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1 CLASSIFICATION OF COW DIET BASED ON MILK MID
2 INFRARED SPECTRA: A DATA ANALYSIS COMPETITION
3 AT THE “INTERNATIONAL WORKSHOP OF
4 SPECTROSCOPY AND CHEMOMETRICS 2022”

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21 **Abstract**

22 In April 2022, the Vistamilk SFI Research Centre organized the second edition of the
23 “International Workshop on Spectroscopy and Chemometrics – Applications in Food and
24 Agriculture”. Within this event, a data challenge was organized among participants of the
25 workshop. Such data competition aimed at developing a prediction model to discriminate
26 dairy cows’ diet based on milk spectral information collected in the mid-infrared region. In
27 fact, the development of an accurate and reliable discriminant model for dairy cows’ diet can
28 provide important authentication tools for dairy processors to guarantee product origin for
29 dairy food manufacturers from grass-fed animals. Different statistical and machine learning
30 modelling approaches have been employed during the workshop, with different pre-processing
31 steps involved and different degree of complexity. The present paper aims to describe the
32 statistical methods adopted by participants to develop such classification model.

33 **Keywords:** Chemometrics, Fourier transform mid-infrared spectroscopy, machine learning,
34 milk quality, food authenticity

35 **1 Introduction**

36 The use of mid-infrared spectroscopy (MIRS) has become a relevant topic in agri-food sciences,
37 due to its capacity to routinely quantify a wide range of important characteristics rapidly and
38 cost-effective. In particular, MIRS is nowadays commonly employed to monitor and quantify

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39 milk quality parameters, such as concentrations of fat, protein, casein, and lactose. These
40 parameters are used for milk quality-based payment schemes, genetic and genomic selection,
41 and as farmers’ support tool. Spectral information generated from MIRS analysis have also
42 proven to be effective in predicting fine milk quality parameters, including protein fractions,
43 free amino acids [Bonfatti et al., 2011; McDermott et al., 2016], individual and groups of fatty
44 acids [Soyeurt et al., 2006; Fleming et al., 2017], milk processing traits [Ferragina et al., 2013;
45 Visentin et al., 2015], animal-related characteristics [McParland et al., 2014; Shetty et al., 2017;
46 Ho et al., 2019], and can be used as a tool for the verification of the authenticity of agricultural
47 foods [Cozzolino, 2012]. A more extended list of applications of MIRS in the dairy science
48 framework can be retrieved from the reviews by De Marchi et al. [2014] and Tiplady et al.
49 [2020].

50 The two-day event “*International Workshop on Spectroscopy and Chemometrics*” was orga-
51 nized by Vistamilk SFI Research Centre in April 2022, following its first edition held in 2021
52 [Frizzarin et al., 2021a]. The workshop focused on describing the main challenges and appli-
53 cations of near and mid-infrared spectroscopy in food, animal, and agricultural sciences with
54 internationally recognised researchers. Moreover, participants, on a voluntary basis, were pro-
55 vided with a large dataset containing individual cow milk spectra with the sole information on
56 animal’s diet for a chemometric data competition. Such data presented many challenges from
57 a methodological and statistical point of view, due to the high dimensionality of the spectral
58 matrices, and strong collinearity between adjacent spectral wavelengths. The chemometric chal-
59 lenge, therefore, encouraged the engagement of participants with different background and skills
60 and required the application of different statistical and machine learning strategies.

61 The purpose of the data challenge was to develop a model to predict the diet fed to dairy
62 cows by exploiting mid-infrared spectral information. Participants, or groups of participants,
63 were required to apply their developed model to a test set containing only individual milk spectra
64 and to submit their prediction of animals’ diet. Although the participation to the chemometric
65 challenge was extremely high among participants, only the best six contributions, in terms of
66 accuracy of prediction and methodological innovativeness, were selected to present their results
67 both at the workshop and in the present manuscript.

68 2 Data description and challenge

69 A dataset consisting of 4,364 individual milk spectra from 120 cows was collected between May
70 and August in 2015, 2016 and 2017 [O’Callaghan et al., 2016]. The samples were from Hol-
71 stein Friesian cows with different parity from Irish Dairy Research Herd in Teagasc Moorepark,
72 Fermoy, Co. Cork. Three dietary groups were evaluated with 54 cows being assigned to each di-
73 etary group each year. The three diet treatments were grass (GRS) which consisted of perennial
74 ryegrass only, clover (CLV) which consisted of perennial ryegrass with 20% annual clover sward,
75 and total mixed ration (TMR) where cows were fed grass silage, maize silage and concentrates
76 while being maintained indoors for the full season. Milk samples were collected in the morning
77 (AM) and evening (PM) milking session; subsequently AM+PM samples were pooled and anal-
78 ysed weekly using Pro-FOSS FT6000 (FOSS). A total of 1060 transmittance data points in the
79 region from 925 cm^{-1} to $5,000\text{ cm}^{-1}$ were collected.

80 The dataset was divided into training (3275 spectra) and test (1089 spectra) data; for the
81 latter only spectral information was provided, while diet information, to be used as a classifi-
82 cation variable, was available for the training set. The training data included 1094 spectra for
83 GRS, 1120 spectra from CLV and 1061 spectra for TMR. There were no missing values in the
84 training or test set. The specific information about the wavenumbers had not been shared with
85 the participants.

86 The three dietary groups were carefully selected based on their characteristics. As described
87 by Frizzarin et al. [2021b], pasture-based diets are easily discriminated from TMR diets, while

88 discriminating between GRS and CLV diets is much more difficult due to the similarities in the
89 sward composition resulting in similar milk composition. However, with the increased pressure
90 to reduce fertilizer use, and the introduction of multi-species swards, the development of a robust
91 discriminant model for classifying milk spectra based on diet is of paramount importance.

92 After the analysis, the participants submitted their predicted values for the test dataset and
93 a short explanation of the methodology used. The best methods were selected based on the
94 novelty of the contribution and on the accuracy of the predictions for the test dataset. The
95 accuracy was calculated as the proportion of the correctly classified samples divided by the total
96 number of samples in the test dataset.

97 3 Modelling approaches and results

98 3.1 Participant 1

99 The data were analyzed following different modelling strategies, focusing both on methods that
100 considered the ordering of the wavelengths and on methods that do not. All the analyses have
101 been mainly conducted using Python libraries `pandas`, `sklearn`, `sktime` and `matplotlib` [see
102 [Pedregosa et al., 2011](#), and references therein]: the code is available at [https://github.com/
103 mlgig/vistamilk_diet_challenge](https://github.com/mlgig/vistamilk_diet_challenge).

104 As a first step, some descriptive statistics were computed, and the outliers have been removed,
105 following both the recommendations given prior to the competition and a visual inspection of the
106 data. In the subsequent step, the labeled dataset was split according to a 3-fold cross-validation
107 (3CV) strategy. Therefore, the best model was selected based on cross-validation accuracy, and
108 then trained on the full training set and used to perform prediction on the provided unlabeled
109 test set.

110 In order to predict the diet, the following classification strategies were considered:

- 111 • **Tabular models:** each sample is considered as a vector of unordered features. In particu-
112 lar, Ridge Classifier and Linear Discriminant Analysis (LDA) were tested. In the following,
113 these methods were coupled both with feature selection strategies and with random polynomial
114 feature transformations. The latter approach, by generating new polynomial variables
115 from the original ones, aimed to check if non-linear interactions improved the classification
116 accuracy. In particular, a new approach is presented which aimed to diversify polynomial
117 features while keeping low computational requirements.
- 118 • **Deep Neural Network Models:** a family of approaches based on deep neural networks,
119 both fully connected and convolutional, were tested. This strategy implicitly generates
120 complex features interactions, as captured by the network architecture.

121 Note that previously obtained results [[Frizzarin et al., 2021a](#)] suggest that tabular methods
122 work quite well with spectroscopy data. Moreover, following the suggestions in [Frizzarin et al.
123 \[2021b\]](#), feature selection strategies were coupled with the information about the presence of
124 water regions in the spectra. In addition, state-of-the-art time series classification algorithms,
125 such as ROCKET [[Dempster et al., 2020](#)], MiniROCKET [[Dempster et al., 2021](#)], MrSQM
126 [[Nguyen and Ifrim, 2021, 2022](#)] and FreshPrince [[Middlehurst and Bagnall, 2022](#)], were tested.
127 Lastly, *ensemble methods* were applied, aiming to mix together time series and tabular models, to
128 combine their predictions and strengths. Nonetheless, these approaches have been outperformed
129 by the ones mentioned above, therefore the corresponding results are not shown in the next
130 sections.

131 3.1.1 Tabular models, feature selection and transformation

132 In Table 1, results for the best tabular methods are presented. Both the ridge classifier, appro-
133 priately tuned, and LDA performed quite well, while being extremely fast to train. Nonetheless,

Table 1: Accuracy results, evaluated on the 3-fold cross-validation, for the tabular methods considered, coupled with feature selection strategies.

Method	Accuracy
Ridge Classifier	0.760
LDA	0.747
Feature Selection + Ridge Classifier	0.777
Feature Selection + LDA	0.778
No water + Ridge Classifier	0.777
No water + LDA	0.783
Feature Selection + Polynomial Features + LDA	0.844
No water + Feature Selection + Polynomial Features + LDA	0.844



Figure 1: LDA visualisation for the model *Feature Selection + Polynomial Features + LDA*, applied to the unlabeled test data to predict class labels.

