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This is the final peer-reviewed author's accepted manuscript (postprint) of the following publication:

Published Version:

Farhad Zeighami, Leonardo Sandoval, Alberto Guadagnini, Vittorio Di Federico (2023). Uncertainty quantification and global sensitivity analysis of seismic metabarriers. ENGINEERING STRUCTURES, 277, 1-13 [10.1016/j.engstruct.2022.115415].

Availability: This version is available at: https://hdl.handle.net/11585/909731 since: 2024-07-03

Published:

DOI: http://doi.org/10.1016/j.engstruct.2022.115415

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(Article begins on next page)

# Uncertainty quantification and global sensitivity analysis of seismic metabarriers

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# Abstract

Seismic metabarriers consist of an array of locally resonant elements (i.e., mechanical resonators) installed over the soil surface, whose design is rationally engineered to reduce ground-induced vibrations and shield vulnerable structures against seismic surface waves. Successful design and implementation of seismic metabarriers require a comprehensive knowledge and characterization of the role played by the model parameters (and their associated uncertainty) governing soil-barrier dynamic interaction. In this context, sensitivity analysis techniques allow assessing the response of a given model through the quantification of the influence and action of model inputs (and model input uncertainties) concerning a target model output. This study relies on global sensitivity analysis techniques to investigate the influence that the uncertainty associated with three key mechanical parameters of a metabarrier (i.e., soil density, soil shear modulus, and mass of mechanical resonators) has on its seismic isolation performance. The latter is measured in terms of transmission coefficient (TC). We do so by employing a two-dimensional wave finite element model developed under the plane-strain conditions to evaluate the dispersion relation and transmission coefficient of a metabarrier interacting with Rayleigh waves in the low-frequency regime (i.e., frequencies between 2Hz and 7Hz). Our results suggest that the shear modulus is the uncertain parameter with the most significant influence on the transmission coefficient of the metabarrier across the entire frequency range of interest. Otherwise, the resonator mass plays a substantial role in the frequency range close to the metabarrier resonant frequency.

Preprint submitted to Engineering Structures

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*Keywords:* Seismic metamaterials, Metabarrier, Seismic surface waves, Global sensitivity analysis, Surrogate modeling, Polynomial chaos expansion.

#### 1 1. Introduction

Elastic metamaterials are artificial composite structures designed to possess un-2 conventional mechanical properties (Devmier et al., 2013). Since their emergence 3 around two decades ago, elastic metamaterials have found several applications in 4 mechanical and civil engineering fields. In the context of earthquake engineering, 5 seismic metamaterials (SMs) are proposed as an innovative isolation technique to 6 safeguard critical and vulnerable structures such as high-rise buildings, urban areas, 7 historical places, and heritage sites (Brûlé et al., 2014; Krödel et al., 2015; Colombi 8 et al., 2016c; Miniaci et al., 2016). SMs are generally classified according to their g application, regulation mechanisms, and arrangement patterns (Mu et al., 2020). 10 From an application perspective, SMs are categorized as periodic (Cheng and Shi, 11 2013; Cheng et al., 2020) and resonant foundations (Basone et al., 2019; Sun et al., 12 2019) that interact with seismic waves to shield unprotected residential buildings 13 and industrial facilities, as well as periodic (Huang and Shi, 2013; Ni and Shi, 2022) 14 and resonant barriers (Palermo et al., 2016; Colombi et al., 2017) to protect critical 15 infrastructures or structures against incident surface waves. Among these systems, 16 locally resonant barriers, namely metabarriers, incorporate wave-impeding devices 17 with feasible dimensions from an engineering attitude that do not require any struc-18 tural intervention to the target infrastructure. 19

A seismic metabarrier is a passive resonant barrier organized as an arbitrary 20 arrangement of resonant structures/units with dimensions much smaller than the 21 wavelength of seismic waves (Palermo et al., 2016). Metabarriers are typically in-22 stalled in the vicinity of target structures and activated by the motion of incoming 23 waves. The operating resonant frequency of a metabarrier is usually tuned in the 24 low-frequency regime (i.e. below 10 Hz), where most of the elastic energy of seismic 25 waves exists (Colombi et al., 2016c; Palermo et al., 2016, 2018b). The dynamic in-26 teraction between metabarrier and seismic waves is described analytically through 27 the effective medium approach (Boechler et al., 2013) and the multiple scattering 28 theory (Pu et al., 2021) and further assessed through finite element (FE) numerical 29 analyses (Palermo et al., 2018b; Zeighami et al., 2019). The attenuation perfor-30 mance of a metabarrier was verified in small-scale laboratory tests for shear vertical 31 (Palermo et al., 2016; Zaccherini et al., 2020a) and shear horizontal surface waves 32 (Zaccherini et al., 2020b). Since then, metabarriers have been associated with vari-33 ous applications in waveguiding (Maznev and Gusev, 2015), wave filtering (Colombi 34

et al., 2016c), wave focusing (Colombi et al., 2016b), and energy harvesting (De Ponti
et al., 2020).

After the introduction of the metabarrier concept in civil and material engineering 37 communities, various design strategies have been proposed to enhance their efficiency 38 in terms of seismic wave attenuation. These include the exploitation of mechanical 39 oscillators (Palermo et al., 2016), resonant pillars (Colombi et al., 2016a), or locally 40 resonant inclusions (Zeighami et al., 2021a) as the fundamental unit of metabarriers. 41 Several studies are then keyed to the assessment of optimal spatial arrangement of 42 mechanical resonators. These resonant elements can be either installed at the soil 43 surface (Boutin and Roussillon, 2006) or buried inside soil layers (Zaccherini et al., 44 2020a; Zeighami et al., 2021a). To the best of our knowledge, previous literature 45 studies evaluate the seismic wave attenuation associated with the metabarriers by 46 considering their design parameters as deterministic quantities. Otherwise, in the 47 context of geophysical sciences, various types of uncertainties are associated with 48 the soil system and mechanical resonators. Henceforth, the aim of this research is 49 two-fold: (i) to identify the uncertain parameters of the coupled soil-barrier dynamic 50 system, and (ii) to quantify the influence of these uncertain parameters on the sur-51 face wave attenuation performance of metabarriers measured as the transmission 52 coefficient (TC). 53

In this work, we employ global sensitivity analysis (GSA) techniques to quan-54 tify the influence of the uncertainties associated with the mechanical properties of 55 metabarrier components on the seismic wave attenuation of the latter. We rely on 56 (i) the classical variance-based Sobol indices, which quantify the expected reduction 57 of a model output variance due to the knowledge of (or conditioning on) a parameter 58 value, and (ii) the moment-based AMA indices, which quantify the normalized ex-59 pected deviation of the statistical moment of a model output due to the knowledge of 60 (or conditioning on) a parameter value. Sobol indices are broadly used in structural 61 engineering problems, including for instance load-carrying capacity analysis of steel 62 plane frames (Kala, 2011) and axial load evaluation of tie-rod elements (De Falco 63 et al., 2021). AMA indices (termed after the initials of the authors) have been re-64 cently proposed by Dell'Oca et al. (2017). These global sensitivity metrics recognize 65 that the uncertainty of a model parameter can be imprinted onto diverse statisti-66 cal moments of model outputs. They have been applied to quantify uncertainty in 67 different civil engineering scenarios, including degradation of contaminants in soils 68 (la Cecilia et al., 2020), groundwater flow (Bianchi Janetti et al., 2019), and gas flow 69 in low permeable materials (Sandoval et al., 2022). In the context of geotechnical 70 and earthquake engineering, other global sensitivity analysis techniques have been 71 employed for uncertainty quantification of layered periodic foundations (Liu et al., 72

<sup>73</sup> 2020), offshore wind turbine foundations (Velarde et al., 2019), and ground motion
<sup>74</sup> modeling in seismic risk assessment (Vetter and Taflanidis, 2012).

