





The evolution of the Milky Way’s thin disc radial metallicity gradient with K2 asteroseismic ages

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ABSTRACT

The radial metallicity distribution of the Milky Way’s disc is an important observational constraint for models of the formation and evolution of our Galaxy. It informs our understanding of the chemical enrichment of the Galactic disc and the dynamical processes therein, particularly radial migration. We investigate how the metallicity changes with guiding radius in the thin disc using a sample of red giant stars with robust astrometric, spectroscopic, and asteroseismic parameters. Our sample contains 668 stars with guiding radii $4 < R_g < 11$ kpc and asteroseismic ages covering the whole history of the thin disc with precision ≈ 25 per cent. We use MCMC analysis to measure the gradient and its intrinsic spread in bins of age and construct a hierarchical Bayesian model to investigate the evolution of these parameters independently of the bins. We find a smooth evolution of the gradient from ≈ -0.07 dex kpc^{-1} in the youngest stars to ≈ -0.04 dex kpc^{-1} in stars older than 10 Gyr, with no break at intermediate ages. Our results are consistent with those based on asteroseismic ages from *CoRoT*, with that found in Cepheid variables for stars younger than 1 Gyr, and with open clusters for stars younger than 6 Gyr. For older stars we find a significantly lower metallicity in our sample than in the clusters, suggesting a survival bias favouring more metal-rich clusters. We also find that the chemical evolution model of Chiappini ’09 is too metal poor in the early stages of disc formation. Our results provide strong new constraints for the growth and enrichment of the thin disc and radial migration, which will facilitate new tests of model conditions and physics.

Key words: asteroseismology – stars: abundances – Galaxy: abundances – Galaxy: disc – Galaxy: evolution – Galaxy: stellar content.

1 INTRODUCTION

Over the last decade, the field of Galactic archaeology has expanded rapidly, with many new discoveries concerning the formation and evolution of the Milky Way (MW). These advances have been facilitated by the availability of astrometry of unprecedented precision from *Gaia* (Gaia Collaboration 2016) and several large spectroscopic surveys, such as the Apache Point Observatory Galactic Evolution Experiment (APOGEE; Majewski et al. 2017), *Gaia*-ESO (Randich et al. 2022), GALactic Archaeology with HERMES (GALAH; Buder et al. 2021), the Large Sky Area Multi-Object Fibre Spectroscopic

Telescope (LAMOST; Deng et al. 2012; Zhao et al. 2012), and the RAdial Velocity Experiment (RAVE; Steinmetz et al. 2020a,b). When combined with stellar ages, these provide meaningful tests of chemo-dynamical models of the MW.

Many such models of spiral galaxies predict that the inner part of the disc forms earlier than the outer regions (e.g. Larson 1976; Matteucci & Francois 1989; Chiappini, Matteucci & Gratton 1997; Frankel et al. 2019), and the idea of ‘inside-out’ formation is now widely accepted. One of the signatures of this formation scenario is a radial metallicity¹ gradient in the Galactic disc, with higher

¹Throughout this work we use iron abundance as a tracer for metallicity: $[\text{Fe}/\text{H}] = \log_{10}(N_{\text{Fe}}/N_{\text{H}})_{*} - \log_{10}(N_{\text{Fe}}/N_{\text{H}})_{\odot}$, where N_{Fe} and N_{H} are the num-

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metallicities in the centre, caused by more generations of stars that enrich the material from which the next generation form. This gradient might change with time as the disc expands and star formation proceeds unevenly. In the MW we have the opportunity to explore this evolution by using tracers of the metallicity gradient with different ages, in contrast to studies of other galaxies where, from a given tracer, we see only a snapshot of the aggregate effect (e.g. Cresci et al. 2010; Magrini et al. 2016).

In addition to its intrinsic interest as a property of the MW, the radial metallicity gradient also helps to constrain dynamical processes in the disc. If we expect that stars are born into the Galaxy with some tight relationship between their metallicity and birth radius, R_b , but the relationship in a mono-age population shows some scatter, then we may infer that some stars have moved away from R_b . This assumption breaks down in the presence of contaminants from the debris of galactic mergers of other processes, but it is an acceptable simplification in a robustly selected *in situ* population. Inferring birth radii is an important step towards recovering the MW's history, and therefore tight observational constraints on the metallicity gradient are very valuable (e.g. Wielen, Fuchs & Dettbarn 1996; Minchev, Chiappini & Martig 2013; Frankel et al. 2018; Minchev et al. 2018).

There are two reasons why a star may be observed with a galactocentric radius, $R_{\text{Gal}} \neq R_b$. First, the eccentricity of the orbit naturally results in a star being observed at different R_{Gal} during the orbit. Stars in the disc are born onto nearly circular orbits, which increase in eccentricity over time as a result of radial heating. This process increases the radial action, J_R , and is referred to as ‘blurring’ (Sellwood & Binney 2002; Schönrich & Binney 2009a). Importantly, for efforts to recover birth radii, blurring does not change the orbital angular momentum, L_z , so the star retains some ‘kinematic memory’ of its birth conditions. By considering the metallicity gradient with guiding radius, R_g (the radius of a circular orbit of the same angular momentum), we can mitigate this effect in our sample.

Second, interactions with non-axisymmetric features of the MW's disc (e.g. the bar or spiral arms) can cause ‘churning’ (Sellwood & Binney 2002), in which an exchange of angular momentum shifts the star into a new orbit. Frankel et al. (2020) found that this effect is roughly an order of magnitude stronger than blurring in the Galactic disc, shifting stars by up to ≈ 3 kpc over 6 Gyr on average. The change of L_z means that $R_g \neq R_b$ and R_b can only be inferred by indirect means, such as the combination of the metallicity gradient and age. Minchev, Chiappini & Martig (2016) found that churning is necessary in their chemo-dynamical simulation in order to reproduce the observed spread of metallicity in stars of a given age. The same model also shows that the presence of churning affects the flaring of a galactic disc in a quiescent setting or during a merger (Minchev 2016).

Constraints on migratory processes like churning require precise measurements of the metallicity gradient in populations spanning the full history of the disc. This necessitates a large sample, covering a wide range of radii, metallicities, and ages. Open clusters (OCs) have been used in such studies (Magrini et al. 2009; Casamiquela et al. 2017, 2019; Spina et al. 2021; Myers et al. 2022; Netopil et al. 2022; Spina, Magrini & Cunha 2022; Gaia Collaboration 2023b), however, dynamical processes are thought to create a survival bias towards high-metallicity OCs, obscuring the underlying chemical evolution of the Galaxy (Lynga & Palous 1987; Anders et al. 2017b; Spina

et al. 2021). Cepheid variables can be used to probe the present-day gradient, as they provide an excellent radial range for targets with $20 < \tau < 400$ Myr (Genovali et al. 2014). Other young tracers such as OB stars (Kaufer et al. 1994; Daflon & Cunha 2004; Bragança et al. 2019) and H II regions (Esteban et al. 2005; Balsa et al. 2011) can be used to trace the [O/H] gradient over large regions of the Galaxy but, as for Cepheids, they cannot reveal the evolution over its history.

Low-mass field stars are ideal tracers, but there are many well-documented challenges associated with obtaining reliable stellar ages for large samples. Ages may be estimated by comparison to isochrones, but they are sensitive to changes in model physics or temperature scale and are generally restricted to lower luminosity phases of stellar evolution. For red giants that exhibit solar-like oscillations, asteroseismic analysis may be used to obtain precise and robust (though not model independent) stellar ages (Soderblom 2010; Chaplin & Miglio 2013; Lebreton, Goupil & Montalbán 2014). Anders et al. (2017b) demonstrated the potential of this approach with the *Convection, Rotation and planetary Transits (CoRoT)*–APOGEE (CoRoGEE) sample (Anders et al. 2017a), combining asteroseismic constraints from two fields observed by *CoRoT* (Baglin et al. 2006) with spectroscopy from APOGEE. The combination of asteroseismology and spectroscopy offers many advantages over classical tracers, as we can probe the full history of the disc over several kpc.

Kepler (Gilliland et al. 2010) represents the ‘gold standard’ in asteroseismic data, enabling ages to be determined to 10 per cent precision (Montalbán et al. 2021). However, while the signature of radial migration can be seen in *Kepler* data (e.g. fig. 6 of Miglio et al. 2021), they are restricted in spatial coverage to a single 105 deg^2 area. In this work, we utilize the results of the successor mission K2 (Howell et al. 2014), which provides observations from all around the ecliptic, split into 20 campaigns each observed for around 80 d. Though the observation time per campaign was much shorter in duration than *Kepler* for a single field, the global oscillation frequencies are sufficient to place good constraints on the stellar mass, M_* , with which the age of low-mass red giants is tightly correlated. Combining these data with chemical abundances from APOGEE Data Release 17 (DR17; Abdurro'uf et al. 2022) and *Gaia* Data Release 3 (DR3; Gaia Collaboration 2023a) unlocks the potential of asteroseismic ages for Galactic archaeology on a large scale.

In this work, we compile a catalogue of K2 targets with robust and homogeneously determined stellar parameters from asteroseismology. From this, we select members of the thin disc and measure the radial metallicity gradient as a function of age with two complementary techniques. We introduce our sample in Section 2 and describe our analysis in Sections 3 and 4. Section 5 contains a detailed discussion of our results and a comparison to the existing literature and theoretical predictions. Finally, our conclusions are presented in Section 6.

2 OBSERVATIONAL CONSTRAINTS

In this section, we describe our sample of K2 solar-like oscillating red giants (Section 2.1), outline how the stellar and orbital parameters were inferred from the observables (Section 2.2), and how members of the thin disc were selected, utilizing both the abundance and kinematic information (Section 2.3).

