen unknowns.

For the studied system, the platform COM lies on the affine space generated by any combination of four points S_i that are not located on the same vertical plane. Hence, neutral equilibrium can be achieved by applying only the four forces corresponding to such combination of points [22]. A possible solution can be found by arbitrarily imposing that forces \mathbf{I}_2 and \mathbf{I}_3 are nought and that only the vertical components (i.e. along the Z-axis, referred to as l_{iz}) of the remaining forces are non-zero. The following linear system of equations is therefore obtained:

$$\begin{bmatrix} 1 & 1 & 1 & 1 \\ p_{1x} & p_{4x} & p_{5x} & p_{6x} \\ p_{1y} & p_{4y} & p_{5y} & p_{6y} \\ p_{1z} & p_{4z} & p_{5z} & p_{6z} \end{bmatrix} \begin{Bmatrix} l_{1z} \\ l_{4z} \\ l_{5z} \\ l_{6z} \end{Bmatrix} = \begin{Bmatrix} -m_p g \\ 0 \\ 0 \\ 0 \end{Bmatrix} \quad (3)$$

Table 2. Balancing constant forces.

Force	Magnitude [N]
l_{1z}	-156.9
l_{4z}	-104.6
l_{5z}	-261.5
l_{6z}	-261.5

For the mechanism of interest the square matrix in (3) can be always inverted to find a unique solution. By assuming a platform mass $m_p = 80$ [kg], the force values reported in Table 2 are obtained.

3.2 Static balancing of the legs

An effective solution to make a generic UPS-leg exert the required constant force (thus turning the leg into a CFG) has been presented in [28]. The method is here briefly recalled.

A schematic of the i th UPS-leg (with generic mass properties) converted in CFG is represented in Figure 2. The leg members are: $part_{i2}$ connected to the fixed base by the U-joint; the sliding member ($part_{i1}$) connected to $part_{i2}$ by the P-joint; a planar parallelogram linkage (featuring identical links of length γ_i , mass m_γ and COM in their respective median points) connected to $part_{i1}$ and $part_{i2}$ in L_{i1} and L_{i2} (which lie on a direction parallel to $U_i S_i$), respectively.

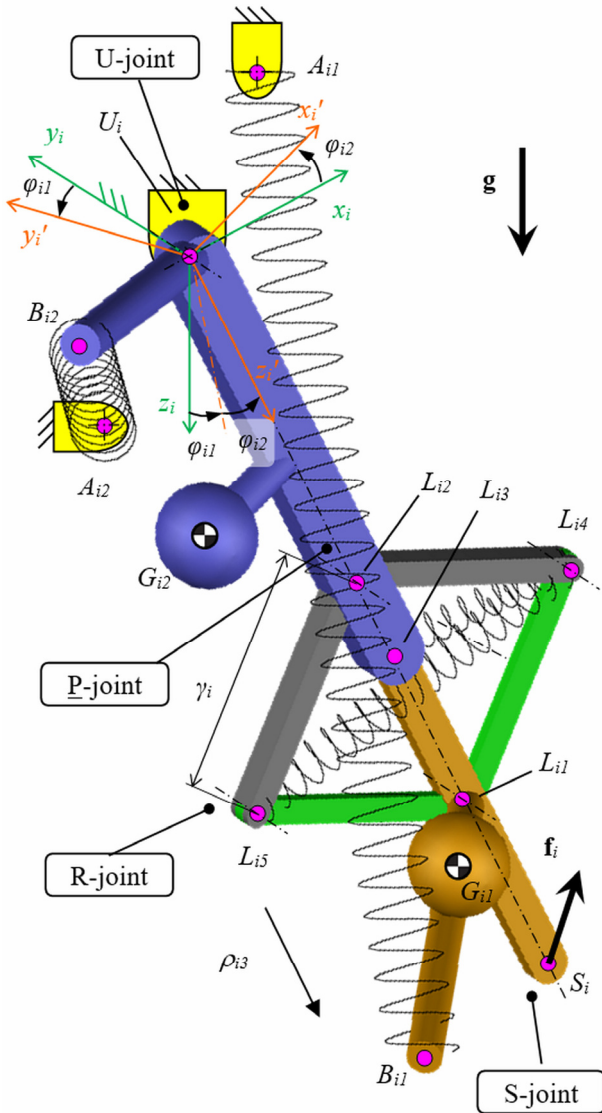


Figure 2. Schematic of the UPS-type CFG.