134 the selection of some specific wavelengths seemed to improve the accuracy further. In fact, both
 135 the removal of the noisy water regions and the data-driven feature selection (performed using
 136 the `SelectFromModel` routine in Python), provides better results.

137 Nevertheless, all these approaches hover around 80% accuracy, therefore, in order to improve
 138 it, the data were augmented considering polynomial features of degree two (using `sklearn`
 139 method `PolynomialFeatures(degree = 2)`). This led to an increase of the accuracy to 84.4%.
 140 The LDA component visualisation for the model with Feature Selection and Polynomial Features,
 141 applied on the unlabeled test dataset, is shown in Figure 1 and a good discrimination between
 142 the three classes is clearly visible.

143 The improvements obtained when considering polynomial features, come at a price in terms
 144 of the computational requirements. In fact, starting from the 1060 original wavelengths, the
 145 addition of second-degree polynomial features resulted in a total number of variables which
 146 made the model estimation task unfeasible. To address this issue, in this work a new *Random*
 147 *Polynomial Features* (`RPolyTransformer` in the following) approach was introduced. The key
 148 idea was to implement random sampling in the non-linear feature space. This led to relevant
 149 advantages as the total number of features can be controlled and it can consider both higher-
 150 degree (> 2) polynomial features and complex mathematical functions (e.g., cosine, exp).

151 This strategy firstly generated K random arithmetic expressions (see Table 2 for some ex-
 152 amples), which are then used to compute K non-linear features. From the new and the original

Table 2: Examples of *RPolyTransformer* features used. Here x_j denote the j -th wavelength.

$$\begin{aligned} &(x_{32} * x_{19}) + x_{103} - x_2 \\ &(x_{102} * (x_{78}) + x_{26}) \\ &(x_1 - x_{150}) + x_{64} * x_4 * x_5 \end{aligned}$$

Table 3: Results for different combinations with *RPolyTransformer*. *SelectFromModel* and *SelectKBest* are feature selection modules to remove noise from data (the former) and select the most discriminative non-linear features (the latter).

Method	Accuracy
Region: FULL	
RPolyTransformer + Ridge Classifier	0.717
RPolyTransformer + LDA	0.619
SelectFromModel + RPolyTransformer + SelectKBest + LDA	0.848
Region: [925:1585, 1720:2989]	
RPolyTransformer + Ridge Classifier	0.805
RPolyTransformer + LDA	0.847
SelectFromModel + RPolyTransformer + SelectKBest + LDA	0.843
Region: [925:1585, 1720:2989, 3738:3807]	
RPolyTransformer + Ridge Classifier	0.811
RPolyTransformer + LDA	0.833
SelectFromModel + RPolyTransformer + SelectKBest + LDA	0.835
Optimized model	
Region: [925:1585, 1720:2989]	
RPolyTransformer($K = 17000$) + SelectKBest($K^* = 7000$) + LDA	0.864

153 features, K^* variables are selected using *SelectKBest* from *sklearn*. The hyperparameters K
 154 and K^* were optimized via cross-validation in the final model (see the final row of Table 3).

155 In Table 3 the results obtained with this method, again combined with different classifiers and
 156 feature selection approaches and tested with the full data and the data after water region removal,
 157 are presented. At first, when combining *RPolyTransformer* with a classifier, a significant drop
 158 in the accuracy was observed, if compared with simple tabular models. Ridge was more accurate
 159 than LDA but it was still far behind the previous results. However, by carefully filtering the
 160 features either automatically with *SelectFromModel* or manually by removing the water regions,
 161 the results improved noticeably. In these experiments, LDA outperforms Ridge consistently.
 162 Compared to the *PolynomialFeatures* method, the one proposed here is faster (a few seconds
 163 versus a few minutes) and just as accurate. However, the initial results without noise reduction
 164 (i.e., feature selection) suggest that this strategy is more sensitive to noise in the data.

165 3.1.2 Deep Learning Models

166 When considering deep learning models, the task of exploding the feature space and learning
 167 feature interactions is completely deferred to the network, without requiring any feature engi-
 168 neering steps. In turn, deep neural networks require a careful design process, to avoid overfitting
 169 and to identify the best model architecture and input modality.

170 The designed model architectures considered here can be grouped into two main categories,
 171 namely, Fully Connected Networks (FCNs) and Convolutional Neural Networks (CNNs). FCNs
 172 do not require any manipulation or adaptation of the input data, as each single wavelength
 173 is treated as an independent feature and fed to an input unit. In contrast, CNNs require the

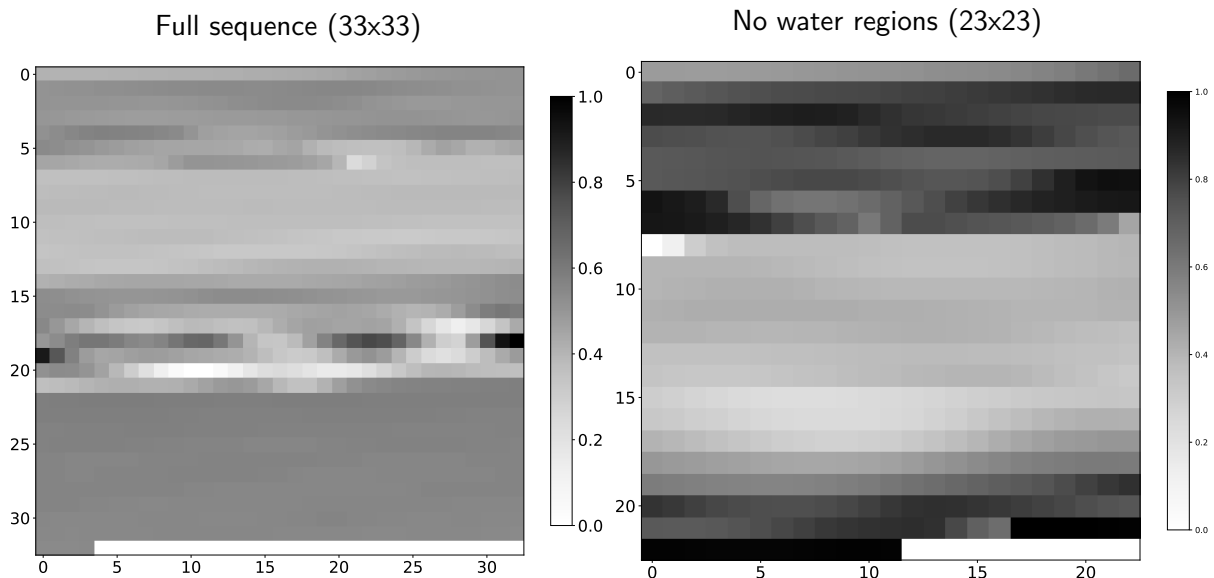


Figure 2: Spectroscopy sequences arranged as image structures. In both examples, the padding values are visible at the bottom of the resulting images. Values are normalised in the 0-1 range for convenience.

174 data to be bi-dimensional, image-like matrices, as they are commonly used to address image
 175 classification problems. For this family of networks, the input waves need then to be vertically
 176 stacked as 2D arrays and therefore, in order to fit the closest squared dimension, padded with
 177 trailing zeros. An example of how the spectroscopy sequences can be presented to the CNNs is
 178 provided in Figure 2. Additionally, a third group of models is tested for this challenge, namely,
 179 CNNs based on dilated kernels (further denoted as CNN_DILATED). Whilst regular CNNs
 180 extract features through compact squared filters, or local receptive fields, the CNN_DILATED
 181 network utilizes filters that are spatially dilated by a fixed factor [Yu and Koltun, 2015]. Dilated
 182 kernels are commonly used in semantic image segmentation.

183 All the models in this group were trained on both the full training dataset and on the water
 184 reduced one. When the CNN models were trained, the full data were shaped into images of
 185 shape 33x33 with a padding of 29 values, while the reduced data were shaped into images of
 186 shape 23x23 with a padding of 11 values. As already mentioned, all padding values were zeros,
 187 and they were appended to the original sequences.

188 The full list of the implemented architectures is presented in Table 11 in Appendix A.1. The
 189 experiments were conducted on the previously described 3-fold cross-validation splits; note that,
 190 for each split, 20% of the training data was held back for validation purposes, to identify network
 191 hyperparameters such as number of training epochs, initial learning rate, or regularisation rates.
 192 Models were trained for a total of 50,000 epochs, with an early stopping policy used to monitor
 193 the validation loss to detect overfitting and save time during the training phase. The final
 194 model used to classify the provided unknown data was selected as the overall best performing
 195 architecture, and trained over the full training data for a number of epochs set as the average
 196 of the epochs reached during the 3CV training.

197 All models were implemented using TensorFlow [Abadi et al., 2016], and trained on a work-
 198 station featuring a single GPU, model Nvidia Titan XP. Results are presented in Table 4, which
 199 contains the training performances obtained over the 3-folds CV experimental campaign. For
 200 all the tested architectures, excluding the water regions from the input waves resulted in a
 201 performance increase of roughly 12-13%. The FCN model working on data after water-region
 202 removal, achieved the highest accuracy across the 3 splits, with an average of 84.7%. Simi-
 203 lar unreported results were obtained also considering a single split validation strategy, which
 204 furthermore demonstrated that convolutional models tend to overfit the input data quite fast.

