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Injective Domain Knowledge in Neural Networks for Transprecision Computing

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Abstract. Machine Learning (ML) models are very effective in many learning tasks, due to the capability to extract meaningful information from large data sets. Nevertheless, there are learning problems that cannot be easily solved relying on pure data, e.g. scarce data or very complex functions to be approximated. Fortunately, in many contexts domain knowledge is explicitly available and can be used to train better ML models.

This paper studies the improvements that can be obtained by integrating prior knowledge when dealing with a context-specific, non-trivial learning task, namely precision tuning of transprecision computing applications. The domain information is injected in the ML models in different ways: I) additional features, II) ad-hoc graph-based network topology, III) regularization schemes. The results clearly show that ML models exploiting problem-specific information outperform the data-driven ones, with an average improvement around 38%.

Keywords: Machine Learning · Domain Knowledge · Transprecision Computing

1 Introduction

In recent years, ML approaches have been exhaustively proved to be successful with a wide range of learning tasks. Typically, ML models are sub-symbolic, black-box techniques capable of effectively exploiting the information contained in large amounts of data. Part of their usefulness is their adaptability, that is the fact that ML models with the same architecture and training algorithm can be applied in very different contexts with good results. This happens because most ML approaches make very few assumptions on the underlying data and the functions that they are trying to learn.

However, data-driven models can be not ideal if, for instance, the data is relatively expensive to obtain and the function to be learned is very hard. At the same time, in many areas domain-specific information is available (e.g. structured data, knowledge about the data generation process, domain experts experience, etc) but not exploited. In such cases, it makes sense to take advantage of this information to improve the performance of the ML techniques, so they do not have to start from scratch while dealing with difficult learning tasks. In other words, *why learn again something that you already know*?

In this paper we discuss a strategy to inject domain knowledge expressed as constraints in an ML model, namely a Neural Network (NN). We limit the experimental

evaluation to a specific area, namely *transprecision computing*, a novel paradigm that allows trade-offs between the energy required to perform the computation and the accuracy of its outcome[8]. We consider different sources of prior information and adopt suitable injection approaches for each of them: I) feature extraction, II) ad-hoc NN structure, and III) data augmentation combined with a regularization strategy. The supervised learning task is very hard, due to non-linearity, non-monotonicity and relatively small data sets (a few thousands of samples). The experimental results clearly show that exploiting prior information leads to remarkable gains. On average over all benchmarks, the knowledge injection provides a 38% improvement in terms of prediction error (error decrease). The rest of the paper is structured as follows: after the discussion about related works (Section 2), Section 3 introduces the injection approaches; Sec. 4 details transprecision computing and the specific learning task, highlighting its difficulty and the domain knowledge that can be extracted; Sec. 5 summarizes the experimental results; finally, Sec. 6 concludes the paper.

2 Related Works

The combination of sub-symbolic models with domain knowledge is an area explored by previous research in many fields[12]. For instance, feature engineering[6] is a common method for improving the accuracy of data-driven ML models by selecting useful features and/or transform the original ones to facilitate the learner's task. In general, this is not a trivial problem and requires much effort, both from system expert and ML practitioners. In this paper, we use a different approach, as we employ domain knowledge to create novel features that render *explicit* the information hidden in the raw data.

Another research direction aims at training NNs while forcing constraints which can be drawn from knowledge domain. [9] presents a method for translating logical constraints in loss functions that guide the training towards the desired output. [11] proposes a different approach to incorporate domain knowledge in an NN by adopting a loss function that merges mean squared error and a penalty measuring whether the NN output respect a set of constraints derived from the domain; the method is limited to constraints enforcing monotonicity and bounds on the target variable. [14] introduces a method to integrate semantic knowledge in deep NNs, again exploiting a loss function; in this case the approach is targeted at semi-supervised learning and not well suited for supervised tasks. Acting on the loss function with a regularization term has been proposed also by [3], with their work on Semantic-Based Regularization (SBR), a method to merge high-level domain information expressed as first-order logic in ML models. We have exploited their technique in combination to a data augmentation strategy to enhance an ML model.