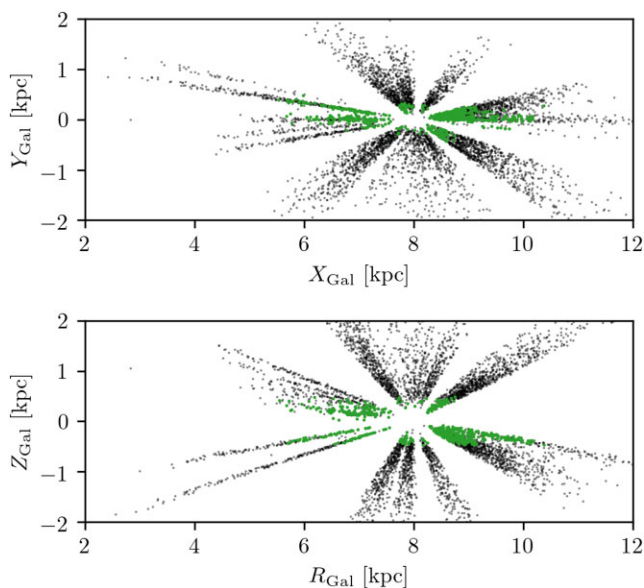


Figure 1. Location of stars in our sample in left-handed Galactocentric Cartesian coordinates (top) and Galactocentric cylindrical coordinates (bottom). The green points show the stars in the thin disc, and the full sample is shown in the background (black points).

2.1 Asteroseismic, spectroscopic, and astrometric constraints

Our sample is based upon the catalogue of Willett et al. (in preparation), which contains asteroseismic parameters from the pipelines of Mosser & Appourchaux (2009) and Elsworth et al. (2020), as well as spectroscopically derived abundances and radial velocities (RVs) from APOGEE DR17 (Abdurro’uf et al. 2022), and five-parameter astrometric solutions from *Gaia* DR3 (Gaia Collaboration 2023a).

In order to obtain a set of homogeneously constrained stellar ages, in this work we consider global asteroseismic parameters ν_{\max} , the frequency of maximum oscillation power, and $\Delta\nu$, the large frequency separation, from the pipeline of Elsworth et al. (2020) only. This pipeline has been shown to produce fewer false positive detections (Mackereth et al. 2021) and the definition of $\Delta\nu$ (which varies between pipelines) is more similar to that used in the stellar parameter estimation code PARAM. The resulting sample is spread across K2 campaigns 1–8 and 10–18 that provides good coverage out to ≈ 3 kpc from the solar position.

The abundances used in this work are those produced by the APOGEE Stellar Parameters and Chemical Abundances Pipeline (ASPCAP; García Pérez et al. 2016). A full description of this pipeline as applied to APOGEE DR17 is given in Holtzman et al. (in preparation). We remove targets with ASPCAPFLAG containing STAR_BAD or STAR_WARN, and those with any RV_FLAG set.

We use five-parameter astrometric solutions $[\alpha, \delta, \varpi, \mu_\alpha, \mu_\delta]$ from *Gaia* DR3. Following Lindegren (2018), we remove targets with $\text{ruwe} > 1.4$ or which are marked as binaries by the `non_single_star` flag.

The final sample comprises 5885 targets, shown in Fig. 1, with median metallicity uncertainty $\sigma_{[\text{Fe}/\text{H}]} = 0.008$ dex. In practice, we enforce a lower limit of $\sigma_{[\text{Fe}/\text{H}]} > 0.05$ dex and $\sigma_{T_{\text{eff}}} > 50$ K during the inference of the stellar parameters (Section 2.2) because the pipeline uncertainties reflect only the internal errors. In addition, inflating the error on T_{eff} helps to mitigate the uncertainties associated with the descriptions of near-surface convection and outer boundary conditions in the stellar models. We use the ASPCAP

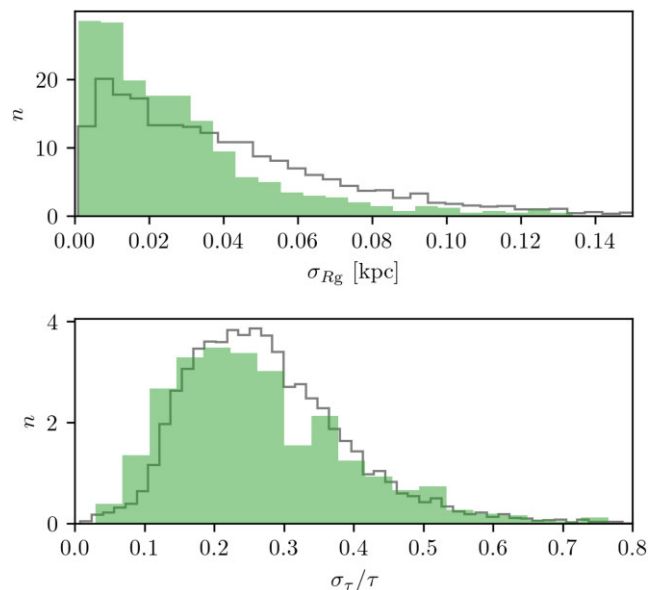


Figure 2. Distribution of the uncertainty on guiding radius (top) and fractional uncertainty on age (bottom) in the full sample (grey line) and thin disc (filled green). The area under each histogram integrates to one.

$\sigma_{[\text{Fe}/\text{H}]}$ in our analysis of the metallicity gradient, but show the negligible effect on our results of inflating the [Fe/H] uncertainty in Appendix A.

2.2 Inferred stellar and orbital parameters

In this work, we use the stellar parameters described in Willett et al. (in preparation), specifically the mass, M_* , age, τ , and distance, D . These parameters are inferred using the PARAM code (Da Silva et al. 2006; Rodrigues et al. 2014, 2017), which performs a Bayesian comparison to a grid of stellar models and returns full posterior information. Asteroseismic constraints are provided by $\Delta\nu$ and ν_{\max} and we use the reference model grid (labelled G2) from the work of Miglio et al. (2021). We remove stars with ν_{\max} more than three standard deviations below $20 \mu\text{Hz}$, as asteroseismic inferences have not been extensively tested in this domain. A detailed discussion of the asteroseismic distances and how they compare to those from *Gaia* can be found in Khan et al. (2023).

Orbital parameters are obtained from the same source and here we use the guiding radius, R_g , and maximum excursion from the Galactic plane Z_{\max} . They are computed using the fast orbit estimation method of Mackereth & Bovy (2018), implemented in GALPY (Bovy 2015). Throughout this work, we adopt the simple MW potential `MWPotential2014` (Bovy 2015) and, following this model, we assume the radial position of the Sun to be $R_{\text{Gal}, \odot} = 8.0$ kpc, where the circular velocity is $v_{\text{circ}} = 220 \text{ km s}^{-1}$ (Bovy et al. 2012). The additional solar motion is given by $[U, V, W]_{\odot} = [-11.1, 12.24, 7.25] \text{ km s}^{-1}$ (Schönrich, Binney & Dehnen 2010), and the Sun’s vertical offset from the Galactic plane is $Z_{\text{Gal}, \odot} = 20.8 \text{ pc}$ (Bennett & Bovy 2019).

For both the stellar and orbital parameters, we use the 68 per cent credible interval throughout our analysis, and sometimes approximate the posteriors as Gaussian, taking half this interval as the standard deviation. The uncertainties on τ and R_g are shown in Fig. 2.

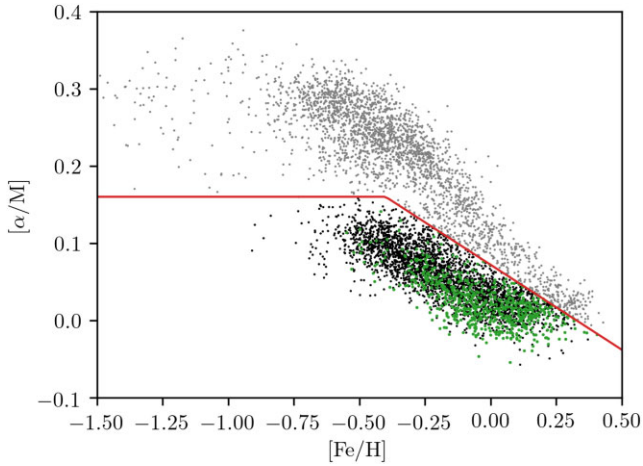


Figure 3. Average α element abundance $[\alpha/M]$ versus $[\text{Fe}/\text{H}]$. The high- and low- α sequences were separated along the red line, with the high- α population (grey) removed from the analysis. Of the remaining low- α population, stars with $Z_{\text{max}} \geq 0.5$ kpc were also removed (black). The final thin disc sample is shown in green.

2.3 Thin disc selection

In this work, we restrict our analysis to the thin disc, where the stellar orbits have been less disturbed by dynamical processes (either rapid ‘non-adiabatic heating’ that can be caused by interactions with other galaxies or scattering from giant molecular clouds, or ‘adiabatic heating’ from the secular evolution of the disc; Ting & Rix 2019, and references therein). The rest of the sample will be studied in future works where we explore other abundance gradients, vertical trends, and stars from the Galactic halo. We select thin disc members from our sample in two stages. First, we make a cut in the $[\alpha/M]$ abundance to remove the α -enhanced population, which is usually associated with the halo and thick disc (Fig. 3). We use $[\alpha/M]$ as a proxy for $[\alpha/\text{Fe}]$ as the differences between them² are negligible. Second, we make a cut to retain stars with $Z_{\text{max}} < 0.5$ kpc that are on kinematically cool orbits. This cut is chosen to be slightly wider than the scale height of the thin disc, to accommodate the flaring of the disc in the outer galaxy (Momany et al. 2006). Though this cut changes the metallicity distribution of our sample, our results are not very sensitive to its exact position (see Appendix B for details).

Our thin disc sample contains a total of 668 stars and is shown in green in Figs 1–3, with median uncertainties $\sigma_{[\text{Fe}/\text{H}]} = 0.007$, $\sigma_{\tau}/\tau = 0.24$, and $\sigma_{R_g} = 0.02$ kpc – though we remind the reader of the comment on $\sigma_{[\text{Fe}/\text{H}]}$ in Section 2.1.