Table 4: Training results on the 3CV splits.

Model	Data	Split 1	Split 2	Split 3	Average
FCN	FULL	0.670	0.677	0.675	0.674
	NO WATER	0.854	0.851	0.837	0.847
CNN	FULL	0.686	0.684	0.670	0.680
	NO WATER	0.806	0.836	0.832	0.824
CNN_DILATED	FULL	0.678	0.684	0.652	0.671
	NO WATER	0.824	0.812	0.807	0.814

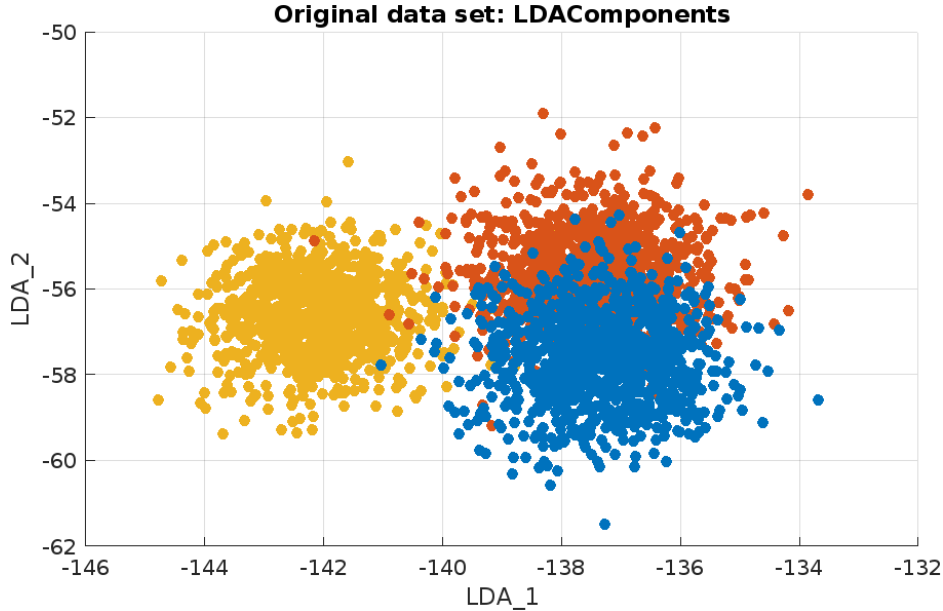


Figure 3: LDA components extracted from the developed model.

205 3.2 Participant 2

206 All the processing steps and the algorithm implementation was completed using MATLAB [MAT-
 207 LAB, 2018]. After having imported the dataset in tabular form, the outliers were identified as
 208 those observations with more than three scaled median absolute deviations from the median
 209 of the dataset. Classification was performed using a set of algorithms such as Support Vector
 210 Machine (SVM), K-Nearest Neighbors (KNN) and Linear Discriminant Analysis (LDA). Hy-
 211 perparameters tuning and evaluation of the classification accuracy were performed via 5-fold
 212 cross-validation.

213 The best results were obtained using LDA, which was able to distinguish outdoor grass-feed
 214 cow's milk from TMR with an accuracy of 95% while differentiating grass and clover with an
 215 accuracy of 68%. Figure 3 allows to visualize class boundaries by plotting the spectra projections
 216 in the latent space spanned by the two discriminant functions. From the figure, a clear boundary
 217 can be observed between the indoor and outdoor feed classes, while there is a significant overlap
 218 between the GRS and CLV classes. Therefore, the extracted components were then considered
 219 as an input to a linear SVM model to improve classification between outdoor feed classes. The
 220 combination of two classifier (LDA + SVM), resulting in a two-step approach, significantly
 221 improved the overall classification accuracy (87.1%) as well as classification accuracy between
 222 classes, as shown in Table 5.

Table 5: Confusion matrix obtained by combining LDA and SVM.

		Predicted class		
		CLV	GRS	TMR
True class	CLV	83.5%	17.4%	0.7%
	GRS	15.8%	81.6%	0.8%
	TMR	0.7%	1.1%	98.5%

223 3.3 Participant 3

224 The present work was developed independently by three group members, following a common
 225 preliminary analysis of spectral data. Results of the prediction on the test set provided for the
 226 chemometric challenge were then compared to assess the agreement between the three different
 227 statistical approaches employed.

228 3.3.1 Preliminary edits on spectral data

229 These edits were conducted on raw spectral data in both the training and test sets using `Python`.
 230 Spectra expressed in transmittance were converted into absorbance by taking the \log_{10} of the
 231 reciprocal of the transmittance. Subsequently, spectral wavelengths associated to water ab-
 232 sorption, as well as non-informative regions, were deleted. This led to a reduced version of
 233 the dataset, that has been used for the subsequent analyses, with 511 remaining wavelengths
 234 in the regions between 2,994 and 1,682 cm^{-1} and between 1,578 and 926 cm^{-1} . A graphical
 235 representation of this procedure is reported in the supplementary material (Figure 9).

236 3.3.2 First approach

237 To explore the multivariate structure of the dataset, Principal Component Analysis (PCA) was
 238 exploited on the training dataset, using `prcomp` function in `stats` package and the `factoextra`
 239 package [Kassambara and Mundt, 2020] in the R environment R Core Team [2020]. The analysis
 240 revealed that most of the data variability was explained by the first two Principal Components
 241 (PCs), accounting together for the 88% of the total variance (see the scree plot on the left top
 242 panel in Figure 4).

243 Afterwards, possible outliers were detected using the algorithm proposed by Filzmoser et al.
 244 [2008] and implemented in the `mvoutlier` package [Filzmoser and Gschwandtner, 2021]; only the
 245 observations being both location and scatter outliers were removed from the training dataset.
 246 As a results, a total of 63 observations were removed from the training dataset.

247 After outliers removal, linear discriminant analysis was considered using `lda` function in the
 248 `MASS` package [Venables and Ripley, 2002]. To test its accuracy, as a first step the discrimi-
 249 nant functions were applied to the training dataset, with the aim of comparing the estimated
 250 classification with the actual one. Therefore, LDA was first applied to maximize the differences
 251 between TMR and the CLV+GRS (in the following named PAST group). The LDA returned
 252 one Linear Discriminant (LD) function, which was then applied to the training dataset to at-
 253 tribute the TMR diet to observations. Afterwards, LDA was applied again by maintaining in
 254 the training set only the observations belonging to the PAST group. The obtained LD function
 255 was then applied to the whole training dataset to discriminate between CLV and GRS diets
 256 previously categorized as PAST. The vector with the predicted classes was then compared with
 257 the vector of actual group classification in the training dataset, thus computing the training
 258 accuracy. This approach resulted in an overall model training accuracy equal to 83.3% (see
 259 Table 6); the scatter plot of the first versus second linear dimension scores is depicted in the
 260 right top panel in Figure 4. Lastly, the LD functions obtained on the training dataset allowed
 261 for the classification of the unknown observations in the test dataset, with the results reported
 262 in Table 6.

Table 6: Summary of the results of the three different approaches.

	Member 1	Member 2	Member 3
Brief description	Two steps DA in R	Canonical DA with stepwise method in SAS	DA with stepwise methods in SPSS
Number of samples (training set)	3180	3116	3153
Number of wavelengths retained	511	88	16
Accuracy (training set)	83.30%	81.32%	71%
Predicted diet for the samples in the test dataset (n cases)			
TMR	344	326	365
CLV	367	342	326
GRS	366	353	386
Agreement between the approaches applied to the test dataset			
Member 1			
Member 2	84.21%		
Member 3	72.90%	70.84%	

263 3.3.3 Second approach

264 Principal component analysis (PROC PRINCOMP, SAS Institute Inc., ver. 9.4) was undertaken
 265 on the training set, as in Section 3.3.2. Coherently, outlier removal was then performed by
 266 calculating the Mahalanobis distance (MD) as the uncorrected sum of squares of the first four
 267 centred and scaled PC scores, explaining up to the 98.21% of the total spectral variance. Outliers
 268 were defined as samples whose MD was greater than the 97.5th percentile of a χ^2 distribution
 269 with 4 degrees of freedom [Brereton, 2015]. Following this approach, a total of 127 samples were
 270 discarded from the training set.

271 The discriminant model was developed following a multiple-step approach. Firstly, a step-
 272 wise discriminant analysis was carried out in order to identify the most significant wavelengths
 273 associated with the three different diets using the PROC STEPDISC. A total of 88 wavelengths
 274 were retained and used for the subsequent canonical discriminant analysis, which was developed
 275 through the PROC DISCRIM. The proportion of samples correctly classified was 73.38% (CLV),
 276 73.70% (GRS), and 97.62% (TMR), with an overall model accuracy of 81.32%. The scatter plot
 277 of the first versus second canonical variables scores is in the bottom left panel of Figure 4. The
 278 wavenumbers with the greatest (in absolute value) canonical discriminant function coefficients
 279 were between 1,154 and 1,162 cm^{-1} , 2,843 cm^{-1} , 2,874 cm^{-1} , and 2,882 cm^{-1} , thus providing
 280 some potentially relevant information to be explored to assess which milk chemical features are
 281 more influenced by the dietary regimen. The discriminant model was then applied to the test
 282 set to obtain the prediction of cows' diet on unknown milk spectra.

