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CLASSIFICATION OF COW DIET BASED ON MILK MID INFRARED SPECTRA: A DATA ANALYSIS COMPETITION AT THE "INTERNATIONAL WORKSHOP ON SPECTROSCOPY AND CHEMOMETRICS 2022"

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Abstract

In April 2022, the Vistamilk SFI Research Centre organized the second edition of the 22 "International Workshop on Spectroscopy and Chemometrics – Applications in Food and 23 Agriculture". Within this event, a data challenge was organized among participants of the 24 workshop. Such data competition aimed at developing a prediction model to discriminate 25 dairy cows' diet based on milk spectral information collected in the mid-infrared region. In 26 fact, the development of an accurate and reliable discriminant model for dairy cows' diet can 27 provide important authentication tools for dairy processors to guarantee product origin for 28 dairy food manufacturers from grass-fed animals. Different statistical and machine learning 29 modelling approaches have been employed during the workshop, with different pre-processing 30 steps involved and different degree of complexity. The present paper aims to describe the 31 statistical methods adopted by participants to develop such classification model. 32

Keywords: Chemometrics, Fourier transform mid-infrared spectroscopy, machine learning,
 milk quality, food authenticity

35 1 Introduction

The use of mid-infrared spectroscopy (MIRS) has become a relevant topic in agri-food sciences, due to its capacity to routinely quantify a wide range of important characteristics rapidly and

 $_{\rm 38}$ $\,$ cost-effective. In particular, MIRS is nowadays commonly employed to monitor and quantify

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milk quality parameters, such as concentrations of fat, protein, casein, and lactose. These 39 parameters are used for milk quality-based payment schemes, genetic and genomic selection, 40 and as farmers' support tool. Spectral information generated from MIRS analysis have also 41 proven to be effective in predicting fine milk quality parameters, including protein fractions, 42 free amino acids [Bonfatti et al., 2011; McDermott et al., 2016], individual and groups of fatty 43 acids [Soyeurt et al., 2006; Fleming et al., 2017], milk processing traits [Ferragina et al., 2013; 44 Visentin et al., 2015, animal-related characteristics [McParland et al., 2014; Shetty et al., 2017; 45 Ho et al., 2019, and can be used as a tool for the verification of the authenticity of agricultural 46 foods [Cozzolino, 2012]. A more extended list of applications of MIRS in the dairy science 47 framework can be retrieved from the reviews by De Marchi et al. [2014] and Tiplady et al. 48 [2020].49 The two-day event "International Workshop on Spectroscopy and Chemometrics" was orga-50 nized by Vistamilk SFI Research Centre in April 2022, following its first edition held in 2021 51 [Frizzarin et al., 2021a]. The workshop focused on describing the main challenges and appli-52 cations of near and mid-infrared spectroscopy in food, animal, and agricultural sciences with 53 internationally recognised researchers. Moreover, participants, on a voluntary basis, were pro-54

vided with a large dataset containing individual cow milk spectra with the sole information on animal's diet for a chemometric data competition. Such data presented many challenges from a methodological and statistical point of view, due to the high dimensionality of the spectral matrices, and strong collinearity between adjacent spectral wavelengths. The chemometric challenge, therefore, encouraged the engagement of participants with different background and skills and required the application of different statistical and machine learning strategies.

The purpose of the data challenge was to develop a model to predict the diet fed to dairy cows by exploiting mid-infrared spectral information. Participants, or groups of participants, were required to apply their developed model to a test set containing only individual milk spectra and to submit their prediction of animals' diet. Since participation was found to be high, six contributions out of twelve were selected, according to criteria based on the accuracy of the predictions and methodological innovativeness, to present their results both at the workshop and in the present manuscript.

68 2 Data description and challenge

A dataset consisting of 4,364 individual milk spectra from individual cows was collected between 69 May and August in 2015, 2016 and 2017 [O'Callaghan et al., 2016]. The samples were from Hol-70 stein Friesian cows with different parity from Irish Dairy Research Herd in Teagasc Moorepark, 71 Fermoy, Co. Cork. Three dietary groups were evaluated with 54 cows being assigned to a di-72 etary group each year. The three diet treatments were grass (GRS) which consisted of perennial 73 ryegrass only, clover (CLV) which consisted of perennial ryegrass with 20% annual clover sward, 74 and total mixed ration (TMR) where cows were fed grass silage, maize silage and concentrates 75 while being maintained indoors for the full season. Milk samples were collected in the morning 76 (AM) and evening (PM) milking session; subsequently AM+PM samples were pooled and anal-77 ysed weekly using Pro-FOSS FT6000 (FOSS). The output spectrum contained a total of 1060 78 transmittance data points in the range from 925 cm⁻¹ to 5,000 cm⁻¹. 79 The dataset was divided into training (3275 spectra) and test (1089 spectra) data; for the 80

latter only spectral (i.e., independent variables) information was provided, while diet information, to be used as a classification (i.e., dependent) variable, was available for the training set.
The training data included 1094 spectra for GRS, 1120 spectra from CLV and 1061 spectra for
TMR. There were no missing values in the training or test set. The specific information about
the wavenumbers had not been shared with the participants.

The three dietary groups were carefully selected based on their characteristics. As described by Frizzarin et al. [2021b], pasture-based diets are easily discriminated from TMR diets, while ⁸⁸ discriminating between GRS and CLV diets is much more difficult due to the similarities in the

sward composition resulting in similar milk composition. However, with the increased pressure
 to reduce fertilizer use, and the introduction of multi-species swards, the development of a robust

⁹¹ discriminant model for classifying milk spectra based on diet is of paramount importance.

After the analysis, the participants submitted their predicted values for the test dataset and a short explanation of the methodology used. The best methods were selected based on the accuracy of the predictions for the test dataset. The accuracy was calculated as the proportion of the correctly classified samples divided by the total number of samples in the test dataset.

⁹⁶ 3 Modelling approaches and results

97 3.1 Participant 1

The data were analyzed following different modelling strategies, focusing both on methods that considered spectral proximity of the wavelengths and on methods that do not. All the analyses have been mainly conducted using Python libraries pandas, sklearn, sktime and matplotbib [see Pedregosa et al., 2011, and references therein]. The open source code is available at https: //github.com/mlgig/vistamilk_diet_challenge and readers can refer to it for the specific details about the implementation of all the methods outlined in this Section.

As a first step, some descriptive statistics were computed, and the outliers have been removed, following both the recommendations given prior to the competition and a visual inspection of the data. In the subsequent step, the labeled dataset was split according to a 3-fold cross-validation (3CV) strategy. Therefore, the best model was selected based on cross-validation accuracy, and then trained on the full training set and used to perform prediction on the provided unlabeled

109 test set.