Successful application of GSA techniques typically requires multiple evaluations 75 of the model to be analyzed. In cases where such evaluation is associated with a 76 heavy computational burden, applying GSA may become unfeasible (Sudret, 2008). 77 In such a case, using a reduced complexity model minimizes the computational bur-78 den associated with the evaluation of the model whilst preserving the relationships 79 between the inputs and outputs of the model (Dell'Oca et al., 2017). In this study, 80 we rely on polynomial chaos expansion (PCE) to construct models of reduced com-81 plexity, our approach being otherwise fully compatible with other model reduction 82 techniques. PCE-based techniques have been widely employed in studies to quantify 83 uncertainty in diverse civil engineering areas such as dam engineering (Hariri-Ardebili 84 and Sudret, 2020), hydraulic fracturing operations (Gläser et al., 2016), and  $CO_2$  se-85 questration (Zhang and Sahinidis, 2013). 86

The paper is structured as follows: first, the analytical expression underlying the 87 design of seismic metabarriers is given in Sec. 2.1. A two-dimensional Finite Element 88 (FE) model of the metabarrier basic module is developed in Sec. 2.2 to demonstrate 89 the dispersive features of a single resonator. Then, a full numerical model of the 90 entire barrier is realized to assess its seismic isolation efficiency in Sec. 2.3. Next, 91 uncertain model parameters influencing the attenuation efficiency of a metabarrier 92 are introduced in Sec. 2.4. Secs. 2.5 and 2.6 describe the GSA and surrogate model-93 ing techniques employed in the study. The accuracy of the surrogate models, as well 94 as the results of the GSA, are presented in Sec. 3. Finally, conclusions and future 95 research directions are addressed in Sec. 4. 96

#### 98 2. Methodology and materials

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In this Section, we explain the design methodology of a locally resonant metabar-99 rier rationally engineered to impede the propagation of seismic surface waves. Metabar-100 riers are composed of a series of passive mechanical resonators organized in a regular 101 grid with identical spacing to be directly placed over the soil surface. The metabarrier 102 is installed in the proximity of a target structure/infrastructure and activated by the 103 motion of incoming waves. The dynamic coupling between a seismic metabarrier and 104 vertically-polarized seismic waves (also called Rayleigh waves) is studied analytically 105 via a closed-form dispersion law proposed by Palermo et al. (2016), where resonators 106 are assumed to have a linear elastic behavior and the soil is modeled as an isotropic 107 and homogeneous half-space. In this dynamic system, the exchange of stress between 108

resonators and the soil generates a low-frequency band gap (BG) in the frequency spectrum of surface waves, where a significant ground-motion attenuation is expected (Colquitt et al., 2017). The band gap width depends on the operating frequency and mass per unit area of the resonators (Palermo et al., 2016). Since no surface mode can propagate within the band gap frequency region, the elastic energy of the seismic waves diverges from the soil surface trajectory to the bulk media (Colquitt et al., 2017).

Recently, more complex theoretical models have been developed to account for the 116 soil heterogeneity (Zeng et al., 2022) and its non-linear behavior (Kanellopoulos et al., 117 2022), as well as exploiting non-linear resonators inside the metabarrier arrangement 118 (Palermo et al., 2022). For the case of stratified soil, the emergence of the band 119 gap in the dispersion relation is discarded by the propagation of higher-order surface 120 modes. Thus, surface-to-shear wave conversion is hindered. However, a substantial 121 ground motion reduction is observed around the collective resonant frequencies of 122 the resonators (Palermo et al., 2018a; Zeng et al., 2022). These additional complex-123 ities are usually ignored in the long-wavelength (low-frequency) regime to develop 124 theoretical frameworks that capture the fundamental physics of wave propagation 125 settings. Hence, we resort to a linear elastic resonator and a linear, homogeneous, 126 and isotropic soil model in this study. 127

The overall workflow and research methodology are depicted in Fig. 1 and discussed extensively in the following. We first present the analytical dispersion law for the seismic metabarrier. We then illustrate the seismic isolation assessment of the barrier through a surrogate model and by a global sensitivity analysis of the uncertain parameters.

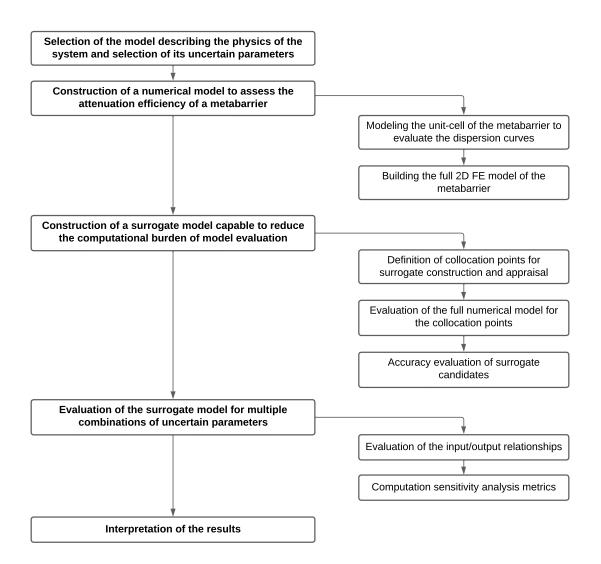


Figure 1: Global sensitivity analysis framework used to assess seismic isolation performance of a compact seismic metabarrier.

## <sup>133</sup> 2.1. Analytical dispersion relation of seismic metabarriers

<sup>134</sup> We study Rayleigh wave propagation through an elastic half-space equipped with <sup>135</sup> a finite-size array of surface resonators, as shown in Fig. 2. Rayleigh waves are <sup>136</sup> propagating in the *x*-direction, while they are polarizing in the *z*-direction. We note <sup>137</sup> that parameters related to resonator and soil are denoted with subscription r and <sup>138</sup> s, respectively. The resonators have a length of  $a_r$  and an out-of-plane depth of  $l_r$  that assumes a unit value in a 2D problem. As such, the resonators have dimensions much smaller than the wavelength of surface Rayleigh waves, i.e.  $a_r \ll \lambda_{RW}$ , and they are distributed in a regular arrangement with an equal spacing of  $a_r$ , identical to the resonator length. Hence, the resonator influence area is  $A_r = a_r \times l_r$ .

The half-space is constituted by an isotropic and homogeneous soil with density  $\rho_s$ , Poisson's ratio  $\nu_s$ , Young's modulus  $E_s$ , and shear modulus  $G_s = E_s/(2(1 + \nu_s))$ . Each resonator of the metabarrier has a mass  $m_r$  linked to the soil surface via linear elastic springs with axial stiffness  $K_r$ . Relying on a 2D instead of a 3D model can enable one to capture the main physics of resonator-soil coupling scenarios (see, e.g. (Palermo et al., 2016; Colquitt et al., 2017; Palermo et al., 2018b)).

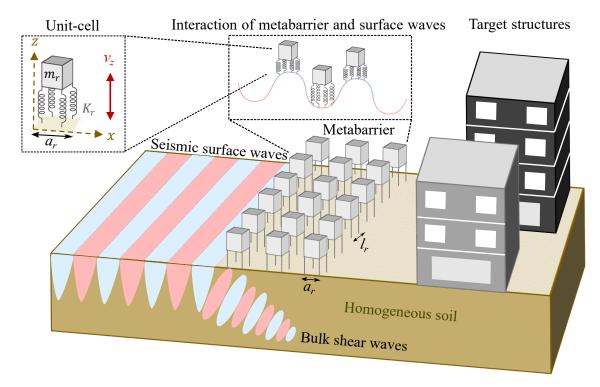


Figure 2: Schematic of a seismic metabarrier composed of surface resonators interacting with incoming seismic surface waves. The inset shows a unit-cell of the metabarrier consisting of a rigid mass and four elastic springs.

The interaction between the sub-wavelength resonators of a metabarrier, the elastic soil domain, and surface Rayleigh waves is defined via the effective medium approach (Maznev and Gusev, 2015). According to the latter, a metabarrier can be seen as a thin resonant boundary layer that exerts uniform vertical stress on the soil <sup>153</sup> surface. This approximation allows for deriving a dispersion law (i.e., the relation-<sup>154</sup> ship between the wavenumber and frequency space) that predicts the fundamental <sup>155</sup> dispersive features of metabarriers and guides their design procedure. We exploit the <sup>156</sup> dispersion relation originally developed by Boechler et al. (2013), and update it in <sup>157</sup> terms of the elastic modulus of a homogeneous soil and of the mechanical parameters <sup>158</sup> of the resonators as:

$$\left(\frac{m_r\omega^2}{K_r}-1\right)\left[\left(2-\frac{\rho_s\omega^2}{G_sk^2}\right)^2-4\sqrt{1-\frac{\rho_sC^2\omega^2}{G_sk^2}}\sqrt{1-\frac{\rho_s\omega^2}{G_sk^2}}\right] = \frac{m_r\rho_s}{a_rl_rG_s^2}\frac{\omega^4}{k^3}\sqrt{1-\frac{\rho_sC^2\omega^2}{G_sk^2}},$$
(1)

where  $\omega = 2\pi f \text{ [rad/s]}$  represents angular frequency, f [Hz] is frequency, k [rad/m] is a wavenumber vector that can vary from 0 to the edge of the first Brillouin zone (i.e.,  $\pi/a_r$ ), and  $C = \sqrt{(1 - 2\nu_s)/(2 - 2\nu_s)} = c_T/c_L$  is a dimensionless quantity expressing the ratio between the shear and longitudinal wave velocities. The dispersion relation can be formulated either in terms of Lamé parameters by exploiting the expressions  $\mu = G_s$  and  $\lambda = 2G_s/(1 - 2\nu_s)$  or via the longitudinal and shear wave speeds, whose expressions are given in Eqs. (2).

$$c_L = \sqrt{\frac{2G_s(1-\nu_s)}{\rho_s(1-2\nu_s)}}, \quad c_T = \sqrt{\frac{G_s}{\rho_s}}.$$
 (2a-b)

Eq. (1) shows that the wavenumber (k) is a function of the frequency (f), the mechanical parameters of the resonator  $(m_r, a_r, l_r, K_r)$ , and the soil parameters  $(\rho_s, G_s, \nu_s)$ . For the sake of completeness, the dispersion relation (Eq. (1)) is recast in a dimensionless format in Appendix A.