3 THE METALLICITY GRADIENT IN BINS OF AGE

We investigate the metallicity as a function of R_g across six bins in age:

$$\begin{aligned} \tau < 1 \text{ Gyr}, & \quad 1 \leq \tau < 2 \text{ Gyr}, \\ 2 \leq \tau < 4 \text{ Gyr}, & \quad 4 \leq \tau < 6 \text{ Gyr}, \\ 6 \leq \tau < 10 \text{ Gyr}, & \quad 10 \text{ Gyr} \leq \tau, \end{aligned}$$

where we use bins of increasing width to accommodate the wider posteriors at older ages. For ease of comparison, these bins are the same as those used by Anders et al. (2017b).

²Defining $[\alpha/\text{Fe}]$ as an average of $[\text{X}/\text{Fe}]$ for O, Mg, Si, S, and Ca.

We utilize a Bayesian fitting procedure to constrain the metallicity gradient, using a ‘linear+Gaussian spread’ model. In physical terms, this means that we expect stars to be normally distributed about some line intrinsically, rather than having been drawn from a narrow relationship and subsequently scattered, so

$$[\text{Fe}/\text{H}] \sim \mathcal{N}(mR_g + c, V). \quad (1)$$

This model has three parameters $\phi = m, c, V$, where m and c are the linear gradient and offset from $[\text{Fe}/\text{H}] = 0$ at $R_g = 0$, and V is the variance of the Gaussian, oriented perpendicular to the direction of the linear component. Using Bayes’ theorem, the posterior probability density function (PDF) of these model parameters given some data d is

$$p(\phi|d) \propto p(\phi)p(d|\phi), \quad (2)$$

where $p(\phi)$ is the prior PDF of the model parameters and $p(d|\phi) = \mathcal{L}$ is the likelihood of observing the data, given the model.

Our fitting procedure follows Hogg, Bovy & Lang (2010) and accounts for uncertainty on both R_g and $[\text{Fe}/\text{H}]$ by utilizing the full covariance matrix of each star i , ζ_i , in the likelihood. In addition, we reparametrize the problem so that we do not directly constrain m and c , but rather the angle to the horizontal, $\cos(\theta) = 1/\sqrt{1+m^2}$, and $c_{\perp} = c \cos(\theta)$, which avoids our wide priors placing too much emphasis on gradients close to vertical. This gives a new set of parameters $\varphi = [\theta, c_{\perp}, V]$. Projecting ζ_i to an orthogonal variance Σ_i^2 , we may write the log-likelihood as

$$\ln(\mathcal{L}) \propto -\frac{1}{2} \sum_i \left[\ln(\Sigma_i^2 + V) + \frac{\Delta_i^2}{\Sigma_i^2 + V} \right], \quad (3)$$

where Δ_i is the orthogonal displacement of star i from the line. We choose very wide, uniform priors on the parameters φ , requiring

$$\begin{aligned} -\pi &< \theta < \pi, \\ -10^3 &< c_{\perp} < 10^3, \\ 0 &\leq V < 10^4. \end{aligned}$$

We explore this parameter space by sampling according to the Markov chain Monte Carlo (MCMC) algorithm, implemented in EMCEE (Foreman-Mackey et al. 2013). We use 32 walkers that each make 5000 steps, with a burn-in time that is dynamically determined to be 10 times the autocorrelation time (removing around 500 samples per walker). To account for the uncertainty on τ , we perform an overarching Monte Carlo (MC) analysis by repeating this procedure for 500 realizations of τ that are generated by approximating the posterior distribution from PARAM as Gaussian. This allows the stars to move between bins in each step of the MC. We combine all the post-burn-in samples and report the median and 68 per cent credible interval as the best-fitting values of the parameters. The age uncertainty contributes approximately 30 per cent to the overall error budget on these results. The lines corresponding to these values are shown in Fig. 4, where the filled region indicates the intrinsic spread, \sqrt{V} , and the points appear in the bin to which the median age of the star belongs. An example corner plot showing the joint and marginal distributions of the fit parameters φ in one bin, for one realization of τ is shown in Fig. 5.

We report the best-fitting values of the gradient, m , metallicity offset at 8 kpc, $b = m \times 8 + c$, and $[\text{Fe}/\text{H}]$ component of the spread $S = \sqrt{V} \cos(\theta)$ in the left-hand side of Table 1. The gradient flattens monotonically with age, and the spread is smallest for the youngest populations, increasing until $\tau \approx 10$ Gyr. The metallicity at 8 kpc is slightly subsolar at all ages.

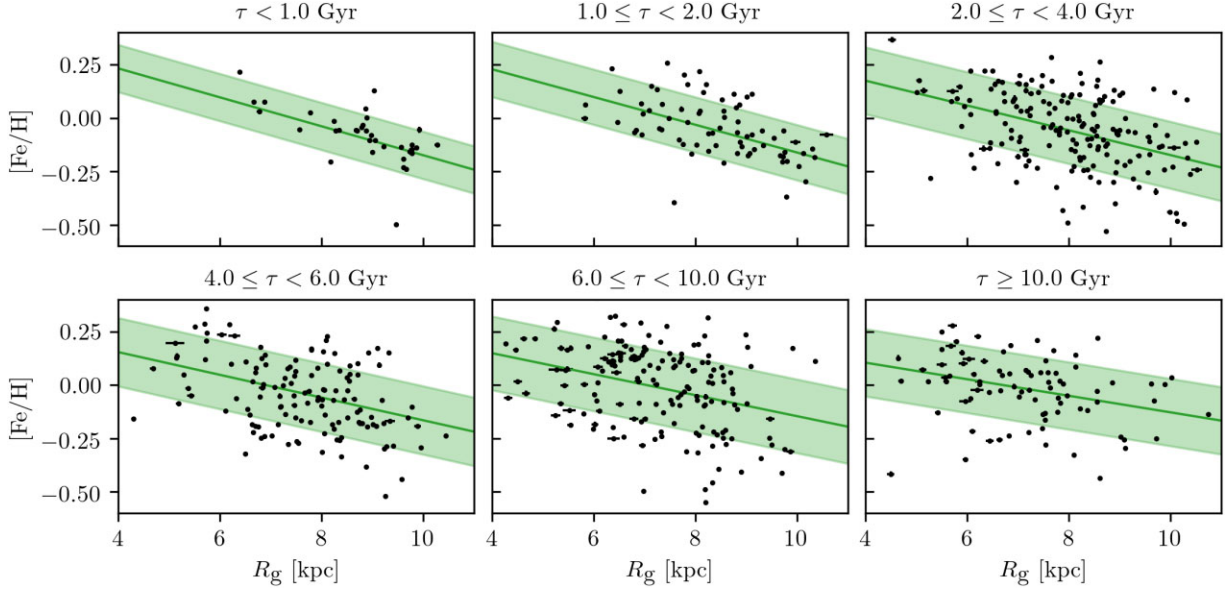


Figure 4. [Fe/H] versus R_g in six bins of age. The thin disc sample is shown in black points, binned according to the median age of each star. The green line shows the best-fitting radial metallicity gradient from the MCMC analysis, with a filled region representing 1σ of the intrinsic spread.

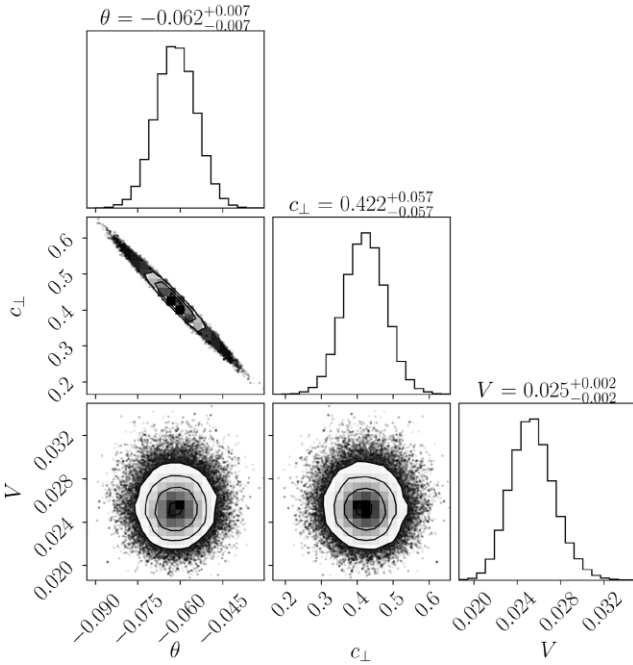


Figure 5. Corner plot (Foreman-Mackey 2016) showing the joint and marginalized sampled posterior distributions of the fit parameters ϕ in the age bin $2 \leq \tau < 4$ Gyr for one step in the MC (one realization of τ).

4 A HIERARCHICAL BAYESIAN APPROACH

Reducing a data set to a small number of bins can lead to misleading and sometimes unreliable results. In the specific context of this work, the intrinsic spread around the linear relationship carries essential information, so conflating it with a scatter caused by the mix of ages in a bin makes robust inference a challenge. This is compounded by the fact that the bins are wider, and therefore the populations are a worse approximation of mono-age, at older ages. In this section, we show that, with our large data set and some simplifying assumptions, it is possible to remove the need for binning altogether.

To constrain the changes in the metallicity distribution with age we constructed a hierarchical Bayesian model (HBM). This allows the fit parameters to vary for each star (they are now the latent parameters), constrained by some population-level rule that describes how they vary with age. We reparametrize to describe the variation with $\log(\tau)$ instead because the increasing age uncertainty as a function of age makes the parameter space difficult to explore. In this case, we assume a linear relationship for m and b with $\log(\tau)$, and (since the spread must have a strictly non-negative value) S follows an exponential in $\log(\tau)$:

$$\begin{aligned} [\text{Fe}/\text{H}] &\sim \mathcal{N}(mR_g + (b - 8m), S^2); \\ m &= k_1 A_m \log(\tau) + k_2 B_m, \\ b &= k_3 A_b \log(\tau) + k_4 B_b, \\ S &= \exp(k_5 A_S \log(\tau) + k_6 B_S). \end{aligned} \quad (4)$$

The parameters $\Psi = A_m, B_m, A_b, B_b, A_S, B_S$ are the population-level hyperparameters and the constants k_i are introduced to rescale each to be close to unity, in order to increase the efficiency of our sampling. These simple relationships are a pragmatic choice, providing a test of the results from the binned analysis for a small number of hyperparameters.