¹¹⁰ In order to predict the diet, the following classification strategies were considered:

• Tabular models: each sample is considered as a vector of unordered features. In 111 particular, Ridge Classifier, where a penalty shrinking parameters towards zero is im-112 posed on the coefficients of a logistic regression model [see e.g., Hoerl and Kennard, 113 1970, and Linear Discriminant Analysis (LDA) were tested. In the following, these 114 methods were coupled both with feature selection strategies and with random polyno-115 mial feature transformations. The latter approach first used sklearn routines to create 116 new features (see, https://scikit-learn.org/stable/modules/generated/sklearn. 117 **preprocessing.PolynomialFeatures.html**). For example, for features a, b, c, a poly-118 nomial transformation of degree 2 will generate the features $1, a, b, c, ab, ac, bc, a^2, b^2, c^2$. 119 By generating these features, this approach aimed to check if non-linear interactions im-120 proved the classification. Finally, a new approach (random polynomial transformation) is 121 presented, which aims to diversify the polynomial features (by random sampling) while 122 keeping low computational requirements. 123

• Deep Neural Network Models: a family of approaches based on deep neural networks, both fully connected and convolutional, were tested. This strategy implicitly generates complex features interactions, as captured by the network architecture.

Note that previously obtained results [Frizzarin et al., 2021a] suggest that tabular methods 127 work quite well with spectroscopy data. Moreover, following the suggestions in Frizzarin et al. 128 [2021b], feature selection strategies were coupled with the information about the presence of 129 water regions in the spectra. In addition, state-of-the-art time series classification algorithms, 130 such as ROCKET [Dempster et al., 2020], MiniROCKET [Dempster et al., 2021], MrSQM 131 [Nguyen and Ifrim, 2021, 2022] and FreshPrince [Middlehurst and Bagnall, 2022], were tested. 132 Lastly, *ensemble methods* were applied, aiming to mix together time series and tabular models, to 133 combine their predictions and strengths. Nonetheless, these approaches have been outperformed 134

Table 1: Accuracy results, evaluated on the 3-fold cross-validation, for the tabular methods considered, coupled with feature selection strategies.

Method	Accuracy
Ridge Classifier	0.760
LDA	0.747
Feature Selection + Ridge Classifier	0.777
Feature Selection $+$ LDA	0.778
No water $+$ Ridge Classifier	0.777
No water $+$ LDA	0.783
Feature Selection $+$ Polynomial Features $+$ LDA	0.844
No water + Feature Selection + Polynomial Features + LDA	0.844

Table 2: Examples of RPolyTransformer features used. Here x_j denote the *j*-th wavelength.

 $\begin{array}{l} (x_{32}*x_{19})+x_{103}-x_2\\ (x_{102}*(x_{78})+x_{26})\\ (x_1-x_{150})+x_{64}*x_4*x_5\end{array}$

by the ones mentioned above, therefore the corresponding results are not shown in the next sections.

137 3.1.1 Tabular models, feature selection and transformation

In Table 1, results for the best tabular methods are presented. Both the ridge classifier, appropriately tuned, and LDA performed quite well, while being extremely fast to train. Nonetheless, the selection of some specific wavelengths seemed to improve the accuracy further. In fact, both the removal of the noisy water regions and the data-driven feature selection (performed using the SelectFromModel routine in Python), provides better results.

Nevertheless, all these approaches hover around 80% accuracy, therefore, in order to improve it, the data were augmented considering polynomial features of degree two (using sklearn method PolynomialFeatures(degree = 2)). This led to an increase of the accuracy to 84.4%. The LDA component visualisation for the model with Feature Selection and Polynomial Features, applied on the unlabeled test dataset, is shown in Figure 1 and a good discrimination between the three classes is clearly visible.

The improvements obtained when considering polynomial features, come at a price in terms 149 of the computational requirements. In fact, starting from the 1060 original wavelengths, the 150 addition of second-degree polynomial features resulted in a total number of variables which 151 made the model estimation task unfeasible. To address this issue, in this work a new Random 152 Polynomial Features (RPolyTransformer in the following) approach was introduced. The key 153 idea was to implement random sampling in the non-linear feature space. This lead to relevant 154 advantages as the total number of features can be controlled and it can consider both higher-155 degree (> 2) polynomial features and complex mathematical functions (e.g., cosine, exp). 156

This strategy firstly generated K random arithmetic expressions (see Table 2 for some examples), which are then used to compute K non-linear features. From the new and the original features, K^* variables are selected using SelectKBest from sklearn. The hyperparameters Kand K^* were optimized via cross-validation in the final model (see the final row of Table 3).

In Table 3 the results obtained with this method, again combined with different classifiers and feature selection approaches and tested with the full data and the data after water region removal, are presented. At first, when combining **RpolyTransformer** with a classifier, a significant drop in the accuracy was observed, if compared with simple tabular models. Ridge was more accurate than LDA but it was still far behind the previous results. However, by carefully filtering the



Figure 1: LDA visualisation for the model Feature Selection + Polynomial Features + LDA, applied to the unlabeled test data to predict class labels.

features either automatically with SelectFromModel or manually by removing the water regions,
 the results improved noticeably. In these experiments, LDA outperforms Ridge consistently.
 Compared to the PolynomialFeatures method, the one proposed here is faster (a few seconds
 versus a few minutes) and just as accurate. However, the initial results without noise reduction

(i.e., feature selection) suggest that this strategy is more sensitive to noise in the data.

171 3.1.2 Deep Learning Models

When considering deep learning models, the task of exploding the feature space and learning feature interactions is completely deferred to the network, without requiring any feature engineering steps. In turn, deep neural networks require a careful design process, to avoid overfitting and to identify the best model architecture and input modality.

The designed model architectures considered here can be grouped into two main categories, 176 namely, Fully Connected Networks (FCNs) and Convolutional Neural Networks (CNNs). FCNs 177 do not require any manipulation or adaptation of the input data, as each single wavelength 178 is treated as an independent feature and fed to an input unit. In contrast, CNNs require the 179 data to be bi-dimensional, image-like matrices, as they are commonly used to address image 180 classification problems. For this family of networks, the input waves need then to be vertically 181 stacked as 2D arrays and therefore, in order to fit the closest squared dimension, padded with 182 trailing zeros. An example of how the spectroscopy samples can be presented to the CNNs is 183 provided in Figure 2. Additionally, a third group of models is tested for this challenge, namely, 184 CNNs based on dilated kernels (further denoted as CNN DILATED). Whilst regular CNNs 185 extract features through compact squared filters, or local receptive fields, the CNN_DILATED 186 network utilizes filters that are spatially dilated by a fixed factor [Yu and Koltun, 2015]. Dilated 187 kernels are commonly used in semantic image segmentation. 188

All the models in this group were trained on both the full training dataset and on the water reduced one. When the CNN models were trained, the full data were shaped into images of shape 33×33 with a padding of 29 values, while the reduced data were shaped into images of shape 23×23 with a padding of 11 values. As already mentioned, all padding values were zeros, and they were appended to the original sequences.

¹⁹⁴ The full list of the implemented architectures is presented in Table S1 in Appendix A.1. The

Table 3: Results for different combinations with **RPolyTransformer**. SelectFromModel and SelectKBest are feature selection modules to remove noise from data (the former) and select the most discriminative non-linear features (the latter).