### 170 2.2. Numerical assessment of the metabarrier through a Wave Finite Element Method

Our study relies on the Wave Finite Element Method (WFEM), initially proposed 171 by Mace and Manconi (2008) and further developed by Palermo et al. (2018b) to 172 assess the ground vibration attenuation capability of locally resonant metabarriers. 173 The WFEM rests on the conventional finite element model of a small portion of the 174 composite waveguide (namely the unit-cell) to quantify its dynamic response against 175 incoming waves. So far, this method has been applied to various composite structures 176 such as beams, pipes, laminated plates, sandwich panels, and thin-walled structures. 177 The efficiency of the WFEM for the case of seismic surface wave propagation through 178 a finite-length barrier placed on top of a soil column has been assessed in recent 179

studies (Zeighami et al., 2019, 2021b,a; Palermo et al., 2022). According to WFEM, 180 a numerical model of a single resonator linked to a 2D soil column can be envisaged to 181 satisfy the analytical dispersion law of Eq. (1). Such an approach allows modeling the 182 entire barrier to evaluate its seismic isolation performance. The coupled resonator-183 soil column represents a unit-cell (fundamental module) of the barrier. The dynamic 184 response of a finite-size chain of unit-cells obtained from frequency domain analysis 185 yields the numerical dispersion curves. The accuracy of the developed FE model will 186 then be verified against analytical solutions of Eq. (1). 187

We develop a two-dimensional FE model of a metabarrier unit-cell according to 188 a realistic engineering design of a metabarrier. The unit-cell (see Fig. 3a) consists 189 of a rigid mass  $(m_r)$  attached to a soil column via two vertical elastic springs, each 190 having an axial stiffness of  $K_r/2$ . The length of the soil column is being taken to 191 coincide with the resonators' spacing,  $a_r$ . The soil depth is considered large enough 192 to mimic a semi-infinite soil media as  $3\lambda_0$ , where  $\lambda_0 = c_R/f_r$ ,  $c_R$  is the Rayleigh wave 193 velocity, and  $f_r = (1/2\pi)\sqrt{K_r/m_r}$  is the resonant frequency of the resonators. The 194 vertical and horizontal displacements of the soil bottom are restricted to avoid any 195 undesirable motion. The horizontal displacement of the resonator mass is suppressed 196 while the springs are allowed to elongate and compress along their vertical axis. 197 Bloch periodicity conditions (Brillouin, 1946) are imposed on the lateral edges of the 198 soil column to construct the numerical dispersion curve. The resonator mass and 199 soil domain are discretized via triangular mesh elements with a minimum dimension 200  $L_m = \lambda_0/10$ . Each spring is represented by a single truss element with one node at 201 each joint. We seek the eigenfrequency solutions of the unit-cell in the wavenumber 202 interval of  $k = [0, \pi/a_r]$ . 203

# 204 2.3. Application to a finite-size metabarrier attached to different homogeneous soil 205 layer

We implement WFEM on a compact metabarrier to assess its seismic surface 206 waves isolation efficiency. The proposed metabarrier is composed of a finite number 207 of equidistant resonators distributed over a total length  $\lambda_0$  which is equivalent to an 208 array of 20 unit-cells with an equal spacing  $a_r = 1 \text{ m}$  (see Fig. 3b). We note that this 209 is the minimum length of the barrier enabling one to detect the attenuation effect. 210 Increasing the length of the barrier (or, conversely, the number of resonators) would 211 result in an enhanced attenuation (Pu et al., 2021). The full 2D model of the barrier 212 is developed on the basis of the reduced numerical model of the unit-cell (see Fig. 213 3a); its height is equal to the depth of unit-cell  $(3\lambda_0)$  and has a total length of  $18\lambda_0$ , as 214 shown in Fig. 3c. A harmonic input source excites the entire domain. The left part 215 of the domain represents a reference soil (i.e., soil without metabarrier), whereas the 216

right side of the domain includes the metabarrier zone. The metabarrier is placed 217 at a distance of  $5\lambda_0$  from the input source to eliminate near-source effects. Both 218 bottom corners of the soil domain are fixed to maintain the static stability of the 219 model during simulations. In addition, Low-Reflective Boundary (LRB) conditions 220 are imposed on the lateral and bottom edges of the model to minimize the back-221 reflection of surface waves from the boundaries. The barrier response is extracted 222 from an output region with a length  $L_{out} = \lambda_0$  placed after the metabarrier zone, 223 namely barrier output. The same quantity is measured for the reference soil from 224 the left part of the model (see soil output in Fig. 3c) to compare the soil response 225 equipped with resonators with bare soil condition. 226

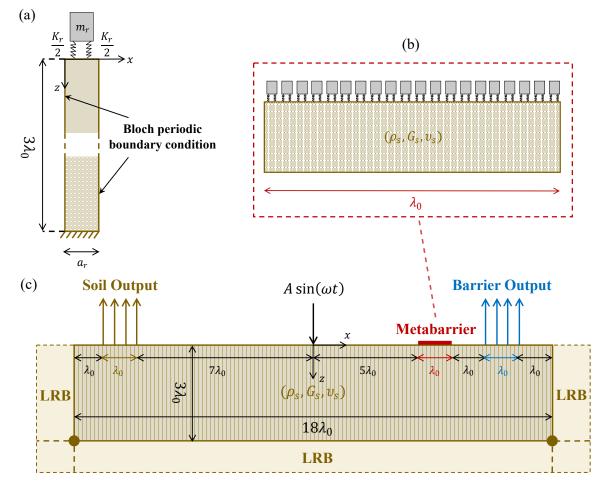


Figure 3: Schematics of the seismic metabarrier FE model. (a) A representative unit-cell of the metabarrier. (b) An array of 20 resonators forms the metabarrier. (c) The 2-D wavefield model used to calculate the Transmission Coefficient (TC).

To quantify the seismic isolation performance of the barrier, one can either per-227 form a time-history analysis and measure the soil response via Fourier transform 228 (Zeighami et al., 2021b) or perform harmonic analysis to explicitly obtain the re-229 sult in the frequency domain (Palermo et al., 2018b). In this study, we employ 230 the latter approach (i) to understand the physics of the problem by evaluating the 231 transmission/attenuation performance of the metabarrier at different frequencies and 232 comparing the results with their counterparts obtained from the dispersion analy-233 sis and (ii) to minimize the computational cost of simulations. In this context, a 234 harmonic displacement excites the model from the center to evaluate the Transmis-235 sion Coefficient (TC) and Attenuation Coefficient (AC) of the metabarrier (Palermo 236 et al., 2018b) as: 237

$$TC(f) = \frac{\int_{0}^{L_{out}} |v_{b}| dx}{\int_{0}^{L_{out}} |v_{s}| dx}, \quad AC(f) = 1 - TC(f),$$
(3a-b)

where  $v_b$  is the vertical nodal displacement of the soil measured from barrier output (see Fig. 3c), to be averaged over the output length  $L_{out}$ , and  $v_s$  is the same quantity evaluated from the reference soil in the absence of the metabarrier.