Graph Convolutional Neural Networks (GCNN) [7,2] are a type of neural networks specialized for learning tasks involving graphs. GCNNs have been recently used in several fields[15], owning to their capability to deal with data whose structure can be described via graphs, thanks to a generalization in the spectral domain of the convolutional layers found in many deep learning networks. GCNNs most common applications involve semi-supervised classification tasks, with the goal of predicting the class of unlabeled nodes in a graph – a case of graph learning.

3 Domain Knowledge Injection

The main goal of this paper is the exploration of how an ML model can be improved through the exploitation of domain knowledge. We claim that data-driven ML models can benefit from the injection of prior knowledge provided by domain experts; Sec. 5 will report the results of the experimental evaluation, conducted on a specific learning task where domain knowledge is available (details in Sec. 4). We consider domain knowledge that can be expressed in the form of logical constraints between variables (input and output features of the ML models) and/or encoded in a graph. Let X be the training set and y the targets, either continuous values (regression) or categorical labels (classification), f the model trained to learn the relation between X and y. A DL model is a family of parametric functions $f(x|\omega)$, i.e. $\{f(x|\omega)|\omega \in \Omega\}$ where the set Ω is called *hypothesis space*. Training exploits data to find the parameter values in Ω that minimize a so called *loss function*. In the most general case this is a function $\mathcal{L}(y|\theta)$, where y corresponds to the output of DNN and θ is the available empirical knowledge (e.g. the labels).

In general, domain knowledge can be expressed as a set of logical constraints between the input features X and the target y. For instance, the monotonicity property holds if $x_1 \leq x_2 \implies y_1 \leq y_2$ for every pair in X. We propose a multi-faceted domain knowledge injection strategy and we introduce three different approaches, each one addressing a specific weakness encountered by data-driven techniques (Fig. 1a portrays the three injection mechanisms):

- feature space manipulation for information implicit but hidden in the raw data if the examples available in the data set are not sufficient nor informative enough to train accurate ML models, a set of additional features can be created using the domain knowledge and reasoning about the relationships among the original features;
- ad-hoc network topology for learning tasks where the relationships among the features and the data structure can be encoded with graphs (hypothesis space exploration);
- 3. *data augmentation* and *regularization function* for a twofold scope: I) learning with very few data (e.g. active learning), by generating artificial examples, II) enforcing desired properties in the output of the ML model by adding a regularization term to the loss function \mathcal{L} .

The feature extraction (1) takes into account prior knowledge that can be expressed via a set of binary constraints C among the input features X; these constraints can be used to obtain an extended training set X' by checking if every example in X satisfies them or not. The regularization method (3) assumes that the knowledge can be expressed as first-order logic constraints between input features X and the target y; data augmentation helps to cope with scarce data and amplify the effect of the regularization.

We introduce the knowledge injection strategy and present three different techniques, each tailored for a specific source of information. At the current stage we were more interested in measuring the specific contribution of each method, thus they were tested separately, but we plan to explore hybrid solutions in future works. As a case study we consider a complex supervised learning task and then we tackle it with multiple data-driven ML models, and in particular we use neural networks (NN). Subse-

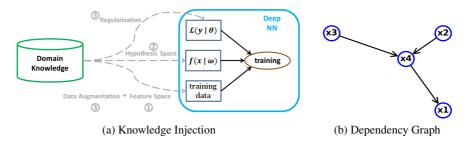


Fig. 1: (a) Domain Knowledge Injection in DNNs - (b) Example of Dependency Graph

quently, we inject the domain knowledge and then we experimentally evaluate the obtained improvements.

4 Transprecision Computing

There exist many techniques for transprecision computing and in this paper we focus on an approach targeting floating-point (FP) variables and operations, as their execution and data transfer can require a large share of the energy consumption for many applications; decreasing the number of bits used to represent FP variables can lead to energy savings, with the side-effect of reduced accuracy on the outcome of the application (also referred to as *benchmark*). Deciding the optimal number of bits for FP variables while respecting a bound on the computation accuracy is referred to as precision tuning. In this context, understanding the relationship between assigned precision and accuracy is a critical issue, and not an easy one, as this relationship cannot be analytically expressed for non-trivial benchmarks[10]. Therefore, we address this problem via a ML model, that is *learning* the relationship between precision and accuracy. For this scope, we use a transprecision library for precision tuning called *FlexFloat*[1] to create a suitable data set; this means running a benchmark with multiple precision configurations and store the associated error. As this is a highly time-consuming task, we work with data sets of relatively limited size (5000 samples at maximum)¹, an issue that complicates the learning task.