Method	Accuracy
Region: FULL	
RPolyTransformer + Ridge Classifier	0.717
RPolyTransformer + LDA	0.619
SelectFromModel + RPolyTransformer + SelectKBest + LDA	0.848
Region: [925:1585, 1720:2989]	
RPolyTransformer + Ridge Classifier	0.805
RPolyTransformer + LDA	0.847
SelectFromModel + RPolyTransformer + SelectKBest + LDA	0.843
Region: [925:1585, 1720:2989, 3738:3807]	
RPolyTransformer + Ridge Classifier	0.811
RPolyTransformer + LDA	0.833
SelectFromModel + RPolyTransformer + SelectKBest + LDA	0.835
Optimized model	
Region: [925:1585, 1720:2989]	
$RPolyTransformer(K = 17000) + SelectKBest(K^* = 7000) + LDA$	0.864

Model	Data	Split 1	Split 2	Split 3	Average
ECN	FULL	0.670	0.677	0.675	0.674
FUN	NO WATER	0.854	0.851	0.837	0.847
CNN	FULL	0.686	0.684	0.670	0.680
UNIN	NO WATER	0.806	0.836	0.832	0.824
CNN DILATED	FULL	0.678	0.684	0.652	0.671
UNN_DILATED	NO WATER	0.824	0.812	0.807	0.814

Table 4: Training results on the 3CV splits.

experiments were conducted on the previously described 3-fold cross-validation splits; note that, 195 for each split, 20% of the training data was held back for validation purposes, to identify network 196 hyperparameters such as number of training epochs, initial learning rate, or regularisation rates. 197 Models were trained for a total of 50,000 epochs, with an early stopping policy used to monitor 198 the validation loss to detect overfitting and save time during the training phase. The final 199 model used to classify the provided unknown data was selected as the overall best performing 200 architecture, and trained over the full training data for a number of epochs set as the average 201 of the epochs reached during the 3CV training. 202

All models were implemented using TensorFlow [Abadi et al., 2016], and trained on a work-203 station featuring a single GPU, model Nvidia Titan XP. Results are presented in Table 4, which 204 contains the training performances obtained over the 3-folds CV experimental campaign. For 205 all the tested architectures, excluding the water regions from the input waves resulted in a 206 performance increase of roughly 12-13%. The FCN model working on data after water-region 207 removal, achieved the highest accuracy across the 3 splits, with an average of 84.7%. Simi-208 lar unreported results were obtained also considering a single split validation strategy, which 209 furthermore demonstrated that convolutional models tend to overfit the input data quite fast. 210



Figure 2: Spectroscopy sequences arranged as image structures. In both examples, the padding values are visible at the bottom of the resulting images. Values are normalised in the 0-1 range for convenience.

			Predicted class	
		CLV	GRS	TMR
	CLV	83.5%	17.4%	0.7%
True class	GRS	15.8%	81.6%	0.8%
	TMR	0.7%	1.1%	98.5%

Table 5: Confusion matrix obtained by combining LDA and SVM.

211 3.2 Participant 2

All the processing steps and the algorithm implementation was completed using MATLAB [MAT-212 LAB, 2018]. After having imported the dataset in tabular form, the outliers were identified as 213 those observations with at least one wavelength with more than three scaled median absolute 214 deviation from the wavelength specific median (see https://uk.mathworks.com/help/matlab/ 215 ref/isoutlier.html for further details). Classification was performed using a set of algorithms 216 such as Support Vector Machine (SVM), K-Nearest Neighbors (KNN) and Linear Discriminant 217 Analysis (LDA). To optimize the number of predicting variables, coefficient's threshold and the 218 regularization parameter was tuned using a 5-fold cross-validation and classification accuracy 219 was evaluated. 220

The best results were obtained using LDA, which was able to distinguish outdoor grass-feed 221 cow's milk from TMR with an accuracy of 95% while differentiating grass and clover with an 222 accuracy of 68%. Figure 3 allows to visualize class boundaries by plotting the spectra projections 223 in the latent space spanned by the two discriminant functions. From the figure, a clear boundary 224 can be observed between the indoor and outdoor feed classes, while there is a significant overlap 225 between the GRS and CLV classes. Therefore, the extracted components were then considered 226 as an input to a linear SVM model to improve classification between outdoor feed classes. The 227 combination of two classifier (LDA + SVM), resulting in a two-step approach, significantly 228 improved the overall classification accuracy (87.1%) as well as classification accuracy between 229 classes, as shown in Table 5. 230



Figure 3: LDA components extracted from the developed model.

231 3.3 Participant 3

The present work was developed independently by three group members, following a common preliminary analysis of spectral data. Results of the prediction on the test set provided for the chemometric challenge were then compared to assess the agreement between the three different statistical approaches employed.

236 3.3.1 Preliminary edits on spectral data

These edits were conducted on raw spectral data in both the training and test sets using Python. Spectra expressed in transmittance were converted into absorbance by taking the \log_{10} of the reciprocal of the transmittance. Subsequently, spectral wavelengths associated to water absorption, as well as non-informative regions, were deleted. This led to a reduced version of the dataset, that has been used for the subsequent analyses, with 511 remaining wavelengths in the regions between 2,994 and 1,682 cm⁻¹ and between 1,578 and 926 cm⁻¹. A graphical representation of this procedure is reported in the supplementary material (Figure S1).

244 3.3.2 First approach

To explore the multivariate structure of the dataset, Principal Component Analysis (PCA) was exploited on the training dataset, using prcomp function in stats package and the factoextra package [Kassambara and Mundt, 2020] in the R environment R Core Team [2020]. The analysis revealed that most of the data variability was explained by the first two Principal Components (PCs), accounting together for the 88% of the total variance (see the scree plot on the left top panel in Figure 4).

Afterwards, possible outliers were detected using the algorithm proposed by Filzmoser et al. [2008] and implemented in the mvoutlier package [Filzmoser and Gschwandtner, 2021]; only the observations being both location and scatter outliers were removed from the training dataset. As a results, a total of 63 observations were removed from the training dataset.

After outliers removal, linear discriminant analysis was considered using lda function in the MASS package [Venables and Ripley, 2002]. To test its accuracy, as a first step the discriminant functions were applied to the training dataset, with the aim of comparing the estimated classification with the actual one. Therefore, LDA was first applied to maximize the differences

	Approach 1	Approach 2	Approach 3
Brief description	Two steps DA in R	Canonical DA with	DA with stepwise meth-
1	1	stepwise method in $\tt SAS$	ods in SPSS
Number of samples (training set)	3180	3116	3153
Number of wavelengths retained	511	88	16
Accuracy (training set)	83.30%	81.32%	71%
Predict	ted diet for the samp	les in the test dataset (n cases)
TMR	344	326	365
CLV	367	342	326
GRS	366	353	386
Agreeme	nt between the appro	paches applied to the te	st dataset
Member 1			
Member 2	84.21%		
Member 3	72.90%	70.84%	

Table 6: Summary of the results of the three different approaches.

between TMR and the CLV+GRS (in the following named PAST group). The LDA returned 259 one Linear Discriminant (LD) function, which was then applied to the training dataset to at-260 tribute the TMR diet to observations. Afterwards, LDA was applied again by maintaining in 261 the training set only the observations belonging to the PAST group. The obtained LD function 262 was then applied to the whole training dataset to discriminate between CLV and GRS diets 263 previously categorized as PAST. The vector with the predicted classes was then compared with 264 the vector of actual group classification in the training dataset, thus computing the training 265 accuracy. This appproach resulted in an overall model training accuracy equal to 83.3% (see 266 Table 6); the scatter plot of the first versus second linear dimension scores is depicted in the 267 right top panel in Figure 4. Lastly, the LD functions obtained on the training dataset allowed 268 for the classification of the unknown observations in the test dataset, with the results reported 269 in Table 6. 270

271 3.3.3 Second approach

Principal component analysis (PROC PRINCOMP, SAS Institute Inc., ver. 9.4) was undertaken on the training set, as in Section 3.3.2. Coherently, outlier removal was then performed by calculating the Mahalanobis distance (MD) as the uncorrected sum of squares of the first four centred and scaled PC scores, explaining up to the 98.21% of the total spectral variance. Outliers were defined as samples whose MD was greater than the 97.5th percentile of a χ^2 distribution with 4 degrees of freedom [Brereton, 2015]. Following this approach, a total of 127 samples were discarded from the training set.