#### 241 2.4. Uncertain model parameters

During the design and implementation phases of a seismic metabarrier, the out-of-242 plane depth  $(l_r)$  and the resonators spacing  $(a_r)$  are typically considered as determin-243 istic parameters. The mass  $(m_r)$  and stiffness  $(K_r)$  of the resonator can be regarded 244 as uncertain parameters due to manufacturing imperfections in their geometries or 245 weight differences. To streamline the analysis, we consider mass as the only uncer-246 tain parameter of the resonator, since the mass per unit area ratio  $(m_r/(a_r l_r))$  in 247 Eq. (1) controls the hybridization of the fundamental surface mode (Palermo et al., 248 2016). Regarding the mechanical parameters of the soil, these data are generally 249 obtained from experiments. Thus, their estimates are typically uncertain, even for 250 homogeneous and isotropic geomaterials. Since the variation of the Poisson ratio  $(\nu_s)$ 251 is generally less pronounced than variations of mass density  $(\rho_s)$ , and given that the 252 shear modulus  $(G_s)$  is related to  $\nu_s$  via the Young modulus  $(E_s)$ , we consider  $\rho_s$  and 253  $G_s$  as the uncertain parameters of the soil and set  $\nu_s$  as a deterministic parameter. 254 In summary, the uncertain model parameters of the present study are  $\rho_s$ ,  $G_s$ , and 255  $m_r$ . 256

To rigorously assess the significance of uncertain parameters on the isolation properties of metabarriers, we consider three common soil scenarios found in nature.

We assume that such soils have homogeneous mechanical properties throughout the 259 depth of the elastic waveguide. The soil types are (i) sedimentary soil (S1), (ii) com-260 pletely weathered granite (S2), and (*iii*) silty-clay soil (S3). These soil types are not 261 ideal for construction purposes and require engineering intervention to increase their 262 bearing capacities. Sedimentary soils are loose sediments usually found near river 263 basins. Weathered granite soils are found in mountainous areas where infrastructures 264 (dams, mountain roads, and railways) are built. Silty clay soil is an intermediate be-265 tween sandy and clay soils that tends to shift due to moisturizing/drying; therefore, 266 they require deep foundations to protect the infrastructures against seismic action. 267

In this study, the uncertain model parameters are considered independent and 268 identically distributed random variables, each characterized by a uniform distribution 269 within the intervals listed in Table 1. The choice of the latter distribution enables 270 one to give the same weight to all parameter values across their support. We assume 271 that the ranges of the variability of  $\rho_s$  and  $G_s$  are centered around the values ex-272 perimentally found by Cai et al. (2021), who documented Rayleigh waves velocities 273  $c_R = [94.91, 64.70, 55.80]$  m/s for S1, S2, and S3, respectively. An effective coupling 274 between the metabarrier and the soil is seen for sedimentary soils with  $c_R < 1000$ 275 m/s (Colombi et al., 2016c). Even as values of the soil parameters of the current 276 study (see Table 1) are representative of sedimentary-basins-like (soft) soils with low 277 Rayleigh wave speeds, the sensitivity of the results discussed in Sec. 3 are not strictly 278 limited to these wave velocity ranges, and can be extended in future studies to the 279 soils with average Rayleigh celerity  $(300 \le c_R \le 500 \text{ m/s})$ . 280

We consider the uniform distributions of  $\rho_s$  and  $G_s$  to be characterized by a 281 coefficient of variation of 10% to encompass a range of values typical of common 282 engineering applications. The lower and upper bound of the support associated with 283 the distribution of the resonator mass are defined upon considering a 5% coefficient 284 of variation. The mean value of the resonator mass is assumed to be 1500 kg. We 285 consider a target resonant frequency of  $f_r = 5$  Hz for the incoming waves. This, in 286 turn, leads to an axial stiffness of the resonator  $K_r = 1480$  kN/m and  $\lambda_0 = 19$  m, 287 13 m, and 11 m for S1, S2, and S3, respectively. Table 1 lists, for each Scenario, 288 the range of variability of the model's uncertain parameters and the value of the 289 deterministic parameters. 290

#### 291 2.5. Global sensitivity analysis (GSA)

We employ GSA techniques to diagnose the influence that the uncertainties on model parameters ( $\rho_s$ ,  $G_s$ ,  $m_r$ ) have on the attenuation performance of the metabarrier (measured as TC and evaluated via Eq. 3a). As stated in Section 1, we rely on (*i*) the classical variance-based approach grounded on the evaluation of the well-known

Model parameters			Scenario 1	Scenario 2	Scenario 3
Parameter	Units	CV [%]	Range/Value		
$G_s$	MPa	10	13.5 - 16.5	9.36 - 11.44	6.14 - 7.50
$\rho_s$	$kg/m^3$	10	1350 - 1650	1890 - 2310	1665 - 2035
$m_r$	kg	5	1425 - 1575	1425 - 1575	1425 - 1575
$\nu_s$	-	-	0.45	0.25	0.32
$K_r$	kN/m	-	1480		
$a_r$	m	-	1		
$l_r$	m	-	1		

Table 1: Ranges of variability for the model uncertain parameters considered in the GSA and values of deterministic model parameters considered in this study. Values of the coefficient of variation of the uncertain model parameters are also listed.

Sobol indices (Saltelli and Sobol', 1995) and (*ii*) the moment-based GSA framework introduced by Dell'Oca et al. (2017).

# 298 2.5.1. Variance-based Sobol Indices

Sobol indices (Saltelli and Sobol', 1995) quantify the relative expected reduction of the variance of a target model output due to knowledge of (or conditioning on) an uncertain model parameter. In this context, considering a model output  $\zeta$ , which depends on P random parameters collected in vector  $\boldsymbol{\theta} = (\theta_1, \theta_2, ..., \theta_P)$  and defined within the space  $\Gamma = \Gamma_1 \times \Gamma_2 \times ... \times \Gamma_P$  ( $\Gamma_p = [\theta_{p,min}, \theta_{p,max}]$  corresponding to the support of the p-th parameter,  $\theta_p$ ), the principal Sobol' index  $S_{\theta_p}$  associated with a given model parameter  $\theta_p$  is evaluated as

$$S_{\theta_p} = \frac{V\left[E\left[\zeta|\theta_p\right]\right]}{V\left[\zeta\right]}.$$
(4)

Here,  $E[\cdot]$  and  $V[\cdot]$  represent expectation and variance operators, respectively; the 306 notation  $\zeta | \theta_p$  denotes conditioning of  $\zeta$  on a value of  $\theta_p$ . Note that  $S_{\theta_p}$  describes 307 the relative contribution to  $V[\zeta]$  due to variability of only  $\theta_p$ . Joint contributions of 308  $\theta_p$  with other model parameters included in  $\boldsymbol{\theta}$  to the variance of  $\zeta$  are embedded in 309 the total Sobol indices (details not shown). Note that by relying on Sobol indices 310 to diagnose the relative importance of uncertain model parameters to model outputs 311 one assumes that the uncertainty of a model output is completely characterized by its 312 variance. Thus, even though Sobol indices are characterized by conceptual simplicity 313 and straightforward implementation and use, they provide only limited information 314 about the way variations of model parameters can influence the complete probability 315

<sup>316</sup> density function (pdf) of model outputs.

#### 317 2.5.2. Moment-Based AMA Indices

The moment-based GSA approach proposed by Dell'Oca et al. (2017, 2020) rests 318 on the idea that quantifying the effects of model parameter uncertainty on various 319 statistical moments of the ensuing pdf of model outputs can provide an enhanced 320 understanding of model functioning. Dell'Oca et al. (2017) introduce Moment-Based 321 sensitivity metrics (termed AMA indices) according to which one can evaluate the 322 influence of uncertain model parameters on key elements of the model output pdf, 323 as embedded in its associated statistical moments. The AMA indices are defined as 324 follows (Dell'Oca et al. (2017)): 325

$$AMAM_{\theta_p} = \frac{1}{|M[\zeta]|} E\left[|M[\zeta] - M\left[\zeta|\theta_p\right]|\right].$$
(5)

Here,  $AMAM_{\theta_p}$  represents the indices associated with a model parameter  $\theta_p$  and a given statistical moment M of the pdf of model output  $\zeta$ . For the purpose of our study we focus on the first two moments (i.e., the mean (M = E) and the variance (M = V)) of the model output pdf. The AMA indices are intended to quantify the relative importance of parameter  $\theta_p$  on a given statistical moment of  $\zeta$ . Large values of these indices indicate that  $\zeta | \theta_p$  strongly deviates from its unconditional counterpart.