Fig. 6 shows the probabilistic graphical model corresponding to this analysis, where the dependencies between the hyperparameters, latent parameters, and observables are indicated by arrows. Bayes' theorem now becomes

$$p(\Psi, \phi|d) \propto p(\Psi) p(\phi|\Psi) p(d|\phi). \quad (5)$$

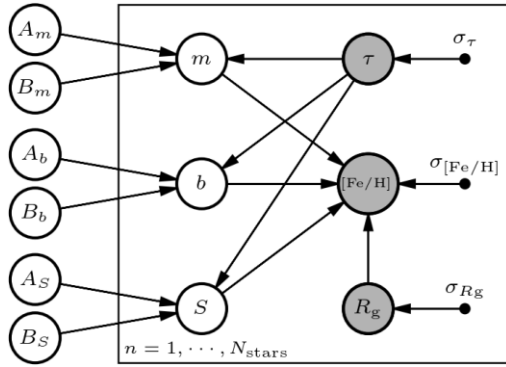
We choose minimally informative priors on the hyperparameters, Ψ , with each drawn from a normal of the form $\mathcal{N}(\mu, \sigma^2)$ such that

$$\begin{aligned} A_m &\sim \mathcal{N}(3, 9), \quad B_m \sim \mathcal{N}(0, 9), \\ A_b &\sim \mathcal{N}(-3, 9), \quad B_b \sim \mathcal{N}(0, 9), \\ A_S &\sim \mathcal{N}(0, 25), \quad B_S \sim \mathcal{N}(0, 25), \end{aligned}$$

and, because the HBM is a generative model, we also require priors on R_g and $\log(\tau)$. We choose these to be broad and likelihood

Table 1. The median and 68 per cent credible interval for each parameter from MCMC analysis in bins of age (left) and the HBM, evaluated at the median age, τ_{med} , of each bin population (right); m is the gradient, b is the [Fe/H] offset at $R_g = 8$ kpc, and S is the component of the intrinsic spread in the [Fe/H] direction.

Bin range [Gyr]	N_{stars}	MCMC parameters			τ_{med} [Gyr]	HBM parameters		
		m [dex kpc $^{-1}$]	b [dex]	S [dex]		m [dex kpc $^{-1}$]	b [dex]	S [dex]
$\tau < 1$	35	$-0.068^{+0.017}_{-0.016}$	$-0.039^{+0.022}_{-0.023}$	$0.111^{+0.015}_{-0.013}$	0.7	$-0.078^{+0.011}_{-0.011}$	$-0.022^{+0.016}_{-0.015}$	$0.115^{+0.010}_{-0.009}$
$1 \leq \tau < 2$	74	$-0.065^{+0.013}_{-0.013}$	$-0.033^{+0.015}_{-0.015}$	$0.130^{+0.012}_{-0.011}$	1.6	$-0.068^{+0.008}_{-0.007}$	$-0.034^{+0.010}_{-0.009}$	$0.130^{+0.007}_{-0.006}$
$2 \leq \tau < 4$	183	$-0.058^{+0.010}_{-0.010}$	$-0.058^{+0.011}_{-0.011}$	$0.157^{+0.008}_{-0.008}$	3.0	$-0.060^{+0.005}_{-0.005}$	$-0.044^{+0.006}_{-0.007}$	$0.145^{+0.005}_{-0.005}$
$4 \leq \tau < 6$	132	$-0.053^{+0.012}_{-0.012}$	$-0.060^{+0.016}_{-0.016}$	$0.160^{+0.011}_{-0.010}$	4.9	$-0.054^{+0.005}_{-0.005}$	$-0.052^{+0.007}_{-0.007}$	$0.157^{+0.004}_{-0.004}$
$6 \leq \tau < 10$	165	$-0.049^{+0.012}_{-0.011}$	$-0.048^{+0.016}_{-0.016}$	$0.173^{+0.011}_{-0.010}$	7.6	$-0.048^{+0.006}_{-0.006}$	$-0.059^{+0.009}_{-0.009}$	$0.169^{+0.006}_{-0.006}$
$10 \leq \tau$	87	$-0.039^{+0.013}_{-0.013}$	$-0.051^{+0.020}_{-0.020}$	$0.158^{+0.012}_{-0.012}$	12.6	$-0.041^{+0.008}_{-0.008}$	$-0.067^{+0.012}_{-0.013}$	$0.184^{+0.010}_{-0.009}$

**Figure 6.** A probabilistic graphical model of the hierarchical Bayesian model (HBM). The properties of individual stars are shown inside the rectangle, and the hyperparameters are shown outside. Grey nodes represent observables and their respective observational uncertainties are given by the small black nodes.

dominated:

$$R_g \sim \mathcal{N}(8, 25),$$

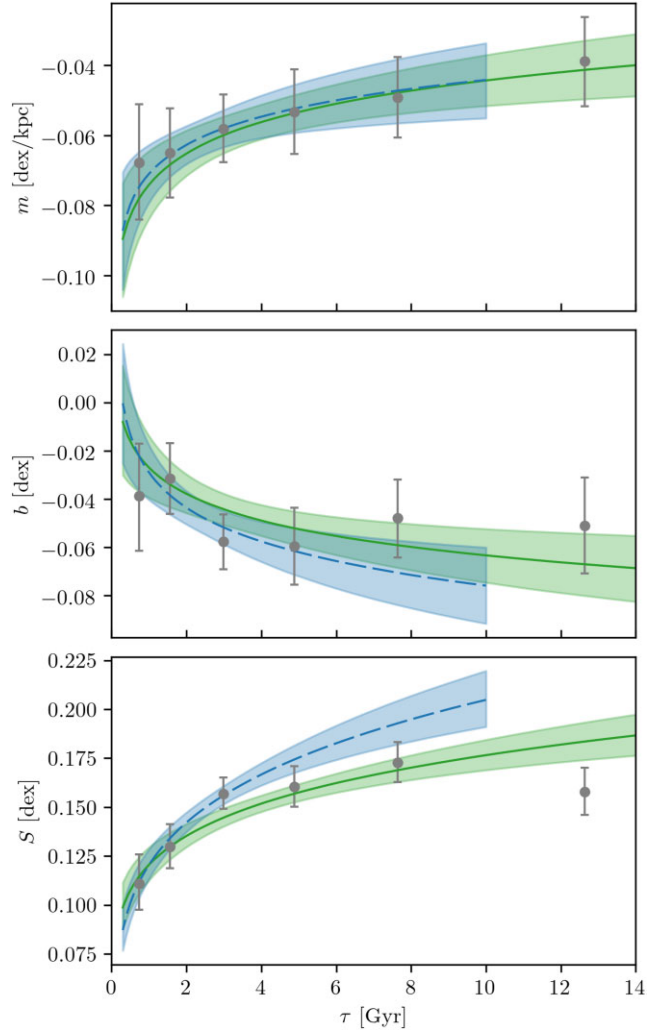
$$\log(\tau) \sim \mathcal{N}(0.7, 0.09).$$

We explore this new parameter space with the No-U-Turn Sampler (NUTS) variant of the MCMC algorithm (Hoffman & Gelman 2011), implemented in NUMPYRO (Bingham et al. 2019; Phan, Pradhan & Jankowiak 2019), using five chains that each make a total of 15 000 samples, 5000 of which are reserved for warm-up. We confirm model convergence by ensuring $\hat{r} < 1.04$ for all parameters (Gelman & Rubin 1992).

The results for this analysis are shown in Fig. 7, where the line indicates the median value of the posterior distribution and the filled band is the 68 per cent credible interval, which is larger for younger and older stars where the data are sparser. For comparison, we show the results of the age-binned analysis, plotted against the median age of the population in each bin, with error bars that show the 68 per cent credible interval. The results of the HBM at the median age of each bin population are reported in Table 1, and both sets of results are discussed more fully in the next section.

5 DISCUSSION

We have shown results from two complementary methods to measure the radial metallicity gradient over the history of the MW's disc. In the next section, we discuss these results in more detail, as well as what can be learned from their comparison. We give special consideration

**Figure 7.** Evolution of the fit parameters as a function of stellar age. The grey points show the best-fitting value and 68 per cent credible interval in each bin from the MCMC analysis (plotted against the median age of the population in the bin). The green line and filled region show the result and 68 per cent credible interval from the HBM. The dashed blue line and filled region show the HBM result when stars older than 10 Gyr are excluded from the analysis.

to the oldest stars in Section 5.2 and comment on the possible biases present in our work in Section 5.3. Finally, in Section 5.4, we compare to predictions from theoretical models of chemo-dynamical evolution and set our work in the context of the literature.

5.1 Results of this work

Our sample of K2 oscillating red giants provides excellent coverage of a wide range of guiding radii and ages, which allows the metallicity evolution of the thin disc to be investigated. Using hierarchical Bayesian analysis we obtain constraints that are free from the additional uncertainties introduced by binning. However, in this analysis, it is necessary to assume a functional form for the evolution of the fit parameters, and therefore the HBM does not have the freedom to trace all features of the data. In this way the MCMC analysis performed on the binned data and the HBM are complementary and it is useful to compare their results in detail.

As shown in Fig. 7 and Table 1, the two methods agree very well (within 1σ) at all ages for the gradient and offset at 8 kpc of the radial metallicity relationship. The largest differences are in the stars younger than 2 Gyr, which may be due to the smaller sample size or the assumed functional forms within the HBM. We find that b is below solar metallicity at all ages, suggesting that the Sun was born closer to the Galactic Centre than its current position, in agreement with Wielen et al. (1996), Minchev et al. (2013, 2018), and Frankel et al. (2018).