The discriminant model was developed following a multiple-step approach. Firstly, a step-279 wise discriminant analysis was carried out in order to identify the most significant wavelengths 280 associated with the three different diets using the PROC STEPDISC. A total of 88 wavelengths 281 were retained and used for the subsequent canonical discriminant analysis, which was developed 282 through the PROC DISCRIM. The proportion of samples correctly classified was 73.38% (CLV), 283 73.70% (GRS), and 97.62% (TMR), with an overall model accuracy of 81.32%. The scatter plot 284 of the first versus second canonical variables scores is in the bottom left panel of Figure 4. The 285 wavenumbers with the greatest (in absolute value) canonical discriminant function coefficients 286 were between 1,154 and 1,162 cm^{-1} , 2,843 cm^{-1} , 2,874 cm^{-1} , and 2,882 cm^{-1} , thus providing 287 some potentially relevant information to be explored to assess which milk chemical features are 288



Figure 4: Explained variance by the first 10 principal components (top left), scatter plot of discriminant models developed by member 1 (right top), member 2 (bottom left) and member 3 (bottom right).

more influenced by the dietary regimen. The discriminant model was then applied to the test set to obtain the prediction of cows' diet on unknown milk spectra.

291 3.3.4 Third approach

Standard assumptions required for multivariate analyses were verified before proceeding to the 292 main analysis. Two diagnostic measures were used to identify the outliers for the predictors 293 and the dependent variables; in the former case Mahalanobis Distance (MD) was used to spot 294 multivariate outliers while, in the latter one, studentized residuals were considered. Samples 295 whose MD was greather than the 97.5th percentile of the MD distribution and studentized 296 residuals greater than 2.5 were removed. During this process, a total of 90 outliers have been 297 identified and excluded. Potential multicollinearity was then verified by Tolerance and Variance 298 Inflation Factors. Moreover, the ratio between the number of cases and predictors was checked 299 as an indicator of the adequacy of the sample size; a ratio of 20 observations for each predictor 300 variable, with the smallest group size exceeding the number of independent variables, is suggested 301 [Meloun and Militky, 2011; Pituch and Stevens, 2015]. 302

LDA was then chosen as the main discriminative approach. The stepwise method, us-303 ing Wilks' lambda Λ as criterion, was adopted to reduce multicollinearity and increase the 304 case/predictors ratio, improving the adequacy of the sample size. Box's test and log determi-305 nants were considered to verify the equality of covariance matrices. The canonical correlation 306 and the proportion of between-group variance that is due to each variate were used as mea-307 sures of effect size [Pituch and Stevens, 2015], while the performance of the LDA was evaluated 308 by classification-related statistics and leave-one-out CV [Hahs-Vaughn, 2016]. The Scoring 309 Wizard command was finally used to apply the discriminant functions (DF) to the test dataset, 310

and the predicted probability was calculated to assess its performance. Analyses were performed with SPSS software [IBM Corp., 2017].

Standardized canonical DF coefficients of the variables selected by DA and measures of effect 313 size are shown in Table S_2 in the Supplementary Material. More than 90% of the total difference 314 between the groups was attributable to the first DF, with the Wilks' Λ (0.330) indicating that it 315 has a significant discriminating capacity (p-value < 0.001). Wavenumber 2,851 cm⁻¹ and 2,890 316 cm^{-1} mostly contributed to the discrimination of cows' diet. The second DF only explained 317 6% of the total variance, being nonetheless still significant (Wilks' $\Lambda = 0.902$; p-value < 0.001). 318 Centroids (Table S3) and the plot of DF scores (bottom right panel in Figure 4) indicated 319 that the first DF appropriately discriminate the TMR group from the others (i.e., CLV and 320 GRS). On the other hand, group separation on the second DF was poor; in particular, CLV and 321 GRS clusters were not clearly distinguished. The cross-validation procedure indicated an overall 322 model accuracy of 71% (see Table 6), with different sensitivity between groups: over 90% for 323 TMR samples, and below 65% for CLV and GRS samples. The application of DFs to predict 324 the diet of cows in the test data set showed a similar trend, with an expected sensitivity of 64%, 325 63%, and 87% for CLV, GRS, and TMR diets, respectively (Table S4). 326

Lastly note that, all the three approaches were applied and the results were compared at the end of the competition. Despite the better prediction performance shown by the first approach on the training set, the second approach proved to be the best for the prediction of the test set.

330 3.4 Participant 4

A conventional machine learning pipeline was used, composed of feature (i.e., wavelength) selec-331 tion and classification, with no outliers being removed from the original dataset. Dimensionality 332 reduction techniques such as Principal Component Analysis (PCA) and Independent Compo-333 nent Analysis (ICA), as well as Extended Multiplicative Scatter Correction (EMSC) and a data 334 augmentation approach were tested to improve the classification results [Bjerrum et al., 2017]. 335 EMSC represents a preprocessing technique which removes multiplicative effects potentially 336 caused by physical phenomena such as light scattering, which is commonly seen in reflectance 337 spectroscopy, thus allowing for easier modelization of chemical effects. On the other hand, the 338 data augmentation scheme increases the data set ten fold by adding random variations in offset, 339 multiplication, and slope, nine times to each sample. The variations were ± 0.1 times the stan-340 dard deviation of the training set for the offset, multiplication was 1 ± 0.1 times the standard 341 deviations, and the slope adjustement was between 0.95 and 1.05 [Bjerrum et al., 2017]. 342

Subsequently a range of different classifiers, which have successfully been adopted before 343 on infrared spectroscopy data, were used. In particular, the considered models were K-nearest 344 Neighbour [K-NN; Balabin and Safieva, 2011], Random Forest [RF; Chen et al., 2021], Sup-345 port Vector Classification [SVC; Ji-yong et al., 2013], Multilayer-perceptron [MLP; Balabin and 346 Safieva, 2008], Linear Discriminant Analysis [LDA; Khuwijitjaru et al., 2020], Decision Tree 347 Classification [Geronimo et al., 2019], Nu-Support Vector Classification [NuSVC; Terouzi et al., 348 2013], AdaBoost Classification [Wu et al., 2017], Gradient Boosting Classification [Munera et al., 349 2021], Gaussian Naive Bayes [Bhati and Bhattacharya, 2020] and Quadratic Discriminant Anal-350 ysis [QDA; Oravec et al., 2019]. Other investigated predictive methods belonged to the group of 351 deep Learning (DL) techniques, and in particular one-dimensional (1D) Convolutional Neural 352 Network (CNN). This 1D CNN makes use of six one dimensional convolutional layers, and a 353 number of max pooling, batch normalization and dropout layers. Each 1D CNN layer is followed 354 by a max-pooling and batch normalization layer. The one-dimensional CNN only used the raw 355 spectra, as the use of PCA and FastICA would be detrimental due to the transformation of the 356 sequence of the data. 357

Prior to the analyses, the dataset was split into a training set (80% of the data), to train different models, and a validation set (remaining 20% of the data), used to optimise the hyperparameters and to identify the best methods to be used for the final testing. This split was



Figure 5: Results of classifiers on a 80/20 test-train split.

made by utilizing the train_test_split function provided through scikit-learn [Pedregosa et al., 2011].