#### 333 2.6. Surrogate model

To employ the previously described GSA techniques, several evaluations of TC334 under diverse combinations of  $\rho_s$ ,  $G_s$ , and  $m_r$  are required. Such a procedure is 335 impractical in our scenario due to the heavy computational burden associated with 336 the evaluation of TC. One single simulation takes approximately 72 seconds on 337 an Intel Core i7-116G7 @ 2.80GHz with 32GB of Memory. Thus, here we rely on 338 a generalized Polynomial Chaos Expansion (gPCE) surrogate of the full numerical 339 model that allows for reducing the computational time associated with the execution 340 of the GSA technique (Dell'Oca et al., 2017; Sudret, 2008). 341

In the context of gPCE, a model  $g(\boldsymbol{\theta})$  can be expressed as a linear combination of the multivariate polynomials,  $\psi_i(\boldsymbol{\theta})$ , i.e.,

$$g(\boldsymbol{\theta}) \approx \sum_{i \in \Lambda^{P,D}} \beta_i \psi_i(\boldsymbol{\theta}),$$
  

$$\psi_i(\boldsymbol{\theta}) = \prod_{p=1}^{P} \psi_p^d(\theta_p).$$
(6)

Here,  $\beta_i$  is the coefficient of the *i*-th term of the model surrogate;  $\psi_p^d(\theta_p)$  is a univariate polynomial of order d of the parameter  $\theta_p$ ; and  $\Lambda^{P,D}$  is a multi-index containing the indices of all the multivariate polynomials ( $\psi_i(\boldsymbol{\theta})$ ) with degree equal or smaller than the surrogate degree, D, (i.e., multivariate polynomials where  $\sum_{p=1}^{P} d \leq D$ ).

Note that in the context of gPCE the univariate polynomials must satisfy the orthonormality condition, i.e.,  $E[\psi_p^j \psi_p^k] = \delta_{jk}$ , where  $\delta_{jk}$  is the Kronecker-delta function,  $\delta_{jk} = 1$  if j = k and zero otherwise. Multiple families of polynomials satisfy this condition; however, the selection of the suitable family of polynomials is made based on the pdf of the model parameters, which in this study are considered uniform. Thus, the Legendre polynomial family is employed to construct the surrogates.

The construction of a gPCE surrogate requires the evaluation of the surrogate 355 model coefficients,  $\beta = \{\beta_i, \forall i \in \Lambda^{P, D}\}$ , and the selection of the surrogate model 356 degree, D (Sudret, 2008). Regarding the evaluation of  $\beta$ , we rely on least-square 357 minimization (also termed as regression approach). According to this technique, 358 the surrogate coefficients  $\beta$  are those that minimize the mean square error between 359 TC values computed with the full numerical model,  $y(\theta)$ , and the corresponding 360 outputs of the surrogate model. Thus, several full numerical simulations need to 361 be performed in order to estimate the coefficients  $\beta$ . Generally, as the number of 362 full numerical simulations employed for the construction of the surrogate increases. 363 also the accuracy of the surrogate increases. In this study, the maximum admissible 364 computational burden allows us to perform 1233 full model evaluations encompassing 365 an equal number of randomly selected sets of parameters, such sets of parameters are 366 randomly sampled employing a Quasi-Monte Carlo approach which guarantees that 367 the parameter space is sampled uniformly. The evaluation of  $\beta$  is then performed by 368 minimizing 369

$$\sum_{s=1}^{1233} \left[ g(\boldsymbol{\theta}_s) - \sum_{i \in \Lambda^{P,D}} \beta_i \psi_i(\boldsymbol{\theta}_s) \right]^2,$$
(7)

where  $\theta_s$  is the s-th randomly selected set of the uncertain model parameters.

In our analyses, the selection of D is performed on the basis of an accuracy test of surrogates with degrees varying between 4 and 13. In such a test, the TC of 50 randomly selected sets of parameters (different from the sets of parameters employed for the estimation of  $\beta$ ) is evaluated with the numerical model and the surrogate. Then, the mean absolute error between these two quantities is evaluated, and the surrogate associated with the smallest error is selected and employed for the GSA.

### 377 3. Results and Discussion

This Section provides the resulting dispersion curves of each soil Scenario analyzed for a single resonator and the transmission coefficients of the entire metabarrier. The accuracy of the surrogate models generated for the GSA is then discussed. Finally, the GSA results are presented, and some conclusions about the impact of uncertain input parameters on the output results are drawn.

#### 383 3.1. Dispersion analysis results

Analytical dispersion curves for each Scenario from Eq. (1) are depicted in Fig. 4a 384 (solid curves). The dispersion curve highlights the hybridization of the fundamental 385 surface mode around the local resonance of the resonators in two avoided-crossing 386 branches observed in previous studies (Boechler et al., 2013; Palermo et al., 2016; 387 Colquitt et al., 2017). The split of the fundamental mode results in the generation 388 of a low-frequency band gap typical of the local resonance mechanism, where the 389 propagation of seismic surface waves is impeded within this frequency range. Having 390 an identical mass and stiffness of the resonators, a comparison between different soil 391 Scenarios reveals that the dynamic coupling between surface waves and metabarrier 392 is stronger for the silty clay soil (S3). This is due to the lower relative density between 393 resonator and soil, noting that Rayleigh and shear wave velocities are slower for silty 394 clay soil in comparison with other Scenarios. Under this rationale, soil type 3 presents 395 a flattened in-phase branch (lower branch in Fig. 4a) and propagates with higher 396 velocity in the frequency ranges above the band gap, as evidenced by the larger slope 397 of its out-of-phase branch (upper branch in Fig. 4a). The band gap width falls in the 398 interval  $f_{BG} = [f_r, f_r(\alpha + \sqrt{\alpha^2 + 1})]$ , where  $\alpha = (\pi m_r f_r)/(a_r l_r)\sqrt{(1 - C^2)/(\rho_s G_s)}$ 399 is a dimensionless number that relates resonator mass to the soil mass excited by 400 Rayleigh waves at the resonance (Palermo et al., 2016). Consequently, the band gap 401 width is  $\Delta f_{BG} = \alpha - 1 + \sqrt{\alpha^2 + 1}$  which takes the values 0.80, 0.70, and 0.97 Hz for 402 S1, S2, and S3, respectively. The largest band gap is associated with the silty clay 403 soil, having the lowest shear modulus and Rayleigh velocity among all the cases. 404

We perform a frequency domain analysis of the FE unit-cell model (see Fig. 3a) in the frequency range of 0 to 10 Hz corresponding to Rayleigh wavelengths between

20 to 240 m in Comsol Multiphysics (COMSOL Multiphysics(R), 2022) under plane-407 strain conditions. The simulations are performed for 1233 realization of collocation 408 points as specified in Sec. 3.3, each containing a set of uncertain parameters. The 409 simulation outcomes are averaged for each Scenario and depicted in Fig. 4a. The 410 eigenfrequency solutions of the FE analysis are marked with dots and super-imposed 411 on the analytical dispersion curves. There is a good agreement between the analyti-412 cal and numerical solutions. Otherwise, it can be noted that the numerical resonant 413 frequencies are shifted toward the lower values. This frequency shift stems from 414 uncertainties associated with the resonator mass or, equivalently, with the resonant 415 frequency, together with a soft soil mechanism that emerged from the inertia dif-416 ference between the resonator and soil. For heavy resonating masses, the soil acts 417 as a soft spring with the longitudinal stiffness of  $K_s$  working in serial configuration 418 with resonators' springs  $K_r$ . The equivalent stiffness of the coupled system would 419 be  $K_{eq} = K_r K_s / (K_r + K_s) < K_r$ . Thus, the numerical resonant frequency will be 420  $f_{r,FE} = 2\pi K_{eq}^{1/2} m_r^{-1/2}$ . Since  $K_{S3} < K_{S2} < K_{S1}$ , the frequency shift is less pro-421 nounced for the soft soil S1. The opposite can be observed for S3. The resulting 422 numerical resonant frequencies are  $f_{r,FE} = [4.5, 4.4, 4.3]$  Hz for S1, S2, and S3, while 423  $f_{r,AN} = [4.91, 4.78, 4.84]$  Hz correspond to their analytically evaluated counterparts. 424

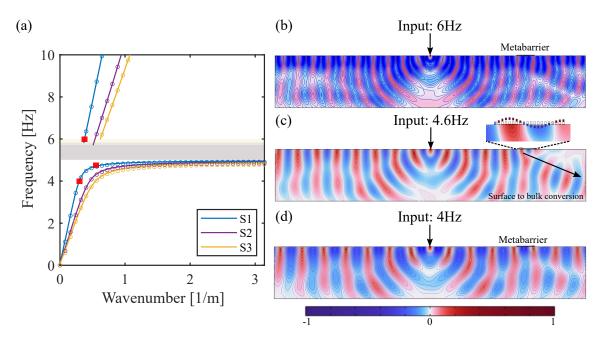


Figure 4: (a) Averaged dispersion curves obtained from the unit-cells of seismic metabarrier for all three Scenarios S1-S3. Analytical surface modes obtained from Eq. (1) are shown with solid lines and FE eigensolutions super-imposed with circles. Highlighted boxes show the band gap region associated with each scenario. The full wavefields are corresponding to (b) out-of-phase surface mode (upper branch the dispersion curve), (c) resonant frequency, and (d) in-phase surface mode (lower branch) of S1. Excitation frequencies are marked with red squares on the dispersion curve.