There are more significant differences between the results for the intrinsic spread. This is not surprising because, in the MCMC analysis, the spread arising from the width of each bin and the sample size within each bin are conflated with the underlying physics. Overall the agreement between the methods suggests that the effects of the binning do not dominate. This verification is important as understanding this spread is an important step towards a measurement of the effects of churning (e.g. Haywood 2008; Kubryk, Prantzos & Athanassoula 2015b), though quantifying the effects of radial migration is beyond the scope of this study. It seems likely that the difference in population size (Table 1) is the cause of the small fluctuations around the trend shown by the HBM, with slightly larger populations correlating with a larger spread. The deviation is largest in the population older than 10 Gyr and, while the smaller sample size in this bin is still relevant, these stars merit special consideration because they were likely born in an epoch prior to the formation of the thin disc.

5.2 Stars older than 10 Gyr

Models of the assembly history of the MW show that the Galactic disc formed ≈ 10 Gyr ago (e.g. Belokurov & Kravtsov 2022). Therefore stars older than this were not born in the thin disc as we know it today, and this bin contains the highest fraction of contaminants from the debris of mergers or other processes in the MW before the onset of disc formation. Since it is necessary to assume a functional form for the evolution of S , the HBM is not able to trace all features present in the data, so the difference between it and the binned result does not necessarily indicate an effect introduced by the binning. However, we can test the effect of the old population in the HBM by removing it and rerunning the analysis.

After removing stars with $\tau > 10$ Gyr, the HBM results for the slope and offset are consistent within their uncertainties (the blue lines in Fig. 7), but we find a significantly steeper increase in the spread with age. This indicates that the reduced spread is, at least partly, a physical effect because the old population flattens the fit of

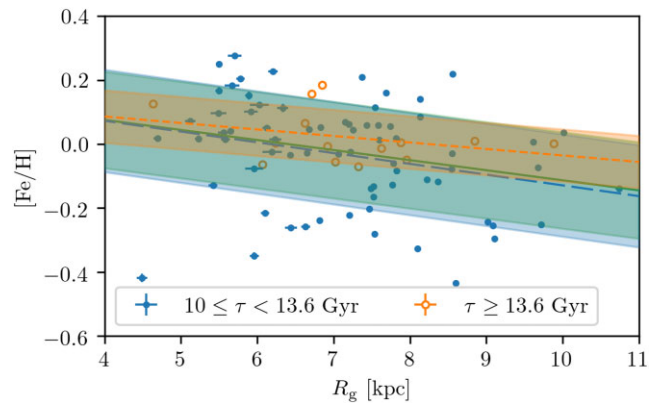


Figure 8. Results of the MCMC analysis for the oldest stars in our sample. The green line and filled region in the background show the result when including all stars with $\tau \geq 10$ Gyr, the long-dashed blue line and filled region (which are almost identical to the green) show the result of the analysis excluding stars with $\tau \geq 13.6$ Gyr, and the short-dashed orange line and filled region show the result based on only those stars.

the HBM overall. This could be a signature of the small radial extent and centrally concentrated star formation in that epoch of the MW. We also test whether the difference in these HBM results could be due to the larger uncertainty on the age of the older stars, but find that the effect is independent of the size of the age uncertainty.

There is a disagreement between these results and the intermediate age bins ($4 \leq \tau < 6$ Gyr and $6 \leq \tau < 10$ Gyr), with the HBM predicting a larger spread, which is driven by the assumption in the HBM of linear dependence on $\log(\tau)$ and the steep increase in spread at young ages.

The age prior in PARAM is deliberately wide and uninformative, which means our sample contains some stars with median age greater than 13.6 Gyr. Since the age posteriors are wide, we do not remove these stars from our analysis, but we confirm that they are not dominating the result in the oldest bin by analysing them separately (Fig. 8). We find that, though these stars do have a gradient that is significantly flatter than those with $10 \leq \tau < 13.6$ Gyr, the final fit in the bin is almost unaffected by their presence, being fully consistent to the result with the very old stars removed.

5.3 Possible sources of bias

In this work, we choose the guiding radius as our primary radial coordinate because it provides a robust estimate of the Galactocentric distance of the star over its whole orbit. For the same sample, this will naturally tend to flatten the radial metallicity gradient because we observe a limited range of R_{Gal} . In the inner Galaxy, it is only possible to observe stars with $R_g < R_{\text{Gal, min}}$ if they are eccentric enough that their apocentre radius $R_{\text{ap}} \geq R_{\text{Gal, min}}$. We cannot observe stars on circular orbits with the same R_g because they never enter our observable region, so we spread our sample over a wider range of radii, without increasing the range in metallicity. We show this in Appendix C, Figs C1 and C2, where for $\tau > 2$ Gyr we do find a steeper gradient with R_{Gal} . For $\tau < 2$ Gyr the effect is reversed, which is likely to be because the flattening effect of R_g is smaller due to the lower eccentricities of the younger population. The irregular distribution of the stars in R_{Gal} (Fig. C1) may then lead to a slight flattening of the gradient.

The equivalent argument can be made for stars with $R_g > R_{\text{Gal, max}}$ and pericentre radius $R_{\text{pe}} \leq R_{\text{Gal, max}}$, but in our sample the two

effects do not appear symmetrically: we have more stars with $R_g < R_{\text{Gal, min}}$ than $R_g > R_{\text{Gal, max}}$. The stellar density in the outer disc is lower, so we would see fewer of such stars in a spatially uniform sample, but we see roughly the same number of stars close to our radial limits ($R_{\text{Gal, min}} \approx 5.5$ kpc, $R_{\text{Gal, max}} \approx 10$ kpc). We can motivate the asymmetry by considering the probability of observing the ‘inner’ star ($R_g < R_{\text{Gal, min}}$) while it is passing through the observable region, compared to the ‘outer’ star. As an example, our sample contains one star with $R_g < 4$ kpc – i.e. which is observed more than 1.5 kpc away from its guiding radius. This means it has an eccentricity of $e \gtrsim 0.3$. An equivalent target in the outer disc with $R_g > 11.5$ kpc has $e \gtrsim 0.2$. Since low eccentricity stars dominate the population in the thin disc, it might seem surprising that we do not observe any stars with $R_g \gtrsim 10.5$ kpc. However, when we consider the probability of each star being in the part of its orbit where it is close enough to the solar position to be observable, as a fraction of its full orbit, we find that $P_{\text{obs, inner}} \approx 2P_{\text{obs, outer}}$. Given the small numbers involved, this is enough to explain the asymmetry in our sample.

Working in R_g may also introduce a kinematic bias since higher eccentricity stars tend to be older and thus more metal poor. This could mean that we miss higher metallicity stars at low R_g and recover an overly flat gradient. Examining Fig. 4, this does not appear to be the case, but as a test we repeat the HBM analysis, removing targets with $R_g < 5.5$ kpc. The result is shown in Fig. C3, where we see a slightly steeper gradient for stars older than 2 Gyr, but it is still fully consistent with the results from the full sample within the uncertainties.

5.4 Comparison to literature

In this section, we compare the results of our analysis to those from other studies based on field stars, Cepheid variables, and OCs, as well as theoretical models.

5.4.1 Field stars and Cepheid variables

Below we compare only to works with ages that are ‘directly’ inferred, either from comparison to isochrones or asteroseismology, similar to those used in this work. A comparison to the numerous age estimates available from machine learning methods is beyond the scope of this work, and will be completed in a later study.

Nordström et al. (2004) and Casagrande et al. (2011) investigated the radial metallicity gradient in the Geneva–Copenhagen Survey (GCS). The large sample of local solar neighbourhood F and G dwarfs extends to ≈ 0.4 kpc from the solar position and has metallicity determinations based on Strömgren photometry and ages obtained from comparison to isochrones. Though the precision of the ages is around 25 per cent, they are subject to significant uncertainties arising from the calibration of the metallicity and temperature scales. The sample is dominated by young stars ($\tau \approx 2$ Gyr) due to the magnitude limits of the survey and its local volume, and between the works of Nordström et al. and Casagrande et al. the ages of many stars change by ≈ 1 Gyr as a result of changes to these calibrations.

Nordström et al. (2004) use the mean radius $R_m = 0.5 \times (R_{\text{ap}} + R_{\text{pc}})$, extending their radial range to $6 < R_m < 9$ kpc, and find a gradient of -0.076 ± 0.014 dex kpc^{-1} for stars younger than 1.5 Gyr, and a steeper gradient of 0.099 ± 0.011 dex kpc^{-1} in an intermediate age population of $4 < \tau < 6$ Gyr. Their oldest population ($\tau > 10$ Gyr) is consistent with no gradient (0.028 ± 0.036 dex kpc^{-1}) and they suggest that this indicates that these stars are not thin disc members. We discuss the stars older than 10 Gyr present in our sample in Section 5.2.

Casagrande et al. (2011) improved on the age estimates of Nordström et al. (2004) and re-analysed the GCS sample to find a metallicity gradient with both R_m and R_g . They found a similar trend of a steeper gradient at intermediate ages than for the youngest stars, before flattening with age to a positive gradient in the older population. Their gradient with R_m is $0.05\text{--}0.01$ dex kpc^{-1} less (in the sense of flattening a negative gradient) than Nordström et al. across the age range, and the main effect of switching to R_g is to soften the trend towards a steeper gradient at intermediate ages so that it is nearly flat.

Anders et al. (2017b) used a sample of around 400 red giants observed by *CoRoT* (from which they obtain asteroseismic age constraints) and APOGEE, with $6 < R_{\text{Gal}} < 13$ kpc and $|Z_{\text{Gal}}| < 0.3$ kpc. After applying a correction for the selection function (derived from comparison to a chemo-dynamical simulation) they find a gradient with R_{Gal} of $-0.058 \pm 0.008 \pm 0.003$ dex kpc^{-1} (statistical and systematic uncertainty) for $\tau < 1$ Gyr, steepening to $-0.066 \pm 0.007 \pm 0.002$ dex kpc^{-1} between 1 and 4 Gyr, before flattening to ≈ 0.03 dex kpc^{-1} between 6 and 10 Gyr.