4.1 Problem Description

We consider numerical benchmarks where multiple FP variables partake in the computation of the result for a given input set, which includes a structured set of FP values (typically a vector or a matrix). The number of variables with controllable precision in a benchmark B is n_{var}^B ; these variables are the union of the original variables of the

¹ The learning task is only a part of a larger project aiming at solving the precision tuning problem with optimization techniques; state-of-the-art algorithms for FP precision tuning (e.g. [5]) dictate a bound on the time to solve the optimization problem – hence, the need of a low data set creation time

program and the additional variables inserted by FlexFloat to handle intermediate results (see [13] for details). FlexFloat allows to run a benchmark with different precision (different numbers of bits assigned to the FP variables) and to measure the reduction in output quality due to the adjusted precision (reduction w.r.t. the output obtained with maximum precision) - we will refer to this reduction as error. If O indicates the result computed with the tuned precision and O^M the one obtained with maximum precision, the error E is given by $E = \max_i \frac{(o_i - o_i^M)^2}{(o_i^M)^2}$ – this is the metric adopted in the transprecision community[5]. As a case study we selected a representative subset of the benchmarks studied in the context of transprecision computing. At this stage, we do not focus on whole applications but rather on micro-benchmarks, in particular the following ones: 1) FWT, Fast Walsh Transform for real vectors, from the domain of advanced linear algebra $(n_{var}^{FWT} = 2)$; 2) saxpy, a generalized vector addition, basic linear algebra $(n_{var}^{saxpy} = 3)$; 3) convolution, convolution of a matrix, ML $(n_{var}^{conv} = 4)$; 4) dwt, Discrete wavelet transform, from signal processing $(n_{var}^{dwt} = 7)$; 5) correlation, compute correlation matrix of input, data mining $(n_{var}^{corr} = 7)$. 6) BlackScholes, estimates the price for a set of options applying Black-Scholes equation, from computational finance $(n_{var}^{BScholes} = 15).$

Beside the precision configuration, another element that impacts a benchmark's output, and thus the error, is the input set fed to the application (e.g., the actual values of the FP variables). The vast majority of transprecision tuning approaches consider the single input set case[5]: a fixed input set is given to the benchmark and the precision of the variables is tuned for that particular input set (no guarantee that the configuration found will suit different input sets). We opted for "stochastic" approach: we consider multiple input sets, so that a distribution of errors is associated to each configuration, rather than a single value. The learning task is then not to predict the error associated to a specific input sets. Learning the relationship between variable precision and *mean error* over all input sets. Learning the relationship between variable precision and error is a hard problem. First, the error metric is very susceptible to differences between output at maximum precision and output at reduced precision, due to the maximization component. Secondly, the precision-error space is non-smooth, non-linear, non-monotonic, and with many peaks (local optima). In practice, increasing the precision of all variables does not guarantee an error reduction.

4.2 Data Set Creation

As a first step, we created a collection of data sets containing examples of the benchmarks run at different precision, with the corresponding error values. We call *configuration* the assignment of a precision to each FP variable. The configuration space was explored via Latin Hypercube Sampling (LHS). As described in the previous section, for each configuration the benchmarks were run with 30 different input sets² and the error associated to each combination of <configuration, input set> was computed. As target we then use the average over the 30 input-specific errors. The majority of configurations lead to small errors, from 10^{-1} to 10^{-30} . However, in a minority of cases

² Long vectors and matrices containing different real values

lowering the precision of critical variables generates extremely large errors; in the transprecision computing context, error larger than 1 are deemed excessive.

After a preliminary analysis, we realized that for an ML model it is very hard to discern between small and relatively close errors (i.e. e^{-20} and e^{-15}); we therefore opted to predict the negative of the logarithm of the error, thus magnifying the relative differences. Moreover, a careful examination revealed that overly large error values were usually due to numerical issues arising during computation (e.g. overflow, underflow, division by zero, or not-a-number exceptions). This intuitively means that the large-error configurations are likely to follow a distinct pattern w.r.t. the configurations having a more reasonable error value. We are much more interested in relatively small error (e.g. $E \le 0.95$, not in logarithmic scale) as in transprecision computing the largest accepted error is typically 0.1 (meaning an output accuracy higher than 90%). Hence, we decide to level out all the errors in the data set above the 0.95 threshold; if the <configuration, input set> combination produced an error $E \ge 0.95$, after pre-processing its error is set to 0.95 (before the conversion to logarithmic scale).