The full wavefield of the plane-strain FE model (see Fig. 3c) is shown for the 425 out-of-phase and in-phase surface modes of S1 in Fig. 4b and d, respectively. The 426 introduction of the metabarrier (right side of the individual figures) modifies the 427 surface wave propagation compared to the reference soil condition (left side of the 428 figures). The excitation frequencies are denoted with red squares in the dispersion 429 curve of Fig. 4a. For a vertical harmonic excitation with a carrier frequency close to 430 the operational frequency of the metabarrier, the surface-to-shear wave conversion 431 due to the local resonance of the resonators is observed in Fig. 4c. This phenomenon 432 originates from the dynamic interaction between the harmonic motion of seismic 433 surface waves (Rayleigh-like waves) and vertical displacement of resonators inside 434 the barrier (see inset of Fig. 4c). The outcomes of the dispersion relation anticipate 435 a considerable surface wave amplitude reduction around the band gap region. Similar 436 results are obtained for S2 and S3 with minor differences in their numerical resonant 437 frequencies. 438

#### 439 3.2. The surface wave attenuation coefficient

We perform a harmonic analysis of the full FE model results of Fig. 3c in the 440 frequency interval of 2 Hz to 7 Hz using a frequency resolution of 0.1 Hz. The 441 triangular mesh elements with identical sizes of the unit-cell model are incorporated 442 in all Scenarios to discretize the models. We obtained TC and AC (Eq. (3)) from the 443 vertical nodal displacements of the barrier output averaged over its length  $(L_{out} = \lambda_0)$ 444 divided by the same quantity measured from the soil output, as described in Sec. 445 2.3. Similar to the unit-cell case, we execute the frequency domain simulations for 446 1233 realization of collocation points and average the outputs of TC and AC for 447 each Scenario. Fig. 5 summarizes the results of the harmonic analysis of the seismic 448 metabarrier. 449

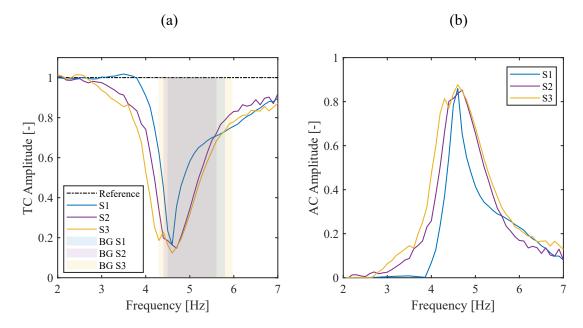


Figure 5: (a) Mean transmission and (b) mean attenuation coefficient of the proposed seismic metabarrier obtained from Eq. (3) in the low-frequency range for all realizations of each Scenario. Shaded areas in Figure 5a represent the band gap (BG) for each Scenario.

The responses of the soils equipped with the resonators are shown with solid lines, while the bare soil response (reference case) is marked with a solid-dashed line. The associated FE band gap regions of each Scenario are highlighted with rectangular boxes. The lower edges of BG zones coincide with the first peak attenuation of each soil model. In all Scenarios, the surface wave attenuation starts around 3 Hz. It becomes more indicative within the BG zone, while the peak attenuation (4.6, 4.7,

and 4.6 Hz for S1, S2, and S3) appears in the proximity of the collective resonant 456 frequencies of the oscillators. In the frequency ranges above the resonance, the 457 transmission/attenuation coefficients present an almost linear increasing/decreasing 458 trend. In the high-frequency regime, the surface wave attenuation in the presence 459 of the metabarrier approaches the reference soil case. The silty-clay soil (S3) is 460 characterized by the broadest attenuation frequency range with the most significant 461 peak analogous to the predictions of the dispersion curve previously discussed in Sec. 462 3.1. Instead, the soft sedimentary soil (S1) has the narrowest attenuation zone as a 463 result of higher relative density difference and weaker dynamic coupling between the 464 metabarrier and the soil. 465

466 3.3. Surrogate models

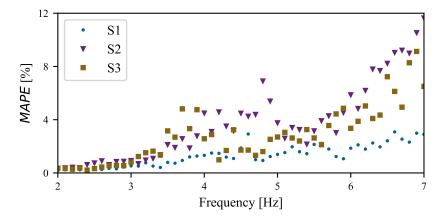


Figure 6: Accuracy of the best surrogate models for diverse frequency values and Scenarios considered in this study.

Fig. 6 presents the accuracy values of the surrogate models constructed for the Scenarios considered in this study. Accuracy is assessed by comparing the results of the surrogate predictions of TC with the results of full numerical simulations; the latter is different from the simulations employed for the surrogate construction. Accuracy is measured with MAPE metric, which is defined as

$$MAPE = \sum_{s=1}^{50} \left[ \frac{TC_{surr} - TC_{full}}{TC_{full}} \right].$$
 (8)

<sup>472</sup> Note that we construct one surrogate per Scenario and per frequency. Therefore, <sup>473</sup> Fig. 6 presents the accuracy of 153 surrogates. These results show that the accuracy of the models is generally good ( $MAPE \leq 5\%$ ), except for frequency values larger than 6 Hz. Regarding the different Scenarios, S1 is characterized by the lowest values of MAPE, whereas S2 is associated with the largest values.

We construct polynomials of order 12 for the 3 Scenarios. Surrogates of lower polynomial order are associated with reduced accuracy while relying on a higher order was not possible due to the ill-conditioning of the minimization problem required for the evaluation of the surrogate coefficients (details not shown).

#### 481 3.4. Global sensitivity analysis

The surrogate models obtained in Section 3.3 are evaluated  $10^6$  times with ran-482 dom combinations of the model parameters. While performing such a task would 483 have required a computational effort of more than two years by employing the full 484 numerical model, relying on the surrogate model considered involves an overall com-485 putational time of about 60 seconds on a laptop with an Intel Core i7-8550 @ 1.8GHz 486 with 8GB of Memory. Note that the number of model evaluations is defined to ensure 487 the stability of the sensitivity metrics considered (details not shown). The results of 488 these model evaluations are then employed for the global sensitivity analysis (GSA). 489

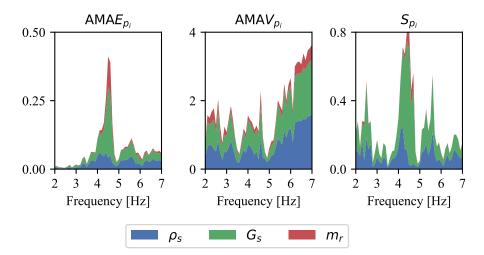


Figure 7: Stacked diagram of the first two moment-based AMA indices (AMA $E_{p_i}$  and AMA $V_{p_i}$ ), and Sobol principal indices  $(S_{p_i})$  of the model uncertain parameters considered in this study for Scenario 1.

Fig. 7 depicts the evolution of the first two moment-based AMA indices and the variance-based Sobol indices of the uncertain model parameters of Scenario 1. The results are presented for frequency values in the interval between 2 and 7 Hz, for

which a unique GSA was performed every 0.1 Hz. GSA metrics of  $\rho_s$ ,  $G_s$ , and  $m_r$ 493 are depicted in blue, green, and red, respectively. Values of AMAE index indicate 494 that for frequencies below 4 Hz and over 5 Hz, the mean of TC is practically inde-495 pendent of the model parameter values. Conversely, in the interval between 4 Hz and 496 5 Hz (i.e., the frequency range near the local resonance of the resonators in which 497 the TC/AC assumes minimum/maximum values), knowledge of (or conditioning on) 498 model parameters may significantly modify the mean of TC. In this interval, all un-499 certain model parameters play an important role in determining the mean of TC, the 500 parameters playing the most and least essential roles being  $G_s$  and  $\rho_s$ , respectively. 501 This suggests that for  $4 \text{ Hz} \le f < 5 \text{ Hz}$ , the shear modulus of the soil, which controls 502 the bulk waves velocities and the resonator mass, plays an indispensable role in the 503 definition of the TC mean. For frequency values close to the resonance and due to 504 the effective coupling between resonators and soil, the influence of resonator mass 505 becomes more prominent. Within the band gap frequency range (5 Hz  $\leq f \leq 5.8$  Hz), 506 the impact of all uncertain model parameters is less pronounced, and resonator mass 507 has the minimum contribution. 508

Values of the AMAV index suggest that the variance of the model output can be significantly modified by the knowledge of (or conditioning on) a model parameter, such variability being large for high-frequency values. In general, TC variance is governed by  $G_s$  and  $\rho_s$ . The results of Sobol indices are consistent with those of AMAE and AMAV indices. Sobol indices suggest that the variance of TC can be reduced significantly by the knowledge of (or conditioning on)  $G_s$  and  $\rho_s$ . The resonator mass  $(m_r)$  may play a non-negligible role also for 4 Hz  $\leq f < 5$  Hz.