Finally, Xiang et al. (2015), Wang et al. (2019), and Vickers, Shen & Li (2021) used large samples of main-sequence turn-off and subgiant stars (0.3 million, with $8 < R_{\text{Gal}} < 11$ kpc; 0.94 million, with $7 < R_{\text{Gal}} < 11$ kpc; and 1.3 million, with $6 < R_g < 10$ kpc, respectively) observed by LAMOST, with ages determined from isochrone comparisons. Xiang et al. and Wang et al. selected stars in slices of $|Z_{\text{Gal}}|$ and investigated the gradient with R_{Gal} . For stars close to the plane, both find the steepest gradient at intermediate ages (6–8 Gyr in Xiang et al. and 4–6 Gyr in Wang et al.), with younger and older stars showing shallower gradients. The gradients of Wang et al. are consistent with our results for the youngest and oldest stars, and steepen to ≈ -0.1 dex kpc^{-1} in between. Vickers et al. (2021) select stars with low Z_{max} and α -abundance (similar to the procedure in this work) and find that the gradient with R_g flattens monotonically with age. Their results agree very well with this work at all ages.

Though most of the results described above agree with each other, and this work, within a few σ , they fall into two groups according to how the gradient varies with age. In this work and in Vickers et al. (2021) the gradient flattens smoothly stellar age, while the other studies show a steeper gradient in intermediate-age stars of $\tau \approx 4$ Gyr than in the younger population (though this is least obvious in the R_g case of Casagrande et al. 2011). Comparisons are complicated by the different selection functions of each sample, but below we consider two other possible causes of this difference: the degree to which the population is contaminated by thick disc stars, and the choice of radial coordinate.

Considering first the contamination by thick disc stars, we refer to the works of Anders et al. (2014) (using R_g and Z_{max}) and Hayden et al. (2014) (using R_{Gal} and Z_{Gal}), in addition to Xiang et al. (2015), Wang et al. (2019), and Vickers et al. (2021), on the vertical dependence of the metallicity gradient. They all found that the radial metallicity gradient flattens with height above the Galactic plane. Including these thicker disc stars could, therefore, flatten the overall gradient. This effect would be especially important in the younger population because the intrinsic scatter is low and, when working in R_g or R_m , because the radial extent tends to be reduced due to the generally low eccentricities compared to the older stars. We show the effect of including stars with higher Z_{max} in Appendix B, where Fig. B1 shows a flatter gradient in the youngest age bin, more similar to previous studies, and Vickers et al. also recover this effect for intermediate Z_{max} ($0.25 < Z_{\text{max}} < 0.75$ kpc). Though the contamination of the GCS sample is likely to be small due to its small range in R_{Gal} and Z_{Gal} , a few stars passing through the thin disc

could be enough to cause this effect. The range of the Anders et al. (2017b) sample is larger and the selection for thin disc members is based on Z_{Gal} , so stars on kinematically hot orbits that are currently close to the plane of the disc are still included. Since the studies of Anders et al. (2014) and Hayden et al. (2014) do not include age information, it is difficult to be sure that the flattening of the gradient in their results is driven by the distance from the plane, rather than an effect of the shift to older age distributions at a greater distance from the disc. However, Xiang et al. (2015), Wang et al. (2019), and Vickers et al. (2021) show this effect across a range of ages, and it will be investigated in our sample in a future study.

The choice of radial coordinate may also play a role: as described in Section 5.3, we would naively expect the change from R_{Gal} to R_{g} to flatten the observed metallicity gradient. We show the results of our analysis using R_{Gal} in Appendix C, where, for stars older than 3 Gyr, we do indeed see a steeper gradient. However, the gradient in the younger population is steeper in the R_{Gal} results, reproducing the effect seen in GCS and the works of Xiang et al. (2015), Anders et al. (2017b), and Wang et al. (2019). As mentioned above, almost all of these stars have very low eccentricity, so the flattening effect of using R_{g} would be reduced, and it is possible that the uneven radial distribution (Fig. C1) in this small sample results in a steeper gradient overall.

Cepheid variables are good tracers of the present-day metallicity gradient as they provide a long radial baseline for targets that are 20–400 Myr old. Genovali et al. (2014) compiled a sample of 450 Cepheids with $4 < R_{\text{Gal}} < 19$ kpc and found a gradient of -0.05 and -0.06 dex kpc^{-1} , depending on the sample used and the cut in Z_{Gal} applied, which is consistent with our MCMC results for the bin containing the youngest stars.

5.4.2 Open clusters

There are many studies in which the radial metallicity gradient is constrained by observations of OCs (e.g. Magrini et al. 2009; Casamiquela et al. 2017, 2019; Spina et al. 2021, 2022; Myers et al. 2022; Netopil et al. 2022; Gaia Collaboration 2023b). Here we mention just three recent examples, which benefit from advances in high-resolution spectroscopy, and both astrometry (for improving membership determination) and all-sky spectral analysis from *Gaia*.

Myers et al. (2022) use a sample of 85 OCs from the Open Cluster Chemical Abundances and Mapping (OCCAM) survey, based on APOGEE DR17 abundances, with a radial range of $6 < R_{\text{Gal}} < 16$ kpc. They find a break in the radial metallicity relationship at around 12 kpc, recovering a gradient of -0.073 ± 0.002 dex kpc^{-1} inside and -0.032 ± 0.002 dex kpc^{-1} outside this radius.

Netopil et al. (2022) use 136 OCs compiled from various surveys and find that the relationship is well fit by a single line with gradient -0.058 dex kpc^{-1} over a similar radial range in R_{Gal} . Their results are supported by photometric observations of a further 10 clusters, and they suggest that the appearance of a break in the relationship as seen in Myers et al. (2022) is strongly dependent on the specific objects included in the study, as well as the adopted distance scale.

Both these studies suffer to some extent from a fairly limited sample size, particularly in resolving the question of a break in the relationship. Spectral analysis from *Gaia* may now start to resolve this, for example, Gaia Collaboration (2023b) have a sample of 503 clusters. However, they restrict their analysis of the metallicity gradient to $R_{\text{Gal}} < 12$ kpc, so do not probe the region in question. They find a gradient of -0.063 ± 0.008 dex kpc^{-1} with R_{g} in the inner disc.

Investigating the evolution of the radial metallicity relationship with OCs presents an additional challenge, as the small samples must be broken into bins with few data in each, and the age range is restricted to a few Gyr at most. Gaia Collaboration (2023b) and Netopil et al. (2022) divide their samples into 4 and 5 age bins, extending up to ≈ 5 and ≈ 7 Gyr, respectively. In both cases, the gradient is found to increase as a function of age: the opposite of the trend observed in field stars. As proposed by Anders et al. (2017b) and Spina et al. (2021), this effect could be due to a survival bias for OCs, as high-metallicity clusters born in the inner disc are more likely to survive if they migrate outwards to Galactic regions where the potentials of the spiral arm and bar are weaker (see also Lynga & Palous 1987). Low-metallicity clusters from the outer disc that migrate towards the Galactic Centre are more likely to be disrupted and are, therefore, missing in the older population, which shows a steeper gradient as a result. We show the clusters used in the work of Myers et al. (2022) in Fig. 9 because they use the same chemical abundances as employed in this work. The metallicity offset can be clearly seen in the $6 \leq \tau < 10$ Gyr bin.

5.4.3 Models

Fig. 9 also shows a comparison to the chemo-dynamical simulation of Minchev et al. (2013, 2014, hereafter MCM) and the underlying chemical evolution model (Chiappini 2009). There is a great diversity of chemical evolution models and simulations (e.g. Schönrich & Binney 2009a,b; Grand, Kawata & Cropper 2015; Kubryk, Prantzos & Athanassoula 2015a,b; Grisoni et al. 2017; Grisoni, Spitoni & Matteucci 2018; Vincenzo & Kobayashi 2020; Spitoni et al. 2021) and we choose the MCM simulation to facilitate easy comparison with the works of Anders et al. (2017b), Casamiquela et al. (2017, 2019), and Myers et al. (2022). The model was computed in instantaneously mixed galactocentric annuli 2 kpc wide, and for this plot we interpolate between those annuli and transform from R_{Gal} to R_{g} . The metallicity is scaled to reproduce the solar value at approximately the time and location of the Sun’s birth (≈ 4 Gyr ago and $R_{\text{Gal}} \approx 6$ kpc; Minchev et al. 2013). To allow a qualitative comparison to our results, the particles from the MCM are restricted to those with $Z_{\text{Gal}} < 1$ kpc, since the scale height of the simulated disc is larger than the MW’s thin disc.

Our results are reasonably consistent with the chemical evolution model and MCM simulation at ages below ≈ 4 Gyr. In the older populations, the simulated particles show a more rapid flattening of the gradient, and an offset towards lower metallicities in the model becomes more apparent. This is likely due to the initial conditions of the model, as the thin disc is not pre-enriched in metals, giving a very metal-poor result at ages close to the start of disc formation. Our results, which are not subject to the metallicity bias that affects the older OCs, demonstrate that this very low metallicity is not a good representation of the thin disc’s early state, and this effect is shown more clearly in comparison to the individual stars in our sample in Fig. 10.