4.3 Knowledge Injection

As the benchmarks are programs composed by a set of interdependent FP variables, the variables' interactions represent a source of valuable information for learning the relationship between precision and error. This domain-level knowledge is encoded in the *dependency graph* of the benchmark, which specifies how the program variables are related. For instance, consider the expression $V_1 = V_2 + V_3$; this corresponds to four precisions that need to be decided $x_i, i \in [1, 4]$. The first three precision-variables x_1 , x_2 , and x_3 represent the precision of the actual variables of the expression, respectively V_1, V_2 , and V_3 ; the last variable x_4 is a *temporary* variable introduced by FlexFloat to handle the (possibly) mismatching precision of the operands V_2 and V_3 (FlexFloat performs a cast from x_2 and x_3 to the intermediate precision x_4). Each variable is a node in the dependency graph, and the relations among variables are directed edges, as depicted in Fig. 1b; an edge entering a node means that the precision of the sourcevariable is linked to the precision of the destination-variable.

Additional Features Extraction As we have seen, the prior information on the benchmarks is encoded in directed graphs; for explanatory purposes, we will take as example the micro-benchmark represented by the graph in Fig. 1b. Using the encoded knowledge, a set of additional features characterizing the precision configurations can be obtained. We consider only one type of relation, that is assignments (e.g. $x_4 \rightarrow x_1$). In this kind of expression, granting a larger number of bits to the value to be assigned x_4 would be pointless since the final precision of the expression is ultimately governed by the precision of the result variable x_1 . Configurations that respect this relationship have a higher probability to lead to smaller errors w.r.t. configurations that do not respect this constraint. In practice, configurations where $x_4 \leq x_1$ are associated to smaller errors.

This information can be added to the training set as a collection of additional features. For each couple of variables involved in an assignment operation $x_i \rightarrow x_j$ we compute the feature $F_{ji} = x_j - x_i^3$, which is then added to the data set. Each feature corresponds to one of the logic binary constraints used to express the domain knowledge. For instance, if we consider again the example of Fig. 1b there are three additional features, one for each assignment expression (highlighted by the three arrows in the graph): $F_{43} = x_4 - x_3$, $F_{42} = x_4 - x_2$, $F_{14} = x_1 - x_4$. Thanks to these additional features an extended data set can be obtained. If we consider two possible configurations for the micro-benchmark in Fig. 1b, $C_1 = [27, 45, 35, 40]$ and $C_2 = [42, 23, 4, 10]$, the original data set would be composed by four features (one for each FP variable) plus the associate error (the target of the regression task). Instead, the extended data set contains seven features plus the error: $C_1^{ext} = [27, 45, 35, 40, 13, -5, -5]$ and $C_2^{ext} = [42, 23, 4, 10, -32, -13, -6]$.

Graphical Convolutional Neural Networks The transprecision learning task is a supervised regression problem whose prior information can be expressed through a graph, that is the dependency graph that links the variable in the benchmark. As mentioned in Section 3, GCNNs are well suited to deal with graph-structured problems. As our problem is different from those considered in the literature, we did not adopt the standard approach but we exploited the main component of GCNNs, the *graph convolution*, implemented via Graph Convolutional Layers (GCL), and applied to the transprecision task. The GCNN has the following structure: first, from the dependency graph we compute the adjacency matrix; then the adjacency matrix and the input feature matrix are combined to form the input of a first GCL, which is then fed to a second one. Its output becomes the input for a fully connected dense layer with 128 neurons, followed by two other fully connected layers of decreasing dimension (respectively, 32 and 8). The final layer is, again, a dense layer with a single neuron, that is the network output.