An initial experiment was performed on all classifiers without the use of data augmentation or feature selection. This was carried out to explore which classification method was performing better with the raw spectral data. Figure 5 shows the results obtained from the initial step with the 80/20 train/validation for different classifiers. All results gathered were averages taken from three training and validation predictions for each model. LDA gave the best results with an accuracy of 76%, whereas the MLP and SVC produce some of the worst performances with accuracies around 33%.

In the second stage, the classifiers were tested in conjunction with PCA, ICA or data aug-370 mentation: for PCA and FastICA scikit-learn methods were used, with the parameters being 371 setted as FastICA(tol = 0.02, max_iter = 4000) and PCA(n_components = 800). The use 372 of PCA and ICA altered the data by reducing the dimensionality, while on the other hand 373 data augmentation increased the number of samples. For data augmentation, the data augment 374 function from Bjerrum et al. [2017] was used. This increased the number of training samples 375 from 3,244 to 19,464. At this stage, only a subset of the previously tested model were con-376 sidered, based on their performances in the previous step. Figure 6 shows the results of each 377 classifier with each pre-processing method (base, ICA, PCA, data augmentation (Aug)). From 378 these results, it was noted that LDA following data augmentation achieved the highest accuracy 379 with 82.7%. The greatest improvement in the predictions was observed using MLP after ICA 380 (improvement of 41%). An additional experiment was then carried out with just the use of the 381 LDA model. This was to show the importance of regions within the spectra, and a number of 382 different wavelength region were tested. Therefore, figure 7 shows the results of the LDA when 383 removing different spectral regions. 384

There was a general increase in accuracy over the base approach when data augmentation was used, with the only exception of CNN. With regard to wavelengths selection, there was no



Figure 6: Results of classifiers on with different pre-processing methods.



Figure 7: Results of Linear Discriminant Analysis for different feature selection.

³⁸⁷ noticeable increase in accuracy when focusing on a specific region in the spectra. Nonetheless, ³⁸⁸ the majority of the relevant information lied within the region from 925 cm⁻¹ and 1597 cm⁻¹, ³⁸⁹ and there was a slight increase in the accuracy of prediction of around 1% when using the range ³⁹⁰ of 925 to 1585 cm⁻¹ and 1717 to 2103 cm⁻¹ compared to the full set of wavelengths.

391 3.5 Participant 5

In order to prepare the data set for predictive analysis, some pre-processing was considered. As directed by the challenge organisers, outlying spectra were removed such that the data set consisted of 3243 transmittance spectra covering 1060 wavelengths. Spectra were transformed to absorbance values by taking \log_{10} of the reciprocal of the transmittance values. In addition, following Frizzarin et al. [2021b], a subset of 534 wavelengths that lay outside the water-related high-noise-level regions were identified as relevant for predicting a cow's diet, although the
water-regions were not excluded at this point in the analysis.

To ensure a robust assessment, the dataset was split into training and validation sets. In this 399 case, the validation set was constructed to control for batch effect confounding, which may bias 400 estimates for out-of-sample prediction [Soneson et al., 2014]. Inspection of the data set revealed 401 that rows were ordered to have several consecutive observations of each diet. Therefore, it 402 was assumed that each set of consecutive diet observations belonged to a single batch. In this 403 manner, 90 batches, 30 for each diet, were identified. In addition, the data was collected over 404 three years [Frizzarin et al., 2021b], and so it was assumed that the first 30 batches were collected 405 in the first year of the study, the next 30 in the second year, and the final 30 in the third. Based 406 on these assumptions, the validation set consisted of 996 spectra from 30 batches collected in 407 the study's third year, which included ten batches for each diet, while models have been trained 408 on the 2247 remaining spectra. Training data was randomly split into V = 10 folds, with each 409 fold including two batches from each diet. Possible batch effect of repeated measurements for a 410 single cow were ignored. 411

In order to describe the predictive model used in this analysis, let $\mathcal{D} = \{y_i, \mathbf{x}_i\}_{i=1}^N$ denote the observed data, where the response variable $y_i \in \{1, \ldots, M\}$ represents the diet of the *i*-th cow and covariates $\mathbf{x}_i \in \mathbb{R}^D$ represent the corresponding milk absorbance spectrum. Note that this analysis considers M = 3 diets, D = 1060 wavelengths, and N = 3243 training observations. The objective of the proposed predictive models is to learn $\mathbb{P}(y \mid \mathbf{x})$, that is, the probability that a given milk sample comes from a grass, clover or TMR-fed cow, given the spectrum for that sample.

The first step in constructing a predictive model is to define a deterministic mapping function 419 $g: \mathbf{x}_i \to \mathbf{z}_i$, for $\mathbf{z}_i \in \mathbb{R}^{D'}$, with D' < D, which describes a feature extraction procedure. Two 420 approaches to feature extraction were considered here. The first simply selected the D' = 534421 relevant wavelengths identified by Frizzarin et al. [2021b] such that \mathbf{z}_i is the *i*-th absorbance 422 spectrum after removing the high-noise-level water regions and standardises each wavelength. 423 The second was based on the wavelet transform, a popular technique for signal processing which 424 can be applied for data compression, smoothing, and multi-resolution analysis [Nason, 2008], and 425 proceeds in three steps. After setting high-noise-level regions of each spectrum to 0, a thresholded 426 wavelet transform provides a set of wavelet coefficients. The feature vector \mathbf{z}_i is then the vector 427 of wavelet coefficients that are non-zero for at least one of the N spectra, in this case D' = 594. 428 The thresholded wavelet transform is available with the wavethresh R package [Nason, 2016], 429 using Daubechies least symmetric wavelet as the mother wavelet and Bayesian approach to 430 thresholding wavelet coefficients [Abramovich et al., 1998]. Note that setting wavelengths in 431 the high-noise-level regions to 0 means the wavelet transform preserves the spectral distance 432 between wavelengths while ensuring that the corresponding wavelet coefficients are 0. 433

Given the feature vector $\mathbf{z}_i = g(\mathbf{x}_i)$, a multinomial regression model for diet was assumed, such that

$$\mathbb{P}\left(y_{i}=m \mid \mathbf{z}_{i}\right) = \frac{\exp\left(\boldsymbol{\beta}_{m}^{\top} \mathbf{z}_{i}\right)}{\sum_{l=1}^{M} \exp\left(\boldsymbol{\beta}_{l}^{\top} \mathbf{z}_{i}\right)},\tag{1}$$

for m = 1, ..., M where $\beta_m \in \mathbb{R}^{D'}$, implicitly assuming that \mathbf{z}_i includes an intercept term. The glmnet package [Friedman et al., 2010] fits this model to data efficiently. For simplicity, a LASSO model was fitted, where 10-fold cross-validation on the training data informs the penalty hyperparameter.