6 CONCLUSIONS

We have used the wide spatial and temporal coverage of the K2–APOGEE sample to study the evolution of the MW’s radial metallicity gradient in the range $4 < R_{\text{g}} < 11$ kpc across the whole history of the thin disc. We find a gradient that flattens monotonically from ≈ -0.07 dex kpc^{-1} in stars of $\tau \approx 0.7$ Gyr to ≈ -0.04 dex kpc^{-1} at $\tau \approx 12.6$ Gyr. The intrinsic spread around this gradient, which is primarily

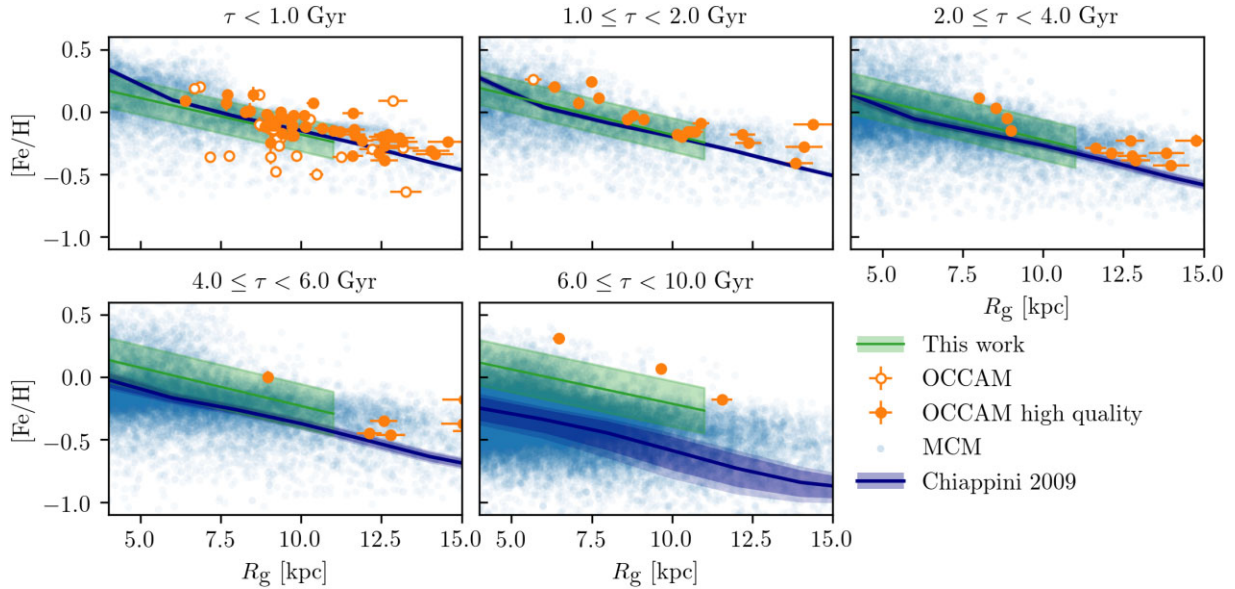


Figure 9. $[\text{Fe}/\text{H}]$ versus R_g in five bins of age. The orange and white points show the high-quality and plausible samples from the OCCAM survey (Myers et al. 2022), respectively. The blue points are the results of the MCM chemo-dynamical simulation (Minchev et al. 2013, 2014), with the underlying chemical evolution model of Chiappini (2009) shown by the blue line and filled region. The green line shows the best-fitting radial metallicity gradient from the MCM analysis of this work, with a filled region representing 1σ of the intrinsic spread.

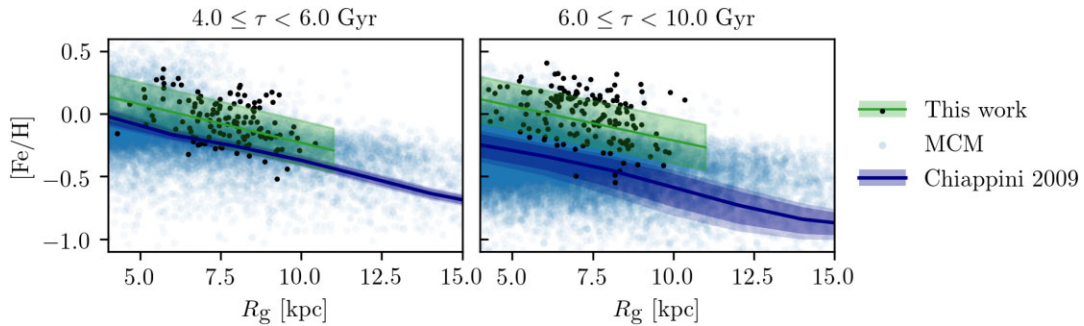


Figure 10. Same as Fig. 9, but for two age bins with the thin disc sample shown in black points, binned according to the median age of each star.

caused by churning, increases with the age of the population until $\tau \approx 10$ Gyr. In older stars, the spread is slightly reduced, which we attribute to this population forming before the thin disc when star formation in the MW was very centrally concentrated. We also find that the metallicity of the solar neighbourhood has increased slightly over the last 5 Gyr to ≈ -0.04 dex, and that it is subsolar throughout the history of the disc, indicating that the Sun migrated out from its birth radius to current position.

We have compared our results to other studies of field stars and explained the differences in our results in terms of the more robust selection of thin disc members and choice of guiding radius as the radial coordinate used in this work. We have also compared to recent studies of OCs and have shown that older clusters appear to be subject to a survival bias, favouring those of higher metallicity. Finally, we have provided a qualitative comparison to the chemical evolution model of Chiappini (2009) and the chemo-dynamical simulation of Minchev et al. (2013, 2014). The most striking difference to our results is their much lower metallicity at ages above ≈ 6 Gyr, which we attribute to the assumptions about the initial conditions in the model. Our results will facilitate new tests of the initial conditions and physics in models and simulations of MW evolution.

In the next decade the ESA *PLANetary Transits and Oscillations of stars (PLATO)* mission (Rauer et al. 2014) can potentially provide ages with 10 per cent precision (Miglio et al. 2017) for a large sample of red giants. These data, combined with astrometry and spectroscopy from ongoing and planned surveys, will allow the early evolution of the MW discs to be probed in detail and give a more precise measurement of the evolution of the metallicity gradient. These insights will throw new light on the open questions concerning the origin, strength, and importance of radial migration in the Galactic archaeology fossil record.

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Software used: ARVIZ (Kumar et al. 2019), ASTROPY (Astropy Collaboration 2013, 2018, 2022), CORNER (Foreman-Mackey 2016), EMCEE (Foreman-Mackey et al. 2013), GALPY (Bovy 2015), JAX (Bradbury et al. 2018), MATPLOTLIB (Hunter 2007), NUMPY (Harris et al. 2020), NUMPYRO (Bingham et al. 2019; Phan et al. 2019), PANDAS (Wes McKinney 2010; The pandas development team 2020), SCIPY (Virtanen et al. 2020), and TOPCAT (Taylor 2005). We also acknowledge the use of the DAFT package to produce figures in this work (<https://docs.daft-pgm.org/en/latest/>).

DATA AVAILABILITY

The data underlying this paper will be shared on reasonable request to the corresponding author.

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APPENDIX A: EFFECT OF [Fe/H] ERROR INFLATION

As described in Willett et al. (in preparation), during the PARAM runs to constrain the stellar parameters used in this work, the uncertainty on [Fe/H] from APOGEE DR17 was inflated to 0.05 dex for all stars with a reported uncertainty below this value. In our subsequent analysis of the metallicity gradient, we use the published values of uncertainty, but here we show the results obtained from the HBM if we follow the same inflation procedure. The evolution and uncertainties for the gradient and offset are almost unchanged from our original analysis and are not shown here, and Fig. A1 shows that, though the intrinsic spread is slightly decreased, it is still fully consistent within uncertainties.

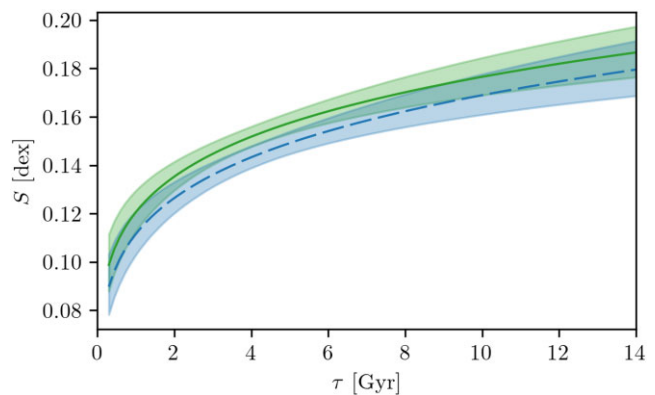


Figure A1. The [Fe/H] component of the intrinsic spread constrained by our HBM using the published [Fe/H] uncertainties (green) or inflating them as in Willett et al. (in preparation, dashed blue).

APPENDIX B: SENSITIVITY TO THE Z_{\max} CUT

In this section, we show the sensitivity of our results to the cut in Z_{\max} used to identify thin disc members. Fig. B1 summarizes the results of the MCMC and HBM analysis under different conditions. The gradient (top panel) recovered with a wider ($Z_{\max} \leq 1.0$ kpc) or narrower ($Z_{\max} \leq 0.3$ kpc) range of Z_{\max} is consistent with our original analysis within the uncertainties. Decreasing the Z_{\max} range does not significantly change the [Fe/H] offset at 8 kpc (middle panel), but the result from the wider cut shows significantly lower metallicity. This is consistent with the wider range of metallicities in this sample (Fig. B2). The intrinsic spread (bottom panel) of the three samples is more sensitive to the Z_{\max} cut, but the relationship between the MCMC and HBM result is the same in a given sample.