Data Augmentation and Regularization As mentioned in Sec. 4, the learning task is made more difficult by the presence of non-mononicity: situations where the normal precision-error relationship is not respected. They arise due to numerical instability, and their presence is magnified by the use of small data sets and a limited number of different input sets; with sufficiently large data sets they would be discarded as outliers. As mentioned before, the learning task addressed in this paper is a step towards an optimization model for precision tuning; with this scope in mind, it would be preferable to have an ML model that does not reproduce non-monotonicity events in its predictions. This is a domain knowledge about an undesirable property that should be corrected. The problem with non-monotonicity would be solved if we could have more training examples, but this is not easily attainable as we should run a benchmark to compute the error associated to a configuration. However, generating new configurations without computing the error is trivial; we can exploit this advantage in conjunction with an appropriate regularization scheme in order to impose monotonicity on the ML model predictions. This process is a form of data augmentation. Injecting the monotonicity constraint in the training process may allow to mitigate the noise and

³ If $F_{ji} \leq 0$ it means that the $x_i \leq x_j$ is not respected, hence a higher error is associated to the configuration

improve generalization, even with smaller training sets. We take into account such constraints at training time by exploiting ideas from SBR[3], that advocates to the use of (differentiable) constraints as regularizers in the loss function. Let us write $x_i \prec x_j$ if configuration x_j dominates x_i , i.e. if every variable in x_j has precision at least as high as x_i ; let P be the set of dominated-dominating pairs in our training set X, $P = (i, j)|x_i \prec x_j$. Then, we can formulate the following regularized loss function: $MSE(X, y) + \lambda \sum_{i,j \in P} max(0, f(x_j) - f(x_i))$, where f is the error predictor being trained, and MSE is the mean squared error. Each regularization term is associated to a pair in P and has non-zero value iff the error for the dominating pair is larger than for the dominated pair, i.e. if the monotonicity constraint is violated. New configurations in P can be generated in order to get a much more stable regularization factor without the need of a bigger train set. SBR is orthogonal to the use of additional features hence the two methods can be combined; we plan to explore the benefits of merging multiple methods in future work.

5 Experimental Evaluation

We selected 5 different data-driven models to obtain a baseline: I) a black-box optimization method (*AutoSklearn*); II) an NN composed of 4 dense layers with $10 \times n_{var}^B$ neurons each, that is, the number of variables in a benchmark multiplied by 10 (NN-I); III) an NN composed of 4 dense layers with $100 \times n_{var}^B$ neurons each (*NN-2*); IV) an NN composed of 10 dense layers with $10 \times n_{var}^B$ neurons each (*NN-3*); V) a NN composed of 20 dense layers with $10 \times n_{var}^B$ neurons each (*NN-3*); V) a NN composed of 20 dense layers with $10 \times n_{var}^B$ neurons each (*NN-4*). All NNs have a single-neuron output layer fully connected with the previous one. The black-box method used was drawn from the *AutoML* area, namely a framework called *autosklearn*[4] which uses Bayesian optimization for algorithm configuration and selection. Our problem can be cast in the AutoML mold if we treat the variables' precision as the algorithm configurations to be explored and the associated computation error as the target.

The code used to run the experiments was written in Python, using Keras and TensorFlow for the implementation of the neural networks. *Autosklearn* is distributed as a Python library and we used the version available online ⁴, with default parameters. The GCNN model was created using the *Spektral* library ⁵. All the results presented in this section were run on 20 different instances and we report the average values. Both input feature and targets were normalized. The code used to run the experiments is available in an online repository⁶. To evaluate the impact of the additional features, the four different neural networks previously defined (NN-1, NN-2, NN-3, NN-4) were trained and tested both with and without the extended data set. At this stage we focus on the number of layers and their width and discarded other hyperparameters; their exploration will be the subject of future research works. In this paper, these are the values for the main hyperparameter used with all methods: number of epochs = 1000; batch size = 32; as training algorithm we opted for *Adam* with standard parameters; Mean Squared Error as the loss function. The data augmentation and SBR approach is used

⁴ https://automl.github.io/auto-sklearn/master/

⁵ https://danielegrattarola.github.io/spektral/

⁶ https://github.com/AndreaBorghesi/knowInject_transComputing

on top of a neural network with the same number of layers and neurons as NN-1. The new configurations are injected in each batch during the training, with a fixed size of 256 elements; the amount of data generated is specified by a ratio, which represents the percentage of samples introduced by the data augmentation.