Finally, the predictive performance of the proposed models was compared by analysing their log-loss on the validation data set. That is, for a validation data set and a model \mathcal{M}_j for $\mathbf{z}_i = g(\mathbf{x}_i)$, the log-loss is defined as

$$\ell_j = -\frac{1}{N'} \sum_{i=1}^{N'} \sum_{m=1}^{M} \mathbb{I}\left(y_i = m\right) \ln \mathbb{P}\left(y_i = m \mid \mathbf{z}_i, \mathcal{M}_j\right),\tag{2}$$

Table 7: Predictive model assessment.

Model	In-sample log-loss	Validation log-loss
Raw Spectra	0.57	0.82
Wavelet Coefficients	0.74	0.88

where N' is the number of observations in the validation set, $\mathbb{I}(\mathcal{A})$ is the usual indicator function 443 that is equal to 1 when \mathcal{A} is true and 0 otherwise and $\mathbb{P}(y_i = m \mid \mathbf{z}_i, \mathcal{M}_i)$ is the probability under 444 \mathcal{M}_i that $y_i = m$ given \mathbf{z}_i . The log-loss is a proper scoring rule for evaluating predictive models 445 [Gneiting and Raftery, 2007], where smaller scores are better, and so encourages the analysts 446 to express their true belief about the data. It is also straightforward to set benchmarks for 447 assessing the quality of predictions a priori. For example, for any M a mean log loss of 0 448 represents perfect predictive performance, while when M = 3 as in the considered case, a mean 449 log loss of $-\ln(1/3) \approx 1.1$ represents "guessing", where we predict each category uniformly at 450 random. For completeness, the classification accuracy of \mathcal{M}_i was also assessed. 451

The results of this analysis are presented in Table 7. The first model considered was a LASSO-452 penalized multinomial regression of the raw milk spectra on the diet, where high-noise-level 453 regions of the spectrum was excluded and the wavelengths standardised. The tuning parameter 454 λ , controlling the strength of the penalization, was selected to minimise the multinomial deviance 455 (a statistic proportional to the mean log-loss) via 10-fold cross-validation. The log-loss of this 456 model on the training set was 0.57, which corresponds to a diet classification accuracy of 77%. 457 A closer examination of the predictions revealed that when CLV and GRS were treated as a single 458 category (pasture-fed), it was possible to predict TMR with an accuracy of 94%. When trying 459 to predict whether the cow was fed CLV, given that it was pasture-fed, an accuracy of 72% was 460 achieved. Predictive performance was much poorer on the validation set, with an overall log-loss 461 of 0.82, corresponding to an accuracy of 58%. The model predicted TMR with an accuracy of 462 88%. However, for cows known to be pasture-fed, it predicted CLV with an accuracy of 49%. 463

The second model considered a multinomial regression of the non-zero thresholded wavelet 464 transform coefficients of the milk spectra on diet. As above, the model was fitted by maximising 465 a penalised log-likelihood and by using 10-fold cross-validation to tune λ . For this model, the 466 log-loss on the training set was equal to 0.74, corresponding to an accuracy of 69%, although it 467 predicted TMR with an accuracy of 88%. For pasture-fed cows, it predicted CLV with an accuracy 468 of 68%. As with the first model, performance dropped for the validation set. The log-loss was 469 0.88 and TMR accuracy was 79%. Given that a cow was pasture-fed, the CLV accuracy was 47%. 470 These results are summarised in Table 7. 471

The obtained results clearly showed that milk spectra carry a signal distinguishing pasture-472 fed cows from TMR, but that it was difficult to distinguish between CLV and GRS. However, the 473 predictive performance was much poorer on the validation dataset than for the training one, 474 indicating that the adopted models did not offer a robust out-of-sample predictions. Without 475 careful consideration of potential batch effect confounders within the sampled spectra, we are 476 likely to overestimate the out-of-sample performance of our models. Collecting data from more 477 cows over a more extended period should alleviate this issue and allow more robust models to 478 be developed. 479

Lastly, no evidence was found to suggest that wavelet transformed spectra provided helpful insight into the cows' diet. However, that is not to say that some alternative basis expansion could improve the current predictive models. In fact, given more data on the relationship between milk spectra and diet, the development of models which allow for non-linear relationships between wavelengths may prove a fruitful avenue for future research.

486 3.6 Participant 6

As a first step, the training set was centered and scaled and the same transformation was applied to the test set. In the following analyses, no outliers were removed while all the spectra were transformed from transmittance to absorbance. Wavelengths from high-noise level spectral regions between 1720 and 1592 cm⁻¹, between 3698 and 2996 cm⁻¹, and greater than 3,818 cm⁻¹ were removed from the analysis following Frizzarin et al. [2021b].

The Fisher score, being the ratio of between to within diet group variance, was calculated for all the wavelengths in the training set. For wavelength j, the Fisher score is given by:

Fisher score_j =
$$\frac{\sum_{m=1}^{M} \sum_{i=1}^{n} \mathbb{I}(y_i = m)(\bar{x}_{.j}^{(m)} - \bar{x}_{.j})^2}{\sum_{m=1}^{M} \sum_{i=1}^{n} \mathbb{I}(y_i = m)(x_{ik} - \bar{x}_{.j}^{(m)})^2}$$

where j denotes the wavelength index, i = 1, ..., n denotes the spectra with n being the number 492 of spectra in the training set, m denotes the diet group with M = 3, $\mathbb{I}(y_i = m)$ is an indicator of 493 diet group spectra i, \bar{x}_{i} is the average of wavelength j for all spectra $(i = 1, ..., n), \bar{x}_{i}^{(m)}$ is the 494 average of wavelength j in diet group m. A wavelength with the highest Fisher score in each 495 of the discarded regions was kept in the analysis. Wavelengths with Fisher score lower than 496 0.002 were removed from further analysis, thus leaving 380 wavelengths. In order to compare 497 algorithms and carry out further feature selection, the training set was itself randomly split 498 75/25 into training and testing sets stratified by diet. A genetic algorithm [Holland, 1992], 499 implemented in library genalg [Willighagen and Ballings, 2022] was used as a stochastic search 500 method to find an optimal subset of input wavelengths for classification. Individuals in the GA 501 population were represented by binary strings denoting wavelengths to be included or excluded 502 for prediction. Objective function was set to be the average accuracy from ten cross-validated 503 fits of linear discriminant analysis (LDA) of the training subset. GA was run for 200 iterations 504 with population size set at 200. Figure 8 shows the spectra absorbance and the corresponding 505 Fisher scores, with points denoting the wavelengths selected by the GA. 506

The best configuration from the final GA population had 70 wavelengths included. These wavelengths were used as inputs to the following classification algorithms:

• Linear discriminant analysis (LDA), library MASS [Venables and Ripley, 2002];

- Partial least squares discriminant analysis (PLS-DA) [Mevik et al., 2020];
- Least absolute shrinkage and selection operator [LASSO; Tibshirani, 1996], library glmnet
 [Friedman et al., 2010];
- Elastic net [EN; Zou and Hastie, 2005], library glmnet;
- Random Forest [RF; Breiman, 2001], library ranger [Wright and Ziegler, 2017];
- Support vector machines [Vapnik, 1998], library kernlab [Karatzoglou et al., 2004];
- Bayesian kernel projection classifier [BKPC Domijan and Wilson, 2011], library BKPC 517 [Domijan, 2018].
- All analyses were done using R [R Core Team, 2020], the code is available in the github repository https://github.com/domijan/KD_Vistamilk2022.