Two coordinate systems, $\sigma_i = x_i y_i z_i$ and $\sigma_i' = x_i' y_i' z_i'$, both centered in U_i , are defined as shown in Figure 2. σ_i is attached to the fixed base, oriented like the machine reference system Σ . σ_i' is attached to $part_{i2}$ and arranged

with z_i' directed from U_i to S_i , and y_i' (which lies along the turning axis of the U-joint) orthogonal to the $z_i' x_i'$ -plane. Euler angles φ_{i1} and φ_{i2} define the orientation of σ_i' with respect to σ_i and describe the motion of $part_{i2}$ around the U-joint: φ_{i1} is the rotation around the x_i -axis, whereas φ_{i2} is the rotation around the y_i' -axis, i.e. the new y_i -axis after rotation φ_{i1} . The sliding motion, described by the parameter ρ_{i3} , is assumed to be parallel to the line passing through U_i and S_i . The initial distance of S_i from U_i is ρ_{i0} .

Each $part_{ij}$ ($j = 1,2$), has mass m_{ij} located in G_{ij} , which also accounts for half the mass of the linkage ($2m_\gamma$) located in L_{ij} .

Vector $\mathbf{f}_i = (f_{ix}, f_{iy}, f_{iz}) = -\mathbf{I}_i$, expressed in Σ , is the force of constant magnitude and direction exerted by the platform on point S_i . A zero-free-length spring of stiffness K_{ij} ($j = 1,2$), connects the two anchor points A_{ij} and B_{ij} , which are located on the fixed base and on $part_{ij}$, respectively. A third spring (spring rate K_{i3}) is attached between the points L_{i4} and L_{i5} (which lie on a plane parallel to the linkage, on the axes of its R-joints, see Figure 2). A fourth spring (spring rate K_{i4}) connects L_{i4} and L_{i3} (coplanar with L_{i4} and lying on a direction parallel to Z). The springs are here considered as massless.

The relevant position vectors for potential energy computation are:

$$\begin{aligned}
 \mathbf{r}_{S_i} &= (0, 0, \rho_{i3} + \rho_{i0}) \\
 \mathbf{r}_{G_{i1}} &= \mathbf{r}_{S_i} + (G_{i1x}, G_{i1y}, G_{i1z}) \\
 \mathbf{r}_{G_{i2}} &= (G_{i2x}, G_{i2y}, G_{i2z}) \\
 \mathbf{r}_{A_{i1}} &= (A_{i1x}, A_{i1y}, A_{i1z}) \\
 \mathbf{r}_{A_{i2}} &= (A_{i2x}, A_{i2y}, A_{i2z}) \\
 \mathbf{r}_{B_{i1}} &= \mathbf{r}_{S_i} + (B_{i1x}, B_{i1y}, B_{i1z}) \\
 \mathbf{r}_{B_{i2}} &= (B_{i2x}, B_{i2y}, B_{i2z}) \\
 \mathbf{r}_{L_{i1}} &= (0, 0, \rho_{i3} + \rho_{i0} + L_{i1z}) \\
 \mathbf{r}_{L_{i2}} &= (0, 0, L_{i2z}) \\
 \mathbf{r}_{L_{i3}} &= (0, 0, L_{i2z} + \lambda_i)
 \end{aligned} \tag{4}$$

where vectors $\mathbf{r}_{A_{ij}}$ are expressed in σ_i , whereas all the other vectors are expressed in σ_i' .

Neutral equilibrium of the leg is achieved if and only if its total potential energy is invariant for any admissible configuration. The following thirteen conditions in nineteen scalar unknowns (namely the constants $K_{i1}, A_{i1x}, A_{i1y}, A_{i1z}, B_{i1x}, B_{i1y}, B_{i1z}, K_{i2}, A_{i2x}, A_{i2y}, A_{i2z}, B_{i2x}, B_{i2y}, B_{i2z}, K_{i3}, L_{i1z}, L_{i2z}, K_{i4}, \lambda_i$) must be verified:

$$f_{ix} + A_{i1x} K_{i1} = 0 \tag{5}$$

$$f_{iy} + A_{i1y} K_{i1} = 0 \tag{6}$$

$$f_{iz} + A_{i1z} K_{i1} + m_{i1} g = 0 \tag{7}$$

$$K_{i1} - K_{i3} = 0 \tag{8}$$

$$\begin{aligned}
 &K_{i1} (\rho_{i0} + B_{i1z}) - K_{i3} (\rho_{i0} + L_{i1z} - L_{i2z}) + \\
 &-\frac{1}{2} K_{i4} \lambda_i = 0
 \end{aligned} \tag{9}$$

$$A_{i1x}B_{i1x}K_{i1} + A_{i2x}B_{i2x}K_{i2} = 0 \quad (10)$$

$$A_{i1x}(\rho_{i0} + B_{i1z})K_{i1} + A_{i2x}B_{i2z}K_{i2} + f_{ix}\rho_{i0} = 0 \quad (11)$$

$$A_{i1y}B_{i1x}K_{i1} + A_{i2y}B_{i2x}K_{i2} = 0 \quad (12)$$

$$A_{i1y}B_{i1y}K_{i1} + A_{i2y}B_{i2y}K_{i2} = 0 \quad (13)$$

$$A_{i1y}(\rho_{i0} + B_{i1z})K_{i1} + A_{i2y}B_{i2z}K_{i2} + f_{iy}\rho_{i0} = 0 \quad (14)$$

$$A_{i1z}B_{i1x}K_{i1} + A_{i2z}B_{i2x}K_{i2} + g(m_{i1}G_{i1x} + m_{i2}G_{i2x}) = 0 \quad (15)$$

$$A_{i1z}B_{i1y}K_{i1} + A_{i2z}B_{i2y}K_{i2} + g(m_{i1}G_{i1y} + m_{i2}G_{i2y}) = 0 \quad (16)$$

$$A_{i1z}(\rho_{i0} + B_{i1z})K_{i1} + A_{i2z}B_{i2z}K_{i2} + f_{iz}\rho_{i0} + g[m_{i1}(\rho_{i0} + G_{i1z}) + m_{i2}G_{i2z}] = 0 \quad (17)$$

For the PKM under investigation, some simplifications can be made. In particular, points G_{i1} can be considered to lie on the lines passing through U_i and S_i ; points G_{i2} can be considered to be coincident with points U_i . Moreover, only the force components f_{iz} are present, as computed in Section 3.1. Consequently, the conditions (5-17) change as follows:

$$A_{i1x}K_{i1} = 0 \quad (18)$$

$$A_{i1y}K_{i1} = 0 \quad (19)$$

$$f_{iz} + A_{i1z}K_{i1} + m_{i1}g = 0 \quad (20)$$

$$K_{i1} - K_{i3} = 0 \quad (21)$$

$$K_{i1}(\rho_{i0} + B_{i1z}) - K_{i3}(\rho_{i0} + L_{i1z} - L_{i2z}) + \frac{1}{2}K_{i4}\lambda_i = 0 \quad (22)$$

$$A_{i1x}B_{i1x}K_{i1} + A_{i2x}B_{i2x}K_{i2} = 0 \quad (23)$$

$$A_{i1x}(\rho_{i0} + B_{i1z})K_{i1} + A_{i2x}B_{i2z}K_{i2} = 0 \quad (24)$$

$$A_{i1y}B_{i1x}K_{i1} + A_{i2y}B_{i2x}K_{i2} = 0 \quad (25)$$

$$A_{i1y}B_{i1y}K_{i1} + A_{i2y}B_{i2y}K_{i2} = 0 \quad (26)$$

$$A_{i1y}(\rho_{i0} + B_{i1z})K_{i1} + A_{i2y}B_{i2z}K_{i2} = 0 \quad (27)$$

$$A_{i1z}B_{i1x}K_{i1} + A_{i2z}B_{i2x}K_{i2} = 0 \quad (28)$$

$$A_{i1z}B_{i1y}K_{i1} + A_{i2z}B_{i2y}K_{i2} = 0 \quad (29)$$

$$A_{i1z}(\rho_{i0} + B_{i1z})K_{i1} + A_{i2z}B_{i2z}K_{i2} + f_{iz}\rho_{i0} + m_{i1}g(\rho_{i0} + G_{i1z}) = 0 \quad (30)$$

A solution that satisfies (18-30) can be found by arbitrarily choosing some parameters and by imposing some algebraic constraints. In particular, by imposing the value of K_{i1} the following parameters can be determined from (18-21):

$$A_{i1x} = A_{i1y} = 0; A_{i1z} = -\frac{f_{iz} + m_{i1}g}{K_{i1}}; K_{i3} = K_{i1} \quad (31)$$