5.1 Models Accuracy

We begin by evaluating the prediction accuracy of the proposed approaches. We measure the accuracy using the MAE. In Table2 we compare the results obtained using a training and test set size of, respectively, 5000 and 1000 examples; test and training set are randomly drawn from the samples generated through LHS. The reported accuracy measures refer to the test set. The first column of the table identifies the benchmark (the last row corresponds to the average over all of them); the second column contains the MAE obtained with the black-box approach, *AutoSklearn*; columns 3 and 4 report the MAE with the first NN (NN-1), respectively without and with the additional features; the three following couples of columns are the results with the other NNs (NN-2, NN-2, NN-3), again split between the base and the extended data set; the final two columns correspond respectively to MAE obtained with GCNN and with SBR. For this table, we consider the SBR approach with 75% of augmented examples.

Benchmark	AutoSklearn	NN-1		NN-2		NN-3		NN-4		GCNN	CDD
		Base	Ext.	Base	Ext.	Base	Ext.	Base	Ext.	GONN	ODIT
FWT	0.394	0.315	0.251	0.056	0.054	0.104	0.061	0.070	0.105	0.351	0.243
saxpy	0.003	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.001
convolution	0.020	0.005	0.005	0.002	0.002	0.003	0.003	0.003	0.003	0.004	0.006
correlation	0.397	0.139	0.120	0.091	0.092	0.111	0.098	0.114	0.102	0.262	0.139
dwt	0.422	0.057	0.034	0.011	0.012	0.029	0.020	0.031	0.022	0.072	0.068
BlackScholes	0.411	0.238	0.047	0.184	0.035	0.239	0.038	0.297	0.172	0.307	0.220
Average	0.274	0.126	0.076	0.057	0.033	0.081	0.037	0.086	0.067	0.166	0.113

Table 1: Knowledge injection approaches comparison: MAE - train set size: 5k

Benchmark	AutoSklearn	NN-1		NN-2		NN-3		NN-4		GCNN	000
		Base	Ext.	Base	Ext.	Base	Ext.	Base	Ext.	GUNN	SBR
FWT	1.185	0.628	0.347	0.069	0.161	0.119	0.146	0.217	0.251	0.401	285
saxpy	0.004	0.001	0.001	0.000	0.001	0.000	0.001	0.000	0.001	0.004	0.003
convolution	0.049	0.006	0.011	0.006	0.004	0.008	0.006	0.005	0.006	0.024	0.012
correlation	0.406	0.400	0.356	0.141	0.288	0.269	0.206	0.284	0.145	0.332	0.152
dwt	0.559	0.062	0.040	0.012	0.038	0.029	0.042	0.076	0.054	0.134	0.094
BlackScholes	0.656	0.394	0.096	0.508	0.046	0.488	0.071	0.593	0.187	0.552	0.308
Average	0.477	0.248	0.142	0.123	0.090	0.152	0.079	0.196	0.107	0.188	0.148

Table 2: Knowledge injection approaches comparison: Root Mean Squared Error - set size 5k

The black-box model *AutoSklearn* has clearly the worst performance, which is not entirely surprising given the complexity of the learning task. The first unexpected and

disappointing result is the poor performance of the GCNN, that is outperformed by all other approaches in almost all benchmarks. We remark that this was a novel application of GCNN and this preliminary analysis merely suggests that a more careful exploration is needed. Changing the network type can produce good results: using a wider NN (from NN-1 to NN-2) greatly reduces the MAE, while deeper NNs provide smaller improvements (e.g. NN-3 and NN-4). Very interestingly, a major MAE reduction is obtained by using the additional features (column Ext.): for all NN types and over all benchmarks, the approach using the extended data greatly outperforms the baseline, with an average improvement of 39.7% (considering all four NN types). The results obtained with data augmentation and SBR show that this method performs better than AutoSklearn and the simplest NN without the additional features (NN-1), but it has a higher MAE compared to all the approaches with the extended data set. This is not an issue as SBR benefits were not expected in terms of prediction accuracy but rather on the enforcing of the monotonicity (see Sec. 5.2). We are also interested in measuring the results with smaller training sets, again using MAE as metric; we keep the test set size fixed at 1000 elements. Table 3 reports the experimental results; it has the same structure of Tab. 2. As expected, the prediction accuracy decreases with the training set size, but the benefits brought by the domain knowledge remain - over all training set size, the improvement brought by the engineered features is 38.7%.