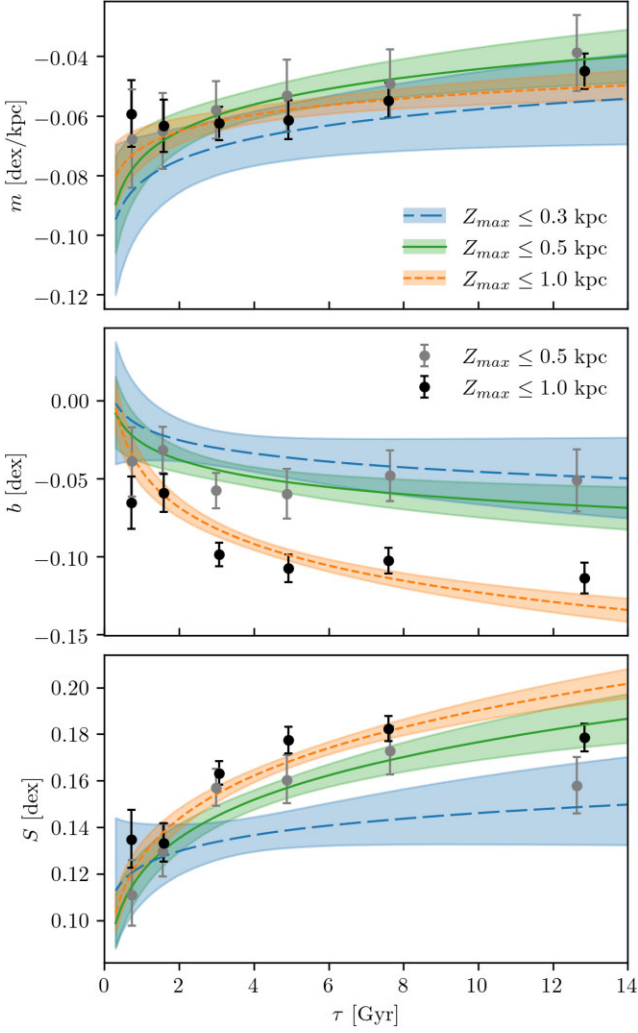


Figure B1. Evolution of the fit parameters as a function of stellar age. The grey points and green line and filled region show the best-fitting value and 68 per cent credible interval in each bin from the MCMC analysis (plotted against the median age of the population in the bin) and the result and 68 per cent credible interval from the HBM from the original analysis. The black points and short-dashed orange line and filled region show the same but for a sample including stars with a wider range of Z_{\max} . The long-dashed blue line and filled region show the HBM result for a narrower Z_{\max} range.

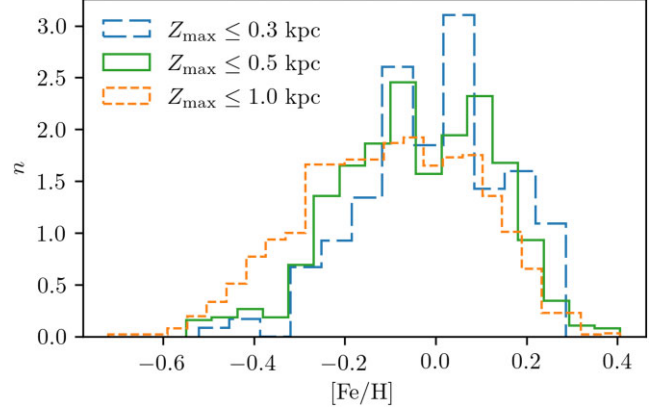


Figure B2. [Fe/H] distributions for samples including stars with a wider (short-dashed orange) or narrower (long-dashed blue) range of Z_{\max} than the original analysis (green). The area under each histogram integrates to one.

APPENDIX C: EFFECT OF R_g OR R_{Gal}

In this section, we provide further detail on the sensitivity of our results to the radial coordinate and range used in the analysis.

First, we show the results of our analysis using R_{Gal} rather than R_g . Fig. C1 shows the results in bins of age, where the uneven radial distribution caused by the K2 field placement can be clearly seen. Fig. C2 summarizes the results from the MCMC and HBM analysis, where in general all parameters agree within their uncertainties. The exception is the HBM result for the [Fe/H] offset at 8 kpc, which is likely a result of the populations clumping up in R_{Gal} .

We also test the sensitivity of our result to stars with $R_g < R_{\text{Gal, min}}$ (see Section 5.3 for details). Excluding these stars does result in a slightly steeper gradient at $\tau > 1$ Gyr, but the two results are consistent within uncertainties (Fig. C3). The offset and intrinsic spread are almost unchanged in the new samples and are not shown here. This indicates that our results are not biased by the choice of R_g as the radial coordinate in our analysis.

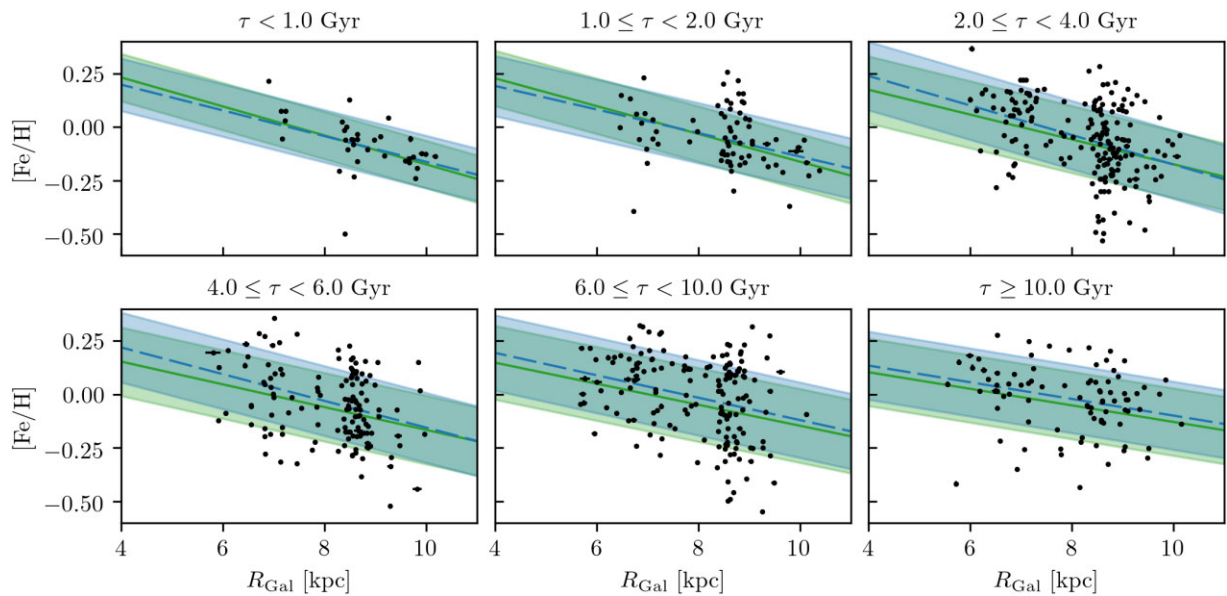


Figure C1. $[\text{Fe}/\text{H}]$ versus R_{Gal} in six bins of age. The thin disc sample is shown in black points, binned according to the median age of each star. The dashed blue line and filled region show the results from the MCMC analysis using R_{Gal} . For comparison, the green line and filled region show the results using R_{g} (plotted against R_{g}).

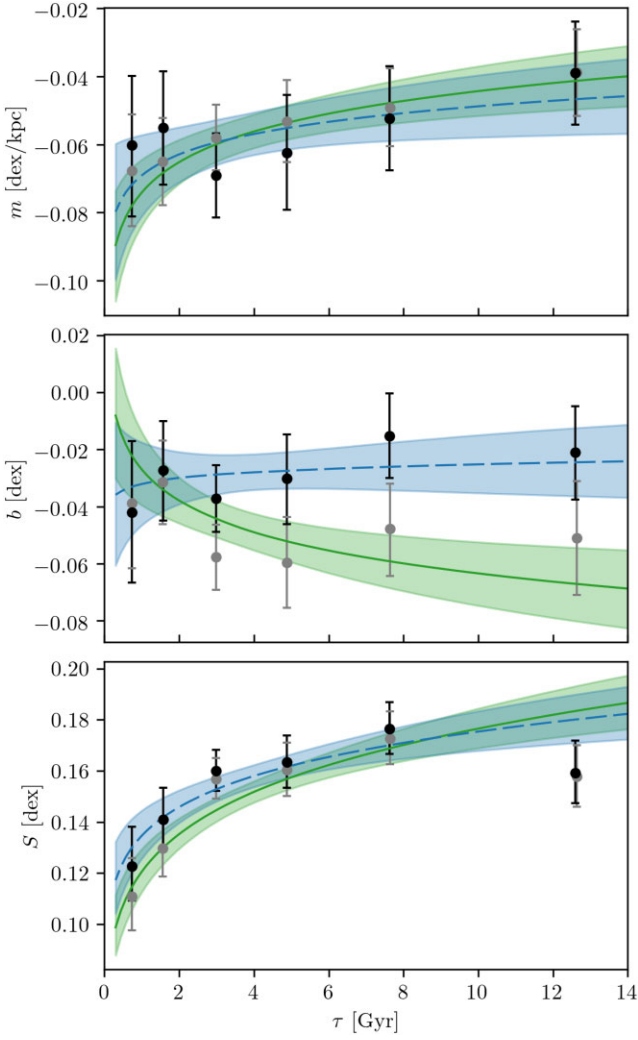


Figure C2. Evolution of the fit parameters as a function of stellar age. The grey points and green line and filled region show the best-fitting value and 68 per cent credible interval in each bin from the MCMC analysis (plotted against the median age of the population in the bin) and the result and 68 per cent credible interval from the HBM from the original analysis using R_g . The black points and dashed blue line and filled region show the same using R_{Gal} .

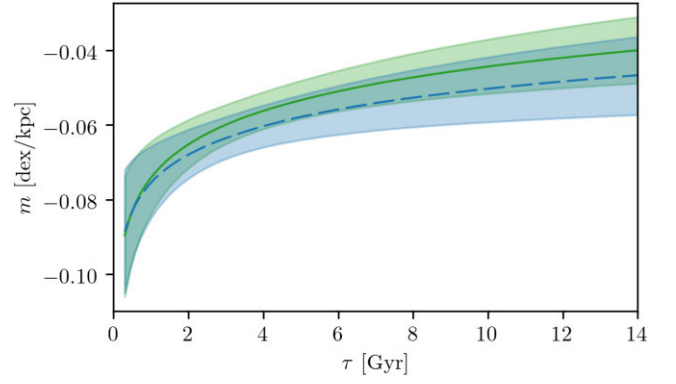


Figure C3. Evolution of the gradient with age for the full sample (green) and excluding stars with $R_g < R_{\text{Gal, min}}$ (dashed blue).

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