283 3.3.4 Third approach

284 Standard assumptions required for multivariate analyses were verified before proceeding to the
 285 main analysis. Two diagnostic measures were used to identify the outliers for the predictors
 286 and the dependent variables; in the former case Mahalanobis Distance (MD) was used to spot
 287 multivariate outliers while, in the latter one, studentized residuals were considered. Samples
 288 whose MD was greater than the 97.5th percentile of the MD distribution and studentized
 289 residuals greater than 2.5 were removed. During this process, a total of 90 outliers have been
 290 identified and excluded. Potential multicollinearity was then verified by Tolerance and Variance
 291 Inflation Factors. Moreover, the ratio between the number of cases and predictors was checked

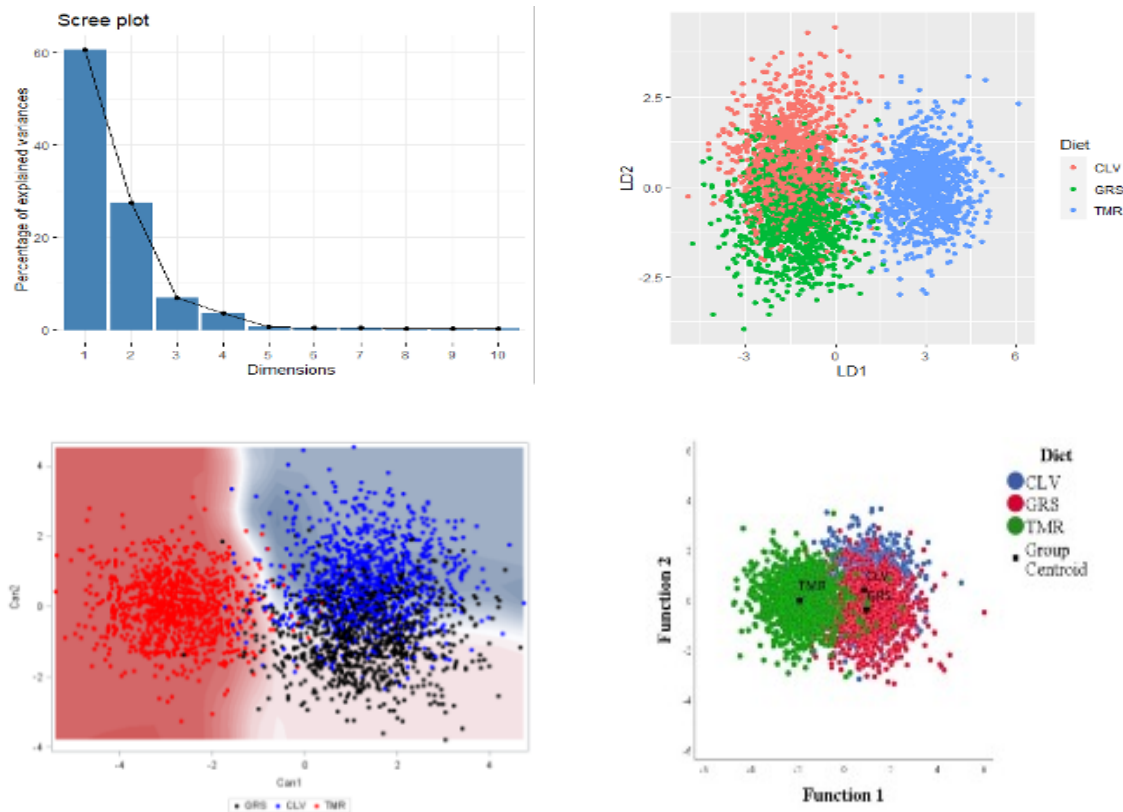


Figure 4: Explained variance by the first 10 principal components (top left), scatter plot of discriminant models developed by member 1 (right top), member 2 (bottom left) and member 3 (bottom right).

292 as an indicator of the adequacy of the sample size; a ratio of 20 observations for each predictor
 293 variable, with the smallest group size exceeding the number of independent variables, is suggested
 294 [Meloun and Militký, 2011; Pituch and Stevens, 2015].

295 LDA was then chosen as the main discriminative approach. The stepwise method, using
 296 Wilks' lambda Λ as criterion, was adopted to reduce multicollinearity and increase the
 297 case/predictors ratio, improving the adequacy of the sample size. Box's test and log determi-
 298 nants were considered to verify the equality of covariance matrices. The canonical correlation
 299 and the proportion of between-group variance that is due to each variate were used as mea-
 300 sures of effect size [Pituch and Stevens, 2015], while the performance of the LDA was evaluated
 301 by classification-related statistics and leave-one-out CV [Hahs-Vaughn, 2016]. The **Scoring**
 302 **Wizard** command was finally used to apply the discriminant functions (DF) to the test dataset,
 303 and the predicted probability was calculated to assess its performance. Analyses were performed
 304 with SPSS software [IBM Corp., 2017].

305 Standardized canonical DF coefficients of the variables selected by DA and measures of effect
 306 size are shown in Table 12 in the Supplementary Material. More than 90% of the total difference
 307 between the groups was attributable to the first DF, with the Wilks' Λ (0.330) indicating that it
 308 has a significant discriminating capacity (p-value < 0.001). Wavenumber $2,851\text{ cm}^{-1}$ and $2,890$
 309 cm^{-1} mostly contributed to the discrimination of cows' diet. The second DF only explained
 310 6% of the total variance, being nonetheless still significant (Wilks' $\Lambda = 0.902$; p-value < 0.001).
 311 Centroids (Table 13) and the plot of DF scores (bottom right panel in Figure 4) indicated
 312 that the first DF appropriately discriminate the TMR group from the others (i.e., CLV and
 313 GRS). On the other hand, group separation on the second DF was poor; in particular, CLV and
 314 GRS clusters were not clearly distinguished. The cross-validation procedure indicated an overall
 315 model accuracy of 71% (see Table 6), with different sensitivity between groups: over 90% for

316 TMR samples, and below 65% for CLV and GRS samples. The application of DFs to predict
317 the diet of cows in the test data set showed a similar trend, with an expected sensitivity of 64%,
318 63%, and 87% for CLV, GRS, and TMR diets, respectively (Table 14).

319 3.4 Participant 4

320 A conventional machine learning pipeline was used, composed of feature (i.e., wavelength) selec-
321 tion and classification, with no outliers being removed from the original dataset. Dimensionality
322 reduction techniques such as Principal Component Analysis (PCA) and Independent Compo-
323 nent Analysis (ICA), as well as Extended Multiplicative Scatter Correction (EMSC) and a data
324 augmentation approach were tested to improve the classification results [Bjerrum et al., 2017].
325 EMSC represents a preprocessing technique which removes multiplicative effects potentially
326 caused by physical phenomena such as light scattering, which is commonly seen in reflectance
327 spectroscopy, thus allowing for easier modelization of chemical effects. On the other hand, the
328 data augmentation scheme increases the data set ten fold by adding random variations in offset,
329 multiplication, and slope, nine times to each sample.

330 Subsequently a range of different classifiers, which have successfully been adopted before
331 on infrared spectroscopy data, were used. In particular, the considered models were K-nearest
332 Neighbour [K-NN; Balabin and Safieva, 2011], Random Forest [RF; Chen et al., 2021], Sup-
333 port Vector Classification [SVC; Ji-yong et al., 2013], Multilayer-perceptron [MLP; Balabin and
334 Safieva, 2008], Linear Discriminant Analysis [LDA; Khuwijitjaru et al., 2020], Decision Tree
335 Classification [Geronimo et al., 2019], Nu-Support Vector Classification [NuSVC; Terouzi et al.,
336 2013], AdaBoost Classification [Wu et al., 2017], Gradient Boosting Classification [Munera et al.,
337 2021], Gaussian Naive Bayes [Bhati and Bhattacharya, 2020] and Quadratic Discriminant Anal-
338 ysis [QDA; Oravec et al., 2019]. Other investigated predictive methods belonged to the group of
339 deep Learning (DL) techniques, and in particular one-dimensional (1D) Convolutional Neural
340 Network (CNN). 1D CNN makes use of six one dimensional convolutional layers, and a number
341 of max pooling, batch normalization and dropout layers. Each 1D CNN layer is followed by
342 a max-pooling and batch normalization layer. One-dimensional CNN was apply only on raw
343 spectra in order to retain the sequence of the data, not required for PCA and ICA.

344 Prior to the analyses, the dataset was split in a training set (80% of the data), to train
345 the different models, and a validation set (remaining 20% of the data), used to optimise the
346 hyperparameters and to identify the best method to be used for final testing.

347 An initial experiment was performed on all classifiers without the use of data augmentation
348 or feature selection. This was carried out to explore which classification method was performing
349 better with the raw spectral data. Figure 5 shows the results obtained from the initial step
350 with the 80/20 train/validation for different classifiers. All results gathered were averages taken
351 from three training and validation predictions for each model. LDA gave the best results with
352 an accuracy of 76%, whereas the MLP and SVC produce some of the worst performances with
353 accuracies around 33%.