Train Set Size	AutoSklearn	NN Base	l-1 Ext.		I-2 Ext.	NN Base	√-3 Ext.		√-4 Ext.	GCNN	SBR
500 (MAE) 1000 (MAE) 2000 (MAE) 5000 (MAE)	0.288 0.285 0.278 0.274	0.178 0.155	0.107 0.085	0.087 0.077	0.048 0.041	0.108 0.094	0.056 0.047	0.142 0.119	0.117 0.060	0.316 0.256 0.210 0.166	0.181 0.162
500 (RMSE) 1000 (RMSE) 2000 (RMSE) 5000 (RMSE)	0.797 0.769 0.530 0.477	0.435 0.284	0.139 0.155	0.152 0.168	0.121 0.072	0.206 0.105	0.095 0.096	0.375 0.260	0.235 0.156		

Table 3: Knowledge injection approaches comparison: average on all benchmarks MAE (rows 1-4) and RMSE (rows 5-8) – varying train set size

5.2 Semantic Based Regularization Impact

This section provides additional details on the experiments on data augmentation and SBR. The model was tested on the previous benchmarks and different ratios of data injected, i.e. 25% and 75%. To have a more precise evaluation of the approach, we relied on another metric beside MAE, that is the number of violated monotonicity constraints – the goal of this approach is to *reduce* their number. We underline that not every benchmark had monotonicity issues (as they are outliers), and in these cases the regularization factor is of no use and might keep the model from a good approximation. For this reason, Table 4 and Table 4, report just the values from significant benchmarks (i.e. benchmarks that exhibit the most marked non-monotonic behavior), these are *con*-

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volution and *correlation*. The third column reports the result obtained with NN-1 without the additional features. Columns 4-6 correspond to the results obtained with data augmentation and SBR, with different percentages of injected data (0%, 25%, 75%).

			V-1 SBR #Viol. MAE #Viol.			-	 SBR 75% MAE #Viol.	
convolution	500 5000					0.013 0.006		
correlation	$500 \\ 5000$	0.263 0.139				0.263 0.059		

Table 4: SBR: MAE and number of violated constraints (#Viol.)

With larger training sets, the benefits of data augmentation and SBR are marginal: the additional constraint on the loss function is not very useful, given the abundance of training samples allowing for better generalization. Similarly, larger training sets lead to a natural decrease in the number of monotonicity constraints violated (as their proportion in the training set diminishes). Nevertheless, the more interesting results can be observed when fewer data points are available, since the models show a decrease in the number of violated constraints opposed to the network without regularization. Furthermore, the networks performed better with higher ratios of data injected, i.e. 18%, on average. Finally, the MAE seems to have values compatible to the results obtained with *NN-1*, a good result since prediction accuracy was not SBR's scope. These results encourage the idea of a hybrid model merging data augmentation plus SBR and additional features (both approaches enabled by the injection of domain knowledge), as future development of this work.

6 Conclusion & Future Works

In this paper we present a strategy for injecting domain knowledge in an ML model. As a case of study, we considered a learning task from the transprecision computing field, namely predicting the computation error associated to the precision used for handling a set of FP variables composing a benchmark. This is a difficult regression problem, hard to be addressed with pure data-driven ML methods; we have shown how critical improvements can be reached by injecting domain knowledge in the ML models.

We introduced three knowledge-injection approaches and applied them on top of NNs with varying structures: feature engineering, a GCNN, and a data augmentation scheme enabled by SBR. The GCNN approach did not improve the accuracy of the ML model w.r.t. the baseline and it should be explored more in detail. Conversely, the creation of extended data set was revealed to be extremely useful, leading to remarkable reduction in prediction error (39.7% on average and up to 47.5% in the best case). Data augmentation plus SBR showed its potential with training sets of limited size, in terms of reduced number of violated monotonicity constraints while preserving the ML models' prediction accuracy. In future works we plan to integrate the learners in an

optimization model for solving the FP tuning precision problem. In this regard we will explore active learning strategies and we expect SBR to have good result, especially when combined with the additional features (the methods are orthogonal). Moreover, we will perform experiments with other domain knowledge injection approaches, for instance by building data sets in accordance with the prior information and by exploiting the knowledge to guide the training of the NN by constraining its output.

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