Then, by imposing K_{i2} , A_{i2x} , A_{i2y} , and A_{i2z} , the following linear system of equations is obtained from (23-30):

$$\begin{bmatrix} 0 & E_{ix} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & E_{ix} \\ 0 & E_{iy} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & E_{iy} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & E_{iy} \\ C_{iz} & E_{iz} & 0 & 0 & 0 & 0 \\ 0 & 0 & C_{iz} & E_{iz} & 0 & 0 \\ 0 & 0 & 0 & 0 & C_{iz} & E_{iz} \end{bmatrix} \begin{Bmatrix} B_{i1x} \\ B_{i2x} \\ B_{i1y} \\ B_{i2y} \\ B_{i1z} \\ B_{i2z} \end{Bmatrix} = \begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ Q_{iz} \end{Bmatrix} \quad (32)$$

where

$$C_{iz} = A_{i1z}K_{i1}; E_{ix} = A_{i2x}K_{i2}; E_{iy} = A_{i2y}K_{i2}; E_{iz} = A_{i2z}K_{i2}; Q_{iz} = -m_{i1}gG_{i1z} \quad (33)$$

A solution can be found provided that the following condition is satisfied:

$$A_{i2x} = A_{i2y} \quad (34)$$

In particular, in case the following condition is imposed:

$$A_{i2x} = A_{i2y} = 0 \quad (35)$$

Also, the parameters B_{i2x} , B_{i2y} , and B_{i2z} can be set arbitrarily, and the remaining unknowns are given by:

$$B_{i1x} = -\frac{E_{iz}}{C_{iz}}B_{i2x}; B_{i1y} = -\frac{E_{iz}}{C_{iz}}B_{i2y}; B_{i1z} = \frac{Q_{iz} - E_{iz}B_{i2z}}{C_{iz}} \quad (36)$$

Otherwise, if the following condition holds

$$A_{i2x} = A_{i2y} \neq 0 \quad (37)$$

it must be necessarily

$$B_{i2x} = B_{i2y} = B_{i2z} = 0 \quad (38)$$

i.e. the spring with stiffness K_{i2} cannot be installed, and the following solution is found:

$$B_{i1x} = B_{i1y} = 0; B_{i1z} = \frac{Q_{iz}}{C_{iz}} \quad (39)$$

This implies that the spring with stiffness K_{i2} is not necessarily required. However, without such spring, it may be difficult to implement in practice the spring with stiffness K_{i1} , since its anchor point on $part_{i1}$ would be univocally determined by the values of f_{iz} , m_{i1} and G_{i1z} .

Finally, by choosing K_{i4} , L_{i1z} and L_{i2z} , the last parameter can be obtained from (22)

$$\lambda_i = 2K_{i1} \frac{B_{i1z} - L_{i1z} + L_{i2z}}{K_{i4}} \quad (40)$$

It is worth noting that the fourth spring would not be required in case $(B_{i1z} - L_{i1z} + L_{i2z}) = 0$. Nonetheless, adding a spring permits a larger flexibility in the design of the leg while not significantly increasing its complexity.

Table 3 shows the main numerical values adopted for the simulations reported in Section 3.3, computed by considering $m_{i1} = 25$ [kg] and $G_{i1z} = -850$ [mm].

Table 3. Parameters adopted for the numerical model.

Parameter	leg # (<i>i</i>)			
	1	2, 3	4	5, 6
K_{i1} [kN/m]	2.000	2.000	2.000	2.000
K_{i2} [kN/m]	2.000	2.000	2.000	2.000
K_{i3} [kN/m]	2.000	2.000	2.000	2.000
K_{i4} [kN/m]	8.000	8.000	8.000	8.000
A_{ilz} [m]	-0.201	-0.123	-0.175	-0.253
A_{i2z} [m]	-0.200	-0.200	-0.200	-0.200
B_{ilx} [m]	-0.099	-0.082	-0.114	-0.079
B_{ily} [m]	-0.099	-0.082	-0.114	-0.079
B_{ilx} [m]	-1.314	-1.339	-1.511	-1.043
B_{i2x} [m]	0.100	0.050	0.100	0.100
B_{i2y} [m]	0.100	0.050	0.100	0.100
B_{i2z} [m]	0.800	0.300	0.800	0.800
L_{ilz} [m]	-1.500	-1.500	-1.500	-1.500
L_{i2z} [m]	0.200	0.200	0.200	0.200
λ_i [m]	0.425	0.425	0.425	0.425

3.3 Numerical model and simulations

Two multibody models are implemented, one for the unbalanced PKM, one for its statically balanced variant. The motor forces required for a quasi-static trajectory through the workspace are evaluated. In particular, a total amount of 27 points of the cubic workspace are taken into account, namely its center, its vertices, and the median points of its edges (Figure 3).