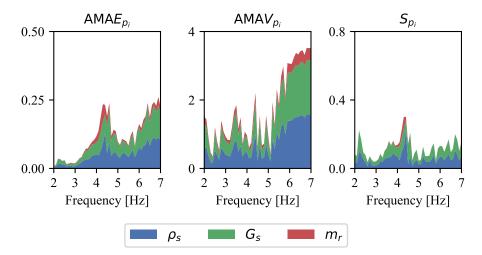


Figure 8: Stacked diagram of the first two moment-based AMA indices (AMA $E_{p_i}$  and AMA $V_{p_i}$ ), and Sobol principal indices  $(S_{p_i})$  of the model uncertain parameters considered in this study for Scenario 2.

Fig. 8 presents the evolution of the first two moment-based AMA indices and the 516 variance-based Sobol indices of the uncertain model parameters of Scenario 2. GSA 517 metrics of  $\rho_s$ ,  $G_s$ , and  $m_r$  are depicted in blue, green, and red, respectively. Values of 518 AMAE index document that for frequencies below 3 Hz the mean of TC is practically 519 independent of the uncertain model parameter values. Differently from Scenario 1, 520 the knowledge of (or conditioning on) model parameters significantly influences the 521 value of the TC mean for almost all the considered frequencies. The most and least 522 influential parameters are  $\rho_s$  and  $m_r$ , respectively. Note that the relative importance 523 of  $\rho_s$  is close to the relative importance of  $G_s$ .  $m_r$  has a marginal contribution only 524 in the frequency range between 3.5 Hz and 4.5 Hz, where resonators start moving 525 in phase with the soil domain and ultimately reach the resonance condition. The 526 resonator mass does not have a remarkable impact on the determination of the TC527 mean outside this frequency interval, and soil parameters govern the overall dynamic 528 behavior of the system. With reference to the AMAV index, the results are similar 529 to those of Scenario 1. This suggests that the variance of the model output can be 530 significantly modified by the knowledge of (or conditioning on) a model parameter, 531 such variability being large for high-frequency values. In general, TC variance is 532 governed by  $G_s$  and  $\rho_s$ . The results of Sobol indices confirm the outcomes of AMAE 533 and AMAV indices. Sobol indices indicate that the variance of TC can be reduced 534 significantly by the knowledge of (or conditioning on)  $G_s$  and  $\rho_s$ . As expected, the 535 resonator mass  $m_r$  comes into play in the frequency range of 4 Hz  $\leq f < 5$  Hz. 536

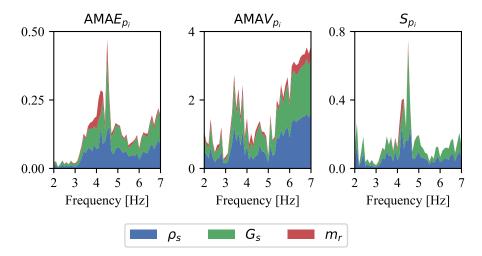


Figure 9: Stacked diagram of the first two moment-based AMA indices (AMA $E_{p_i}$  and AMA $V_{p_i}$ ), and Sobol principal indices  $(S_{p_i})$  of the model uncertain parameters considered in this study for Scenario 3.

Fig. 9 presents the same indices as previous Scenarios. GSA metrics of  $\rho_s$ ,  $G_s$ , and 537  $m_r$  are depicted in blue, green, and red, respectively. Similar to the previous cases, 538 the AMAE index values do not depend on the uncertain model parameters in the 539 low-frequency range below 3 Hz. Unlike Scenario 1, the knowledge of (or conditioning 540 on) model parameters considerably influences the values of the TC mean for almost 541 all the considered frequencies. The most and least influential parameters are  $\rho_s$  and 542  $m_r$ , respectively.  $m_r$  plays a substantial role in the determination of TC mean for 543 3.5 Hz  $\leq f \leq 4.5$  Hz, close to the frequency range where the maximum ground-544 motion attenuation is predicted (see Fig. 5a). Regarding AMAV index, the results 545 are similar to Scenario 1, indicating that the variance of the model output can be 546 significantly modified by the knowledge of (or conditioning on) a model parameter, 547 such variability being large for high-frequency values. In general, TC variance is 548 governed by  $G_s$  and  $\rho_s$ . According to the outcomes of Sobol indices, the variance of 549 TC can be reduced remarkably by the knowledge of (or conditioning on) uncertain 550 soil parameters. The influence of the resonator mass is negligible for the frequency 551 ranges far from resonance. The results of Sobol indices are consistent with those of 552 AMAE and AMAV indices. 553

The values of the AMAE metric associated with different Scenarios indicate that the mechanical parameters of the soil are more influential than the resonator mass in producing a wider attenuation frequency range for stiff soils such as the weathered granite soil considered in Scenario 3. Such a phenomenon arises from a more

extensive transfer of stress from heavy resonators to the stiff soil and is consistent 558 with the outcomes of the full numerical model (see Fig. 5). Conversely, results of the 559 sensitivity analysis performed for a softer soil like the one considered in Scenario 1 560 suggest that the resonator mass becomes more dominant only in a narrow frequency 561 range between 4.3 Hz  $\leq f \leq 4.7$  Hz. These results are also consistent with those of 562 the WFEM numerical simulations. Soils of moderate stiffness like the one consid-563 ered in Scenario 2 present an intermediate case, similar to the results of dispersion 564 analysis and attenuation/transmission coefficients. 565

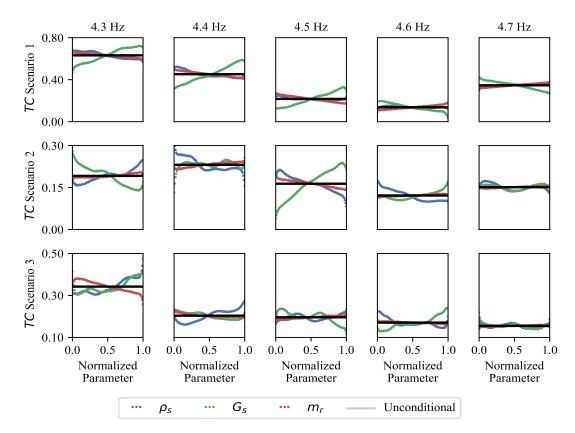


Figure 10: TC conditional on values of the uncertain model parameters considered in this study ( $\rho_s$  in blue,  $G_s$  in green, and  $m_r$  in red). The corresponding unconditional mean is also depicted (black bold horizontal lines). Intervals of variation of the uncertain model parameters are scaled within the unit interval for graphical representation purposes. Results are presented for Scenario 1 (first row), Scenario 2 (second row) and Scenario 3 (third row).