354 In the second stage, the classifiers were tested in conjunction with PCA, ICA (`scikit-learn`
355 methods of PCA and FastICA [Pedregosa et al., 2011] were used) or data augmentation. The
356 use of PCA and ICA altered the data by reducing the dimensionality, while on the other hand
357 data augmentation increases the number of samples. For data augmentation, the data augment
358 function from Bjerrum et al. [2017] was used. This increased the number of training samples
359 from 3,244 to 19,464. At this stage, only a subset of the previously tested model were considered,
360 based on their performances in the previous step. Figure 6 shows the results of each classifier
361 with each pre-processing method (base, ICA, PCA, data augmentation (Aug)). From these
362 results, it was noted that LDA following data augmentation achieved the highest accuracy
363 with 82.7%. The greatest improvement in the predictions was observed using MLP after ICA
364 (improvement of 41%). An additional experiment was then carried out with just the use of the
365 LDA model. This was to show the importance of regions within the spectra, and a number of

366 different wavelength region were tested. Therefore, figure 7 shows the results of the LDA when
367 removing different spectral regions.

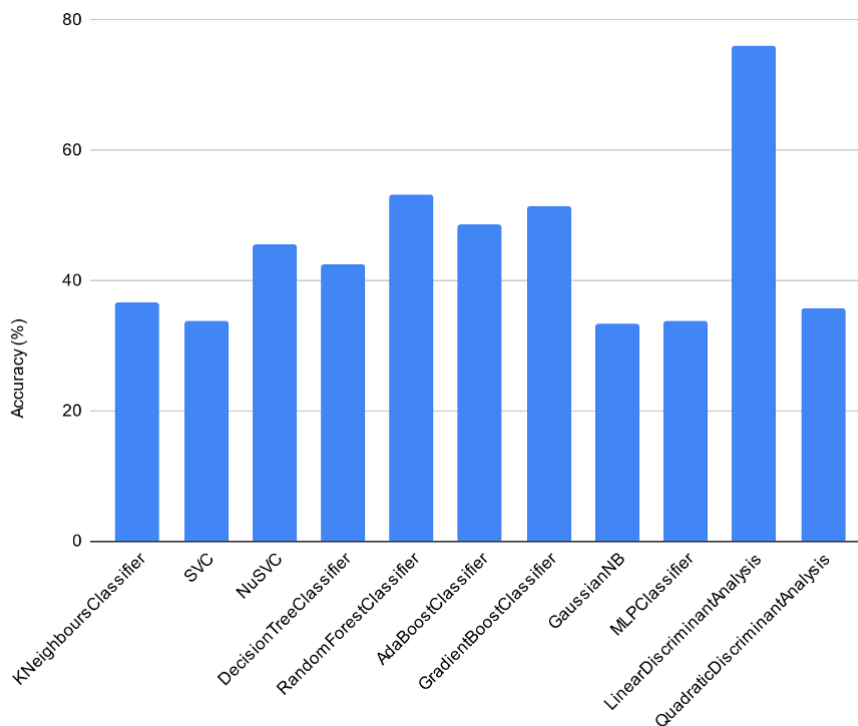


Figure 5: Results of classifiers on a 80/20 test-train split.

368 There was a general increase in accuracy over the base approach when data augmentation
369 was used, with the only exception of CNN. With regard to wavelengths selection, there was no
370 noticeable increase in accuracy when focusing on a specific region in the spectra. Nonetheless,
371 the majority of the relevant information lied within the region from 925 cm^{-1} and 1597 cm^{-1} ,
372 and there was a slight increase in the accuracy of prediction of around 1% when using the range
373 of 925 to 1585 cm^{-1} and 1717 to 2103 cm^{-1} compared to the full set of wavelengths.

374 3.5 Participant 5

375 In order to prepare the data set for predictive analysis, some pre-processing was considered.
376 As directed by the challenge organisers, outlying spectra were removed such that the data set
377 consisted of 3243 transmittance spectra covering 1060 wavelengths. Subsequently, spectra were
378 transformed to absorbance values by taking \log_{10} of the reciprocal of the transmittance values.
379 In addition, following Frizzarin et al. [2021b], a subset of 534 wavelengths that lay outside
380 the water-related high-noise-level regions were identified as relevant for predicting a cow's diet,
381 although the water-regions were not excluded at this point in the analysis.

382 To ensure a robust assessment, the dataset was split into training and validation sets. In this
383 case, the validation set was constructed to control for batch effect confounding, which may bias
384 estimates for out-of-sample prediction [Soneson et al., 2014]. Inspection of the data set revealed
385 that rows were ordered to have several consecutive observations of each diet. Therefore, it
386 was assumed that each set of consecutive diet observations belonged to a single batch. In this
387 manner, 90 batches, 30 for each diet, were identified. In addition, the data was collected over
388 three years [Frizzarin et al., 2021b], and so it was assumed that the first 30 batches were collected
389 in the first year of the study, the next 30 in the second year, and the final 30 in the third. Based
390 on these assumptions, the validation set consisted of 996 spectra from 30 batches collected in

Base, ICA, PCA and Aug

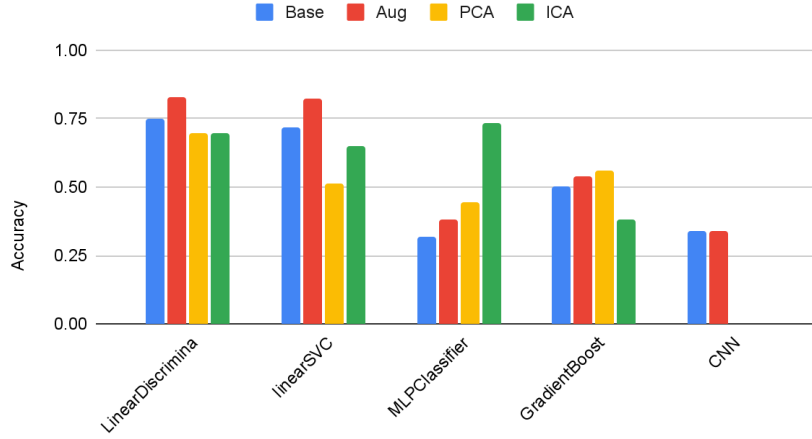


Figure 6: Results of classifiers on with different pre-processing methods.

391 the study’s third year, which included ten batches for each diet, while models have been trained
 392 on the 2247 remaining spectra. Training data was randomly split into $V = 10$ folds, with each
 393 fold including two batches from each diet. Possible batch effect of repeated measurements for a
 394 single cow were ignored.

395 In order to describe the predictive model used in this analysis, let $\mathcal{D} = \{y_i, \mathbf{x}_i\}_{i=1}^N$ denote the
 396 observed data, where the response variable $y_i \in \{1, \dots, M\}$ represents the diet of the i -th cow
 397 and covariates $\mathbf{x}_i \in \mathbb{R}^D$ represent the corresponding milk absorbance spectrum. Note that this
 398 analysis considers $M = 3$ diets, $D = 1060$ wavelengths, and $N = 3243$ training observations.
 399 The objective of the proposed predictive models is to learn $\mathbb{P}(y | \mathbf{x})$, that is, the probability that
 400 a given milk sample comes from a grass, clover or TMR-fed cow, given the spectrum for that
 401 sample.

402 The first step in constructing a predictive model is to define a deterministic mapping function
 403 $g : \mathbf{x}_i \rightarrow \mathbf{z}_i$, for $\mathbf{z}_i \in \mathbb{R}^{D'}$, with $D' < D$, which describes a feature extraction procedure. Two
 404 approaches to feature extraction were considered here. The first simply selected the $D' = 534$
 405 relevant wavelengths identified by Frizzarin et al. [2021b] such that \mathbf{z}_i is the i -th absorbance
 406 spectrum after removing the high-noise-level water regions and standardises each wavelength.
 407 The second was based on the wavelet transform, a popular technique for signal processing which
 408 can be applied for data compression, smoothing, and multi-resolution analysis [Nason, 2008], and
 409 proceeds in three steps. After setting high-noise-level regions of each spectrum to 0, a thresholded
 410 wavelet transform provides a set of wavelet coefficients. The feature vector \mathbf{z}_i is then the vector
 411 of wavelet coefficients that are non-zero for at least one of the N spectra, in this case $D' = 594$.
 412 The thresholded wavelet transform is available with the `wavethresh` R package [Nason, 2016],
 413 using Daubechies least symmetric wavelet as the mother wavelet and Bayesian approach to
 414 thresholding wavelet coefficients [Abramovich et al., 1998]. Note that setting wavelengths in
 415 the high-noise-level regions to 0 means the wavelet transform preserves the spectral distance
 416 between wavelengths while ensuring that the corresponding wavelet coefficients are 0.