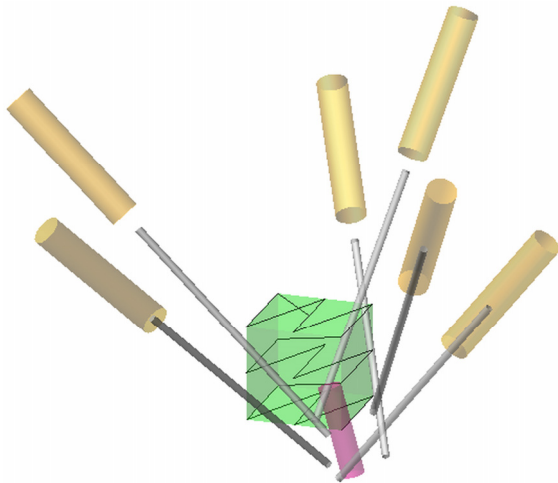


Figure 3. Simulated quasi-static trajectory.

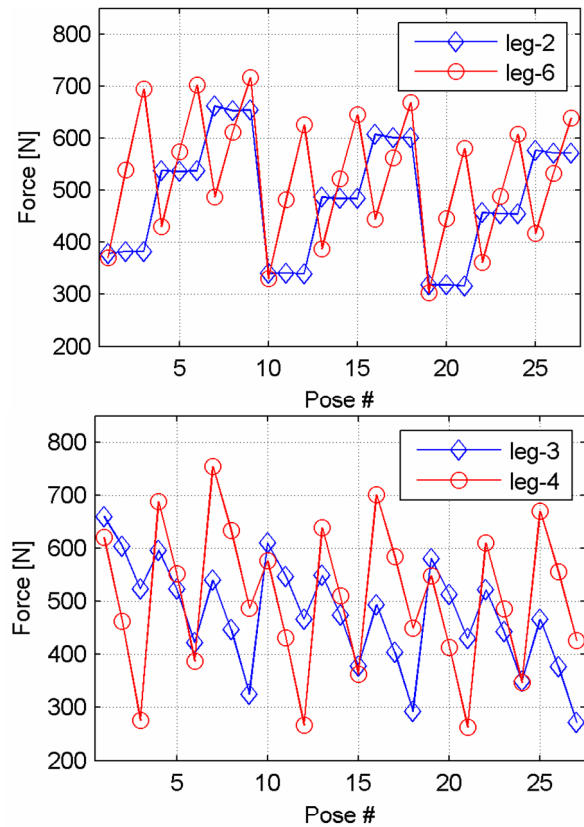
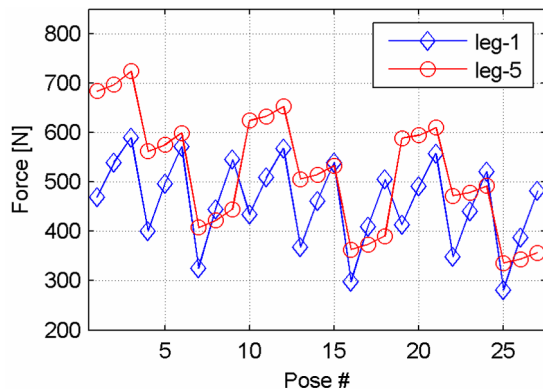
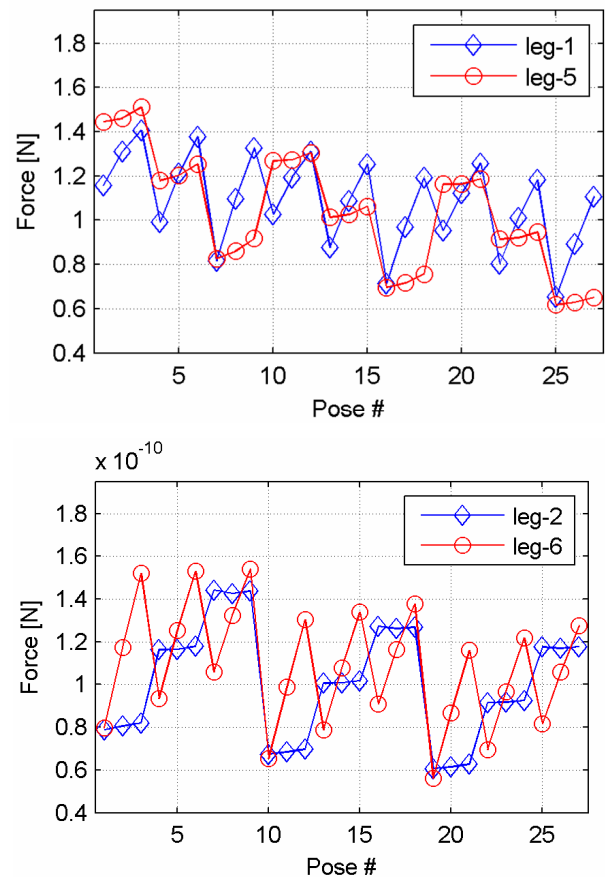