We extend our investigations by analyzing the effect of each uncertain parameter on TC at specific frequency values. Since most of the elastic energy of seismic surface

waves is trapped in the frequency range of 4 Hz  $\leq f \leq 6$  Hz (see Fig. 5a), we calculate 568 TC values conditioned to values of uncertain model parameters for diverse values of 569 f = [4.3, 4.4, 4.5, 4.6, and 4.7] Hz where resonant frequencies and frequencies of peak 570 surface wave attenuation can be found for all Scenarios. Fig. 10 presents TC values 571 conditioned to values of  $\rho_s$  (in blue),  $G_s$  (in green), and  $m_r$  (in red). The range of 572 variability of the uncertain parameters is scaled to the unit interval for graphical 573 representation purposes. The unconditional value of TC is also depicted (in black) 574 as a reference. 575

Fig. 10 indicates that across all 3 Scenarios, at the frequency of maximum at-576 tenuation (4.6 Hz, 4.7 Hz, and 4.6 Hz for Scenarios 1, 2, and 3, respectively) the 577 influence of uncertain model parameters on TC is less marked than what can be 578 documented at resonance frequencies (4.5, 4.4, and 4.3 Hz for Scenarios 1, 2, and 3 579 respectively). At the frequency of maximum attenuation, the influence of  $m_r$  on the 580 mean of TC is minute compared to the influence that  $\rho_s$  and  $G_s$  have on the mean of 581 TC. Instead, the resonator mass becomes more influential in the resonant frequency 582 of all Scenarios. In Scenario 1 the resonator mass has a directly proportional effect 583 on the TC mean (i.e., the larger the values of  $m_r$ , the larger the values of TC). 584 Whereas in Scenarios 2 and 3, the influence of  $m_r$  on the values of TC is virtually 585 negligible. 586

#### 587 4. Conclusions

A seismic metabarrier is a passive barrier composed of locally resonant elements 588 devised to control the propagation of seismic surface waves in the long-wavelength 589 regime. Metabarriers have found application in safeguarding unprotected structures 590 and infrastructures by reducing the ground motion generated from seismic surface 591 waves during an earthquake. The engineering implementation of metabarriers de-592 mands detailed knowledge of the uncertain parameters affecting their seismic atten-593 uation capability during their design phase. Within the context of seismic isolation, 594 the current study proposes a rigorous methodology to quantify the impact of the 595 uncertainty associated with system parameters on the seismic attenuation efficiency 596 of a metabarrier. 597

In this study, we analyze the effect that the uncertainty associated with three parameters driving the physical behavior of a metabarrier (i.e., the mass of resonators  $m_r$ , soil density  $\rho_s$ , and soil shear modulus  $G_s$ ) has on its attenuation efficiency. A numerical model is developed to obtain the dispersion relation of the proposed metabarrier; its results coincide with those derived via analytical dispersion curves. A low-frequency band gap typical of the local resonance mechanism appears in the

dispersion curve, where a significant seismic surface wave attenuation is anticipated. 604 The narrowest and widest band gap regions are associated with granite (S2) and 605 silty-clay (S3) soils, respectively. In the latter case, stronger dynamic coupling oc-606 curs between the resonators and soil due to their higher relative inertia. A companion 607 full numerical model is developed, and frequency domain analysis is performed to 608 measure the transmission/attenuation coefficients of the metabarrier. The stiffest 609 soil, silty-clay soil of S3, presents the largest peak attenuation with the widest atten-610 uation frequency range. On the contrary, the sedimentary soil (S1) has the narrowest 611 global attenuation with the smallest peak attenuation due to its weak dynamic in-612 teraction with heavy resonating masses of resonators; this stems from the soft soil 613 mechanism. 614

The uncertainty of the transmission coefficient TC (i.e., a measure of the attenu-615 ation efficiency of a metabarrier) is governed by the uncertain parameters associated 616 with the mechanical properties of the soil ( $\rho_s$  and  $G_s$ ). The influence that such 617 parameters have on TC varies with the frequency at which Rayleigh waves propa-618 gate. In general, for Rayleigh waves oscillating at frequencies close to the resonant 619 frequency of the metabarrier,  $G_s$  is the parameter with the largest influence on TC, 620 followed by  $\rho_s$  and by  $m_r$ , a parameter whose influence is not negligible only for 621 frequencies close to the resonance. 622

The influence of the resonator mass  $(m_r)$  on the attenuation efficiency of the 623 metabarrier depends on the type of soil analyzed. For soft soils (e.g., the soils of 624 Scenario 1 and Scenario 2), an increase in the mass of the resonator enhances the 625 attenuation efficiency of the metabarrier (i.e., decreases TC values) by increasing 626 the relative density of resonators with respect to the soil; whereas for the stiffest soil 627 analyzed in Scenario 3 variations of  $m_r$  do not significantly modify the values of TC. 628 Overall, our approach provides new insights into the design and analysis of locally 629 resonant devices to extend current knowledge of metabarriers in different application 630 areas by including the uncertainties associated with the design parameters. The 631 presented methodology does not include some complexities which might arise during 632 the practical implementation of metabarriers. These include, e.g., soil stratigraphy, 633 the presence of groundwater, and soil bearing capacity failure under heavy resonating 634 masses. Otherwise, our approach, in spite of its simplified assumptions, can still be 635 used as a benchmark for advanced numerical models typically adopted in the context 636 of actual geophysical scenarios. The results of this study can impact several segments 637 of engineering, including earthquake engineering, geotechnical engineering, road and 638 railway traffic, and acoustics. Future extensions of the proposed methodology can 639 be tailored to include dampening effects of soil and resonators, the presence of a 640 water table and (possibly) its dynamics, non-linear effects of the soil, and scenarios 641

encompassing sedimentary soils characterized by large Rayleigh velocities to assess
 the shielding efficiency of seismic metabarriers.

#### 644 CRediT authorship contribution statement

Farhad Zeighami: Conceptualization, Methodology, Software, Data curation,
 Writing - original draft, Writing - review and editing. Leonardo Sandoval: Method ology, Software, Data curation, Writing - original draft, Writing - review and editing.
 Alberto Guadagnini: Conceptualization, Methodology, Writing - review and edit ing, Supervision. Vittorio Di Federico: Conceptualization, Methodology, Writing
 - review and editing, Supervision, Funding acquisition.

## 651 Conflict of interest

The authors declare that they have no conflict of interest. There are no data sharing issues since all numerical information is provided in the figures produced by solving the equations in the paper.

#### 655 Acknowledgments

V. Di Federico acknowledges support from the University of Bologna through the Ricerca Fondamentale Orientata (RFO) Grant 2021.

#### <sup>658</sup> Appendix A. Dimensionless analysis of the dispersion relation

This Section provides the dimensionless form of the dispersion law of Eq. (1). We exploit the resonator parameters  $(m_r, K_r, \text{ and } a_r)$  as scales. Hence, we introduce a set of dimensionless parameters as follows:

$$\omega' = \frac{\omega}{K_r^{1/2} m_r^{-1/2}} = \frac{\omega}{\omega_r}, \quad k' = \frac{k}{k_{max}} = \frac{k}{\frac{\pi}{a_r}}, \quad G' = \frac{G_s}{\frac{K_r}{a_r}}, \quad l' = \frac{l_r}{a_r}, \quad \rho' = \frac{\rho_s}{\frac{m_r}{a_r^3}} \approx \frac{\rho_s}{\rho_r}, \quad (A.1)$$

where,  $\omega'$  is the angular frequency normalized by the angular resonant frequency of the resonator, k' the wavenumber normalized by the maximum wavenumber at the edge of Brillouin zone, G' the shear modulus normalized by the approximate longitudinal modulus of the resonator, l' the dimensionless shape parameter of the resonator, and  $\rho'$  the ratio between the mass density of soil and resonator. The  $_{667}$  dimensionless dispersion law is derived by substituting the dimensionless parameters  $_{668}$  of Eq. (A.1) into Eq. (1) to obtain

$$\left(\omega'^{2} - 1\right) \left[ \left(2 - \frac{\rho'}{G'} \left(\frac{\omega'}{\pi k'}\right)^{2}\right)^{2} - 4\sqrt{1 - \frac{\rho'}{G'} \left(\frac{C\omega'}{\pi k'}\right)^{2}} \sqrt{1 - \frac{\rho'}{G'} \left(\frac{\omega'}{\pi k'}\right)^{2}} \right]$$

$$= \frac{\rho'\omega'}{l'G'^{2}} \left(\frac{\omega'}{\pi k'}\right)^{3} \sqrt{1 - \frac{\rho'}{G'} \left(\frac{C\omega'}{\pi k'}\right)^{2}}.$$
(A.2)

In the original dispersion equation of Eq. (1) and taking into account Eq. 669 (2), the angular frequency is an implicit function of eight parameters, i.e.  $\omega =$ 670  $fun(k, K_r, m_r, a_r, l_r, \rho_s, G_s, \nu_s)$ , while in the dimensionless equation, the dimension-671 less angular frequency is an implicit function of five parameters, including i.e.  $\omega' =$ 672  $fun(k', l', \rho', G', \nu')$ . This is in agreement with the Buckingham  $\pi$  theorem, stating 673 that the original dispersion law with n = 8 dimensional physical variables can be 674 written in a dimensionless format using p = n - m = 5 pure numbers, where m = 3675 is the number of dimensionally independent scales, chosen to coincide with the vari-676 ables describing the resonator. As an alternative to the procedure adopted in the 677 main body of the paper, GSA could be performed on Eq. (A.2), where the number 678 of model parameters is reduced. 679

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