417 Given the feature vector $\mathbf{z}_i = g(\mathbf{x}_i)$, a multinomial regression model for diet was assumed,
 418 such that

$$\mathbb{P}(y_i = m | \mathbf{z}_i) = \frac{\exp(\beta_m^\top \mathbf{z}_i)}{\sum_{l=1}^M \exp(\beta_l^\top \mathbf{z}_i)}, \quad (1)$$

419 for $m = 1, \dots, M$ where $\beta_m \in \mathbb{R}^{D'}$, implicitly assuming that \mathbf{z}_i includes an intercept term.
 420 The `glmnet` package [Friedman et al., 2010] fits this model to data efficiently. For simplicity, a
 421 LASSO model was fitted, where 10-fold cross-validation on the training data informs the penalty

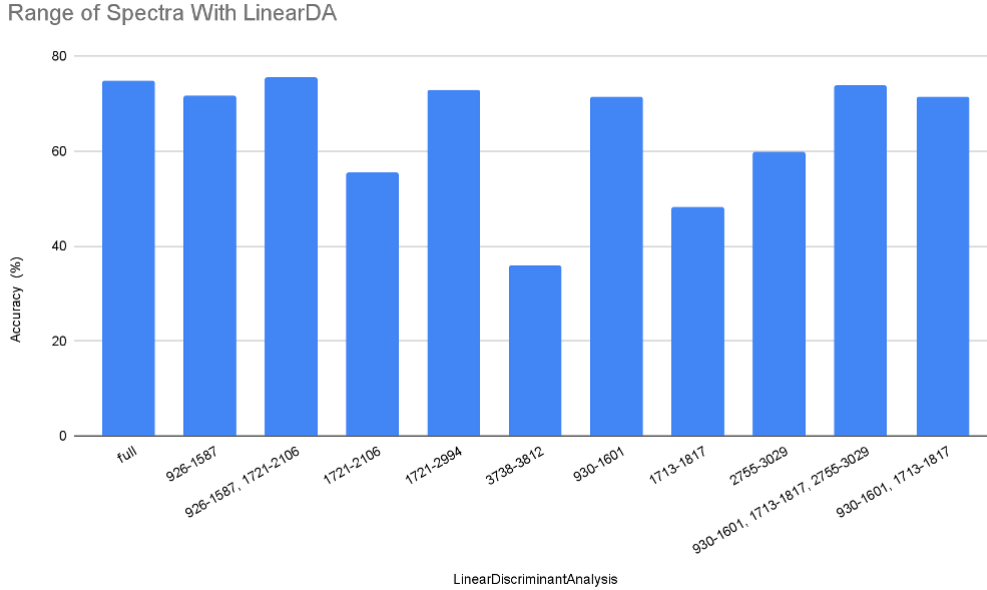


Figure 7: Results of Linear Discriminant Analysis for different feature selection.

422 hyperparameter.

423 Finally, the predictive performance of the proposed models was compared by analysing their
 424 log-loss on the validation data set. That is, for a validation data set and a model \mathcal{M}_j for
 425 $\mathbf{z}_i = g(\mathbf{x}_i)$, the log-loss is defined as

$$\ell_j = -\frac{1}{N'} \sum_{i=1}^{N'} \sum_{m=1}^M \mathbb{I}(y_i = m) \ln \mathbb{P}(y_i = m \mid \mathbf{z}_i, \mathcal{M}_j), \quad (2)$$

426 where N' is the number of observations in the validation set, $\mathbb{I}(\mathcal{A})$ is the usual indicator function
 427 that is equal to 1 when \mathcal{A} is true and 0 otherwise and $\mathbb{P}(y_i = m \mid \mathbf{z}_i, \mathcal{M}_j)$ is the probability under
 428 \mathcal{M}_j that $y_i = m$ given \mathbf{z}_i . The log-loss is a proper scoring rule for evaluating predictive models
 429 [Gneiting and Raftery, 2007], where smaller scores are better, and so encourages to express the
 430 true belief about the data. It is also straightforward to set benchmarks for assessing the quality
 431 of predictions a priori. For example, for any M a mean log loss of 0 represents perfect predictive
 432 performance, while when $M = 3$ as in the considered case, a mean log loss of $-\ln(1/3) \approx 1.1$
 433 represents “guessing”, where we predict each category uniformly at random. For completeness,
 434 the classification accuracy of \mathcal{M}_j was also assessed.

435 The results of this analysis are presented in Table 7. The first model considered was a LASSO-
 436 penalized multinomial regression of the raw milk spectra on the diet, where high-noise-level
 437 regions of the spectrum was excluded and the wavelengths standardised. The tuning parameter
 438 λ , controlling the strength of the penalization, was selected to minimise the multinomial deviance
 439 (a statistic proportional to the mean log-loss) via 10-fold cross-validation. The log-loss of this
 440 model on the training set was 0.57, which corresponds to a diet classification accuracy of 77%.
 441 A closer examination of the predictions revealed that when CLV and GRS were treated as a single
 442 category (pasture-fed), it was possible to predict TMR with an accuracy of 94%. When trying
 443 to predict whether the cow was fed CLV, given that it was pasture-fed, an accuracy of 72% was
 444 achieved. Predictive performance was much poorer on the validation set, with an overall log-loss
 445 of 0.82, corresponding to an accuracy of 58%. The model predicted TMR with an accuracy of
 446 88%. However, for cows known to be pasture-fed, it predicted CLV with an accuracy of 49%.

447 The second model considered a multinomial regression of the non-zero thresholded wavelet
 448 transform coefficients of the milk spectra on diet. As above, the model was fitted by maximising

Table 7: Predictive model assessment.

Model	In-sample log-loss	Validation log-loss
Raw Spectra	0.57	0.82
Wavelet Coefficients	0.74	0.88

449 a penalised log-likelihood and by using 10-fold cross-validation to tune λ . For this model, the
 450 log-loss on the training set was equal to 0.74, corresponding to an accuracy of 69%, although it
 451 predicted TMR with an accuracy of 88%. For pasture-fed cows, it predicted CLV with an accuracy
 452 of 68%. As with the first model, performance dropped for the validation set. The log-loss was
 453 0.88 and TMR accuracy was 79%. Given that a cow was pasture-fed, the CLV accuracy was 47%.
 454 These results are summarised in Table 7.

455 The obtained results clearly showed that milk spectra carry a signal distinguishing pasture-
 456 fed cows from TMR, but that it was difficult to distinguish between CLV and GRS. However, the
 457 predictive performance was much poorer on the validation dataset than for the training one,
 458 indicating that the adopted models did not offer a robust out-of-sample predictions. Without
 459 careful consideration of potential batch effect confounders within the sampled spectra, we are
 460 likely to overestimate the out-of-sample performance of our models. Collecting data from more
 461 cows over a more extended period should alleviate this issue and allow more robust models to
 462 be developed.

463 Lastly, no evidence was found to suggest that wavelet transformed spectra provided helpful
 464 insight into the cows' diet. However, that is not to say that some alternative basis expansion
 465 could improve the current predictive models. In fact, given more data on the relationship be-
 466 tween milk spectra and diet, the development of models which allow for non-linear relationships
 467 between wavelengths may prove a fruitful avenue for future research.

468

469 3.6 Participant 6

470 As a first step, the training set was centered and scaled and the same transformation was
 471 applied to the test set. In the following analyses, no outliers were removed while all the spectra
 472 were transformed from transmittance to absorbance. Wavelengths from high-noise level spectral
 473 regions between 1720 and 1592 cm^{-1} , between 3698 and 2996 cm^{-1} , and greater than 3,818
 474 cm^{-1} were removed from the analysis following Frizzarin et al. [2021b].

The Fisher score, being the ratio of between to within diet group variance, was calculated
 for all the wavelengths in the training set. For wavelength j , the Fisher score is given by:

$$\text{Fisher score}_j = \frac{\sum_{m=1}^M \sum_{i=1}^n \mathbb{I}(y_i = m) (\bar{x}_j^{(m)} - \bar{x}_{\cdot j})^2}{\sum_{m=1}^M \sum_{i=1}^n \mathbb{I}(y_i = m) (x_{ik} - \bar{x}_{\cdot j}^{(m)})^2}$$

475 where j denotes the wavelength index, $i = 1, \dots, n$ denotes the spectra with n being the number
 476 of spectra in the training set, m denotes the diet group with $M = 3$, $\mathbb{I}(y_i = m)$ is an indicator of
 477 diet group spectra i , $\bar{x}_{\cdot j}$ is the average of wavelength j for all spectra ($i = 1, \dots, n$), $\bar{x}_{\cdot j}^{(m)}$ is the
 478 average of wavelength j in diet group m . A wavelength with the highest Fisher score in each
 479 of the discarded regions was kept in the analysis. Wavelengths with Fisher score lower than
 480 0.002 were removed from further analysis, thus leaving 380 wavelengths. In order to compare
 481 algorithms and carry out further feature selection, the training set was itself randomly split
 482 75/25 into training and testing sets stratified by diet. A genetic algorithm [Holland, 1992],
 483 implemented in library `genalg` [Willighagen and Ballings, 2022] was used as a stochastic search
 484 method to find an optimal subset of input wavelengths for classification. Individuals in the GA
 485 population were represented by binary strings denoting wavelengths to be included or excluded