Figure 4. Motor forces of the unbalanced PKM.

Figure 4 shows the required motor forces of the unbalanced PKM for the tested trajectory, with an imposed rotation of the moving platform of +15° around the Y-axis. Figure 5 reports the motor forces of the compensated machine tool under the same conditions.



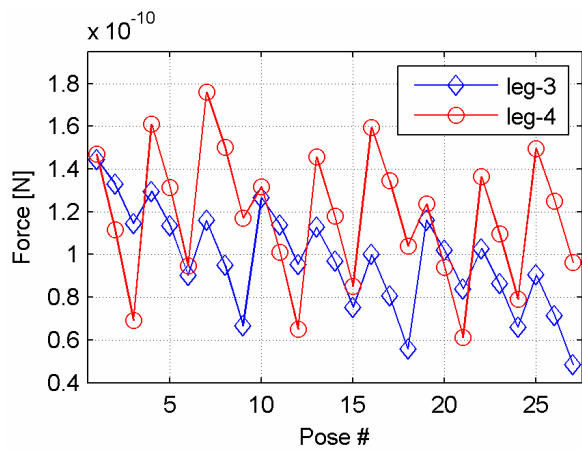


Figure 5. Motor forces of the balanced PKM variant.

The motor forces (which are quite remarkable given the total moving mass of about 230 kg) are completely cancelled by gravity compensation. In particular, the residual motor forces of the balanced variant closely match the trends of the loads exhibited by the unbalanced PKM, but their magnitudes are negligible, since they are twelve orders of magnitude lower (such values being basically ascribable to numerical approximations). Hence, the simulation results confirm the effectiveness of the proposed solution.

4. CONCLUSION

This work presented an effective strategy for the exact gravity compensation of a parallel kinematics machine tool with six UPS legs. The parameters of the balancing components to be installed for achieving static balancing, by means of constant-force generators, were analytically determined. The validity of the proposed solution was confirmed through numerical simulations.

The proposed balancing strategy may be applied to other parallel robots with the same architecture of the legs and it is expected to provide a significant enhancement of the system energy efficiency.

The future steps of the research will aim at optimizing the balancing components for operation in the most common working cycles, thus possibly further improving the machine performance.

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**ГРАВИТАЦИЈСКА КОМПЕНЗАЦИЈА 6-УПС
МАШИНЕ АЛАТЕ СА ПАРАЛЕЛНОМ
КИНЕМАТИКОМ ПОМОЋУ ЕЛАСТИЧНО
УРАВНОТЕЖЕНИХ КОНСТАНТНИХ СИЛА
ГЕНЕРАТОРА**

А. Мартини

Компензација гравитације је одржива стратегија за побољшање перформанси манипулатора, нарочито у погледу потрошње енергије. Овај рад проучава статичко балансирање прототипне 5-осовинске машине алатке са паралелном кинематиком УПС ослонцима. Прецизна компензација гравитације се постиже пребацавањем ослонаца у генераторе са константном снагом, путем еластичних опруга. Нумерички вишестелесни модел се имплементира и симулира у комерцијалном софтверском окружењу (MSC Adams™) како би се проценила ефикасност предложене стратегије балансирања.