The training set was randomly split into ten further training/testing sets of equal size, 520 stratified on diet. The average accuracy and standard deviation over the ten random splits 521 for all the classification algorithms are given in Table 8. LDA performed best with average 522 accuracy of 77.4%. PLS-DA and EN overall accuracy was of 76.9%, 76.5% respectively. The 523 algorithms were tuned using further cross-validation of the training sets. For BKPC and SVM, 524 the best results were obtained with a linear kernel. The predictions of the LDA were submitted 525 to the competition. Moreover, genetic algorithm was able to select a much smaller subset of 526 wavelengths without loss of classification performance. 527



Figure 8: Spectra absorbance and the corresponding Fisher score with points on the x-axis denoting the wavelengths selected by the GA.

Table 8: Average accuracy for over ten random splits of the training set for classifiers. LDA: linear discriminant analysis; PLS: partial least squares regression; EN: elastic net; BKPC: Bayesian kernel projection classifier; SVM: support vector machine; LASSO: Least absolute shrinkage and selection operator; RF: random forest.

Accuracy	LDA	PLS	\mathbf{EN}	BKPC	SVM	LASSO	\mathbf{RF}
Mean	0.774	0.769	0.765	0.759	0.738	0.736	0.509
SD	0.008	0.009	0.007	0.008	0.007	0.006	0.014

$_{528}$ 4 Discussion

While the dataset provided for the data competition included three different classes to dis-529 criminate (i.e. TRM, GRS, and CLV), the main difficulty of the present data competition was 530 concerned with the discrimination between GRS and CLV diets. In fact, the ability of dis-531 tinguishing pasture and TMR dietary regimens has been already documented [Frizzarin et al., 532 2021b], with the discrimination being driven mainly by the different content of fatty acids (FA) 533 in milk [Agradi et al., 2020]. In particular, milk from pasture based diet is generally richer in 534 saturated FA such as linoleic acid, poorer in saturate FA, and have a lower omega6/omega3 535 ratio [see e.g. Chilliard et al., 2007; Dewhurst et al., 2006; Ferlay et al., 2013, 2017]. As MIR is 536 known to be able to predict, with a certain degree of accuracy, the different FA in milk Soyeurt 537 et al., 2011, spectral data are therefore capable to discriminate also TMR and pasture diets. 538

On the other hand, since GRS and CLV dietary regimens differed only for the inclusion of 20% annual clover in perennial ryegrass sward for the CLV diet, induced differences in the FA might be less clear. As a consequence, to discriminate GRS and CLV exploiting spectral information only, a careful and accurate tuning of the modelling choices was required. In this regard, interestingly, some participants proposed two-steps classification approaches, with the first step focusing on TMR and pasture based diets, while the second one aimed at distinguishing CLV from GRS samples. As an example, participant 2 highlighted a potentially significant gain

Table 9: Accuracy computed on the test dataset for all the participants.

Participant	Sect 3.1.1	Sect 3.1.2	Sect 3.2	Sect 3.3.2	Sect 3.3.3
Test accuracy	0.871	0.837	0.798	0.711	0.783
Participant	Sect 3.3.4	Sect 3.4	Sect 3.5	Sect 3.6	
Test accuracy	0.796	0.786	0.724	0.766	

in terms of accuracy when considering an ensemble approach, where components extracted from LDA was used to train a linear SVM, better discriminating between GRS and CLV. Again, in Section 3.3.2 two consecutive LDA models have been fitted, with the first one being used to discriminate TMR from pasture while the second, exploiting the discriminant function on the pasture samples only, was trained to classify GRS and CLV.

Generally speaking, linear approaches introduce a gain in interpretability of the results, 551 while paying a price in terms of accuracy. Nonetheless, the review of the different approaches 552 presented in this paper showed that strong performances were achieved resorting to linear clas-553 sifiers. In fact, remarkable results were obtained when adopting LDA-based approaches (see, 554 e.g., participants 1, 2, 4 and 6), which were certainly proven effective in discriminating TMR 555 and pasture diets and, as highlighted above, were also used as a building block for promising 556 two-steps procedures. Nevertheless, the approaches presented in Sections 3.1.1 and 3.1.2, which 557 attained the best test set prediction accuracies as it is displayed in Table 9, pointed towards the 558 need of considering non-linearities, especially when the aim is to discriminate between GRS and 559 CLV. This is confirmed by the confusion matrix displayed in Table 10, where it is shown that 560 these two different dietary regimens are discriminated remarkably well, especially if considering 561 their similarities from a compositional standpoint. Note that, while with FCN interpretation 562 of the results and exploration of the most informative wavelengths are compromised, the ap-563 proach in Section 3.1.1, which is considering again LDA as the final classifier, tends to be more 564 transparent. However, the clever random polynomial variables generation proposed tends to 565 produce new features which are difficult to interpret from a chemical standpoint. Therefore, as 566 it often happens in modern data analysis routine, the adopted approaches have to be tailored 567 on the specific aim to pursue, often dealing with the standard trade-off between accuracy and 568 interpretability. 569

570

Data transformations, such as first and second derivative, are extensively used in near in-571 frared spectroscopy. In the current study with MIRS data, as widely undertaken, the only 572 transformation applied to the spectral data was their conversion from transmittance to ab-573 sorbance, since the other tested transformations did not show a strong impact on the quality of 574 the predictions. On the other hand the removal of noisy and non-informative spectral regions 575 seemed to be of fundamental importance, as reported by the participants which tested their pre-576 diction methods before and after their removal. For example, results from Section 3.1 showed an 577 improvement of 11.6% and of 25.7% when ridge regression and LDA were respectively used in 578 combination of new polynomial variables generation after water regions removal. Again, in Sec-579 tion 3.1.2 an improvement of the prediction performance, from 17.5% (CNN) to 20.5% (FCN), 580 after removing the water regions also when using deep learning methods is shown. Participant 581 1 also demonstrated the possibility to select the important variables directly from the spectra, 582 in fact they achieved the best prediction results using a variables selection approach starting 583 from all the spectral information (see Table 1). Variable selection was also tested in Section 3.6, 584 where a genetic algorithm was used to select a smaller subset of wavelengths without substantial 585 loss in classification performance. 586

In Section 3.3, the participants investigated the pairwise agreement among the three different approaches, to calculate by comparing the observations and quantifying the percentage of

Table 10: Final confusion matrix obtained with the approach outlined in Section Sect 3.1.1.