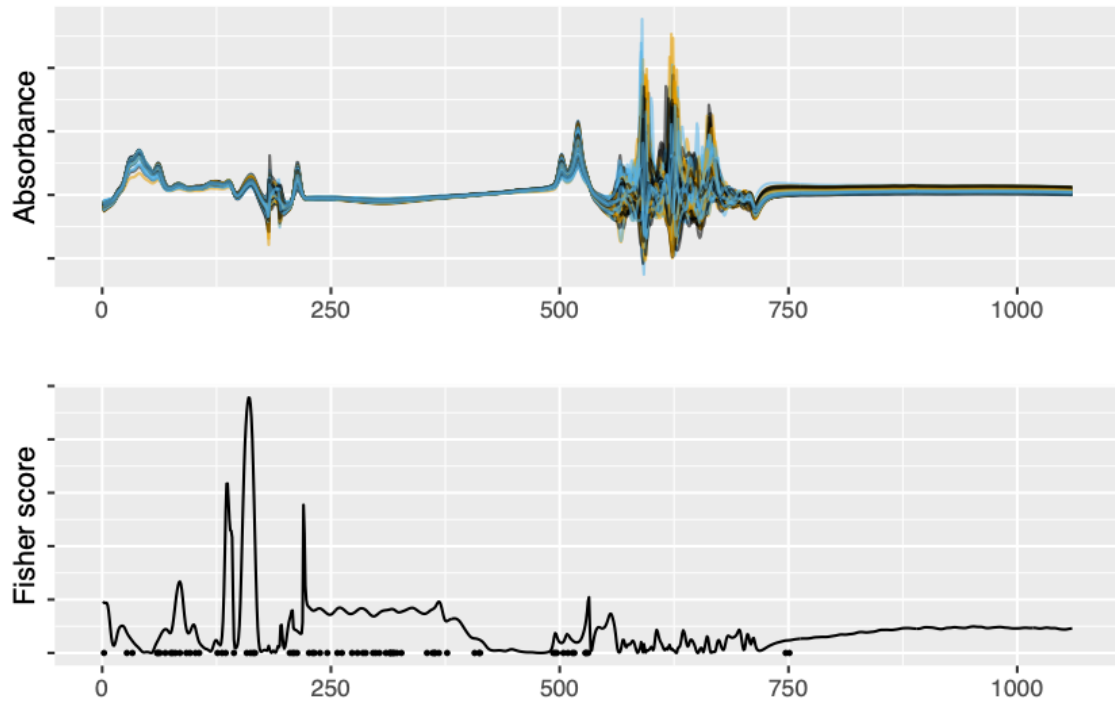


Figure 8: Spectra absorbance and the corresponding Fisher score with points on the x-axis denoting the wavelengths selected by the GA.

486 for prediction. Objective function was set to be the average accuracy from ten cross-validated
 487 fits of linear discriminant analysis (LDA) of the training subset. GA was run for 200 iterations
 488 with population size set at 200. Figure 8 shows the spectra absorbance and the corresponding
 489 Fisher scores, with points denoting the wavelengths selected by the GA.

490 The best configuration from the final GA population had 70 wavelengths included. These
 491 wavelengths were used as inputs to the following classification algorithms:

- 492 • Linear discriminant analysis (LDA), library MASS [Venables and Ripley, 2002];
- 493 • Partial least squares discriminant analysis (PLS-DA) [Mevik et al., 2020];
- 494 • Least absolute shrinkage and selection operator [LASSO; Tibshirani, 1996], library glmnet
 495 [Friedman et al., 2010];
- 496 • Elastic net [EN; Zou and Hastie, 2005], library glmnet;
- 497 • Random Forest [RF; Breiman, 2001], library ranger [Wright and Ziegler, 2017];
- 498 • Support vector machines [Vapnik, 1998], library kernlab [Karatzoglou et al., 2004];
- 499 • Bayesian kernel projection classifier [BKPC Domijan and Wilson, 2011], library BKPC
 500 [Domijan, 2018].

501 All analyses were done using R [R Core Team, 2020], the code is available in the github
 502 repository https://github.com/domijan/KD_Vistamilk2022.

503 The training set was randomly split into ten further training/testing sets of equal size,
 504 stratified on diet. The average accuracy and standard deviation over the ten random splits
 505 for all the classification algorithms are given in Table 8. LDA performed best with average
 506 accuracy of 77.4%. PLS-DA and EN overall accuracy was of 76.9%, 76.5% respectively. The
 507 algorithms were tuned using further cross-validation of the training sets. For BKPC and SVM,

Table 8: Average accuracy for over ten random splits of the training set for classifiers. LDA: linear discriminant analysis; PLS: partial least squares regression; EN: elastic net; BKPC: Bayesian kernel projection classifier; SVM: support vector machine; LASSO: Least absolute shrinkage and selection operator; RF: random forest.

Accuracy	LDA	PLS	EN	BKPC	SVM	LASSO	RF
Mean	0.774	0.769	0.765	0.759	0.738	0.736	0.509
SD	0.008	0.009	0.007	0.008	0.007	0.006	0.014

508 the best results were obtained with a linear kernel. The predictions of the LDA were submitted
 509 to the competition. Moreover, genetic algorithm was able to select a much smaller subset of
 510 wavelengths without loss of classification performance.

511 4 Discussion

512 While the dataset provided for the data competition included three different classes to dis-
 513 criminate (i.e. TRM, GRS, and CLV), the main difficulty of the present data competition was
 514 concerned with the discrimination between GRS and CLV diets. In fact, the ability of dis-
 515 tinguishing pasture and TMR dietary regimens has been already documented [Frizzarin et al.,
 516 2021b], with the discrimination being driven mainly by the different content of fatty acids (FA)
 517 in milk [Agradi et al., 2020]. In particular, milk from pasture based diet is generally richer in
 518 saturated FA such as linoleic acid, poorer in saturate FA, and have a lower omega6/omega3
 519 ratio [see e.g. Chilliard et al., 2007; Dewhurst et al., 2006; Ferlay et al., 2013, 2017]. As MIR is
 520 known to be able to predict, with a certain degree of accuracy, the different FA in milk [Soyeur
 521 et al., 2011], spectral data are therefore capable to discriminate also TMR and pasture diets.

522 On the other hand, since GRS and CLV dietary regimens differed only for the inclusion
 523 of 20% annual clover in perennial ryegrass sward for the CLV diet, induced differences in the
 524 FA might be less clear. As a consequence, to discriminate GRS and CLV exploiting spectral
 525 information only, a careful and accurate tuning of the modelling choices was required. In this
 526 regard, interestingly, some participants proposed two-steps classification approaches, with the
 527 first step focusing on TMR and pasture based diets, while the second one aimed at distinguishing
 528 CLV from GRS samples. As an example, participant 2 highlighted a potentially significant gain
 529 in terms of accuracy when considering an ensemble approach, where components extracted from
 530 LDA was used to train a linear SVM, better discriminating between GRS and CLV. Again, in
 531 Section 3.3.2 two consecutive LDA models have been fitted, with the first one being used to
 532 discriminate TMR from pasture while the second, exploiting the discriminant function on the
 533 pasture samples only, was trained to classify GRS and CLV.

534 Generally speaking, linear approaches introduce a gain in interpretability of the results,
 535 while paying a price in terms of accuracy. Nonetheless, the review of the different approaches
 536 presented in this paper showed that strong performances were achieved resorting to linear clas-
 537 sifiers. In fact, remarkable results were obtained when adopting LDA-based approaches (see,
 538 e.g., participants 1, 2, 4 and 6), which were certainly proven effective in discriminating TMR
 539 and pasture diets and, as highlighted above, were also used as a building block for promising
 540 two-steps procedures. Nevertheless, the approaches presented in Sections 3.1.1 and 3.1.2, which
 541 attained the best test set prediction accuracies as it is displayed in Table 9, pointed towards the
 542 need of considering non-linearities, especially when the aim is to discriminate between GRS and
 543 CLV. This is confirmed by the confusion matrix displayed in Table 10, where it is shown that
 544 these two different dietary regimens are discriminated remarkably well, especially if considering
 545 their similarities from a compositional standpoint. Note that, while with FCN interpretation
 546 of the results and exploration of the most informative wavelengths are compromised, the ap-
 547 proach in Section 3.1.1, which is considering again LDA as the final classifier, tends to be more

Table 9: Accuracy computed on the test dataset for all the participants.

Participant	Sect 3.1.1	Sect 3.1.2	Sect 3.2	Sect 3.3.2	Sect 3.3.3
Test accuracy	0.871	0.837	0.798	0.711	0.783
Participant	Sect 3.3.4	Sect 3.4	Sect 3.5	Sect 3.6	
Test accuracy	0.796	0.786	0.724	0.766	

Table 10: Final confusion matrix obtained with the approach outlined in Section Sect 3.1.1.

		Actual		
		CLV	GRS	TMR
Predicted	CLV	312	55	5
	GRS	61	300	5
	TMR	6	7	326

transparent. However, the clever random polynomial variables generation proposed tends to produce new features which are difficult to interpret from a chemical standpoint. Therefore, as it often happens in modern data analysis routine, the adopted approaches have to be tailored on the specific aim to pursue, often dealing with the standard trade-off between accuracy and interpretability.

553

Data transformation is widely used in near-infrared analyses, as the analysed samples are generally more noisy. Differently, samples analysed using MIRS are generally less noisy, therefore these transformations, with the exception for the transformation of the wavelengths from transmittance to absorbance, are not widely used. In the present study some data transformations were tested, but the reported results confirmed that they do not have a strong impact on the quality of the prediction results. Differently from data transformation, the removal of the spectral regions related to water is of fundamental importance, as reported by the participants which tested their prediction methods before and after their removal. For example, results from Section 3.1 showed an improvement of 11.6% and of 25.7% when ridge regression and LDA were respectively used in combination of new polynomial variables generation after water regions removal. Again, in Section 3.1.2 an improvement of the prediction performance, from 17.5% (CNN) to 20.5% (FCN), after removing the water regions also when using deep learning methods is shown. Participant 1 also demonstrated the possibility to select the important variables directly from the spectra, in fact they achieved the best prediction results using a variables selection approach starting from all the spectral information (see Table 1). Variable selection was also tested in Section 3.6, where a genetic algorithm was used to select a smaller subset of wavelengths without substantial loss in classification performance.

In Section 3.3, the participants investigated the pairwise agreement among the three different approaches, to calculate by comparing the observations and quantifying the percentage of classifications in agreement on the total number of observations (Table 6). Methods applied by members 1 and 2 gave similar predictions (agreement of 84.21%), whereby agreement between predictions from member 3 was between 70.84% (with member 2) and 72.90% (with member 1). Although strong, the discrepancies among the three predictions could be due to: i) the different number of samples retained for model development, and ii) the different number of predictors (i.e., wavelengths) used for training, considering that the first member used the entire edited spectra, whereby the second and third applied different algorithms for wavelengths selection. This investigation from the third participant permits to understand that differences in data editing and different methodologies selected for the predictions, even if similar, brought to consistently different class predictions.

583 A final discussion point was related to the creation of the test dataset. The dataset was
584 created by the organizers, who splitted the original dataset in 75% training and 25% test dataset,
585 considering a correct division of the classes across years into the 2 datasets. The discussion
586 revolved around whether or not divide the dataset into 75% training and 25% testing, or dividing
587 the dataset according to time components, like keeping the samples recorded in 2015 and 2016
588 into the training dataset, and the samples recorded in 2017 in the test dataset. Such temporal
589 division would permit to understand if samples recorded in previous years can predict future
590 information.

591 **5 Conclusion**

592 Thanks to the high number of participants, with different backgrounds, who provided their
593 prediction results, the data competition was a thought-provoking occasion to discuss some of
594 the challenges arising when analyzing spectral data and provided insightful indications.

595 As mentioned in the paper and as it was previously shown in [Frizzarin et al. \[2021b\]](#), the
596 stronger compositional dissimilarities between pasture-based diet and TMR-based ones induced
597 an easier discrimination between the corresponding classes. This generally led to overall good
598 performances, in terms of accuracy, for the adopted methods (see [Table 9](#)). On the other hand,
599 the distinction between milk samples originated from GRS and CLV was more challenging.
600 Nonetheless, as it is shown in [Table 10](#), some hand-crafted strategies specifically proposed for
601 this competition showed more than promising results also when employed to detect differences
602 in the composition between distinct pasture-based feeding regimens. In particular, non-linear
603 transformations of the original wavelengths and two-steps classification approaches, outlined in
604 [Section 3.1](#) and [3.3](#), seemed to be effective in solving this problem.

605 Pre-treatments were generally not beneficial for the improvement of the prediction equations,
606 while the deletion of the spectral regions related to water (with manual selection of these regions
607 or by means of automatic variable selection procedures) improved the prediction results. The
608 utilization of linear models, in particular LDA, provided some of the best results, and the
609 overall best prediction was achieved using LDA applied after wavelengths selection and random
610 polynomial generation, as it was shown in [Table 9](#). When spectral analyses are undertaken it
611 is important to know not only the best possible statistical methods to use for the analyses, but
612 also what is the best data editing for such data.

613 **A Supplementary material**

614 **A.1 Deep neural network architecture**

Table 11: List of the deep model architectures considered in Section 3.1.2, including the number of trainable parameters for each model and the type of input data they accept.

Model Architecture	Parameters	Input Data and Shape
FCN		
- Dense layers of 1024, 512, 128, 64 and 32 units	1,785,923	- Linear, full (1060) - Linear, reduced (518)
- Output layer of 3 units		
- Dropout for dense layers, drop rate of 0.2		
- elu activation for hidden layers		
- softmax activation for output layer		
- Adam optimiser, initial learning rate of 0.0001		
- Categorical cross entropy as loss function		
CNN		
- Convolutional layers with 32, 64 and 128 filters	55,332,419	- Squared, full (33x33) - Squared, reduced (23x23)
- Filters of shape (3, 3), (2, 2) and (2, 2)		
- Flattening layer		
- Dense layers of 512, 256, 128, 64, and 32 units		
- Output layer of 3 units		
- elu activation for hidden layers		
- softmax activation for output layer		
- Adam optimiser, initial learning rate of 0.0001		
- Categorical cross entropy as loss function		
CNN_DILATED		
- Same architecture as CNN	41,176,643	- Squared, full (33x33) - Squared, reduced (23x23)
- Kernels built with a dilation rate of (2, 2)		

615 **A.2 Participant 3**

Table 12: Standardized canonical discriminant function coefficients of the variables selected by DA and effective size measures.

Wavenumber, cm^{-1}	Function	
	1	2
1069	2.899	0.298
1130	-3.790	0.416
1181	-2.003	5.371
1269	-7.321	-2.495
1292	10.544	-3.045
1377	-5.860	-0.482
1416	-5.885	1.267
1439	12.710	1.112
1474	-4.689	3.714
1539	-3.816	-2.385
1577	4.442	1.247
1752	11.958	6.035
2782	-1.459	0.875
2851	-15.686	-13.612
2890	16.085	3.459
2932	-4.166	0.916
Eigenvalue	1.732	0.109
& of variance	94.1%	5.9%
Canonical correlation	0.796	0.313

Table 13: Group means (centroids) for the Discriminant Functions

Diet	Function	
	1	2
CLV	0.872	0.403
GRS	0.954	-0.400
TMR	-1.895	-0.012

Table 14: Classification related statistics and leave-one-out cross-validation. ^a 71% of original grouped cases correctly classified. ^b Cross-validation is done only for those cases in the analysis. In cross-validation, each case is classified by the functions derived from all cases other than that case. 70.5% of cross-validated grouped cases correctly classified.

	Diet	Predicted Group Membership			Total	
		CLV	GRS	TMR		
Original ^a	Count	CLV	629	363	83	1075
		GRS	323	668	62	1053
		TMR	39	44	942	1025
	%	CLV	58.5	33.8	7.7	100.0
		GRS	30.7	63.4	5.9	100.0
		TMR	3.8	4.3	91.9	100.0
Cross-validated ^b	Count	CLV	620	369	86	1075
		GRS	326	663	64	1053
		TMR	39	47	939	1025
	%	CLV	57.7	34.3	8.0	100.0
		GRS	31.0	63.0	6.1	100.0
		TMR	3.8	4.6	91.6	100.0

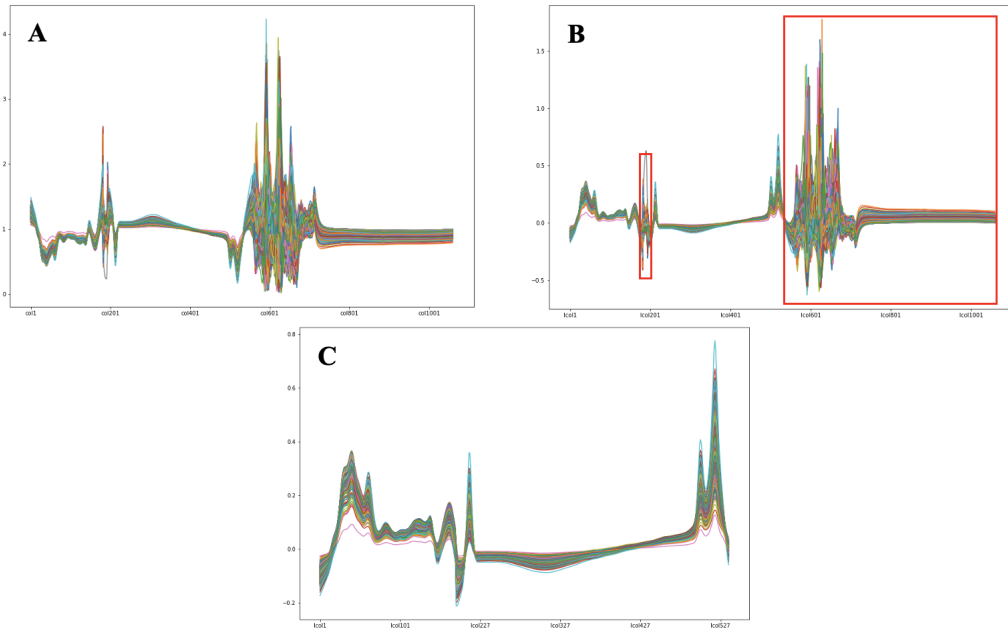


Figure 9: Line plot of raw spectra expressed in transmittance (A), conversion of raw spectra from transmittance to absorbance (B; red boxes indicate low signal-to-noise regions), and raw spectra in absorbance after noisy area removal (C).

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623 Declaration of interests

624 The authors declare that they have no known competing financial interests or personal relation-
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