		Actual		
		CLV	GRS	TMR
	CLV	312	55	5
Predicted	GRS	61	300	5
	TMR	6	7	326

classifications in agreement on the total number of observations (Table 6). Methods applied by 589 members 1 and 2 gave similar predictions (agreement of 84.21%), whereby agreement between 590 predictions from member 3 was between 70.84% (with member 2) and 72.90% (with member 591 1). Although strong, the discrepancies among the three predictions could be due to: i) the 592 different number of samples retained for model development, and ii) the different number of 593 predictors (i.e., wavelengths) used for training, considering that the first member used the en-594 tire edited spectra, whereby the second and third applied different algorithms for wavelengths 595 selection. This investigation from the third participant permits to understand that differences 596 in data editing and different methodologies selected for the predictions, even if similar, brought 597 to consistently different class predictions. 598

A final discussion point was related to the creation of the test dataset. The dataset was 599 created by the organizers, who splitted the original dataset in 75% training and 25% test dataset, 600 considering a correct division of the classes across years into the 2 datasets. The discussion 601 revolved around whether or not divide the dataset into 75% training and 25% testing, or dividing 602 the dataset according to time components, like keeping the samples recorded in 2015 and 2016 603 into the training dataset, and the samples recorded in 2017 in the test dataset. Such temporal 604 division would permit to understand if samples recorded in previous years can predict future 605 information. 606

607 5 Conclusion

Thanks to the high number of participants, with different backgrounds, who provided their prediction results, the data competition was a thought-provoking occasion to discuss some of the challenges arising when analyzing spectral data and provided insightful indications.

As mentioned in the paper and as it was previously shown in Frizzarin et al. [2021b], the 611 stronger compositional dissimilarities between pasture-based diet and TMR-based ones induced 612 an easier discrimination between the corresponding classes. This generally led to overall good 613 performances, in terms of accuracy, for the adopted methods (see Table 9). On the other hand, 614 the distinction between milk samples originated from GRS and CLV was more challenging. 615 Nonetheless, as it is shown in Table 10, some hand-crafted strategies specifically proposed for 616 this competition showed more than promising results also when employed to detect differences 617 in the composition between distinct pasture-based feeding regimens. In particular, non-linear 618 transformations of the original wavelengths and two-steps classification approaches, outlined in 619 Section 3.1 and 3.3, seemed to be effective in solving this problem. 620

Pre-treatments were generally not beneficial for the improvement of the prediction equations, 621 while the deletion of the spectral regions related to water (with manual selection of these regions 622 or by means of automatic variable selection procedures) improved the prediction results. The 623 utilization of linear models, in particular LDA, provided some of the best results, and the 624 overall best prediction was achieved using LDA applied after wavelengths selection and random 625 polynomial generation, as it was shown in Table 9. When spectral analyses are undertaken it 626 is important to know not only the best possible statistical methods to use for the analyses, but 627 also what is the best data editing for such data. 628

629 A Supplementary material

630 A.1 Deep neural network architecture

Table S1: List of the deep model architectures considered in Section 3.1.2, including the number of trainable parameters for each model and the type of input data they accept.

Model Architecture	Parameters	Input Data and Shape			
FCN					
- Dense layers of 1024, 512, 128, 64 and 32 units					
- Output layer of 3 units					
- Dropout for dense layers, drop rate of 0.2	1 795 099	- Linear, full (1060)			
- ELU activation for hidden layers	1,765,925	- Linear, reduced (518)			
- softmax activation for output layer					
- Adam optimiser, initial learning rate of 0.0001					
- Categorical cross entropy as loss function					
CNN					
- Convolutional layers with 32, 64 and 128 filters					
- Filters of shape $(3, 3), (2, 2)$ and $(2, 2)$					
- Flattening layer		- Squared, full (33×33)			
- Dense layers of 512, 256, 128, 64, and 32 units	55 222 /10				
- Output layer of 3 units	55,552,419	- Squared, reduced (23×23)			
- ELU activation for hidden layers					
- softmax activation for output layer					
- Adam optimiser, initial learning rate of 0.0001					
- Categorical cross entropy as loss function					
CNN_DILATED		Squared full (33×33)			
- Same architecture as CNN	$41,\!176,\!643$	- Squared, reduced (22×22)			
- Kernels built with a dilation rate of $(2, 2)$		- Squared, reduced (23×23)			

631 A.2 Participant 3

Wavenumber, cm^{-1}	Function	
	1	2
1069	2.899	0.298
1130	-3.790	0.416
1181	-2.003	5.371
1269	-7.321	-2.495
1292	10.544	-3.045
1377	-5.860	-0.482
1416	-5.885	1.267
1439	12.710	1.112
1474	-4.689	3.714
1539	-3.816	-2.385
1577	4.442	1.247
1752	11.958	6.035
2782	-1.459	0.875
2851	-15.686	-13.612
2890	16.085	3.459
2932	-4.166	0.916
Eigenvalue	1.732	0.109
& of variance	94.1%	5.9%
Canonical correlation	0.796	0.313

 $Table \ S2: \ Standardized \ canonical \ discriminant \ function \ coefficients \ of \ the \ variables \ selected \ by \ DA \ and \ effective \ size \ measures.$

Table S3: Group means (centroids) for the Discriminant Functions

Diet	Function	
	1	2
CLV	0.872	0.403
GRS	0.954	-0.400
TMR	-1.895	-0.012

Table S4: Classification related statistics and leave-one-out cross-validation. ^a 71% of original grouped cases correctly classified. ^b Cross-validation is done only for those cases in the analysis. In cross-validation, each case is classified by the functions derived from all cases other than that case. 70.5% of cross-validated grouped cases correctly classified.

		Diet	Predicted Group Membership		Total	
		Diet	CLV	\mathbf{GRS}	\mathbf{TMR}	Total
Original ^a	Count	CLV	629	363	83	1075
		\mathbf{GRS}	323	668	62	1053
		\mathbf{TMR}	39	44	942	1025
	%	CLV	58.5	33.8	7.7	100.0
		\mathbf{GRS}	30.7	63.4	5.9	100.0
		\mathbf{TMR}	3.8	4.3	91.9	100.0
$\mathbf{Cross-validated}^b$	Count	CLV	620	369	86	1075
		GRS	326	663	64	1053
		\mathbf{TMR}	39	47	939	1025
	%	CLV	57.7	34.3	8.0	100.0
		GRS	31.0	63.0	6.1	100.0
		\mathbf{TMR}	3.8	4.6	91.6	100.0



Figure S1: Line plot of raw spectra expressed in transmittance (A), conversion of raw spectra from transmittance fo absorbance (B; red boxes indicate low signal-to-noise regions), and raw spectra in absorbance after noisy area removal (C).

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⁶³⁹ Declaration of interests

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

642 Data availability

⁶⁴³ Data used in the present paper are available upon request from the corresponding author.

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